

# 1 **Response-based bridge deck limit state considering component-level failure** 2 **under extreme wave**

3 Deming Zhu<sup>1</sup>, You Dong<sup>2</sup>, Peng Yuan<sup>3,\*</sup>, and Guoji Xu<sup>4</sup>

## 4 **Abstract**

5 Coastal bridges are crucial components of transportation systems; however, they are  
6 susceptible to increasing failure risk from extreme waves due to climate change scenarios.  
7 Previously, most of the studies focused on the extreme wave forces on the bridge superstructure,  
8 while the effects of the overturning moment, bearing constraints, and local damage were  
9 seldom discussed. This research conducts an in-depth investigation on the wave-bridge  
10 interaction to explore the structural limit state of the coastal bridges subjected to extreme waves  
11 considering component failure. Firstly, a three-dimensional (3D) Computational Fluid  
12 Dynamics (CFD) model is established and validated to simulate the wave-bridge interaction  
13 under various wave scenarios. To lend confidence to the CFD model, laboratory experiments  
14 are conducted to improve and validate the simulation results. Subsequently, based on the  
15 numerical results, wave force prediction methods are proposed by considering the solitary wave  
16 characteristics. Accordingly, the time histories of wave forces are imported into a spatial Finite  
17 Element (FE) model of the investigated bridge FE model to compute dynamic structural  
18 responses, including bearing reaction forces, bridge displacements, and bearing working states.  
19 Then, based on the dynamic structural response, a novel structural limit state incorporating  
20 component damage is developed to prevent bearing damages under the wave impacts and  
21 corresponding structural demand is parametrically studied and quantified with different wave  
22 parameters. Such a study could help optimal and robust designs of coastal bridges and  
23 modifications of existing ones.

24 **Keywords:** Coastal bridges; Laboratory experiments; 3D numerical models; Overturning  
25 effects; Bearing performance; Wave force.

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## 36 **1. Introduction**

37 Coastal bridges are vulnerable to extreme waves generated by hurricanes and tsunamis in the  
38 climate change scenario. For instance, 81 coastal bridges connecting the Banda Aceh and  
39 Malabon were severely destroyed by the 2004 Indian Ocean Tsunami (Unjoh and Endoh 2006).  
40 As reported in Padgett et al. (2008), Hurricane Katrina (2005) caused significant damage to the  
41 transportation system in the Gulf Coast region, and the overall cost of the repair and  
42 reconstruction was estimated at over \$1 billion. These repeated disasters punctuate the need to  
43 better understand the structural performances of coastal bridges under wave impacts.  
44 Additionally, the fast development in bridge systems has continued to occur in coastal  
45 communities along with the rapid population growth (Cheng et al. 2018a; Padgett et al. 2012).  
46 Moreover, the global climate change effects yield sea level rise and amplification of intensity  
47 and frequency of storms (Knutson et al. 2010), which generates increasing risks to the coastal  
48 bridges. Therefore, it is valuable to improve our understanding of the wave-bridge interaction  
49 mechanisms for the robust and optimize designs of coastal bridges against natural hazards.

50 Previous studies focusing on wave impacts on the bridge superstructure have led to the  
51 first Guide Specification for Bridges Vulnerable to Coastal Storms (AASHTO 2008); however,  
52 more relevant research is required to fully comprehend the complex wave-bridge interaction  
53 (Fang et al. 2019). For instance, the AASHTO formulas are not suitable for waves with  
54 relatively large periods and wavelengths. Specific physical tests or computational models are  
55 recommended for an accurate result (AASHTO 2008). There were several studies comparing  
56 AASHTO estimation methods with their test results (Azadbakht and Yim 2016; Guo et al. 2015;  
57 Seiffert et al. 2015) and bias removal methods (Ataei 2013; G. Xu et al. 2017), but a precise  
58 estimation method has not been reached. Additional work is valuable to improve the accuracy  
59 of the predictive equations of wave forces on bridge superstructures (Kulicki 2010; Zhu et al.  
60 2021).

61 On the other hand, most studies focused on the maximum wave force on the deck, while  
62 the time series effects during the wave-bridge interaction have attracted attention in recent  
63 years. Xu et al. (2018) performed time-domain simulations of wind and wave loads on a three-

64 span suspension bridge and found it challenging to select the combinations of the  
65 environmental parameters to be used in the design of the structural component. Ding et al.  
66 (2018) investigated the combined earthquake and wave-current effects on bridge piers through  
67 experimental tests. Furthermore, the time-series effects of overturning (or rotation) on deck  
68 failure has aroused concern in recent years (Cheng et al. 2018a, 2018b; Hayatdavoodi and  
69 Ertekin 2015), but the solutions are controversial. For instance, AASHTO (2008)  
70 recommended selecting the reference point of the moment at the bottom of the landward girder,  
71 while Cai et al. (2018) suggested it at the center of the bent beam. However, Xu (2020) pointed  
72 out such a method could underestimate the effects of horizontal wave force. Therefore, more  
73 relative studies are required to further investigate the uneven load distribution and overturning  
74 moment on coastal bridges.

75       Moreover, the bearing (or constraint) performance under the wave impacts, which plays  
76 an important role in the connection between superstructure and substructure, has not been  
77 investigated thoroughly. Since the uplift wave forces are opposed to the traditional downward  
78 traffic loads, the bearing responses under wave impacts are rather complicated. The  
79 significance of investigations on bearings was highlighted in Bradner et al. (2011), which  
80 conducted a 1:5 scale laboratory experiment to explore wave impacts on the bridge  
81 superstructure and effects of bearing stiffness. In the following studies, there were some  
82 simplified numerical models representing bearings by using springs (Xu and Cai 2015), while  
83 which could not fully simulate bearing connections under real-bridge conditions. Saeidpour et  
84 al. (2018) performed a static analysis to investigate structural responses under anchor bolt  
85 constraints, but the results may deviate from practical dynamic conditions. Ataei and Padgett  
86 (2015) investigated bridge responses based on a fluid-structure interaction model, but the  
87 bearing constraints were not considered. Salem et al. (2014, 2016) conducted field surveys of  
88 damaged bridges by Tohoku Tsunami and utilized Applied Element Method to simulate the  
89 structural progressive collapse under wave impacts. They also emphasized the significance of  
90 a more detailed analysis based on a three-dimensional (3D) model. Thus, it is vital to study the  
91 bearing performance during the wave-bridge interaction utilizing a more sufficient (3D) model

92 and this aspect is conducted in this study.

93 Recognizing all the issues above, an in-depth investigation of the wave-bridge interaction,  
94 wave force prediction method, and the limit states considering component damage based on  
95 structural responses is conducted using experiments and 3D numerical models in this study.  
96 Specifically, a 3D Computational Fluid Dynamics (CFD) model is established to simulate the  
97 wave-bridge interaction, which could calculate changing wave profiles, wave-induced forces,  
98 overturning moments, and pressure distributions, improving the understandings of the complex  
99 hydrodynamic problem. To lend confidence of the established CFD model, laboratory  
100 experiments are conducted to improve and validate the simulation results. Based on the  
101 numerical results, wave force prediction methods are proposed and discussed by considering  
102 the solitary wave characteristics. Moreover, to formulate the limit state of the coastal bridge  
103 under the wave impacts, including overturning moments, displacements, and bearing  
104 performance, a 3D bridge FE model considering the effects of material properties, structural  
105 dimensions, and system damping on the structural responses is built and corresponding  
106 structural demand is discussed and quantified with different wave parameters. The numerical  
107 models are improved based on our previous work (Zhu et al. 2021) in the following aspects:  
108 (a) the new models simulate more structural details as compared with the previous one,  
109 including diaphragms and deck overhangs; (b) the bridge superstructure is divided into 6 girder  
110 components and 5 deck components, so that the wave-induced forces on each component could  
111 be computed; and (c) dynamic structural analyses are performed by importing the time-history  
112 wave forces into the FE model. To the best knowledge of the authors, this is the first time that  
113 a limit state which considers the component (bearing) damage is proposed for coastal bridges  
114 subjected to solitary wave forces by considering the time histories effects of the overturning  
115 moment and bearing performance.

116 The paper is organized as follows. The experimental and numerical methodologies are  
117 introduced in section 2. The experimental results, validations for the CFD model, and simulated  
118 wave-bridge interactions are presented in section 3. Wave force prediction methods are  
119 proposed in section 4. The structural limit states based on dynamic structural response are

120 formulated and discussed in section 5. Conclusions are drawn in section 6.

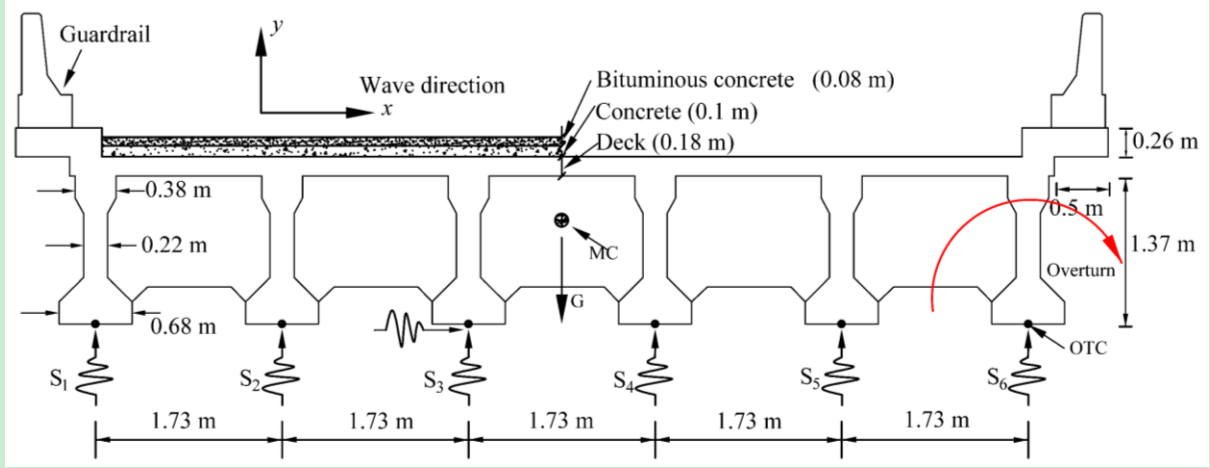
## 121 **2. Experimental setups and 3D numerical modeling**

122 Laboratory experiments of a typical bridge model are conducted, and solitary wave-induced  
123 forces are measured to validate the built 3D CFD numerical model. Considering that most of  
124 the coastal bridges are located in shallow water regions near shorelines (Chen et al. 2009), the  
125 shallow water solitary wave model is adopted in this study, which could simulate the tsunami-  
126 induced waves well (Seiffert et al. 2014). Since the storm waves are periodic, such a solitary  
127 wave model may not be appropriate to represent storm waves (Seiffert 2014). Besides, to  
128 further assess the structural limit states under wave force time histories, the spatial FE model  
129 of the bridge is established by using the ANSYS Mechanical APDL package.

### 130 2.1 Experimental setups

#### 131 2.1.1 Investigated bridge and wave model

132 Based on the post-disaster reconnaissance reports on coastal natural hazards, most of the  
133 severely damaged bridges were inadequately designed to resist extreme wave loads (Douglass  
134 et al. 2004; Robertson et al. 2007; Suppasri et al. 2013). This study selects a typical type of  
135 simply supported bridge significantly damaged in previous hazards (Hayatdavoodi et al. 2014a;  
136 Li et al. 2020; Padgett et al. 2008), as shown in Fig. 1. The span length is 15.85 m, girder height  
137 is 1.37 m, and deck thickness is 0.18 m. Diaphragms are set in the middle and two ends of the  
138 span. Pavement overlays are composed of a 0.1 m thick concrete surface and a 0.18 m thick  
139 bituminous concrete pavement on the deck. Concrete guardrails are set at the two sides of the  
140 deck. The distance between two neighboring girders equals 1.73 m. The clearance calculated  
141 from the initial water level to the girder bottom is set as 4 m. The bridge deck under the wave  
142 impacts from seaward tends to be overturned around the overturning center (OTC, see Fig. 1).  
143 Deck weight and material properties are listed in Table 1.



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**Fig. 1** The schematic diagram of a typical coastal bridge subjected to extreme waves. MC is the mass center of the bridge; OTC is the overturning center; and  $S_i$  is bearing connection.

**Table 1** Material properties of the investigated bridge model

	Density	Quantity	Weight
Main structure	$2.6 \times 10^3 \text{ kg/m}^3$	$84.2 \text{ m}^3$	$218.9 \times 10^3 \text{ kg}$
Bituminous concrete	$2.4 \times 10^3 \text{ kg/m}^3$	$0.08 \times 8.65 \times 15.85 \text{ m}^3$	$26.3 \times 10^3 \text{ kg}$
Concrete	$2.6 \times 10^3 \text{ kg/m}^3$	$0.1 \times 8.65 \times 15.85 \text{ m}^3$	$35.6 \times 10^3 \text{ kg}$
Guardrail	$2 \times 10^3 \text{ kg/m}$	$15.85 \text{ m}$	$31.7 \times 10^3 \text{ kg}$
Total weight = $312.5 \times 10^3 \text{ kg/span} = 3,063 \text{ kN/span}$			

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The shallow water solitary wave is adopted in this study to simulate the huge waves, which has been frequently used to model some important features of the extreme wave for its stable form and large amplitude (Goring 1978; Yeh et al. 1994). The stable form also benefits measurements at the laboratory and comparisons between experimental and numerical results (Zhu and Dong 2020). The free surface profile  $\eta$  of the solitary wave is as (Miles 1981)

$$\eta(x, t) = H \operatorname{sech}^2 \sqrt{\frac{3}{4} \frac{H}{D^3}} (x - ct) \quad (1)$$

$$t_0 = \frac{\tanh^{-1}(0.999)}{c \sqrt{\frac{3}{4} \frac{H}{D^3}}} = \frac{3.8}{c \sqrt{\frac{3}{4} \frac{H}{D^3}}} \quad (2)$$

155 where  $H$  = wave height;  $D$  = water depth;  $c$  = wave celerity;  $x$  = coordinate;  $t$  = time; and  $t_0$  =  
156 the time interval between the wave crest and still water level. In Eq. (1), the wave function  $\eta$   
157 tends to be 0 as  $t$  goes infinity, which means the intercept of the leading and trailing edges of  
158 the wave  $t_0$  occurs at  $\pm\infty$ . To meet the wave generating device and numerical analyses,  $t_0$  is  
159 defined with a precision expression of three significant figures as Eq. (2) (Goring 1978).  
160 Accordingly, the wave period of the solitary wave  $T$  equals  $2t_0$ , and the wavelength  $\lambda$  is  
161 calculated as the product of celerity and period.

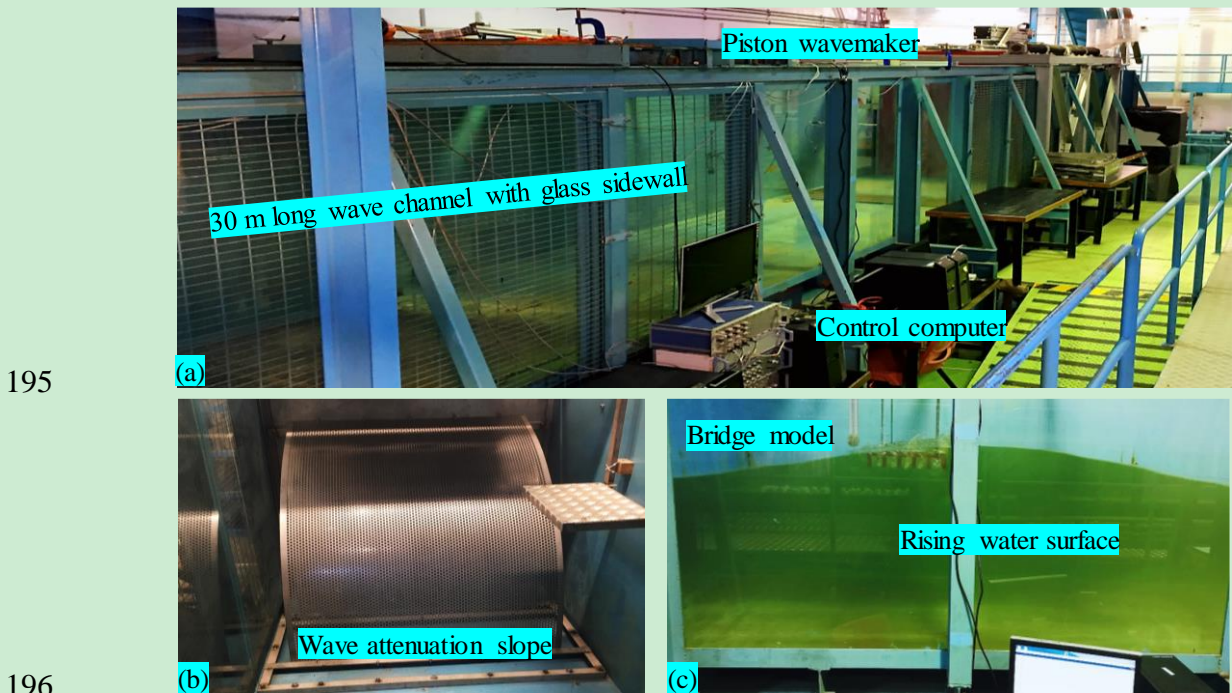
### 162 2.1.2 Experimental setups

163 A 1:30 scale experiment on the investigated bridge model is conducted in the wave channel at  
164 the Hydraulics Laboratory of the Hong Kong Polytechnic University for validation of the 3D  
165 CFD model. The wave channel is 30 m long, 1.5 m deep, and 1.5 m wide, with a sidewall made  
166 of glass for observation as shown in Fig. 2 (a). Solitary wave is generated by using a piston-  
167 type wavemaker at one side of the channel, and a wave attenuation slope is set at the other side  
168 to minimize wave reflection effects as Fig. 2 (b). The push panel of the wavemaker is controlled  
169 by the DHI's (Danish Hydraulics Institute) control system. The changing water surfaces are  
170 measured by three wave gauges around the bridge model. Wave forces on the bridge model in  
171 the  $x$ ,  $y$ , and  $z$  directions are measured by a multi-axis load cell at a frequency of 100 Hz.  
172 Instrument calibrations are performed for all the wave gauges, piston wavemaker, and load cell.  
173 A typical photo of the wave-bridge interaction in the test is shown in Fig. 2 (c). The  
174 experimental measurements are compared with the CFD numerical results to validate the model.  
175 Each case tested is repeated 5 times, and maximum and minimum results and results with a  
176 standard deviation larger than  $\pm 5.5\%$  from the mean are removed from the presented results to  
177 minimize experimental errors.

178 The experiment is designed according to the Froude similitude (Chakrabarti 2005). Since  
179 the same fluid (i.e., water) is used for both model and prototype, it is hard to achieve exact  
180 dynamic similarity for water waves. In the design of the experiment, the effects of surface  
181 tension and compressibility are relatively small in this open channel wave flow. The viscosity  
182 could also be neglected in this free-surface model when the model is not too small (Briggs



183 2013). Thus, the Froude similitude is the major scaling criterion in this study. As a result, the  
184 Reynolds numbers are inevitably slightly different between the experimental and prototype  
185 scales (on the order of  $10^4 \sim 10^5$  for the experimental scale and  $10^6 \sim 10^7$  for the prototype  
186 scale). The authors also examine the effects of the different Reynolds numbers under these two  
187 circumstances through different scales of CFD models. It is observed that after conversion, the  
188 maximum vertical forces from the 1:30 scale model are no more than 3% larger than those from  
189 the prototype model, and the horizontal forces are very close. It means the scale models could  
190 provide more conservative results in the engineering field. Nevertheless, additional works on  
191 reducing these differences are still encouraged such as adjusting the fluid viscosity in the lab  
192 tests. For the Weber number, the surface tension force is negligible as compared with the wave  
193 impacts on the bridge, since the latter one could reach over 200 N during the wave-bridge  
194 interaction.



197 Fig. 2 (a) 30 m long wave channel; (b) wave attenuation slope with meshes; and (c) wave-  
198 bridge interaction in the test

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## 200 2.2 3D Numerical models

### 201 2.2.1 CFD modeling and boundary conditions

202 The fluid motion is simulated using the software ANSYS Fluent, which is improved based on  
203 the model in the previous research (Zhu et al. 2021). In this study, the refined model contains  
204 more structural details, including diaphragms between the girders and the overhangs at the two  
205 sides of the bridge deck (as shown in Fig. 6). Solitary waves are generated from the velocity  
206 inlet plane ABCD by using User Defined Functions (UDF), and plane EFGH is set as pressure  
207 outlet. The dynamic free surface is prescribed by the Volume of Fluid (VOF) method (Hirt and  
208 Nichols 1981) with air set as primary phase and water-fluid set as secondary phase. The whole  
209 numerical domain is 140 m long ( $x$  direction), 30 m high ( $y$  direction), and 20.85 m wide ( $z$   
210 direction). The bridge model is located 20 m from the velocity inlet plane, and the distance to  
211 the outlet plane is long enough to minimize wave reflection effects. **The bridge model is also  
212 set as no-slip stationary walls. Wall-layer models were added to produce a smooth distribution  
213 along the fluid-wall interfaces following the authors' previous work (Xu et al. 2017). The  $y^+$   
214 values at the grid cells at the bridge deck surface are around 50 in the established model.** The  
215 vertical and horizontal wave particle velocities ( $u$  and  $v$ ) are used to generate solitary waves at  
216 the velocity inlet plane following Sarpkaya and Isaacson (1981).

217 In the numerical model, a Boolean subtract is applied for the bridge model. Tetrahedron  
218 meshes are utilized to fit the irregular shapes of the girders and diaphragms. To eliminate the  
219 influence of the grid on the calculation results, mesh sensitivity analysis is performed, and  
220 different fixed time steps are tested to satisfy the Courant Number (Robertsson and Blanch  
221 2020). After several calculations and comparisons of different combinations of mesh sizes and  
222 time steps, the mesh size is determined as 0.6 m, the fixed time step is 0.01 s. In addition, the  
223 shear stress transport (SST)  $k-\omega$  model with the turbulence damping factor set as 10 is utilized  
224 as the viscous model for the wave-structure interaction. The turbulent intensity of the boundary  
225 is set as 2% and the turbulent viscosity ratio is set as 10%. The Pressure-Implicit with Splitting  
226 of Operators (PISO) scheme is adopted, and the pressure staggering option (PRESTO) scheme  
227 is set for the pressure spatial discretization. The least squares cell-based scheme is used for the

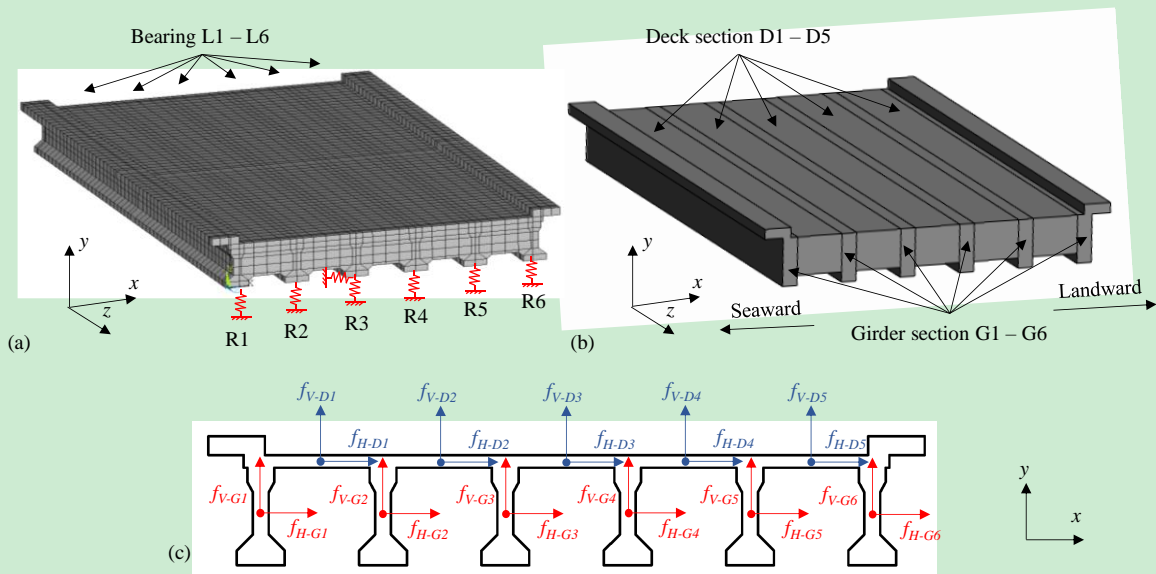
228 gradient discretization, and the second-order upwind is used for momentum advection terms,  
229 the spatial discretization of the turbulent kinetic energy, and the specific dissipation rate.  
230 Moreover, the stability of the generated solitary wave is also examined that the established  
231 CFD model could simulate stable solitary waves with a  $H/D$  ratio (wave height/water depth)  
232 ranging from 0.15 to 0.45. It should be noted that the effects of added mass, which could be  
233 estimated by Morison equations (Gao et al. 2020, 2021; Morison et al. 1950), are relatively  
234 small as compared with the impulse force, so that they are neglected in the structural analysis.  
235 Also, the allowable structural displacement is relatively small during the wave-bridge  
236 interaction due to the large stiffness of the bearing constraints between the bridge superstructure  
237 and substructure (Xu et al. 2015), so the bridge is assumed as a rigid body in the ANSYS Fluent  
238 model, which could also significantly improve the computational efficiency. Detailed  
239 information on the established model could be found in Zhu et al. (2021). The 3D numerical  
240 model could also be applied to investigate the effects of the bridge substructures on the results  
241 by modeling the piers and abutments, which is a critical step to have a deeper understanding of  
242 the wave-bridge interaction mechanism (Wei and Dalrymple 2016).

### 243 2.2.2 FE modeling of the bridge

244 The CFD model could simulate the wave-bridge interaction, while the complex bearing  
245 reaction, structural deformation, and structural force for the bridge under wave could not be  
246 well solved. To investigate structural limit states under the wave impacts, a spatial FE model  
247 for the bridge is established by using the ANSYS Mechanical APDL package as shown in Fig.  
248 3. The time-history wave-induced forces from CFD results are imported into the FE model to  
249 calculate the dynamic structural responses, including structural displacements and bearing  
250 reaction forces.

251 As indicated in Fig. 3 (a), a full bridge deck with girders and diaphragms is modeled and  
252 meshed. All the bearing constraint types are listed in Table 2 with considering practical  
253 engineering design (AASHTO 2017; Caltrans 1994). Specifically, all the bearings are set as  
254 compression-only in the vertical direction ( $y$  direction) since they are usually designed to not  
255 allow uplift tension force (Khaleghi et al. 2019). Constraints in the longitudinal direction ( $z$

256 direction) are assumed at the  $R$  end for the investigated simply supported bridge model. With  
 257 respect to constraints in the horizontal direction ( $x$  direction), only the bearings L3 and R3 are  
 258 constrained to release the thermal movement at two ends in the horizontal direction (Khaleghi  
 259 et al. 2019). Only the constrained bearings would produce reaction forces in the corresponding  
 260 direction under wave forces. A slight difference in the responses of bearings connecting to the  
 261 same girder at the two ends (e.g., bearing reaction forces on the second pair of bearings  $S^2_l$  and  
 262  $S^2_r$ ) could be captured due to the different constraints in the longitudinal direction. It should be  
 263 noted that to ensure a stable computation after the bearing disengagement occurs, a small  
 264 tensile stiffness coefficient is assumed for the constraints in the vertical direction, which has  
 265 little influence on practical results. To accurately extract wave forces from CFD and apply them  
 266 to the bridge, the deck is divided into 5 deck sections (D1 – D5) and 6 girder sections (G1 –  
 267 G6) as marked in Fig. 3 (b), and wave forces from the CFD model are import into the FE model  
 268 as shown in Fig. 3 (c), where  $f_{V-Gi}$  is the vertical force on the girder component;  $f_{H-Gi}$  is the  
 269 horizontal force on the girder component;  $f_{V-Di}$  is the vertical force on the deck component; and  
 270  $f_{H-Di}$  is the horizontal force on the deck component. In this FE model, SOLID 65 and COMBIN  
 271 39 are used to simulate the concrete and bearings, respectively. The ultimate concrete  
 272 compressive strength is set as 37.1 MPa and the axial tensile cracking stress is 3.25 MPa (ACI  
 273 2014). The shear transfer coefficient for concrete open and close crack are set as 0.3 and 0.5,  
 274 respectively, and the Poisson's ratio is taken as 0.167.



275

276 **Fig. 3** (a) spatial model of the bridge deck in ANSYS Mechanical APDL; (b) structural  
 277 segmentation for wave load application; and (c) schematic diagram of the load application  
 278 method

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**Table 2** Boundary conditions of the bearings

No.	$x$	$y$	$z$	No.	$x$	$y$	$z$
L1	/	C_O.	/	R1	/	C_O.	Con.
L2	/	C_O.	/	R2	/	C_O.	Con.
L3	Con.	C_O.	/	R3	Con.	C_O.	Con.
L4	/	C_O.	/	R4	/	C_O.	Con.
L5	/	C_O.	/	R5	/	C_O.	Con.
L6	/	C_O.	/	R6	/	C_O.	Con.

281 **Note:** / refers to no constraint in the corresponding direction; C\_O. refers to compression-  
 282 only bearing; and Con. refers to constraints in the corresponding direction.

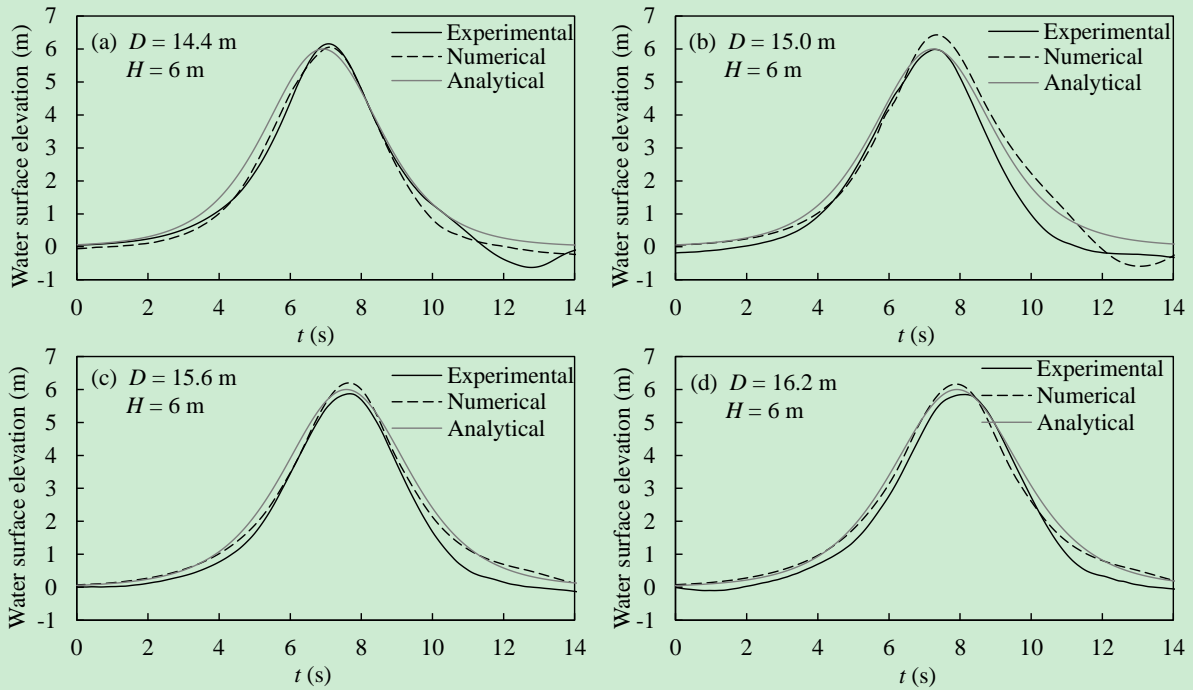
### 283 3. Experimental and numerical investigations of wave-bridge interactions

284 Firstly, experimental validations for the CFD model are presented by comparing the measured  
 285 wave profiles and wave forces with the numerical results. Then, the validated 3D CFD model  
 286 is used to simulate the wave-bridge interactions and compute wave force distributions on the  
 287 bridge for an extensive set of wave conditions. The results of a typical wave case with  $D = 14.4$   
 288 m,  $Z_c = 2.1$  m, and  $H = 4.2$  m are presented for illustrative purposes, and time histories of wave-  
 289 induced forces, overturning moments, and pressure distributions are investigated. Additionally,  
 290 maximum wave force and overturning moment under different wave scenarios are discussed.

#### 291 3.1 Measurement-based validation of CFD model

292 In the experiment, the changing wave profiles under different cases and wave-induced force  
 293 time histories are measured and compared with numerical results to improve and validate the  
 294 established CFD model. The generated solitary wave profiles obtained from experimental tests,  
 295 CFD computations, and analytical solutions (from Eq. (1)) are presented in Fig. 4. Different

296 cases are examined including (a)  $D = 14.4$  m,  $H = 6$  m; (b)  $D = 15$  m,  $H = 6$  m; (c)  $D = 15.6$  m,  
 297  $H = 6$  m; and (d)  $D = 16.2$  m,  $H = 6$  m. Note that the 1:30 scale experimental results are  
 298 converted to prototype scale according to Froude similitude (Chakrabarti 2005). As indicated,  
 299 Eq. (1) calculates theoretical results with completely symmetrical leading and trailing wave  
 300 edges, while the water surface could fluctuate at the trailing edge after the wave crest passes,  
 301 which is observed in both experimental and numerical results. The wave profiles generated by  
 302 the three methods are well consistent with each other, and the differences at the peak surface  
 303 elevations are 3% - 6% for all the cases, which are acceptable for the established model  
 304 (Hayatdavoodi et al. 2014b; Seiffert et al. 2014).

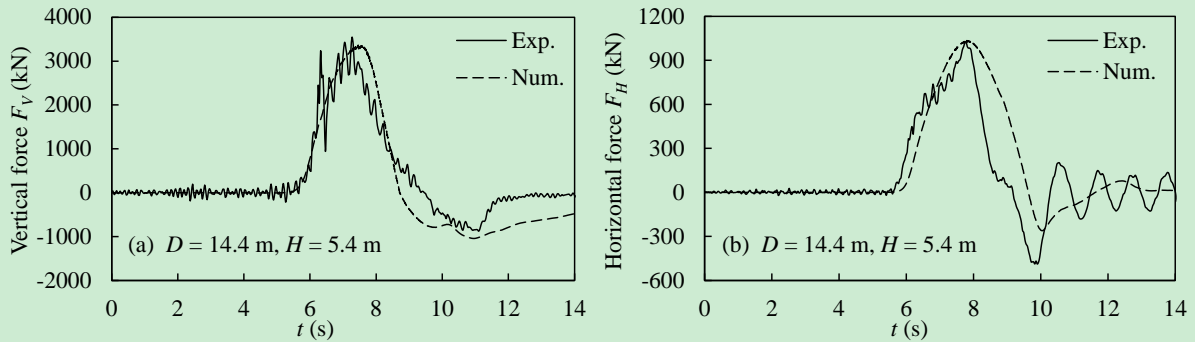


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 306 **Fig. 4** Comparisons of wave profiles obtained from experimental measurements, CFD  
 307 models, and analytical function (Eq. (1)) for cases: (a)  $D = 14.4$  m,  $H = 6$  m; (b)  $D = 15$  m,  $H$   
 308  $= 6$  m; (c)  $D = 15.6$  m,  $H = 6$  m; and (d)  $D = 16.2$  m,  $H = 6$  m

309  
 310 To further validate the established CFD model, comparisons of the vertical and horizontal  
 311 wave force time histories ( $F_V$  and  $F_H$ ) between experimental measurements and CFD  
 312 computations for a typical case with  $D = 14.4$  m,  $H = 5.4$  m are shown in Fig. 5. The vertical  
 313 wave forces are in close agreement (see Fig. 5 (a)). In Fig. 5 (b), the simulated horizontal wave  
 314 forces are slightly different from the experimental measurements, which may be caused by the



315 damping effects of the experimental devices even though they are equipped with relatively  
 316 rigid connections. Overall, good agreement is observed between the computations and  
 317 laboratory measurements for both the wave profile and wave force time histories, which proves  
 318 the reliability of the established 3D CFD model.

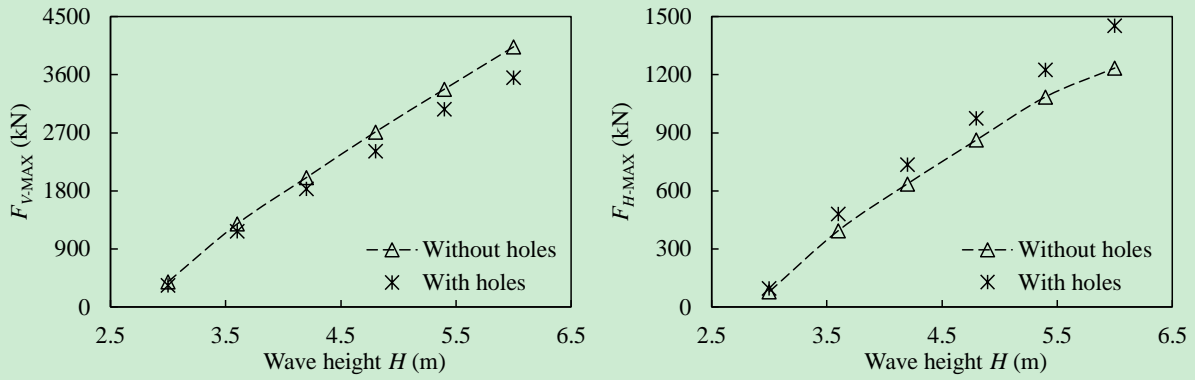


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320 **Fig. 5** Comparisons of vertical and horizontal wave force time histories from CFD models  
 321 and experimental measurements for the case with  $D = 14.4$  m,  $H = 5.4$  m

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323 During the wave-bridge interaction, it is observed that the air could be partially trapped  
 324 between the rising water level and the bridge structure, while some of it could escape outside.  
 325 Such trapped air can increase the total wave loads on the bridge deck, and the partially escaped  
 326 air would bring uncertainties to the analyses (Bricker and Nakayama 2014). To further explore  
 327 the contribution of the trapped air on the results, this study compares two scenarios with and  
 328 without the presence of the trapped air by setting air venting holes on the bridge deck to release  
 329 the air (Cuomo et al. 2009; Xu et al. 2016). After tests for a wide range of wave excitations,  
 330 typical results are plotted in Fig. 6. It is observed that through setting air venting holes to release  
 331 the trapped air, the vertical force  $F_{V-MAX}$  could be reduced by no more than 8%, while the  
 332 horizontal force  $F_{H-MAX}$  may be enlarged. Such characteristics may be caused by the increase  
 333 in the contact area between the waves and the bridge in the lateral direction after the escapement  
 334 of the trapped air. This study mainly focuses on the limit state of the conventional bridge deck  
 335 (i.e., no air venting holes), which means the effects of the partially escaped air would be less  
 336 than 8%. Nevertheless, more investigations are encouraged to further quantify the effects of  
 337 trapped air in the future.



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342

**Fig. 6** Comparisons of the maximum vertical and horizontal wave forces ( $F_{V-MAX}$  and  $F_{H-MAX}$ ) on the bridge deck with and without setting air venting holes for the cases with  $D = 14.4$  m,  $Z_c = 2.1$  m

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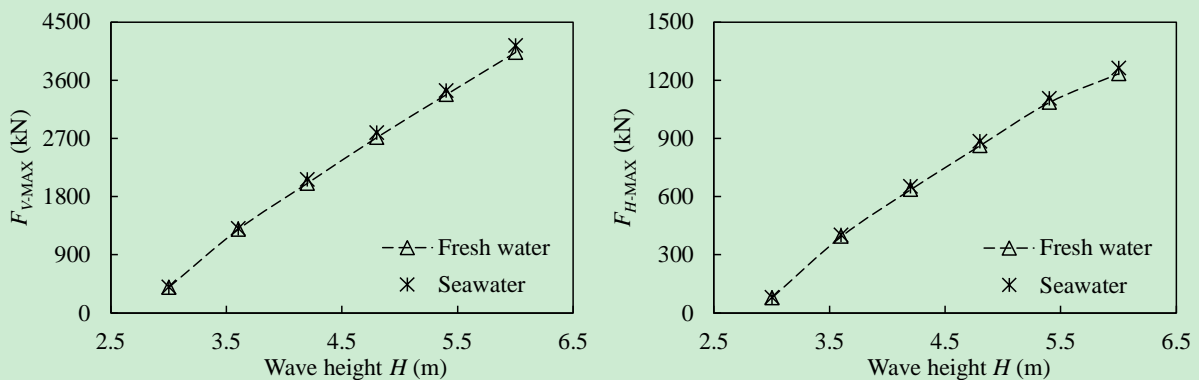
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In addition, this study also compares and examines the effects of freshwater (with a density of  $1,000 \text{ kg/m}^3$ ) and seawater (with a density of  $1,025 \text{ kg/m}^3$ ) on the maximum vertical and horizontal wave forces on the bridge deck ( $F_{V-MAX}$  and  $F_{H-MAX}$ ), so that the computational results could be applied to real bridges located in coastal regions. As shown in Fig. 7, the wave forces are very close under these two scenarios, and the seawater-induced forces are a bit larger. By comparing multiple datasets of the wave forces, the differences between these two scenarios are no more than 3%, which indicates the established CFD model is applicable for different water conditions.



351

352

353

**Fig. 7** Effects of fresh water and seawater on the maximum vertical and horizontal wave forces ( $F_{V-MAX}$  and  $F_{H-MAX}$ ) for the cases with  $D = 14.4$  m,  $Z_c = 2.1$  m

354

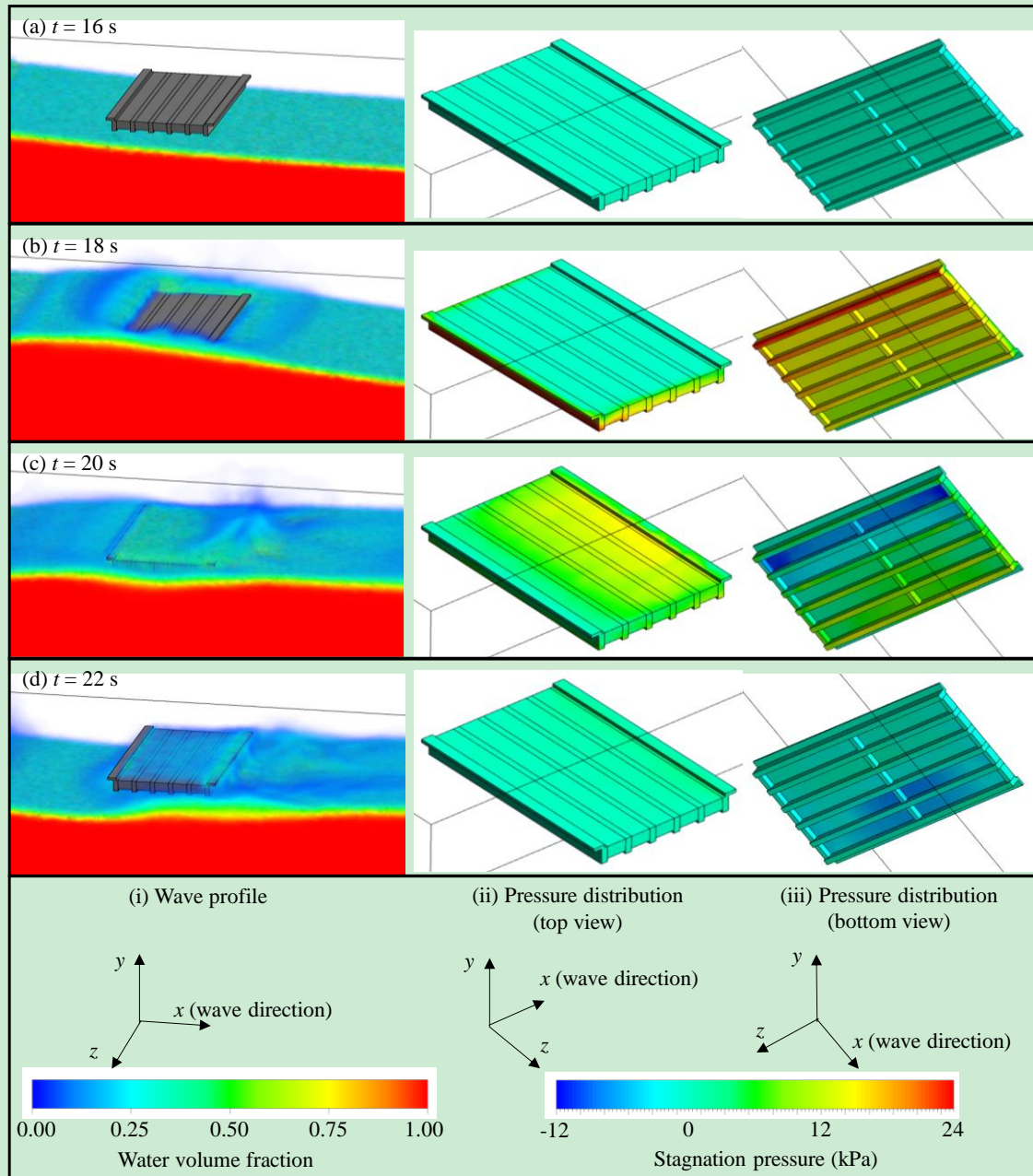
### 3.2 Wave-bridge interaction in the 3D CFD model

355

To observe the hydrodynamic wave-bridge interaction, a typical wave case with  $D = 14.4$  m,



356  $Z_c = 2.1$  m, and  $H = 4.2$  m is illustrated. In this case, the initial water level is lower than the  
357 bridge deck, while the wave is large enough to hit and exceed the deck. Four representative  
358 moments of wave profiles and stagnation pressure distributions on the bridge deck are shown  
359 in Fig. 8. The fluid phases are represented by different colors based on the VOF method (1 for  
360 water phase and 0 for air phase). Lists (ii) and (iii) present stagnation pressure distributions on  
361 the deck from the top and bottom views, respectively. When the solitary wave forwards along  
362 the  $x$  axis and overtopping occurs as shown in Fig. 8 (b), the stagnation pressure on the seaward  
363 side of the deck sharply increases, while that on the landward side changes little. The uneven  
364 pressure distribution leads to a large overturning moment on the deck, and the deck could be  
365 uplifted from the seaward side if the concentrated wave load exceeds the local capacity. Local  
366 bearing damages may occur, and structural constraints may be weakened under this condition,  
367 threatening structural safety. Fig. 8 (c) indicates the moment when the wave crest has passed  
368 the deck. At the trailing edge of the solitary wave, the water surface drops rapidly, resulting in  
369 negative pressure beneath the deck (smaller than one atmosphere) as the blue region in Fig. 8  
370 (c). Meanwhile, the deck's upper surface is suffering downward pressure. Hence, there is a  
371 momentary downward force on the bridge deck after the uplift slamming as Fig. 5.



372

373 **Fig. 8** Wave-bridge interactions and pressure distributions of a typical case with  $D = 14.4$  m,

374

$$Z_c = 2.1 \text{ m, and } H = 4.2 \text{ m}$$

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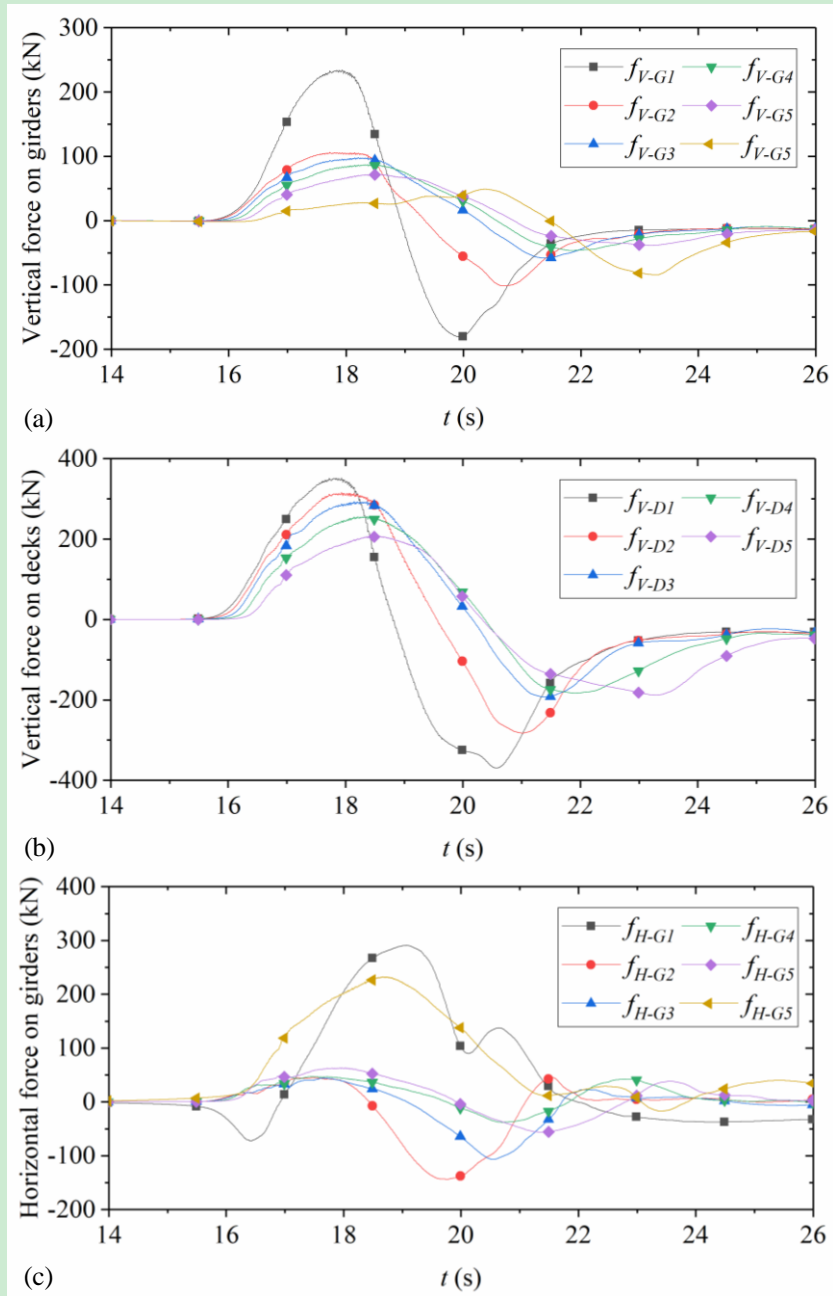
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Wave induced forces on different girder ( $f_{V-Gi}$  for vertical force and  $f_{H-Gi}$  for horizontal force) and deck ( $f_{V-Di}$  for vertical force and  $f_{H-Di}$ ; for horizontal force) sections (as shown in Fig. 4 (b)) are plotted in Fig. 9. Fig. 9 (a) shows that maximum values of vertical forces on girder 1 to girder 6 reduce in order.  $f_{V-G1}$  has an extremely large peak value at  $t = 18$  s, which is caused by the protruding part of the deck. Similarly, Deck section 1 has the largest vertical force  $f_{V-D1}$  at  $t = 18$  s as indicated in Fig. 9 (b), and the peak values of  $f_{V-D1} - f_{V-D5}$  decrease from seaward

381 to the landward side. Minimum values of  $f_{V-Di}$  occur at around 20 s, which are caused by the  
382 partial vacuum area between the deck and girders (as the blue region shown in Fig. 8 (c)).  
383 Horizontal forces on the girders are shown in Fig. 9 (c), where  $f_{H-G1}$  and  $f_{H-G6}$  have larger peak  
384 values than the other girders, which is also due to the protruding part of the deck. Horizontal  
385 wave forces on deck components  $f_{H-Di}$  are relatively small such that they are not plotted here.  
386 Figs. 8 and 9 reveal the uneven load distributions on the deck during the wave-bridge  
387 interaction and potential local structural damages prior to the whole structural damage. The  
388 obtained results will be used to predict the wave force extremum and imported into the FE  
389 model to investigate the limit state of the bridge in the following sections.



390

391 **Fig. 9** Time histories results of the case with  $D = 14.4$  m,  $Z_c = 2.1$  m, and  $H = 4.2$  m: (a)

392 vertical wave forces on 6 girder sections  $f_{V-Gi}$ ; (b) vertical wave forces on 5 deck sections  $f_{V-$

393  $D_i$ ; and (c) horizontal wave forces on 6 girder sections  $f_{H-Gi}$

### 394 3.3 Maximum wave force and overturning moment

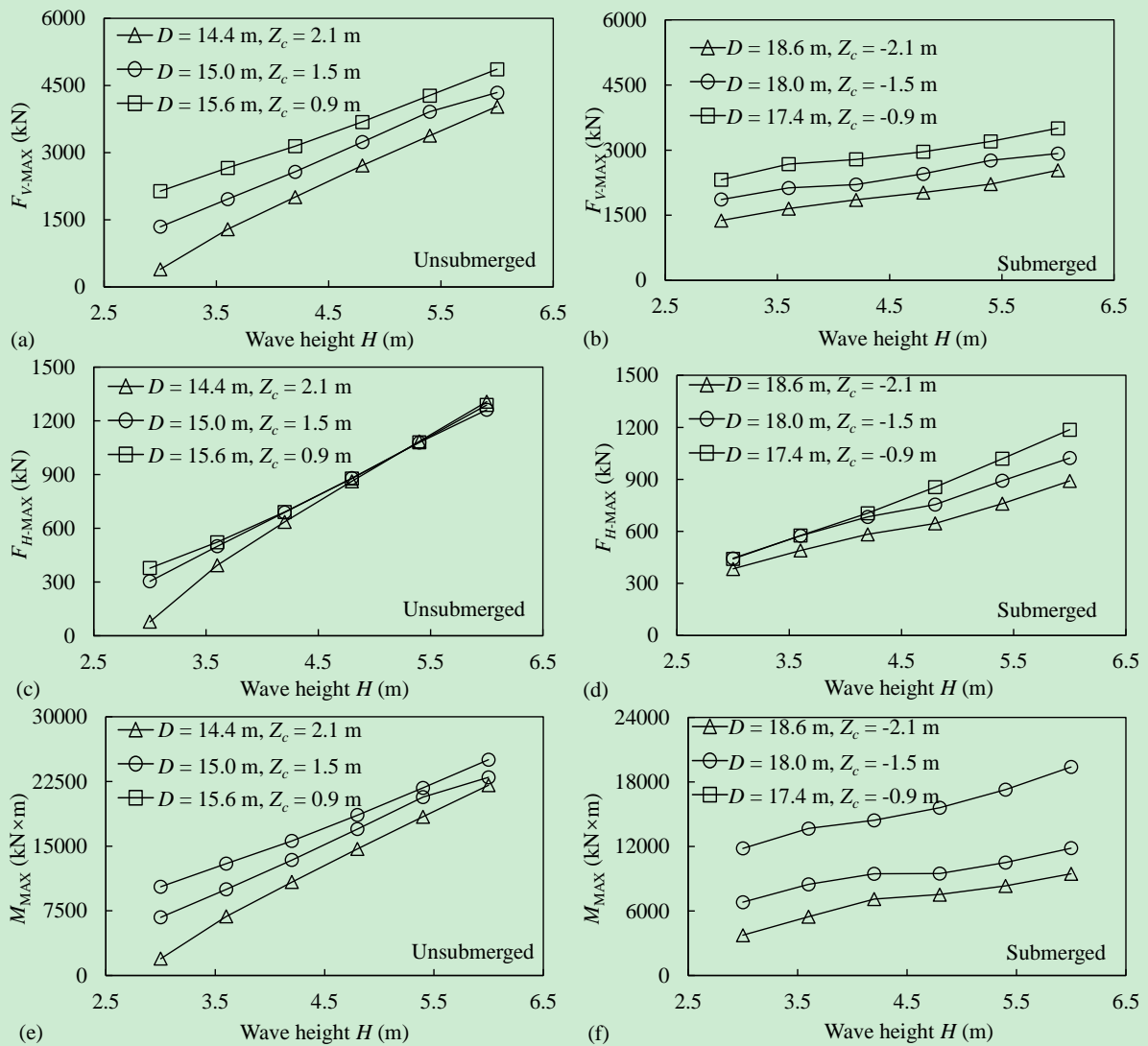
395 By tracking the time histories of wave-induced forces and overturning moments, the maximum

396 values of vertical force ( $F_{V-MAX}$ ), horizontal forces ( $F_{H-MAX}$ ), and overturning moments ( $M_{MAX}$ )

397 occur almost simultaneously. Representative results under different inundation and wave

398 conditions are presented in Fig. 10. For unsubmerged scenarios shown in Figs. 10 (a), (c), and

399 (e),  $F_{V-MAX}$ ,  $F_{H-MAX}$ , and  $M_{MAX}$  become larger as wave height  $H$  increases.  $F_{V-MAX}$  increases  
 400 with smaller clearance  $Z_c$ , while  $F_{H-MAX}$  remains nearly constant except for  $H = 3.0$  m. Figs. 10  
 401 (b), (d), and (f) show the results for submerged conditions. Different characteristics are  
 402 observed that  $F_{V-MAX}$  significantly reduces for larger inundation depth (smaller  $Z_c$ ) but changes  
 403 little with  $H$ . Both  $F_{V-MAX}$  and  $F_{H-MAX}$  have larger values as  $Z_c$  increases in submerged cases.  
 404  $M_{MAX}$  changes closely with  $F_{V-MAX}$ , which means the vertical wave force contributes more to  
 405 the overturning moment.



406  
 407 **Fig. 10** Maximum wave forces and overturning moments under different inundation and  
 408 wave conditions

409 **4. Prediction method of wave force extremum**

410 Based on the numerical results above, the prediction methods of wave force extremums are

411 achieved by modifying coefficients of the AASHTO estimation formulas (AASHTO 2008).  
412 The AASHTO methods are proposed based on the tests of periodic waves, so the characteristics  
413 of solitary waves need to be considered when quantifying solitary wave results. For instance,  
414 a soliton has an infinite wave period and wavelength theoretically. Although Goring's method  
415 (Goring 1978) is used to estimate the period and wavelength in the tests, the calculated results  
416 are still large as compared with those of periodic waves, especially for the long distance at the  
417 leading and trailing edges. Hence, this study modifies several parameters of this method to fit  
418 the solitary wave results. In AASHTO 2008, the maximum vertical and horizontal wave forces  
419 ( $F_{V-MAX}$  and  $F_{H-MAX}$ ) can be calculated as:

$$F_{V-MAX} = F_{VS} + F_s = \gamma_w \bar{W} \beta \left( -1.3 \frac{H}{D} + 1.8 \right) \left[ 1.35 + 0.35 \tanh(1.2T - 8.5) \right] \left( b_0 + b_1 x_v + \frac{b_2}{y_v} + b_3 x_v^2 + \frac{b_4}{y_v^2} + \frac{b_5 x_v}{y_v} + b_6 x_v^3 \right) (TAF) + A \gamma_w H^2 \left( \frac{H}{\lambda} \right)^B \quad (3)$$

$$\bar{W} = \left[ \lambda - \left( \frac{\lambda}{H} \right) \left( Z_c + \frac{H}{2} \right) \right] \quad (4)$$

$$x_v = \frac{H}{\lambda}, \text{ and } y_v = \frac{\bar{W}}{\lambda} \quad (5)$$

$$A = \begin{cases} 0.0149 \left( \frac{Z_c}{\eta_{\max}} \right) + 0.0316 & \text{if } \frac{Z_c}{\eta_{\max}} \geq 0 \\ \left[ -1562.9 + 1594.5 e^{-\left( \frac{Z_c}{\eta_{\max}} \right)} \right]^{-1} & \text{if } \frac{Z_c}{\eta_{\max}} < 0 \end{cases} \quad (6)$$

$$B = 0.6538 \left( \frac{Z_c}{\eta_{\max}} \right)^2 + 0.5368 \left( \frac{Z_c}{\eta_{\max}} \right) - 1.193 \quad (7)$$

$$F_{H-MAX} = \gamma_w H^2 \left[ a_0 + a_1 (x_h) + a_2 (x_h)^2 + a_3 (x_h)^3 + a_4 (x_h)^4 + a_5 (x_h)^5 + a_6 \ln(y_h) \right] \left[ a_7 + a_8 \left( \frac{W}{\lambda} \right) \right] \quad (8)$$

$$x_h = \left( \frac{\eta_{\max} - Z_c}{d_b + r} \right) \text{ and } y_h = \frac{H}{\lambda} \quad (9)$$

420 where  $\gamma_w$  = unit weight of water;  $TAF$  = the trapped air factor;  $r$  = rail height;  $d_b$  = the sum of

421 girder height and deck thickness;  $W$  = horizontal projection of overhang; and other coefficients  
 422 could be calculated from the guide specifications (AASHTO 2008).

#### 423 4.1 Maximum vertical force prediction

424 To account for the solitary wave characteristics and get an accurate prediction of  $F_{V-MAX}$ , the  
 425 authors examine and compare several methods, including taking the effective section of the  
 426 solitary wave, adjusting the wavelength and wave height parameters, and adopting the  
 427 correction coefficient. The coefficient of determination  $R^2$  and the root-mean-square error  
 428 RMSE are utilized to examine the goodness of the fitting results. After several calculations and  
 429 comparisons, concepts of effective period  $T_e$  and effective wavelength  $\lambda_e$  (as shown in Fig. 11  
 430 (a)) are proposed to help predict the maximum wave forces.  $T_e$  and  $\lambda_e$  are defined as the period  
 431 when the water surface elevation is larger than the effective wave height  $H_e$ . Such a method  
 432 could better describe the characteristics of the solitary wave crest since that is where the solitary  
 433 wave energy mostly concentrates (Longuet-Higgins 1974). The effective wave height  $H_e$  is  
 434 calculated from the wave height  $H$  and effective coefficient  $\varepsilon$  as indicated in Eq. 10, and the  
 435 relevant period and wavelength ( $T_e$  and  $\lambda_e$ ) can be further determined from the wave profiles  
 436 (Longuet-Higgins 1974).

$$H_e = \varepsilon H \quad (10)$$

437 Sensitivity analyses are performed to determine the value of  $\varepsilon$ , and the results are listed in  
 438 Table 3. By comparing  $R^2$  and RMSE values, it is identified that the best predicting  
 439 performance occurs when  $\varepsilon = 40\%$ , and the  $R^2$  and RMSE are 0.9607 and 359.16, respectively.  
 440 The corresponding  $T_e$  and  $\lambda_e$  can be calculated from the solitary wave profiles. Replacing  $T$   
 441 with  $T_e$  and  $\lambda$  with  $\lambda_e$  as Eqs. (11) - (13) could get more accurate  $F_{V-MAX}$  for solitary waves.

$$F_{V-MAX} = F_{VS} + F_s = \gamma_w \bar{W} \beta \left( -1.3 \frac{H}{D} + 1.8 \right) \left[ 1.35 + 0.35 \tanh(1.2T_e - 8.5) \right] \left( b_0 + b_1 x_v + \frac{b_2}{y_v} + b_3 x_v^2 + \frac{b_4}{y_v^2} + \frac{b_5 x_v}{y_v} + b_6 x_v^3 \right) (TAF) + A \gamma_w H^2 \left( \frac{H}{\lambda_e} \right)^B \quad (11)$$

$$\bar{W} = \left[ \lambda_e - \left( \frac{\lambda_e}{H} \right) \left( Z_c + \frac{H}{2} \right) \right] \quad (12)$$

$$x_v = \frac{H}{\lambda_e}, \text{ and } y_v = \frac{\bar{W}}{\lambda_e} \quad (13)$$

442

443

**Table 3** R<sup>2</sup> and RMSE values for different  $\varepsilon$  scenarios

$\varepsilon$	25%	30%	35%	<b>40%</b>	45%	50%	55%
R <sup>2</sup>	0.8084	0.8283	0.8977	<b>0.9607</b>	0.9405	0.8731	0.8246
RMSE	613.60	522.98	458.65	<b>359.16</b>	366.91	414.67	428.45

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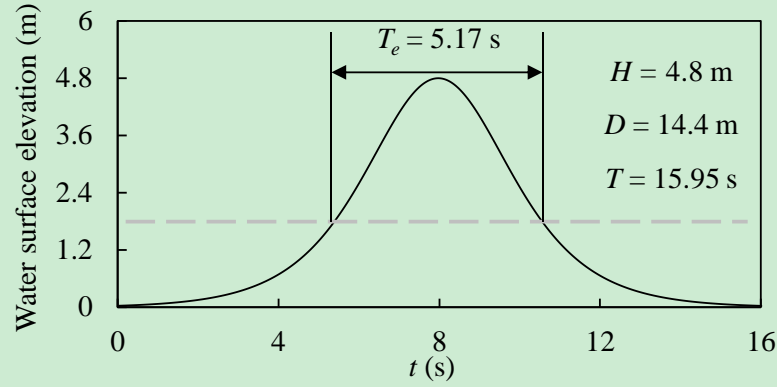
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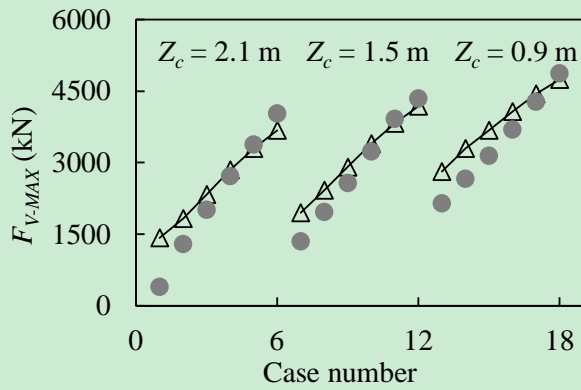
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An illustrative example of the case with  $D = 14.4$  m and  $H = 4.8$  m is presented in Fig. 11 (a). The period calculated from Goring's method equals 15.95 s, and apparently, the leading and trailing edges are very long but with small elevations. Taking  $T_e = 5.17$  s, which is about one-third of the original wave period, could better describe the characteristics of wave crest. Comparisons of the various cases under unsubmerged and submerged conditions are shown in Figs. 11 (b) and (c). The predicted values using the modified method match CFD simulated results well in both situations, which means the proposed prediction method has good performance in estimations of solitary wave forces.

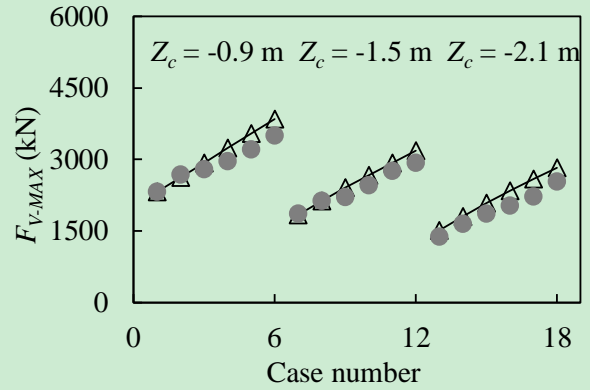




(a) Definition of effective wave period  $T_e$



(b) CFD simulated and predicted  $F_{V-MAX}$  under unsubmerged conditions



(c) CFD simulated and predicted  $F_{V-MAX}$  under submerged conditions

Note: 6 cases are selected for each clearance ( $Z_c$ ) with wave height  $H$  ranges from 3 m to 6 m.  $\triangle$  : CFD simulated results and  $\bullet$  : predicted results.

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#### 458 4.2 Maximum horizontal force prediction

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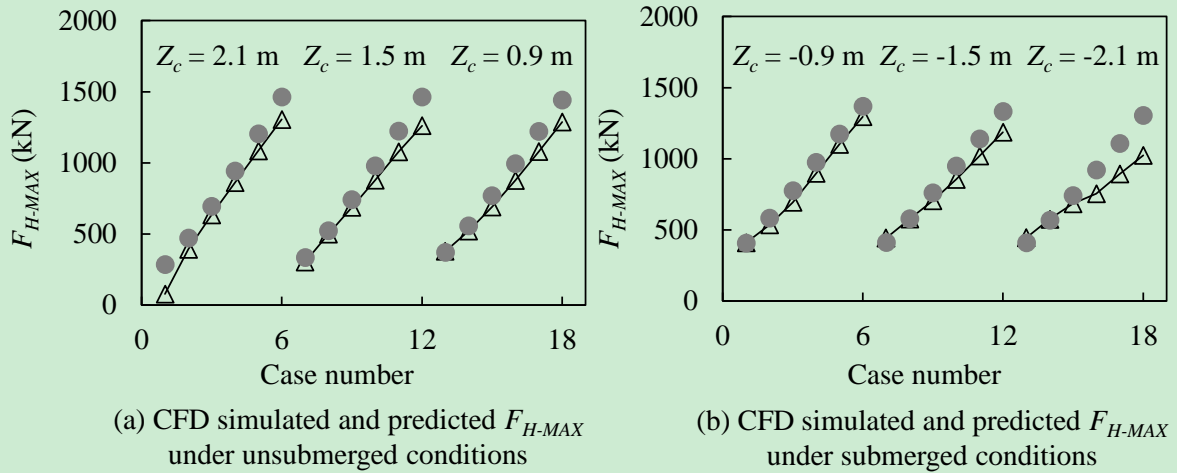
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464

In the previous method for periodic waves (AASHTO 2008), the horizontal wave force is calculated by fitting the periodic wave parameters as Eqs. (8) and (9). To better account for the characteristics of the solitary wave crest, the effective period  $T_e$  and effective wavelength  $\lambda_e$  are also adopted as Eq. (14). The coefficients  $x_h$  and  $y_h$  are refitted based on the computed horizontal wave forces using the nonlinear least-squares method (Johnson 2008) as  $a_1 = 0.26128$ ,  $a_2 = -0.07207$ ,  $a_3 = 0.00601$ , and  $a_4 = -0.47239$ . Comparisons of CFD simulated

465 results and predicted  $F_{H-MAX}$  under unsubmerged and submerged conditions are presented in  
 466 Fig. 12, and good agreements are observed.

$$F_{H-MAX} = \gamma_w H^2 \left[ a_1 (x_h) + a_2 (x_h)^2 + a_3 (x_h)^3 + a_4 (y_h) \right] \quad (14)$$



Note: 6 cases are selected for each clearance ( $Z_c$ ) with wave height  $H$  ranges from 3 m to 6 m.  $\triangle$  : CFD simulated results and  $\bullet$  : predicted results.

467

468 **Fig. 12** Comparisons of  $F_{H-MAX}$  under (a) unsubmerged conditions and (b) submerged

469

conditions

## 470 5. Structural limit states considering component failure

471 Using obtained wave force histories, structural responses under different wave scenarios are  
 472 calculated to evaluate the bearing performance and structural limit states. A component-level  
 473 damage evaluation method is formulated and discussed.

### 474 5.1 Dynamic structural responses

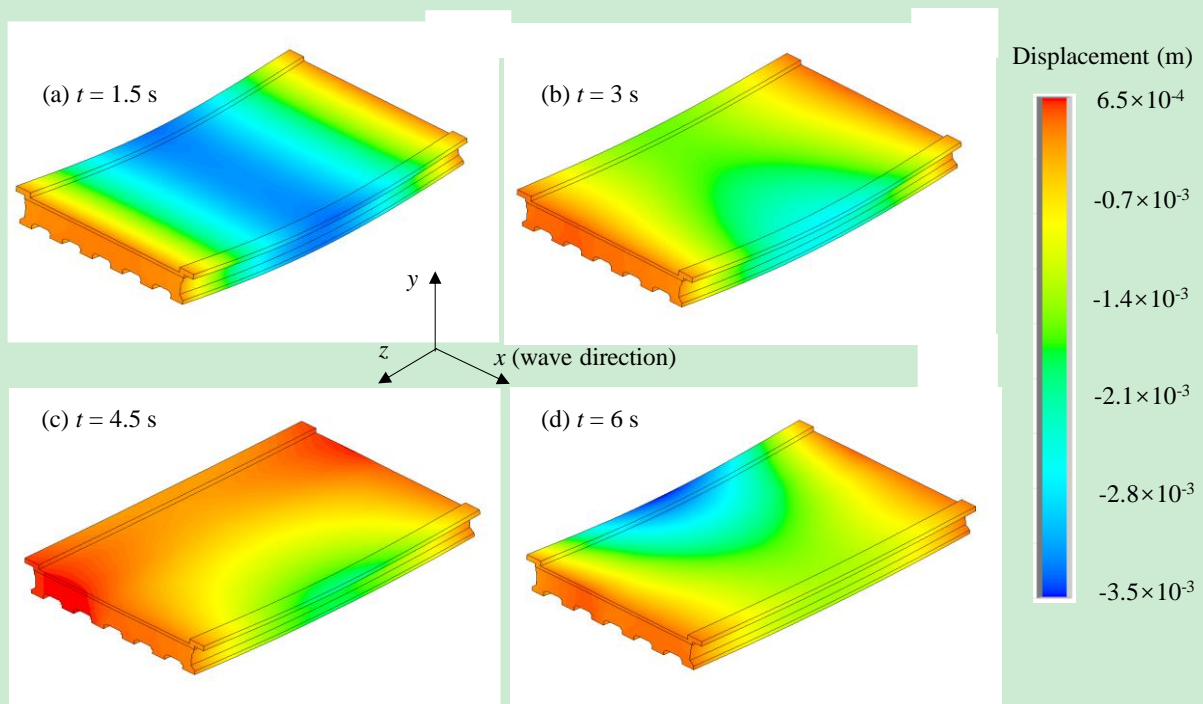
475 By collecting wave force histories on each component calculated from the CFD model and  
 476 applying them to the spatial FE model at corresponding positions of the bridge deck, the  
 477 displacement of the deck, bearing reaction forces, and bearing working states can be calculated.

478 A typical case with  $D = 15$  m,  $Z_c = 1.5$  m, and  $H = 4.2$  m is selected for illustration purposes.

479 The origin of time  $t$  is taken when the wave starts to interact with the bridge to save  
 480 computational time in the FE analysis (i.e., the period when the water surface rises but has not  
 481 reached the bridge is not considered). The displacement of the deck at representative moments

482 are presented in Fig. 13. The scale factor is 156.76. At the initial stage before the wave arrives

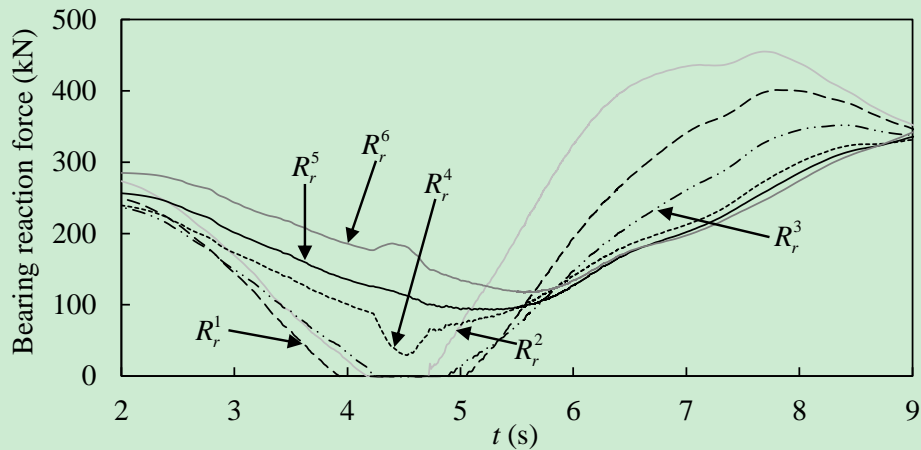
483 ( $t = 1.5$  s as shown in Fig. 13 (a)), the middle section of the deck sags naturally due to the  
 484 gravity, while the two ends are supported by the bearings. When the wave arrives at  $t = 3$  s, the  
 485 downward displacement is reduced by the vertical wave force. Fig. 13 (c) shows the moment  
 486 when the bridge is partially uplifted by the wave, and bearings L1 – L3 and R1 – R3 are  
 487 disengaged (damaged) at this stage. It is observed that the displacement and damage state of  
 488 each bearing is different under the wave impacts, and the local damaged bearings could  
 489 influence structural safety. Thus, it is necessary to perform structural analysis to explore the  
 490 bearing damage and the associated structural limit states.



491  
 492 **Fig. 13** Displacement of the deck at different moments for a typical case with  $D = 15$  m,  $Z_c =$   
 493  $1.5$  m, and  $H = 4.2$  m  
 494

495 Time histories of bearing reaction forces are shown in Fig. 14. The bearing reaction forces  
 496 on two ends of the deck (L and R ends) change similarly, so only the results on one end (R end)  
 497 are shown. In Fig. 14, positive values represent compressed (normal) bearing working states.  
 498 The “damage” of the bearings herein refers to the disengagement of the bearings caused by the  
 499 uplift wave impacts, which is often not allowed for the bridge safety (Caltrans 1994; Khaleghi  
 500 et al. 2019). During the wave-bridge interaction process, reaction forces of bearings R1, R2,

501 and R3 become zero (damaged) at about 4 s successively, since the huge wave comes from the  
 502 seaward side. Due to the concentrated wave load and extreme overturning moment, local  
 503 bearing constraints could be destroyed (i.e., reaction force becomes 0 and disengages). Such a  
 504 local component-level (bearing) damage could occur before the overall failure of the structure  
 505 (total wave force exceeds the sum of deck weight and connection strength). Hence,  
 506 identification of the limit states concerning the bearing damages and calculation of the  
 507 threshold value targeting the phenomenon is necessary.



508  
 509 **Fig. 14** Time histories of bearing reaction forces for a typical case with  $D = 15$  m,  $Z_c = 1.5$  m,  
 510 and  $H = 4.2$  m  
 511

512 5.2 Bridge limit state  $C_{Limit}$  considering component damage

513 By tracing the dynamic structural responses under wave forces, it is identified that the extreme  
 514 wave force and overturning moment can destroy seaward bearings and overturn the bridge deck.  
 515 Note that this research focuses on the limit state of overturning effect, that is the phase when  
 516 the structural (bearing) disengagement occurs, but the whole bridge has not been overturned  
 517 by the waves, and hence the overturning center of the bridge deck OTC is selected at the bottom  
 518 of the girder 6 based on the computational results (as Fig. 1). The force schematic diagram of  
 519 the bridge is also plotted in Fig. 1. The deck tends to be uplifted at the seaward side and rotate  
 520 around OTC. To address this issue, the novel limit state of a coastal bridge subjected to  
 521 overturning effects from the waves is formulated in this section.

522 To calculate the limit state preventing bearing damages, some definitions are clarified first

523 as follows. The total deck capacity against overturning effect  $C_M$  is mainly contributed by the  
 524 static weight of the main structure, bituminous concrete, guard rail, etc., and vertical constraints  
 525 from the connections between the bridge superstructure and substructure if existed. The anti-  
 526 overturning capacity from the static weight can be calculated as the product of the gravity and  
 527 the distance from the gravity center to OTC. Hence, the limit state  $C_{Limit}$  can be obtained as:

$$C_{Limit} = \xi C_M = \xi (mg \times 2.5L + C_c) \quad (15)$$

528 where  $\xi$  = the safety coefficient associated with overturning moment;  $L$  = the distance between  
 529 two neighboring bearings (see Fig. 1); and  $C_c$  = the capacity provided from connections, which  
 530 equals 0 since the constraints are assumed to provide no tension force in this study. Substituting  
 531  $\xi = 1$ ,  $m = 312.5 \times 10^3$  kg, and  $L = 1.73$  m,  $C_{Limit}$  is calculated as 13,704 kN×m. The value of  $\xi$   
 532 will be further discussed in the following content.

533 The bearing reaction forces reduce under the effects of horizontal/uplift wave forces, and  
 534 the residual resistance from the bearings  $R_M$  can be calculated by accumulating the product of  
 535 reaction forces and corresponding force arms of each bearing as:

$$R_M = \sum_{i=1}^6 (R_l^i(t) + R_r^i(t)) \times (i-1)L \quad (16)$$

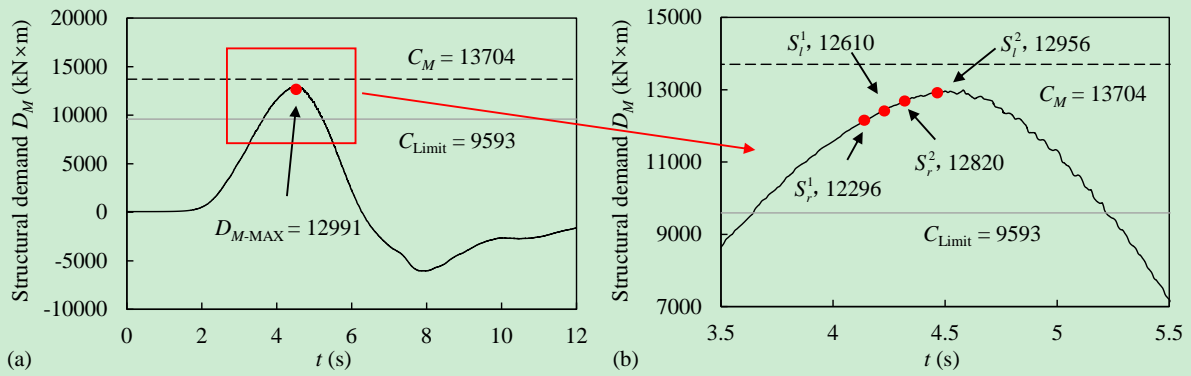
536 where  $R_l^i(t)$  and  $R_r^i(t)$  = structural reaction forces of the  $i$ th girder on the left and right ends of  
 537 the deck; and  $t$  = time. Similarly, positive values of  $R_l^i(t)$  and  $R_r^i(t)$  represent a compressed state  
 538 of the bearing. Thus, the structural demand associated with the overturning effect caused by  
 539 the waves  $D_M$  can be calculated as

$$D_M = C_M - R_M \quad (17)$$

540 It should be noted that the overturning-moment-associated structural demand  $D_M$  is  
 541 different from the overturning moment  $M$  calculated by accumulating the wave force  
 542 distributions on the superstructure. The latter one is a measurement of external excitation from  
 543 wave impacts, while the former one is the structural response which comprehensively considers  
 544 the effects of structural properties and bearing constraints. Most of the previous studies focused  
 545 on the investigations of  $M$  (AASHTO 2008; G. Xu et al. 2016; Zhao et al. 2020), and this paper  
 546 explores the influences of  $D_M$  for the first time.

547 Furthermore, when  $\zeta = 1$ , once the  $R_M$  becomes zero or  $D_M \geq C_M$ , it means all the bearings  
548 are disengaged and no longer provide any constraint, and the bridge could be washed away.  
549 However, a positive  $R_M$  cannot ensure a safe state for all the bearings, since uneven wave force  
550 distribution on the deck could damage several local bearings as discussed in section 5.1 (See  
551 Fig. 14). For instance, a typical time series of the structural demand  $D_M$  is plotted in Fig. 15. In  
552 this case, water depth  $D = 14.4$  m, clearance  $Z_c = 2.1$  m, and wave height  $H = 4.2$  m. As the  
553 wave uplift force increases,  $D_M$  gradually increases, reaching maximum value when  $t \approx 4.2$  s  
554 ( $D_{M-MAX} = 12991$  kN×m). Then, the uplift force reduces, and downward wave force occurs.  
555 Under the combined effects of horizontal/vertical wave forces and deck weight,  $D_M$  reduces to  
556 negative and reaches its minimum value at  $t = 8$  s. During this process, bearing disengagement  
557 occurs as shown in a detailed diagram Fig. 15 (b). As indicated, disengaged bearing ( $S^i_l$  and  $S^i_r$ )  
558 and corresponding damage states (time and demand) are marked by red points. Since the  
559 constraints in the  $z$  direction are only set at the R side of the bridge, the limit states of bearings  
560 at the two ends are slightly different (e.g.,  $S^2_l$  and  $S^2_r$ ; and  $S^3_l$  and  $S^3_r$ ). Although the structural  
561 demand  $D_M$  is always lower than  $C_M$ , the component-level damage (bearing) still occurs, which  
562 is dangerous for structural safety. Hence, it is necessary to reserve additional capacity to prevent  
563 component (bearing) damages, and the safety coefficient  $\zeta$  should be adopted to modify the  $C_M$   
564 to a threshold value (See Fig. 15).

565 Based on the numerical results in this study, a safety coefficient  $\zeta$  of 0.7 is suggested, and  
566 the limit state  $C_{Limit}$  is calculated as 9593 kN×m from Eq. (14) as plotted with a gray line in  
567 Fig. 15. Nevertheless, such a coefficient could be modified for specific cases given other  
568 structural conditions and climate and hydrological environments, and more relevant studies are  
569 required to examine the threshold value. For instance, a smaller value should be adopted in the  
570 design stage in hazard-prone areas to prevent structural damage. In addition, the value of  $C_{Limit}$   
571 also depends on  $C_M$ . Several methods could be utilized to enhance the overall capacity,  
572 including increasing the width and weight of the bridge span, using different types of bearings  
573 such as tension-compression bearings, and setting additional constraints between  
574 superstructure and substructure.



575

576 **Fig. 15** Time series of bearing resistant  $R_M$  and overturning limit state  $C_{Limit}$  for the case with

577  $D = 14.4$  m,  $Z_c = 2.1$  m, and  $H = 4.2$  m. Disengaged bearings and corresponding damage

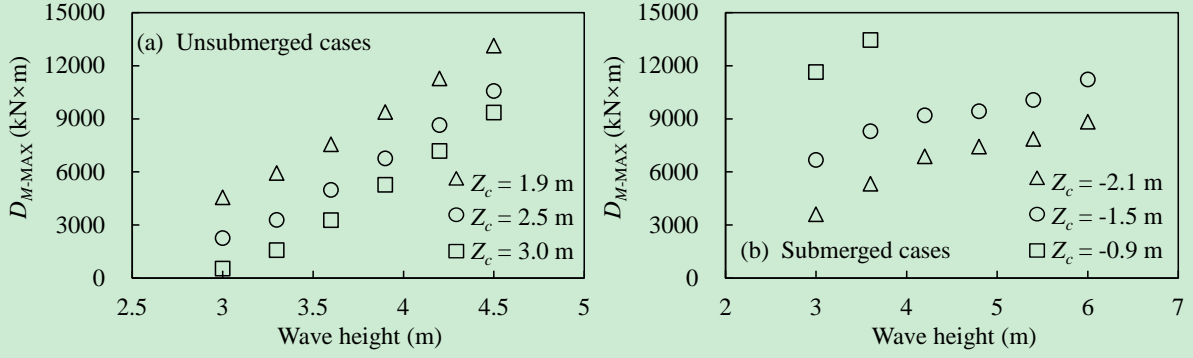
578 states are marked as by the red points

### 579 5.3 Discussion of the structural demand $D_M$

580  $D_M$  is the structural demand associated with the overturning moment under wave impacts. Once  
 581 it reaches the limit state  $C_{Limit}$ , the bridge structure and bearing connections are considered at  
 582 a high failure risk.  $D_M$  depends on both the structural characteristics and wave parameters. With  
 583 respect to the former one, it could be found that  $D_M$  is mainly influenced by the bearing  
 584 properties, including bearing reaction forces  $R_{l(t)}^i$  and  $R_{r(t)}^i$ , the number of bearings  $i$ , and the  
 585 distance between the neighboring bearings  $L$ . Hence, to get a smaller value of  $D_M$  under a  
 586 constant wave condition, the bridge should be designed with more bearing constraints and the  
 587 types and strengths of the bearings should be considered.

588 To illustrate the effects of wave parameters on the value of  $D_M$ , the maximum structural  
 589 demand  $D_{M-MAX}$  for the investigated bridge model under the different wave and submergence  
 590 conditions are plotted in Fig. 16. In unsubmerged cases,  $D_{M-MAX}$  increases linearly with the  
 591 increase of wave height  $H$  as indicated in Fig. 16 (a). Also, a larger clearance  $Z_c$  could lead to  
 592 a smaller  $D_{M-MAX}$  under the same wave height  $H$ . The wave height  $H$  tested under submerged  
 593 conditions, as shown in Fig. 16 (b), is different from those under unsubmerged conditions to  
 594 meet the requirement of the  $H/D$  ratio. With respect to the  $Z_c = -0.9$  m scenario, the maximum  
 595  $D_{M-MAX}$  exceeds  $C_M$  when  $H > 3.5$  m because of the extreme wave impact and is not plotted in  
 596 Fig. 16 (b). Generally,  $D_{M-MAX}$  increases with both wave height  $H$  and clearance  $Z_c$ , showing  
 597 different characteristics from submerged conditions.





598

599 **Fig. 16** Maximum structural demand  $D_{M-MAX}$  under (a) unsubmerged and (b) submerged

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cases

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To facilitate the following research and comparisons, the correlations between  $D_{M-MAX}$  and wave parameters are quantified for different submergence scenarios based on the numerical results. After several calculations and comparisons, a second-order polynomial surface model is fitted as

$$D_{M-MAX} = \alpha_{00} + \alpha_{10}H + \alpha_{01}Z_c + \alpha_{20}H^2 + \alpha_{11}HZ_c + \alpha_{02}Z_c^2 \quad (18)$$

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where  $\alpha_{ij}$  = fitting coefficients. The fitting results and coefficients are listed in Table 3. The root-mean-square error (RMSE) and goodness of fit ( $R^2$ ) are adopted to examine the fitting model, and a relatively small RMSE and an  $R^2$  close to 1 prove the convergence of the fitting model (Segura et al. 2019).

**Table 3** Fitting coefficients for  $R_{M-MIN}$

	RMSE	$R^2$	$\alpha_{00}$	$\alpha_{10}$	$\alpha_{01}$	$\alpha_{20}$	$\alpha_{11}$	$\alpha_{02}$
Unsubmerged	312.3	0.983	6438	1211	-7242	573.3	166.8	560.2
Submerged	382.7	0.971	15880	3914	18210	-334.4	-332.7	3490

## 610 6. Conclusions

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This study conducts an in-depth investigation on the wave-bridge interaction, wave force prediction method, and the limit states considering bearing damages based on structural responses. Laboratory experiments are conducted as a validation method. The time histories of wave-induced force are measured in the laboratory test, which helps to improve and validate the CFD model. 3D dynamic numerical analyses are performed based on the validated CFD



616 and FE models. A novel limit state based on component failures is proposed for coastal bridges  
617 subjected to extreme wave forces.

618 In the light of the results of the numerical and experimental studies on the wave-bridge  
619 interaction, it is observed that the extreme wave could induce huge loads concentrated on the  
620 seaward side of the bridge. The uneven load distribution on the bridge superstructure leads to  
621 a large overturning moment and tends to lift the bridge from one side. The overturning center  
622 of the bridge deck OTC is found at the bottom of the landward girder based on the  
623 computational results.

624 By tracing the wave force time series in different cases, the maximum wave-induced  
625 forces on the bridge deck are identified and extreme wave force prediction methods are  
626 quantified. It is found that maximum wave forces show different characteristics under  
627 unsubmerged and submerged conditions. In unsubmerged cases,  $F_{V-MAX}$ ,  $F_{H-MAX}$ , and  $M_{MAX}$   
628 become larger as wave height  $H$  increases;  $F_{V-MAX}$  increases with smaller clearance  $Z_c$ ; while  
629  $F_{H-MAX}$  remains nearly constant with a change in  $Z_c$ . For submerged conditions,  $F_{V-MAX}$   
630 significantly reduces for larger inundation depth (larger  $D$ ) but changes little with  $H$ ;  $F_{H-MAX}$   
631 decreases with larger  $D$ ;  $M_{MAX}$  shows similar trends with  $F_{V-MAX}$ . To quantify the maximum  
632 wave force, a concept of effective wave period and wavelength ( $T_e$  and  $\lambda_e$ ) is proposed based  
633 on the wave characteristics and estimation formulas are modified accordingly. It is  
634 demonstrated that the wave force prediction methods can estimate accurate results for most of  
635 the cases.

636 Based on the numerical results, it is concluded that a local component-level (bearing)  
637 damage could occur before the overall failure of the structure (total wave force exceeds the  
638 sum of deck weight and connection strength). Hence, identification of the limit state  
639 incorporating bearing damages and calculation of the threshold value targeting the  
640 phenomenon is of vital importance.

641 The local bearings could be uplifted under the uneven wave load before the overall wave  
642 force exceeding deck weight, which may affect the structural safety. Thus, a safety coefficient  
643  $\xi$  is presented to modify the total structural capacity  $C_M$  to calculate the new limit state  $C_{Limit}$ ,

644 which could reserve enough capacity to prevent structural failure and bearing damages. A  
645 safety coefficient of 0.7 is suggested based on the investigations in this study and could be  
646 modified for specific cases given other structural conditions and climate and hydrological  
647 environments.

648 Furthermore, based on the discussion on the structural demand  $D_M$  under various wave  
649 parameter scenarios, it is concluded that to improve the structural resistance against the  
650 overturning effects, that is to increase the capacity  $C_M$  and to decrease the demand  $D_M$ , and  
651 additional connections against tensile force should be settled for coastal bridges.

652 In future studies, more investigations are encouraged to quantify the effects of trapped air  
653 on the wave impacts and perform sensitivity analyses on the uncertainties in multiple physical  
654 parameters. Besides, it is necessary to further explore the effects of bridge substructures (e.g.,  
655 piers and abutments) and different bridge types, so that the results could be generalized to a  
656 range of conditions.

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## 662 **References**

- 663 AASHTO. (2008). *Guide specifications for bridges vulnerable to coastal storms*.
- 664 AASHTO. (2017). AASHTO LRFD bridge design specifications. *Washington: American*  
665 *Association of State Highway and Transportation Officials*.
- 666 ACI Committee 318. (2014). Building Code Requirements for Structural Concrete. *American*  
667 *Concrete Institute*, 524.
- 668 ANSYS. (2018). *ANSYS User Manual*. ANSYS INC.
- 669 Ataei, N. (2013). *Vulnerability assessment of coastal bridges subjected to hurricane events*.
- 670 Ataei, N., & Padgett, J. E. (2015). Influential fluid–structure interaction modelling parameters  
671 on the response of bridges vulnerable to coastal storms. *Structure and Infrastructure*

672           *Engineering*, 11(3), 321–333.

673 Azadbakht, M., & Yim, S. C. (2016). Effect of trapped air on wave forces on coastal bridge  
674           superstructures. *Journal of Ocean Engineering and Marine Energy*, 2(2), 139–158.

675 Bradner, C., Schumacher, T., Cox, D., & Higgins, C. (2011). Experimental setup for a large-  
676           scale bridge superstructure model subjected to waves. *Journal of Waterway, Port, Coastal  
677           and Ocean Engineering*, 137(1), 3–11.

678 Bricker, J. D., & Nakayama, A. (2014). Contribution of trapped air, deck superelevation, and  
679           nearby structures to bridge deck failure during a tsunami. *Journal of Hydraulic  
680           Engineering*, 140(5), 05014002.

681 Briggs, M. J. (2013). *Basics of physical modeling in coastal and hydraulic engineering*. Coastal  
682           and Hydraulics Lab, Engineering Research and Development Center, Vicksburg, MS.

683 Cai, Y., Agrawal, A., Qu, K., & Tang, H. S. (2018). Numerical Investigation of Connection  
684           Forces of a Coastal Bridge Deck Impacted by Solitary Waves. *Journal of Bridge  
685           Engineering*, 23(1), 04017108.

686 Caltrans. (1994). *Bridge memo to designers. Section 7: Bridge Bearings*. California  
687           Department of Transportation Sacramento, CA.

688 Chakrabarti, S. K. (2005). Physical Modelling of Offshore Structures. In *Handbook of Offshore  
689           Engineering* (1001–1054).

690 Chen, Q., L. Wang, and H. Zhao. 2009. “Hydrodynamic Investigation of Coastal Bridge  
691           Collapse During Hurricane Katrina.” *Journal of Hydraulic Engineering*, 135(3), 175–186.

692 Cheng, Z., Gao, Z., & Moan, T. (2018a). Hydrodynamic load modeling and analysis of a  
693           floating bridge in homogeneous wave conditions. *Marine Structures*, 59, 122–141.

694 Cheng, Z., Gao, Z., & Moan, T. (2018b). Wave load effect analysis of a floating bridge in a  
695           fjord considering inhomogeneous wave conditions. *Engineering Structures*, 163, 197–214.

696 Cuomo, G., Shimosako, K. I., & Takahashi, S. (2009). Wave-in-deck loads on coastal bridges  
697           and the role of air. *Coastal Engineering*, 56(8), 793-809.

698 Ding, Y., Ma, R., Shi, Y. D., & Li, Z. X. (2018). Underwater shaking table tests on bridge pier  
699           under combined earthquake and wave-current action. *Marine Structures*, 58, 301–320.

700 Douglass, S. L., Hughes, S. a, Rogers, S., & Chen, Q. (2004). The Impact of Hurricane Ivan  
701 on the Coastal Roads of Florida and Alabama: A Preliminary Report. *Rep. to Coastal*  
702 *Transportation Engineering Research and Education Center, Univ. of South Alabama,*  
703 *Mobile, Ala, 1–19.*

704 Fang, Q., Hong, R., Guo, A., & Li, H. (2019). Experimental Investigation of Wave Forces on  
705 Coastal Bridge Decks Subjected to Oblique Wave Attack. *Journal of Bridge Engineering,*  
706 *24(4), 1–10.*

707 Gao, Z., Efthymiou, M., Cheng, L., Zhou, T., Minguéz, M., & Zhao, W. (2020). Hydrodynamic  
708 damping of a circular cylinder at low KC: experiments and an associated model. *Marine*  
709 *Structures, 72, 102777.*

710 Gao, Z., Efthymiou, M., Cheng, L., Zhou, T., Minguéz, M., & Zhao, W. (2021). Towards a  
711 model of hydrodynamic damping for a circular cylinder with helical strakes at low KC.  
712 *Marine Structures, 78, 103025.*

713 Goring, D. G. (1978). Tsunamis - the Propagation of Long Waves Onto a Shelf. *Calif Inst*  
714 *Technol WM Keck Lab Hydraul Water Resour Rep KH-R, 38.*

715 Guo, A., Fang, Q., Bai, X., & Li, H. (2015). Hydrodynamic Experiment of the Wave Force  
716 Acting on the Superstructures of Coastal Bridges. *Journal of Bridge Engineering, 20(12),*  
717 *1–11.*

718 Hayatdavoodi, M., & Ertekin, R. C. (2015). Wave forces on a submerged horizontal plate-Part  
719 II: Solitary and cnoidal waves. *Journal of Fluids and Structures, 54, 580–596.*

720 Hayatdavoodi, M., Seiffert, B., & Ertekin, R. C. (2014). Experiments and computations of  
721 solitary-wave forces on a coastal-bridge deck. Part II: Deck with girders. *Coastal*  
722 *Engineering, 88, 210–228.*

723 Hirt, C. W., & Nichols, B. D. (1981). Volume of fluid (VOF) method for the dynamics of free  
724 boundaries. *Journal of Computational Physics, 39(1), 201–225.*

725 Johnson, M. L. (2008). Nonlinear least-squares fitting methods. *Methods in cell biology, 84,*  
726 *781-805.*

727 Khaleghi, B., Warren, L., Fu, Z., Zeldenrust, R., Kestory, E., Stanton, J. F., Mongi, A. N.,

728 Walsh, J., Nix, R., & others. (2019). *Experiences in the Performance of Bridge Bearings*  
729 *and Expansion Joints Used for Highway Bridges.*

730 Knutson, T. R., McBride, J. L., Chan, J., Emanuel, K., Holland, G., Landsea, C., Held, I.,  
731 Kossin, J. P., Srivastava, A. K., & Sugi, M. (2010). Tropical cyclones and climate change.  
732 *Nature Geoscience*, 3(3), 157–163.

733 Kulicki, J. M. (2010). Development of the AASHTO guide specifications for bridges  
734 vulnerable to coastal storms. *Bridge Maintenance, Safety, Management and Life-Cycle*  
735 *Optimization - Proceedings of the 5th International Conference on Bridge Maintenance,*  
736 *Safety and Management*, 2844–2851.

737 Li, Y., Dong, Y., & Zhu, D. (2020). Copula-Based Vulnerability Analysis of Civil  
738 Infrastructure Subjected to Hurricanes. *Frontiers in Built Environment*, 6, 170.

739 Longuet-Higgins, M. S. (1974). On the mass, momentum, energy, and circulation of a solitary  
740 wave. *Proceedings of the Royal Society of London. A. Mathematical and Physical*  
741 *Sciences*, 337(1608), 1-13.

742 Miles, J. W. (1981). The Korteweg-de Vries equation: A historical essay. *Journal of Fluid*  
743 *Mechanics*, 106(2), 131–147.

744 Morison, J. R., Johnson, J. W., & Schaaf, S. A. (1950). The force exerted by surface waves on  
745 piles. *Journal of Petroleum Technology*, 2(05), 149-154.

746 Padgett, J., Desroches, R., Nielson, B., Yashinsky, M., Kwon, O. S., Burdette, N., & Tavera,  
747 E. (2008). Bridge damage and repair costs from Hurricane Katrina. *Journal of Bridge*  
748 *Engineering*, 13(1), 6–14.

749 Padgett, J. E., Spiller, A., & Arnold, C. (2012). Statistical analysis of coastal bridge  
750 vulnerability based on empirical evidence from Hurricane Katrina. *Structure and*  
751 *Infrastructure Engineering*, 8(6), 595–605.

752 Robertson, I. N., Riggs, R. H., Yim, S. C. S., & Young, Y. L. (2007). Lessons from Hurricane  
753 Katrina storm surge on bridges and buildings. *Journal of Waterway, Port, Coastal and*  
754 *Ocean Engineering*, 133(6), 463–483.

755 Robertsson, J. O. A., & Blanch, J. O. (2020). *Numerical Methods, Finite Difference* (pp. 1–9).

756 Saeidpour, A., Chorzepa, M. G., Christian, J., & Durham, S. (2018). Parameterized fragility  
757 assessment of bridges subjected to hurricane events using metamodels and multiple  
758 environmental parameters. *Journal of Infrastructure Systems*, 24(4).

759 Salem, H., Mohssen, S., Kosa, K., & Hosoda, A. (2014). Collapse analysis of Utatsu Ohashi  
760 bridge damaged by Tohoku Tsunami using applied element method. *Journal of Advanced*  
761 *Concrete Technology*, 12(10), 388–402.

762 Salem, H., Mohssen, S., Nishikiori, Y., & Hosoda, A. (2016). Numerical Collapse Analysis of  
763 Tsuyagawa Bridge Damaged by Tohoku Tsunami. *Journal of Performance of*  
764 *Constructed Facilities*, 30(6), 04016065.

765 Sarpkaya, T., & Isaacson, M. (1981). *Mechanics of wave forces on offshore structures*.

766 Segura, R. L., Padgett, J. E., & Paultre, P. (2019). Polynomial Response Surface-Based Seismic  
767 Fragility Assessment of Concrete Gravity Dams. *12th Canadian Conference on*  
768 *Earthquake Engineering*, June, 1–8.

769 Seiffert, B. R. (2014). *Tsunami and storm wave impacts on coastal bridges*. University of  
770 Hawai'i at Manoa

771 Seiffert, B., Hayatdavoodi, M., & Ertekin, R. C. (2014). Experiments and computations of  
772 solitary-wave forces on a coastal-bridge deck. Part I: Flat plate. *Coastal Engineering*, 88,  
773 194–209.

774 Seiffert, B. R., Hayatdavoodi, M., & Ertekin, R. C. (2015). Experiments and calculations of  
775 cnoidal wave loads on a coastal-bridge deck with girders. *European Journal of*  
776 *Mechanics-B/Fluids*, 52, 191–205.

777 Suppasri, A., Shuto, N., Imamura, F., Koshimura, S., Mas, E., & Yalciner, A. C. (2013).  
778 Lessons Learned from the 2011 Great East Japan Tsunami: Performance of Tsunami  
779 Countermeasures, Coastal Buildings, and Tsunami Evacuation in Japan. *Pure and Applied*  
780 *Geophysics*, 170(6–8), 993–1018.

781 Unjoh, S., & Endoh, K. (2006). Damage investigation and the preliminary analyses of bridge  
782 damage caused by the 2004 Indian Ocean tsunami. *Proceedings of the 38th UJNR Joint*  
783 *Panel Meeting*, 38, 267.

- 784 Xu, G. (2020). Discussion of “numerical Investigation of Connection Forces of a Coastal  
785 Bridge Deck Impacted by Solitary Waves” by Yalong Cai, A. Agrawal, Ke Qu, and H. S.  
786 Tang. *Journal of Bridge Engineering*, 25(1), 1–2.
- 787 Wei, Z., & Dalrymple, R. A. (2016). Numerical study on mitigating tsunami force on bridges  
788 by an SPH model. *Journal of Ocean Engineering and Marine Energy*, 2(3), 365-380.
- 789 Xu, G., Cai, C., & Deng, L. (2017). Numerical prediction of solitary wave forces on a typical  
790 coastal bridge deck with girders. *Structure and Infrastructure Engineering*, 13(2), 254–  
791 272.
- 792 Xu, G., & Cai, C. S. (2015). Wave forces on Biloxi Bay Bridge decks with inclinations under  
793 solitary waves. *Journal of Performance of Constructed Facilities*, 29(6), 4014150.
- 794 Xu, G., Cai, C. S., Hu, P., & Dong, Z. (2016). Component Level–Based Assessment of the  
795 Solitary Wave Forces on a Typical Coastal Bridge Deck and the Countermeasure of Air  
796 Venting Holes. *Practice Periodical on Structural Design and Construction*, 21(4),  
797 04016012.
- 798 Xu, Y., Øiseth, O., & Moan, T. (2018). Time domain simulations of wind- and wave-induced  
799 load effects on a three-span suspension bridge with two floating pylons. *Marine Structures*,  
800 58, 434–452.
- 801 Yeh, H., Liu, P., Briggs, M., & Synolakis, C. (1994). Propagation and amplification of tsunamis  
802 at coastal boundaries. *Nature*, 372(6504), 353–355.
- 803 Zhao, E., Sun, J., Tang, Y., Mu, L., & Jiang, H. (2020). Numerical investigation of tsunami  
804 wave impacts on different coastal bridge decks using immersed boundary method. *Ocean*  
805 *Engineering*, 201.
- 806 Zhu, D., & Dong, Y. (2020). Experimental and 3D numerical investigation of solitary wave  
807 forces on coastal bridges. *Ocean Engineering*, 209, 107499.
- 808 Zhu, D., Li, Y., & Dong, Y. (2021). Reliability-based retrofit assessment of coastal bridges  
809 subjected to wave forces using 3D CFD simulation and metamodeling. *Civil Engineering*  
810 *and Environmental Systems*, 38(1), 59–83.
- 811 Zhu, D., Yuan, P., & Dong, Y. (2021). Probabilistic performance of coastal bridges under



812 hurricane waves using experimental and 3D numerical investigations. *Engineering*  
813 *Structures*, 242, 112493.  
814