

1 Route and speed optimization for liner ships under emission control policies

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5 Abstract

Pollutants such as nitrogen oxides (NO_x), sulfur dioxide (SO₂), and particulate matters (PM) generated by shipping industry are increasing in recent years. In order to control the ship emission pollution, the International Maritime Organization (IMO) has established the Emission Control Areas (ECAs). In the fierce competition of the shipping market, liner shipping companies are looking for strategies to maintain their core competencies under the emission control policy. To achieve this goal, this paper first proposes a bi-objective mixed integer linear programming model, aiming to optimize sailing routes and speeds within and outside the ECA while minimizing the total fuel cost and SO₂ emissions. Then, a new algorithm is developed to solve the proposed model by combining the two-stage iterative algorithm and fuzzy logic method based on ϵ -constraint. Finally, this paper compares and analyzes the navigation plan of a real sailing route considering and not considering the effects of ECA. Some experiments are conducted to analyze the effects of fuel cost, decision makers, and ECA boundaries on the total fuel cost and SO₂ emissions. The results indicate that the proposed model and algorithm can contribute to save fuel cost and reduce SO₂ emissions under the ECA policy and provide different Pareto optimal solutions. Thus, the effectiveness of the model and the efficiency of the algorithm are validated.

6 *Keywords:* Emission Control Area (ECA), Bi-objective programming, Two-stage iterative
7 algorithm, Route optimization, Sailing speed optimization.

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8 1. Introduction

9 Shipping industry is an integral part of the global supply chain for global trade. Nearly 80%
10 of the trade is carried out by sea, among which liner shipping transportation plays an important
11 role. Recently, the impact of emission pollution on the environment caused by this low-cost trans-
12 portation has received widespread attention. Research shows that emissions from the shipping
13 industry are closely related to the fuel consumption, and the total fuel consumption is estimated to
14 be between 279 million and 400 million tons per year (Cullinane and Bergqvist, 2014). Container
15 liners emit large amounts of sulfur dioxide (SO_2), nitrogen oxides (NO_x), carbon dioxide (CO_2),
16 and particulate matters (PM) in shipping process which seriously violate the concept of “green
17 shipping”.

18 Protecting the ecological environment is the prerequisite for long-term and sustainable use of
19 resources. In order to reduce the serious environmental pollution brought about by the emissions of
20 SO_2 , NO_x , PM, and other pollutants, the International Maritime Organization (IMO) introduced
21 the concept of Emission Control Area (ECA) in Annex VI of the International Convention for the
22 Prevention of Pollution from Ships (MARPOL). The ECA includes the Baltic Sea area, the North
23 Sea area, the North America area, and the United States Caribbean Sea area. Only fuel with no
24 more than 0.1% of sulfur content can be used by ships within the ECAs since January 1, 2015
25 according to the regulations of IMO. Meanwhile, outside the ECA, only fuel with no more than
26 3.5% of sulfur content can be used.

27 In order to improve China’s maritime environment, according to the national regulations and
28 the international conventions, China has also promulgated related rules in 2015 and established the
29 Domestic Emission Control Area (DECA) in three port areas, including Pearl River Delta, Yangtze
30 River Delta and Bohai Rim (Beijing, Tianjin, Hebei). In December 2018, China further developed
31 the related regulations to extend the ECA along the shoreline which has been implemented since
32 January 1, 2019, as illustrated in Fig. 1. Since then, the ships within the DECA are required to
33 use marine fuel with sulfur content no more than 0.5%.

34 Three emission reduction methods are widely used to meet the ECA sulfur standards (Fagerholt
35 et al., 2015). (1) The first method is to use liquefied natural gas (LNG). LNG is one type of clean
36 fuels with low sulfur contained and can fundamentally reduce SO_2 emissions. The drawback is the

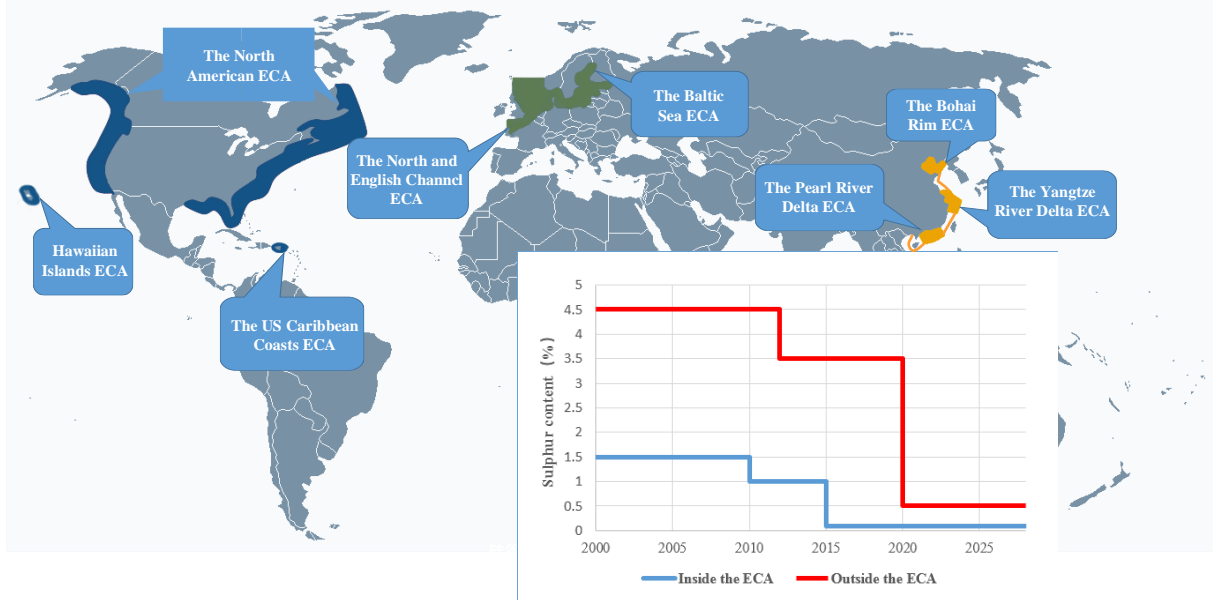


Figure 1: Emission Control Areas and the emission limits

37 high ship investment for storing and combusting the LNG on ships. In addition, it needs to be
 38 guaranteed that there are enough LNG supply facilities to provide the fuel for ships. (2) Installing
 39 the exhaust emission scrubber devices to filter the sulfur content in the exhaust gas is also an
 40 effective method. This method is mainly adopted by short-range offshore operators. For example,
 41 a shipping company called DFDS Seaways has begun a large-scale scrubber device installation
 42 plan, among which the costs for 21 ships reach 125 million dollars. As a result, the high cost for
 43 installing scrubber devices seriously confines their usage. (3) The third method is fuel switching,
 44 i.e., using fuel with a lower percentage of sulfur (e.g., marine gas oil (MGO)) within the ECA
 45 while using heavy fuel oil (HFO) outside the ECA, which is the most easily operated and widely
 46 used method under the condition of “green shipping”. In this paper, we will focus on the route
 47 and speed optimization to minimize the total fuel cost and SO_2 emissions when adopting the fuel
 48 switching method. Referring to some existing literature (Browning et al., 2012; Fagerholt et al.,
 49 2015; Gu and Wallace, 2017; Zhen et al., 2018), we assume that switching fuel is an instantaneous
 50 process in our paper for simplification.

51 The remainder of the paper is organized as follows. In section 2, we review the related literature.
 52 In section 3, we describe the problem and data used in this paper. In section 4, we introduce the
 53 mathematical model and the algorithm. Section 5 provides the results of the numerical experiment

54 and discusses the experiment results. Concluding remarks are presented in the last section.

55 **2. Literature review**

56 With the fast development of the maritime industry, liner shipping has been widely studied and
57 discussed. Meng and Wang (2012) put forward problems about liner ship planning under uncertain
58 container transportation demand. Song and Dong (2012, 2013) studied issues related to container
59 liner transportation. Bell et al. (2013) proposed a cost-based container allocation model for sea
60 freight to minimize the total operating costs. Based on this study, Ng (2014, 2015) further studied
61 the problems of the deployment of liner transport in a stochastic environment. Wang et al. (2015)
62 analyzed the management of seasonal transportation revenue of the container companies. Song et
63 al. (2015) constructed a cost optimization model to determine the number of ships, the maximum
64 planned speed of navigation and the liner service schedule. Ng (2018) proposed a new approach
65 to make a trade-off between ship sailing speed and the number of vessels required to maintain a
66 given service frequency. Kisialiou et al. (2018, 2019) designed metaheuristic algorithms to analyze
67 a tactical supply vessel planning problem. For the recent review on ship sailing speed optimization,
68 readers are referred to Meng et al. (2014) and Wang and Meng (2017). As mentioned above, several
69 practical optimization tools have been proposed.

70 There is also extensive literature focusing on reducing the emissions of SO_2 to improve the
71 maritime environment by considering the three emission reduction methods mentioned above, i.e.,
72 using liquefied natural gas, installing the exhaust emission scrubber devices, and switching fuel
73 by using MGO. Acciaro (2014) indicated that there was a balance between low fuel prices and
74 LNG investment spending, and the development of LNG mainly depended on its future price,
75 LNG ships capital cost and LNG engine's retrofitting cost. Jiang et al. (2014) made comparisons
76 between scrubber devices installation and fuel switching and concluded that the final choice of
77 the two approaches depended on the price gap between MGO and HFO. Boscaratoa et al. (2015)
78 claimed that the development of a scrubber system for sea transport was still not mature enough
79 as it was unable to process all pollutants produced by marine engines. Meanwhile, Hilmola (2015)
80 reported that scrubber systems had not been widely used yet. The shipping companies were unable
81 to complete the research for scrubbers and put them into use due to the insufficient time. The
82 above two papers discussed some typical problems about the applications of the scrubber system

83 in maritime transportation. Panasiu and Turkina (2015) analyzed the investment efficiency of
84 scrubber device installation and calculated and evaluated the cost throughout the life cycle of the
85 scrubber devices. Comparisons with the fuel switching method were made. Patricksson et al.
86 (2015) formulated a stochastic model by using ECA as a key factor in the decision-making process.
87 Minimization of the total expected cost was achieved by choosing from installation scrubber devices
88 and fuel switching. Msakni and Haouari (2018) proposed a mixed integer programming model for
89 an LNG short-term delivery planning problem that included several variables and constraints, such
90 as time window, berth availability, bunker restriction, and inventory, with the objective to maximize
91 the net profit.

92 Many scholars have studied the optimization of ship navigation scheme based on the concept of
93 ECA or “green shipping”. There are two main research areas. The first research area is to minimize
94 total cost. Norstad et al. (2011) discussed a problem of tramp ship routing and scheduling while
95 optimizing its sailing speed. In addition, a multi-start local search heuristic was proposed to
96 solve the problem. Schinas and Stefanakos (2012) proposed a stochastic linear optimization model
97 by minimizing the cost to determine the optimal ship matching scheme of the fleet under the
98 restriction of ECA when the demand was uncertain. Experiment results indicated that some ships
99 needed to re-arrange the routes if ECA was established. Lindstad et al. (2013) used fuel cost
100 minimization as the objective function to evaluate the effects of ECA on emission reduction. The
101 results showed that the best effect of reducing emissions depends on factors such as the power of
102 the ship’s engine, annual fuel consumption within ECA, and future fuel prices. Doudnikoff and
103 Lacoste (2014) proposed a cost minimization model to estimate the combination of speed and the
104 pollutant emissions from liner services when minimizing the internal and external costs. Fagerholt
105 and Psaraftis (2015) and Fagerholt et al. (2015) proposed optimization models to minimize the
106 operating costs of ships that travel along a particular sequence of ports. Zhen et al. (2018) put
107 forward a mixed integer programming optimization model and minimized the total cost under
108 the condition of ECA based on Tabu search algorithm. Wang et al. (2018) developed a mixed
109 integer programming model which jointly designed the optimal ship sailing speed and the optimal
110 amount of bunker fuel to purchase at each port in a shipping network in order to minimize the
111 sum of ship operating costs and fuel costs. Psaraftis (2019) analyzed the combination problem
112 of ship sailing speed and route optimization under the ECA policy. The regulatory dimension of

113 speed reduction via speed limits was also discussed. Sheng et al. (2019) developed a mixed-integer
114 convex minimization model to determine the optimal vessel speed and ship fleet size for an industrial
115 shipping service operating within the ECAs. Minimizing SO₂ emissions is the second main research
116 area. Kontovas (2014) proposed a general model for green ship routes and scheduling problems.
117 Several alternatives are also offered to model ship emissions. Dulebenets et al. (2015) came up
118 with an innovative mixed integer nonlinear programming model for green ship scheduling problems
119 while taking the emission controls into consideration. Svindland (2018) introduced a method to
120 calculate the SO₂ emissions in container liner and made a comparative analysis of SO₂ emissions
121 before and after the implementation of ECA policy. The results showed that the emissions of
122 SO₂ were reduced after the policy was implemented. Chen et al. (2018) constructed models on
123 routes in container shipping to analyze the effect of ECA on the global shipping industry. It was
124 identified that the emissions in the ECA would be highly reduced, while some ships had to re-plan
125 the routes due to the implementation of ECA. Regarding single-objective optimization problems,
126 some heuristic algorithms are proposed, such as x and y -clusters algorithm (Kim and Moon, 2003),
127 dynamic programming technique (Park, 2003), time-space sequence pair (Moorthy and Teo, 2006)
128 and construction heuristic based on priority list (Meisel and Bierwirth, 2009). Our model differs
129 from the above studies in that we develop a bi-objective model that consider both costs and SO₂
130 emissions.

131 Bi-level models are generally difficult to solve and a number of scholars are interested in de-
132 veloping algorithms to solve them. Some algorithms, such as evolutionary algorithm and ant
133 colony algorithm, are adopted to address bi-objective planning problems (Cheong and Tan, 2008).
134 However, the algorithms can only be applied to solve the discrete problems instead of continuous
135 problems. To address the continuous multi-objective problems, the existing literature focuses on
136 preference-based method and generating method (Yeung and Man, 2011; Demir et al., 2014). The
137 former method considers the preferences of the decision makers through goal programming and
138 global criterion methods but can only provide a single solution. There are many ways to generate
139 solutions by using the latter method, such as weighted sum, evolutionary method, and ϵ -constraint
140 method, to generate a set of Pareto optimal solutions. The advantage of the latter method is that it
141 can provide a set of solutions for the decision makers to choose from (Tian et al., 2016a, 2016b). In
142 the above mentioned methods, different weight combinations in the weighted sum may lead to the

143 same solution, and the objective function must be transformed to the same scale before a weighted
144 sum is formed. In addition, it is difficult to control the number of Pareto solutions. Although
145 evolutionary methods can provide a set of approximate Pareto solutions, these solutions could be
146 far away from the optimal Pareto solutions. The ϵ -constraint method (Bérubé et al., 2009) is the
147 most effective method especially for bi-objective optimization problems. It can convert the original
148 bi-objective problem into a set of single-objective problems and take less time to obtain the required
149 number of Pareto solutions (Mavrotas, 2009; Li et al., 2016). Therefore, the paper proposes a two-
150 stage iterative method based on ϵ -constraint method. This method covers a larger search space so
151 that it can find a more reasonable trade-off solution for the bi-objective optimization problem.

152 To sum up, most of the literature focuses on establishing a single objective function to optimize
153 the shipping process. There is a lack of research on the construction of bi-objective models and
154 algorithms for speed and route optimization problems. With the development of “green shipping”,
155 the ECA policy will undoubtedly influence the choices of container transport navigation programs.
156 This paper constructs a bi-objective optimization model to minimize the total fuel cost and total
157 SO₂ emissions as well as analyzes the effectiveness of the proposed algorithm by using historical
158 operating data from a liner shipping company. The CPLEX solver is used to solve the model.
159 We also conduct some experiments to examine the effects of fuel cost, decision makers, and ECA
160 boundaries on the total cost and SO₂ emissions.

161 **3. Problem description and basic data**

162 *3.1. Problem description*

163 The global maritime environment has been improved after the ECA is introduced by the IMO,
164 but it also brings some new problems to the shipping industry. For example, how to design the
165 navigation plans under the ECA policy and how to minimize shipping emissions are important
166 issues that need to be considered by the shipping industry. In order to address the above problems,
167 this paper proposes a bi-objective optimization mathematical model for container liner ship route
168 design and speed optimization under the ECA policy. Considering several port cities and the arrival
169 time, we minimize the total fuel cost and total SO₂ emissions by optimizing the sailing route and
170 the speed within and outside the ECA.

171 The first objective of the model is to minimize the total cost. There are many costs involved in
172 the container shipping process. Based on related literature, route and speed selection will have little
173 impact on some nearly fixed costs, including labor cost, repair cost, and inventory cost. Therefore,
174 this paper only considers the fuel cost as it will be affected by the change of route and speed and
175 it constitutes a large percentage of the total operating cost.

176 Apart from that, the main pollutants emitted by container liners during navigation are SO_2 ,
177 CO_2 and NO_x . SO_2 emissions from ocean-going ships are proportional to the sulfur content of the
178 total fuel used, fuel consumption, and a proportional constant called the “sulfur index”, which can
179 be calculated as multiplying the total fuel consumption (tons) by the percentage of sulfur in the
180 fuel (e.g., 4%, 1.5%, 0.5%), and then multiplied by 0.02 (Dulebenets, 2017; Bergqvist et al., 2015).
181 The whole process can be explained by the chemical reaction of sulfur and oxygen, in which only
182 2% of the sulfur can react with oxygen to generate SO_2 . For example, 100 tons of fuel containing
183 3.5% sulfur can emit 7 tons of SO_2 , and the same amount of fuel with a sulfur content of 0.1%
184 produces only 0.2 tons. Thus, reducing SO_2 emissions can be achieved by burning less high sulfur
185 fuel or using cleaner fuel with lower sulfur content. The calculation formula of the amount of SO_2
186 emissions is as follows:

187 The amount of SO_2 emissions = $0.02 \times \text{total fuel consumption} \times \text{percentage of sulfur in fuel}$.

188 According to the regulations of IMO, since 2012, ships all over the world are required to use
189 fuel with a sulfur percentage at most 3.5 (e.g., HFO) (Kontovas, 2014). After introducing the ECA
190 in 2015, ocean ships need to use MGO instead of HFO during their voyage in ECAs such as the
191 Baltic Sea area, the North Sea area, the North America area and the United States Caribbean Sea
192 area. Since January 1, 2019, sea-going ships entering the DECA in China need to use marine fuel
193 with a sulfur content no more than 0.5% (e.g., MGO) and may follow the international standard
194 of 0.1% in the future. Thus, MGO with no more than 0.1% sulfur and HFO with 3.5% sulfur are
195 studied in our experiments.

196 Ships will also emit considerable CO_2 and NO_x . The amount of CO_2 emissions is proportional
197 to the amount of fuel used, and the proportionality constant is often called the “carbon factor”.
198 The factor was 3.17 (tonnes of CO_2 per ton of fuel) in the first IMO greenhouse gas study published
199 in 2000. However, the factor value was updated to a lower value in the second IMO greenhouse
200 gas study in 2009, ranging from 3.021 of HFO to 3.082 of MGO (Psaraftis and Kontovas, 2013).

201 The carbon factor of natural fuels such as LNG can be between 2.6 and 2.8. CO₂ emissions can be
202 calculated based on the total fuel consumption and CO₂ emission factor of the voyage, i.e.,

203 The amount of CO₂ emissions = Total fuel consumption × Carbon dioxide emission factor.

204 Similarly, the amount of NO_x can be calculated by using the total fuel consumption and NO_x
205 emission factor, where the NO_x emission factor is between 0.057 and 0.087 (Dulebenets, 2017), i.e.,

206 The amount of NO_x emissions = Total fuel consumption × Nitrogen oxides emission factor.

207 We focus on SO₂ emissions in this paper. According to the research by Zhen et al. (2018),
208 the total amount of SO₂ emitted by ocean-going vessels in the world is about 4.7-6.5 Tg per year,
209 which accounts for more than 8% of anthropogenic emissions. SO₂ is a major pollutant emitted
210 by ocean-going ships, which may produce acid rain and cause serious harm to human, animals and
211 plants. At the same time, under the action of light and oxidant, SO₂ will react to form a sulfate
212 gas solution, which will aggravate the deterioration of haze. Hence, the second objective of the
213 model is to minimize the total SO₂ emissions.

214 3.2. Basic data

215 3.2.1. Fuel price

216 Fuel prices vary among different ports. Based on data from the website of “eworldship”, the
217 price of HFO fluctuates between 345 and 465 USD/ton from December 2017 to December 2018,
218 while the price for MGO fluctuates between 500 and 1160 USD/ton. Taking the uncertainty of fuel
219 prices into account, the prices of HFO and MGO are key factors for the speed and route decision-
220 making in this paper. It is possible for a ship to refuel at any port during its voyage, and thus this
221 paper adopts the average fuel price of different regions all over the world in our experiments, i.e.,
222 the price for MGO used within the ECA is set to be 750 USD/ton, and the price for HFO used
223 outside the ECA is set to be 405 USD/ton.

224 3.2.2. Fuel consumption

225 The research conducted by Du et al. (2011), Wang and Meng (2012), and Psaraftis and Kontovas
226 (2013, 2014) showed that the relationship between the sailing speed and bunker consumption is
227 nonlinear, and the daily bunker consumption is approximately proportional to the sailing speed
228 cubed. Thus, the fuel consumption per unit of distance is a function proportional to the sailing
229 speed squared, i.e., a convex function of speed.

230 The shipping company will record the fuel consumption of each ship at some speeds during
 231 its actual voyage. As the speed and fuel consumption have an approximate non-decreasing con-
 232 vex function relationship, by combining with the piecewise linear interpolation method, the fuel
 233 consumption at any speed can be estimated. For example, suppose that two speed point a and
 234 b are recorded, a speed point c between a and b can be calculated by using the piecewise linear
 235 interpolation method. The computational results are slightly higher than the actual values. Since
 236 the speed point recorded by the shipping company is generally a series of integer value points in
 237 continuous time, the deviations of the corresponding fuel consumption of the non-integer velocity
 238 are quite small, and hence the errors can be ignored.

239 In our experiments, fuel consumption values (tons) corresponding to discrete speed values are
 240 given by Fig. 2 (i.e., the fuel consumptions of ships sailing per 500 nautical miles). The minimum
 241 and maximum sailing speeds are 15 knots and 21 knots, respectively. It can be seen from Fig. 2
 242 that the fuel consumption gradually increases with the increase of speed and the upward trend
 243 continues to expand.

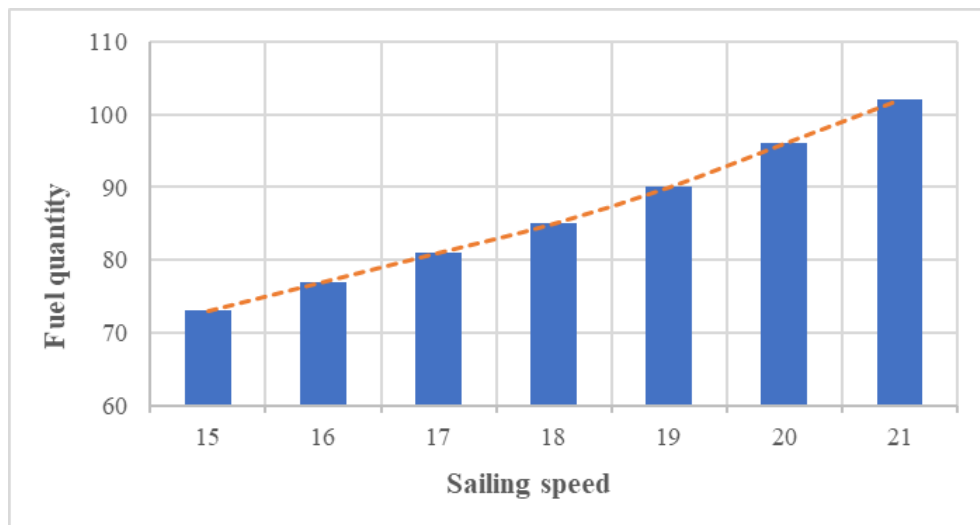


Figure 2: Fuel consumption of ships sailing 500 nautical miles (Zhen et al., 2018)

244 3.2.3. Time window

245 In this study, each port on a route is related to a time window so that ships will visit each
 246 port at the proper time. These time windows can be derived from contracts on the loading and
 247 unloading of goods with the customers and can also be a time period agreed between the shipping

248 companies and the port operators. Taking the convenience of operation into consideration, all the
 249 arrival times are set at daytime. For example, in the case of Shanghai Zhonggu Shipping Group
 250 Co., Ltd, the ships depart from Dalian at 12 AM on day 0 and arrive at the second port (Yantai)
 251 during 8 AM and 4 PM on the x^{th} ($0 \leq x \leq 10$) day. The ships are supposed to stay at the port for
 252 11 hours to load and unload cargoes before departing for the next port. The arrival time window
 253 and staying time at each port are the same. The latest time for the ship to return to the first port
 254 (Dalian) is 4 PM on the tenth day.

255 4. Mathematical model

256 Indices and Sets

- 257 i, j Index of port .
- 258 k Number of days of the voyage from port i to j .
- 259 v Sailing speed of ships.
- 260 r Index of path options of a ship, $r=1,2,3 \dots$.
- 261 A Set of ports of call, $A=\{0,1,\dots,N,N+1\}$, in which 0 and $N+1$ are the home port.
- 262 G Set of two consecutive ports of call, $G=\{ij|a \text{ ship first visits port } i \text{ then visits}$
 $j=i+1\}$, $i=0,\dots,N$.
- 263 K Set of voyage days from port i to port j .
- 264 V Set of speeds at discrete points.
- 265 R_{ij} Set of path options from port i to port j .
- 266 RE_{ij} Set of path options containing stretches within the ECA from port i to port j ,
 $RE_{ij} \in R_{ij}$.
- 267 RN_{ij} Set of path options containing stretches outside the ECA from port i to port j ,
 $RN_{ij} \in R_{ij}$.

268 Input parameters

- 269 P^{ECA} Fuel price within the ECA.
- 270 P^N Fuel price outside the ECA.
- 271 F_{ijrv}^{ECA} Fuel consumption within the ECA for a sailing from port i to port j when choosing
 path option r and sailing at speed v .
- 272 F_{ijrv}^N Fuel consumption outside the ECA for a sailing from port i to port j when choosing
 path option r and sailing at speed v .

273 T_{ijrv}^{ECA} Sailing time within the ECA for a sailing from port i to port j when choosing path
option r and sailing at speed v .

274 T_{ijrv}^N Sailing time outside the ECA for a sailing from port i to port j when choosing path
option r and sailing at speed v .

275 C_{ijrv}^{ECA} Emissions of SO₂ within the ECA for a sailing from port i to port j when choosing
path option r and sailing at speed v .

276 C_{ijrv}^N Emissions of SO₂ outside the ECA for a sailing from port i to port j when choosing
path option r and sailing at speed v .

277 γ_i Waiting time of ships at port i .

278 L_{jk} Lower bound of time window when the ships arrive at port j on day k .

279 E_{jk} Upper bound of time window when the ships arrive at port j on day k .

280 M A sufficiently large positive number.

281 Decision variables

282 t_j Time when the ship arrives at port j .

283 s_{ij} Sailing time of a ship between port i and port j .

284 y_{ijrv}^{ECA} Weight of sailing speed v within the ECA for a sailing from port i to port j under
the path option r .

285 y_{ijrv}^N Weight of sailing speed v outside the ECA for a sailing from port i to port j under
the path option r .

286 z_{ijr} Binary variable, equal to one if path option r is chosen when the ship sails from port
 i to port j , and zero otherwise.

287 β_{jk} Binary variable, equal to one if the ship arrives at port j on day k , and zero otherwise.

288 Mathematical model

$$\min Z_1 = \sum_{i,j \in G} \left(\sum_{r \in RE_{ij}} \sum_{v \in V} P^{ECA} F_{ijrv}^{ECA} y_{ijrv}^{ECA} + \sum_{r \in RN_{ij}} \sum_{v \in V} P^N F_{ijrv}^N y_{ijrv}^N \right) \quad (1)$$

$$\min Z_2 = \sum_{i,j \in G} \left(\sum_{r \in RE_{ij}} \sum_{v \in V} C_{ijrv}^{ECA} y_{ijrv}^{ECA} + \sum_{r \in RN_{ij}} \sum_{v \in V} C_{ijrv}^N y_{ijrv}^N \right) \quad (2)$$

290 subject to:

$$s_{ij} = \sum_{r \in R_{ij}} \sum_{v \in V} (T_{ijrv}^{ECA} y_{ijrv}^{ECA} + T_{ijrv}^N y_{ijrv}^N) \quad \forall i, j \in G \quad (3)$$

$$t_i + \gamma_i + s_{ij} \leq t_j \quad \forall i, j \in G \quad (4)$$

$$t_j - M(1 - \beta_{jk}) \leq E_{jk} \quad \forall j \in A, k \in K \quad (5)$$

$$t_j + M(1 - \beta_{jk}) \geq L_{jk} \quad \forall j \in A, k \in K \quad (6)$$

$$\sum_{k \in K} \beta_{jk} = 1 \quad \forall j \in A \quad (7)$$

$$\sum_{v \in V} y_{ijrv}^{ECA} = z_{ijr} \quad \forall i, j \in G, r \in RE_{ij} \quad (8)$$

$$\sum_{v \in V} y_{ijrv}^N = z_{ijr} \quad \forall i, j \in G, r \in RN_{ij} \quad (9)$$

$$\sum_{r \in R_{ij}} z_{ijr} = 1 \quad \forall i, j \in G \quad (10)$$

$$y_{ijrv}^{ECA} \geq 0 \quad \forall i, j \in G, r \in RE_{ij}, v \in V \quad (11)$$

$$y_{ijrv}^N \geq 0 \quad \forall i, j \in G, r \in RN_{ij}, v \in V \quad (12)$$

$$t_i \geq 0 \quad \forall i \in A \quad (13)$$

$$\beta_{jk} \in \{0, 1\} \quad \forall j \in A, k \in K \quad (14)$$

$$z_{ijr} \in \{0, 1\} \quad \forall i, j \in G, r \in R_{ij} \quad (15)$$

291 The objective (1) aims to minimize the sum of the fuel cost within and outside the ECA. As
 292 the fuel consumption and speed have a nonlinear relationship, the piecewise linear interpolation
 293 method is adopted to estimate the fuel consumption at a certain speed based on the decision vari-
 294 ables y_{ijrv}^{ECA} and y_{ijrv}^N . The target of objective (2) is to minimize the total SO₂ emissions within
 295 and outside the ECA. Constraints (3) and (4) guarantee that the allowable arrival time to a port
 296 plus the port time and sailing time to the next port will not exceed the allowable arrival time to
 297 the next port. Constraints (5-7) ensure that the allowable arrival time is within the time win-
 298 dow. Constraints (8) and (9) connect the path option with voyage speed weight, i.e., if path
 299 option r is chosen, the sum of speed weight within and outside the ECA is equal to one, re-
 300 spectively. Constraint (10) ensures that one path option must be selected from port i to port
 301 j . Constraints (11-13) guarantee that the speed weight and arrival time are nonnegative. Con-

302 straint (14) and (15) ensure the domains of β_{jk} and z_{ijr} . As the proposed model is an NP-hard
 303 problem, this paper designs a two-stage iterative and fuzzy decision algorithm based on ϵ -constraint
 304 to solve the model.

305 Bi-objective decision making method for mathematical planning is a popular method used to
 306 address the bi-objective optimization problems. Generally, the bi-objective problem is turned to
 307 single-objective problems at first, and then multiple solutions are found for these single-objective
 308 problems in order to get the Pareto optimal solution set. One of the efficient methods to get the
 309 Pareto solution is the ϵ -constraint method (Haimes et al., 1971). It has other advantages including
 310 but not limited to working without other parameters and with a unified dimension. The bi-objective
 311 optimization problem in this paper is presented as follows,

$$\min F_1 = \varphi(x) \tag{16}$$

$$\min F_2 = \omega(x) \tag{17}$$

$$\text{s.t. } x \in X, \tag{18}$$

312 where x is the decision vector for all decision variables, $\varphi(x)$ and $\omega(x)$ represent the total fuel cost
 313 and total SO₂ emissions, respectively, and X is the feasible region of x defined by constraints (3-
 314 15). If $\varphi(x) \leq \varphi(x')$, $\omega(x) \leq \omega(x')$, and at least one of the two objectives is strict inequality,
 315 a feasible solution $x \in X$ is strictly better than and hence can replace another feasible solution
 316 $x' \in X$. Meanwhile, if no feasible solution $x' \in X$ can replace the existing feasible solution $x^* \in X$,
 317 then the existing solution is irreplaceable, i.e., it is a Pareto optimal solution. The corresponding
 318 value of the objective $(\varphi(x^*), \omega(x^*))$ is the Pareto point, and the Pareto optimal solution set is
 319 defined as $P_s = \{x^* \in X | x^* \text{ is a Pareto optimal solution}\}$. The Pareto frontier is defined as
 320 $P_f = \{(\varphi(x^*), \omega(x^*)) | x^* \in P_s\}$.

321 The basic idea for the ϵ -constraint method is to transform the initial bi-objective programming
 322 problem (i.e., the problem defined by (16) to (18)) into a single-objective programming problem
 323 with a primary objective. In other words, we need to turn the initial objective (e.g., to minimize
 324 $\omega(x)$) into the constraint limited by parameter ϵ ($\omega(x) \leq \epsilon$) and solve the sequences (i.e., to
 325 minimize $\varphi(x)$). In this paper, the goal is to turn the bi-objective function into two single-objective
 326 optimization problems. The whole problem can be viewed as two sub-problems: problem A: setting

327 the minimization of total fuel cost as the goal while the total SO₂ emissions as the constraint;
 328 problem B: setting the minimization of the total SO₂ emissions as the goal while the total fuel cost
 329 as the constraint. The definitions of the two problems are as follows.

$$\text{Problem A : } \quad \min \{ \varphi(x) | \omega(x) \leq \epsilon, x \in X \} \quad (19)$$

$$\text{Problem B : } \quad \min \{ \omega(x) | \varphi(x) \leq \epsilon, x \in X \} \quad (20)$$

330 The possible values of ϵ lie in an interval in this problem. In order to construct the Pareto
 331 optimal solution set, a two-stage iterative approach of the ϵ -constraint method can be adopted to
 332 obtain the ideal point (f_1^I, f_2^I) and farthest point (f_1^N, f_2^N) to determine the value range. The lower
 333 and upper bounds of the Pareto optimal solution value are defined by the ideal and farthest points
 334 respectively. They can be generated by solving the following single-objective problems.

$$f_1^I = \min \{ \varphi(x) | x \in X \} \quad (21)$$

$$f_2^I = \min \{ \omega(x) | x \in X \} \quad (22)$$

$$f_1^N = \min \{ \varphi(x) | \omega(x) = f_2^I, x \in X \} \quad (23)$$

$$f_2^N = \min \{ \omega(x) | \varphi(x) = f_1^I, x \in X \} \quad (24)$$

335 Firstly, the lower bounds of the two objective functions can be solved according to the two
 336 single-objective problems respectively. Then, the upper bound of the two objective functions can
 337 be figured out based on problems defined by (19) and (20). In this way, the approximate ideal
 338 point (f_1^I, f_2^I) and approximate farthest point (f_1^N, f_2^N) can be generated, and the value of ϵ can
 339 also be identified based on the range of $[f_2^I, f_2^N]$. By setting the step Δ to find out the value of
 340 ϵ , a series of single-objective optimization problems can be formed and the Pareto frontier or its
 341 approximation can be obtained after solving them. In other words, after fixing the value of ϵ , there
 342 is always a solution $x' = x(\epsilon)$ for each single-objective function. If there is no $x \in X$ that satisfies
 343 $f(x) < f(x')$, then x' is the optimal Pareto solution of the initial problem, and all Pareto optimal
 344 solutions form the surfaces of the Pareto frontier.

345 As several sub-problems of ϵ need to be addressed in the two-stage iterative approach, the Pareto
 346 solution set will contain several solutions. In order to obtain the optimal solution according to the

347 demand of the decision makers, fuzzy decision method is used to get an optimal solution, as this
 348 method can generate the optimal degree of the selected solution according to the decision makers'
 349 preference. Linear membership functions of the Pareto objective functions are first generated by
 350 the following formulas:

$$\delta_i(f_i^s) = \begin{cases} 1 & f_i^s \leq f_i^I \\ \frac{f_i^N - f_i^s}{f_i^N - f_i^I} & f_i^I < f_i^s < f_i^N, i = 1, 2; 1 \leq s \leq S, \\ 0 & f_i^s \geq f_i^N \end{cases} \quad (25)$$

351 where $\delta_i(f_i^s)$ represents the i^{th} objective function of the s^{th} solution, and f_i^I and f_i^N are the lower
 352 bound and upper bound of the i^{th} objective function, while f_i^s is the s^{th} Pareto solution in the i^{th}
 353 objective function. The total membership degree δ^s is calculated by the following formula:

$$\delta^s = \sum_{i=1}^2 \omega_i \delta_i(f_i^s), \quad (26)$$

354 where ω_i is the weight of the i^{th} objective, and in this model $\sum_{i=1}^2 \omega_i = 1$. It can be determined by
 355 the preference of the decision makers and the optimal solution is the solution with the maximum
 356 δ^s .

357 It is worth mentioning that the selected method is better than the weighted sum. Although
 358 the two methods both need to consider the preference of the decision makers, the meanings of
 359 the weights are different. In the weighted sum, weights are attached directly to each objective.
 360 Nevertheless, it can be challenging as these objectives usually have different units and dimensions.
 361 In addition, if the decision makers change their minds, a new set of weights need to be estimated
 362 to reflect their preference and new problems need to be addressed. On the contrary, in the fuzzy
 363 decision method, the weights are attached to the membership degrees of each objective and all
 364 these membership degrees are standardized into scalar ranging from 0 to 1 which makes it possible
 365 to get the Pareto optimal solution set at the selecting stage. More importantly, when the decision
 366 makers change their mind, all that need to do is to estimate a new set of weights and choose a new
 367 solution in the Pareto optimal solution set.

368 **5. Numerical examples**

369 *5.1. Example description*

370 According to the IMO regulations of sulfur emission controls on ships, from January 1, 2015,
371 ships should use fuel containing no more than 0.1% of sulfur in the ECA of the Baltic Sea area, the
372 North Sea area, the North America area, and the United States Caribbean Sea area. Since January
373 1, 2020, sulfur contained in ship fuel should be no more than 0.5% worldwide. This means that it
374 is necessary to take appropriate measures to reduce sulfur emissions from ships. At the same time,
375 container liner routes in other regions of the world will also be affected by the European and North
American ECA regulations.



Figure 3: Navigation plans of the example

376

377 Based on the newly introduced regulations from December 2018, China has expanded its ECA
378 along the coastline. To better demonstrate the influence of ECA on liner shipping and validate the
379 effectiveness of the proposed model, a shipping route in Shanghai Zhonggu Shipping Group Co.,
380 Ltd., is discussed as a case in this section. The container liners depart from Dalian which is located
381 in the DECA, then call at Yantai, Shanghai, Ningbo, and Shenzhen, and finally return to Dalian.
382 The locations of the ports are illustrated in Fig. 3, where the boundary of ECA is marked by a



Figure 4: Five path options from Ningbo to Shenzhen

383 blue dotted line, and the route is shown by a red line.

384 The route is generated by BLM-Shipping, which is based on several electronic maps. It can
 385 position and search the current and history ship tracks based on the AIS data. It can also be used to
 386 calculate the distances between two ports, design shipping routes, and monitor the voyages. Based
 387 on the coordinates of DECA given by the Ministry of Transport of the People's Republic of China,
 388 the boundaries of DECA can be illustrated in Fig. 3 and the shipping routes can be generated
 389 based on the designated points at sea. According to the ports on the shipping routes of Shanghai
 390 Zhonggu Shipping Group Co., Ltd., our study takes a route with five legs into consideration. The
 391 possible path options for a leg from Ningbo to Shenzhen are illustrated in Fig. 4 in red solid lines.

392 The sailing distances within and outside the ECA corresponding to the five legs are illustrated
 393 in Table 1.

Table 1: Sailing distances within and outside the ECA for five legs in each path option

Cities	Option 1	Option 2	Option 3	Option 4	Option 5
1 Dalian – 2 Yantai	183/0	164/21	144/42	123/63	102/84
2 Yantai – 3 Shanghai	113/216	184/315	153/346	125/375	96/403
3 Shanghai – 4 Ningbo	193/0	163/69	132/137	91/176	49/214
4 Ningbo – 5 Shenzhen	738/0	237/562	195/603	155/644	114/684
5 Shenzhen – 1 Dalian	359/1399	363/1468	366/1547	326/1673	285/1788

Note: For “183/0”, “183” is the distance within the ECA and “0” is the distance outside the ECA.

394 5.2. Numerical experiments

395 To solve the model proposed in Section 4, in this section, numerical experiments are conducted
 396 on a PC (processor Intel Core i7, 2.50 GHz, 8GB RAM). The model is solved by using C# to call
 397 the interface of CPLEX 12.6 on VS2015.

398 5.2.1. Performance of the model considering the effects of ECA

399 A case study of a shipping route operated by Shanghai Zhonggu Shipping Group Co., Ltd. is
 400 conducted in our study. In this case, the ships depart from Dalian, then visit Yantai, Shanghai,
 401 Ningbo, and Shenzhen in sequence, and finally return to Dalian. The path and speed solution
 402 without considering the effects of ECA is obtained as follows. To begin with, we do not consider
 403 the ECA regulations. Option 1 which provides the shortest distance between any two ports is
 404 selected and the total distance of the route is 3,201 nautical miles. Based on Fig. 2 and the
 405 piecewise linear interpolation method introduced in Section 3.2.2, the fuel consumption can be
 406 calculated by the real sailing speed and the shortest sailing path. Then, different types of fuel used
 407 within and outside the ECA are taken into consideration to calculate the total fuel cost and SO₂
 408 emissions, and the results are illustrated in Table 2. The total fuel cost is about 352,595.24 USD,
 409 and the total SO₂ emissions is 23.917 tons. The fuel consumption within the ECA is 290.098 tons
 410 while the amount outside the ECA is 333.387 tons, and the total fuel assumption is 623.485 tons.

411 When the weights of the membership degrees are the same for the two objectives, the results
 412 considering the effects of ECA are illustrated in Table 3. It can be seen that the fuel cost is about
 413 258,899.15 USD. Compared with the fuel cost not considering the effects of ECA, about 93,696.09
 414 USD (26.57%) can be saved. The total SO₂ emission is increased to 29.148 tons, with a rise of

Table 2: The results without considering the effects of ECA

Leg	Speed (knots)		Fuel consumption (tons)			Fuel cost (USD)	SO ₂ emissions (tons)
	Within ECA	Outside ECA	Within ECA (MGO)	Outside ECA (HFO)	Total fuel consumption		
1-2	15.000	–	26.718	–	26.718		
2-3	20.560	20.560	22.455	82.924	105.379		
3-4	19.300	–	35.435	–	35.435	352595.24	23.917
4-5	19.946	–	141.218	–	141.218		
5-1	18.903	18.903	64.272	250.463	314.735		
Total	–	–	290.098	333.387	623.485		

Table 3: The results considering the effects of ECA

Leg	Option	Speed (knots)		Fuel consumption (tons)			Fuel cost (USD)	Cost saved (USD)	SO ₂ emissions (tons)	Emission increased (tons)
		Within ECA	Outside ECA	Within ECA	Outside ECA	Total fuel consumption				
1-2	5	15.000	15.471	14.892	12.581	27.473				
2-3	5	15.222	15.222	14.186	59.554	73.740				
3-4	2	15.000	16.000	23.798	10.626	34.424	258899.15	93696.09	29.148	5.231
4-5	5	15.322	19.338	16.938	125.894	142.832				
5-1	1	15.000	15.000	52.414	204.254	256.668				
Total	–	–	–	122.228	412.909	535.137				

415 5.231 tons. As shown in Table 3, the shipping fuel consumption within the ECA is 122.228 tons,
416 while the consumption outside the ECA is 412.909 tons, and the total fuel consumption is 535.137
417 tons. The total distance of the route is 3,473 nautical miles. In this case, three legs choose option
418 5, meaning the container liners prefer the routes with longer total distance but shorter distance
419 in the ECA to reduce the cost. However, the price of fuel within the ECA (MGO) is higher than
420 the price of fuel outside the ECA (HFO), and the sailing speed outside the ECA is larger than or
421 equal to the speed within the ECA. For instance, for the sailing leg from Dalian to Yantai, the
422 ship sails at the lowest speed of 15 knots within the ECA to minimize the fuel consumption, while
423 when sailing outside the ECA, the sailing speed needs to be increased to make up for the extra
424 time spent within the ECA. The results of the optimization model validate the influence of ECA

425 on shipping industry as presented in the introduction part.

426 5.2.2. Effect of fuel price

427 Different fuel prices within and outside the ECA will have a great impact on the navigation
428 cost. In the baseline scenario, the price for MGO is 750 USD/ton. Assume that the price for HFO
429 remains unchanged and we analyze the impact of fuel price on total costs by setting the price of
430 MGO as 850, 950, 1,050 and 1,150 USD/ton respectively. By adopting the calculation process
431 proposed in Section 5.2.1, the fuel cost considering and not considering the effects of ECA are
432 presented in Table 4.

Table 4: Comparison of the fuel cost under different prices of MGO

MGO price (USD/ton)	Fuel cost (USD)		Cost saved (USD)
	Not considering the effects of ECA	Considering the effects of ECA	
750	352595.24	258899.15	93696.09
850	381605.04	271121.95	110483.09
950	410614.84	283344.75	127270.09
1050	439624.64	295567.55	144057.09
1150	468634.44	307790.35	160844.09

433 As illustrated in Table 4, the proposed model can reduce the fuel cost under each of the price
434 condition significantly. From the perspective of cost saving, the higher the price of MGO, i.e., the
435 larger difference of the fuel prices within and outside the ECA, the more costs can be saved when
436 the effects of ECA are considered. When the price of MGO is 1,150 USD/ton, the cost saving
437 reaches 160,844.09 USD, which is about 34.32% of the fuel cost when the effects of ECA are not
438 considered. Therefore, the model can help the shipping companies to reduce the cost by optimizing
439 the sailing speed and routes. It should be noted that the savings listed in the table are just for one
440 voyage. For a ship company with more similar routes, more savings can be obtained by adopting
441 the proposed model. If the companies take the impact brought by the ECA into account, each ship
442 is expected to save hundreds of thousands of or even millions of dollars in fuel cost each year if the
443 sailing speed and routes can be optimized after re-designing the voyage scheme. Also, the model
444 can be applied to other routes.

445 5.2.3. *Effect of decision maker*

446 It is shown in Section 5.2.1 that the objectives of minimizing the total fuel cost and SO₂
447 emissions are difficult to be achieved simultaneously. In this section, the impact of decision makers
448 on the objectives is taken into account. If the decision makers have preferences in the two objections,
449 the two objectives should be considered at the same time. Thus, this paper combines the proposed
450 method and CPLEX to obtain a set of Pareto solutions for the decision makers. The Pareto
451 solutions are presented in Fig. 5, in which the horizontal and vertical axes represent the total fuel
452 cost and total SO₂ emissions, respectively. The model can provide a solution for the decision maker
453 after obtaining a set of Pareto solutions. It can be seen from Fig. 5 that 50 Pareto solutions can
454 be generated by using the proposed model. From the Pareto frontier solution obtained, it is clear
455 that there is a conflict between the two objectives. In addition, this paper can help the decision
456 makers choose the best solution for each stage.

457 It can be concluded from the figure that when SO₂ emissions are ignored, the total cost for
458 shipping can be reduced to $f_1^I = 256,714.30$ USD, and the total SO₂ emissions are $f_2^N = 39.285$
459 tons. When the impact of the total fuel cost is ignored, the total SO₂ emissions can be reduced to
460 $f_2^I = 23.589$ tons, but the total fuel cost increases to $f_1^N = 263,056.40$ USD. That is to say, using SO₂
461 emissions as an objective function can reduce the pollutant by 15.696 tons, but the total cost will
462 increase 6,342.10 USD. This also indicates that there are contradictions between the two objectives.

463 To help the decision makers to obtain their preferred solutions, we assume that there are three
464 types of preferences. In the first scenario, the weight for the first objective is $\omega_1 = 0.8$. In the second
465 scenario, the two objectives are treated equally, i.e., $\omega_1 = 0.5$. In the last scenario, the decision
466 makers pay more attention to environmental pollution, so $\omega_1 = 0.2$. The three solutions are shown
467 in Fig. 5. It can be seen that different weights can lead to different Pareto solutions. The solutions
468 are illustrated in Table 5, in which Δf_1 is the cost growth rate for f_1^I , i.e., $\Delta f_1 = (F_1 - f_1^I)/(f_1^N - f_1^I)$,
469 and Δf_2 is the reduction rate of total SO₂ emissions, i.e., $\Delta f_2 = (f_2^N - F_2)/(f_2^N - f_2^I)$.

470 It can be seen from Table 5 that the total membership degree of a single optimal solution is
471 high, which is from 0.651 to 0.784. If the decision makers pay more attention to the cost, the
472 selected solution ($\omega_1 = 0.8$) shows that the cost will only grow 9.69%, while the total SO₂ emissions
473 will be reduced by 25.00%. If the decision makers concern more about the environment issues,
474 the selected solution ($\omega_1 = 0.2$) shows that the total cost will increase 91.37% with SO₂ emissions

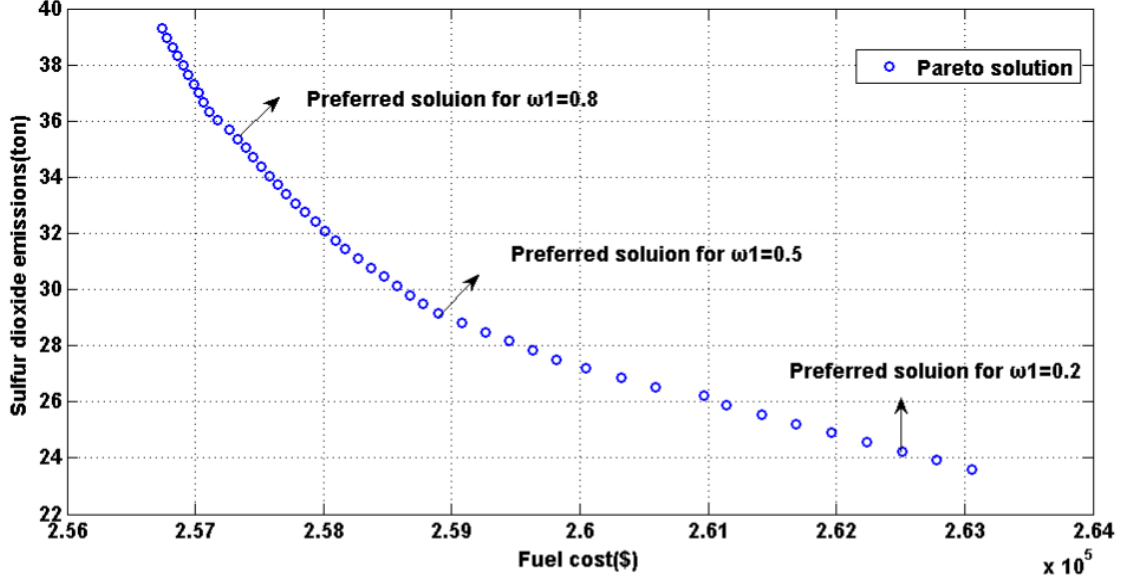


Figure 5: The approximate Pareto frontier of the example

Table 5: Details of the solutions based on different preferences of decision makers

ω_1	δ^s	F_1 (USD)	F_2 (tons)	$\Delta f_1(\%)$	$\Delta f_2(\%)$
0.8	0.772	257329.15	35.361	9.69	25.00
0.5	0.651	258899.15	29.148	34.45	64.58
0.2	0.784	262508.82	24.243	91.37	95.83

475 reduced by 95.83%.

476 5.2.4. Effect of ECA boundary

477 In this section, the impact brought by the ECA policy is analyzed by changing the boundary
478 of ECA. Five situations are considered based on the existing ECA: setting the boundary of ECA 4
479 nautical miles closer to the coastline (L_1), 2 nautical miles closer to the coastline (L_2), remaining
480 the boundaries of ECA unchanged (L_3), setting the boundary of ECA 2 nautical miles further from
481 the coastline (L_4), 4 nautical miles further from the coastline (L_5). From Table 6, we can see that
482 among all situations, the average sailing speed outside the ECA in situation L_2 is at the maximum
483 value, while the average sailing speed within the ECA in situation L_3 is at the minimum value.
484 The total fuel consumption increases from L_1 to L_5 within the ECA, while decreases outside the
485 ECA. It can also be seen that in the three cases, with the expansion of the ECA, the total cost of

486 fuel increases, while the total SO₂ emissions decrease. The ECA boundary is set up primarily to
 487 minimize the total SO₂ emissions and reduce environmental pollution at a reasonable cost. In this
 488 example, different boundaries of ECA will have different impacts on shipping industry. The results
 489 show that L_3 is a suitable ECA boundary.

Table 6: The total fuel cost and SO₂ emissions under different boundaries of ECA

Five situations		L_1	L_2	L_3	L_4	L_5
Average speed (knots)	Inside ECA	15.212	15.623	15.101	15.802	15.634
	Outside ECA	16.491	16.532	16.206	16.307	16.145
Total fuel consumption (tons)	Inside ECA	113.939	119.144	122.228	135.153	137.535
	Outside ECA	421.502	415.966	412.909	403.618	399.908
Total cost (USD)	$\omega_1 = 0.8$	253963.180	254780.820	257329.150	261738.340	262717.050
	$\omega_1 = 0.5$	256162.560	257824.230	258899.150	264830.040	265113.990
	$\omega_1 = 0.2$	258514.340	260237.020	262508.820	268456.230	269266.860
	$\omega_1 = 0.8$	35.946	35.569	35.361	34.737	34.481
Total SO ₂ emissions (tons)	$\omega_1 = 0.5$	29.733	29.356	29.148	28.524	28.269
	$\omega_1 = 0.2$	24.828	24.451	24.243	23.619	23.363

490 We select 10 routes (denoted by S_1 - S_{10}) from regions all over the world: the Baltic Sea area,
 491 the North Sea area, the North America area, the United States Caribbean Sea area, the sea areas
 492 near China and other sea areas. Specific routes are presented in Fig. 6 and Table 7.

Table 7: Detailed information about the 10 routes

No.	Paths
S_1	1 Tianjin – 2 Shanghai – 3 Wenzhou – 4 Guangzhou
S_2	5 Weihai – 6 Qingdao – 2 Shanghai – 7 Xiamen
S_3	2 Shanghai – 7 Xiamen – 8 Hong Kong – 9 Tokyo
S_4	10 Kodiak – 11 Steattle – 12 Los Angeles – 13 Manzanillo
S_5	14 Vancouver – 15 San Francisico – 12 Los Angeles – 16 Honolulu
S_6	17 New York – 18 Port Canaveral – 19 Miami – 20 Great Strirrup Cay – 21 Nassau
S_7	22 Halifax – 17 New York – 19 Miami – 23 San Juan(Puerto Rico)
S_8	22 Halifax – 17 New York – 24 Wilmington – 25 Ponta delgada
S_9	26 Bibuo – 27 Cherbourg – 28 Dublin – 29 Kristiansand
S_{10}	30 Lisbon – 27 Cherbourg – 31 Glasgow – 32 Hamburg



Figure 6: The Distribution of ports around the ten routes

493 The results are presented in Fig. 7. The dashed lines indicate the total fuel cost and the
 494 solid lines represent the total SO₂ emissions. The blue, black, and red lines represent $\omega = 0.8$,
 495 $\omega = 0.5$ and $\omega = 0.2$, respectively. The horizontal coordinates represent five scenarios of the ECA
 496 boundary, and the longitudinal coordinates represent the total fuel cost and total SO₂ emissions.
 497 The results show that there are three situations. First, from case 1 and case 4, the trends of the two
 498 objective functions are “V-shaped”. In situation L_3 , the total fuel cost and SO₂ emissions reach
 499 the minimization values, and the optimal solution is L_3 . Second, from case 5, case 6, and case 8, it
 500 can be concluded that under the three situations, the total fuel cost increases with the expansion of
 501 ECA boundaries, while the trend of total SO₂ emissions is “V-shaped”, and the minimal solution
 502 is obtained near situation L_3 . The main goal of ECA is to minimize the total SO₂ emissions at the
 503 possible lowest cost, and thus the optimal boundary of ECA should be at L_3 . Third, from case 2,
 504 case 3, case 7, case 9, and case 10, experimental results show that the total fuel cost increases and
 505 the total SO₂ emissions reduce with the expansion of ECA boundary in three different decision-
 506 making situations. Therefore, the optimal solution should be near L_3 . Based on the average value
 507 of the results from the 10 routes, although there may exist situations in which the performance of

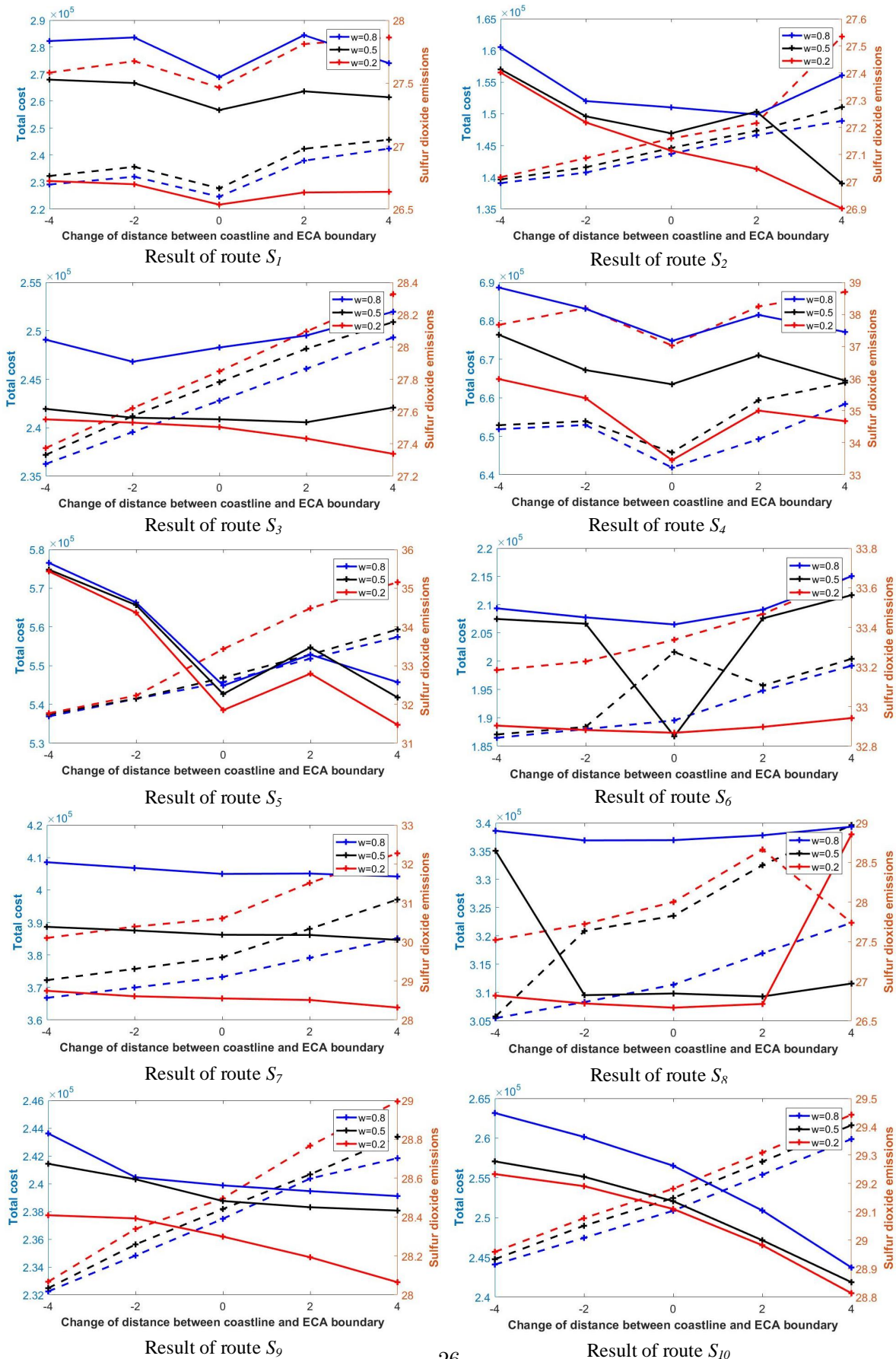


Figure 7: Changes of the total fuel cost and SO_2 emissions with boundaries of the ECA for the 10 routes

508 the two objective functions is better than that in situation L_3 , the overall optimal choice of the
509 ECA boundary should still be L_3 .

510 To sum up, the bi-objective route and speed optimization model proposed in this paper is
511 effective under the restriction of ECA policy. When the membership weights of the two objective
512 functions are the same, the total fuel cost and SO_2 emissions of the container liners within and
513 outside the ECA will be significantly reduced by the proposed model considering the effects of ECA.
514 In real situations, the decision makers can choose suitable solutions according to their preference.
515 The model can also be used to validate the effectiveness of the design of the ECA boundary, save
516 the operating costs of companies, and reduce SO_2 emissions to improve their social image.

517 **6. Conclusions**

518 Under the emission control policy, shipping routes and speeds optimization are important strate-
519 gic decisions for liner shipping companies. In this paper, a bi-objective mixed integer programming
520 model is constructed, and the voyage plan is reformulated by optimizing the shipping speed and
521 routes. The objectives of this model are to minimize the total fuel cost and SO_2 emissions within
522 and outside the ECA. The model is solved by adopting a two-stage iterative method based on
523 ϵ -constraint. Finally, the actual container liner navigation data of the company is used for the
524 numerical experiments. The effectiveness and practicability of the ECA boundary division are vali-
525 dated by the model, and different solutions are provided for the decision makers. The contributions
526 of this paper are as follows.

527 (1) This paper proposes a bi-objective model to optimize the shipping routes and speed of the
528 container liners. The results show that when the membership degrees of the two objective functions
529 are the same and the ECA regulations are considered, the container liners are more likely to opt
530 for longer routes to reduce the shipping distance within the ECA. In addition, the shipping speed
531 in the ECA will be reduced while the speed outside the ECA will be increased to satisfy the time
532 window requirements of the ports.

533 (2) This paper also takes the fluctuation of the fuel price all over the world into consideration
534 and analyzes the cost savings under different fuel prices. It can be seen that the larger difference the
535 fuel price within and outside the ECA, the more savings the model can achieve. The optimization

536 analysis of the example further validates the effectiveness of the model and can also provide great
537 significance to the development of shipping industry.

538 (3) In order to solve the proposed bi-objective mixed integer linear programming optimization
539 model, a two-stage iterative method based on ϵ -constraint is designed. Based on the two objective
540 functions, the searching space of the proposed ϵ -constraint method is narrowed, and thus the
541 searching time for the Pareto optimal solutions is reduced. Moreover, this method can provide a
542 set of Pareto optimal solutions for the decision makers to help them choose the optimal solution
543 under the policy of emission control.

544 (4) Ten shipping routes are included and analyzed by searching the ports within ECAs in China,
545 America, and Europe. By changing the boundaries of the ECAs, the efficiency and practicality
546 of the design of ECA are validated. It is suggested that the shipping companies should use clean
547 energy, low sulfur fuel, filter devices, and on-line monitoring devices, as well as eliminate the
548 old ships to better respond to the increasingly strict sulfur-limiting measures and promote the
549 development of green shipping.

550 The main goal of establishing the ECAs is to reduce SO_2 emissions (as well as NO_x in North
551 America). According to related research, the reduction of SO_2 , NO_x and PM emissions within
552 ECAs is significant and promising. Although there are a large number of sea areas and shipping
553 routes all over the world, the 10 shipping routes in different sea areas are representative. ECA
554 is an important part under the concept of “green shipping”. The choices of shipping speeds and
555 routes under the policy of ECA are key and complex issues, which include model construction and
556 solution, and the choice of subjective and objective factors. When stricter rules on sulfur emissions
557 are implemented, this paper can shed light on the redesign of ECA’s boundaries. This research can
558 not only present the solution of the optimal shipping speeds and routes for companies and states
559 but also be applied to ECA establishment in other areas. For example, the ECA establishment in
560 the Mediterranean.

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