

DDF-ISM: Internal Structure Modeling of Human Head Using Probabilistic Directed Distance Field

Zhuoman Liu, Yan Luximon*, Wei Lin Ng, and Eric Chung

Abstract—The increasing interest surrounding 3D human heads for digital avatars and simulations has highlighted the need for accurate internal modeling rather than solely focusing on external approximations. Existing approaches rely on traditional optimization techniques applied to explicit 3D representations like point clouds and meshes, leading to computational inefficiencies and challenges in capturing local geometric features. To tackle these problems, we propose a novel modeling method called DDF-ISM. It leverages a probabilistic *Directed Distance Field for Internal Structure Modeling*, facilitating efficient and anatomically accurate deformation of different parts of the human head. DDF-ISM comprises two key components: 1) a probabilistic DDF network for implicit representation of the target model to provide crucial local geometric information, and 2) a conditioned deformation network guided by the local geometry. Additionally, we introduce a large-scale dataset of human heads with internal structures derived from high-quality Computed Tomography (CT) scans, along with well-designed template models encompassing skull, mandible, brain, and head surface. Evaluation on this dataset showcases the superiority of our approach over existing methods, exhibiting superior performance in both modeling quality and efficiency.

Index Terms—Head modeling, anatomical model, mesh deformation, distance field.

I. INTRODUCTION

The burgeoning demand for precise 3D human head modeling, driven by advancements in digital avatars [1, 2, 3] and simulation technologies [4, 5], has underscored the critical need to accurately represent not only the external appearance but also the complex internal anatomies of the human head. Such detailed representations are critical for applications ranging from surgical simulations to anthropometric analyses [6, 7], necessitating models that encompass intricate internal structures like bone tissues and the brain. However, obtaining an anatomically accurate model of the internal structures of human heads poses significant challenges.

The first challenge lies in acquiring data related to internal head structures. While external surfaces can be readily captured through conventional scanning technologies and multi-view reconstructions [8, 9, 10], securing detailed internal structural data necessitates more sophisticated approaches. Medical imaging techniques, such as Magnetic Resonance

Imaging (MRI) and Computed Tomography (CT) scans, offer a pathway but come with their own problems, including noises and difficulties in aligning these detailed scans with predefined templates. Furthermore, the oversimplification of template models for internal structures [7, 11, 12] are limited to provide enough information for further applications.

The second challenge is that traditional methods [7, 12, 13, 14] primarily employ optimization techniques on explicit 3D representations like meshes and point clouds, aiming to match correspondences and model internal structures. However, these methods often encounter severe limitations, including computational inefficiency and difficulties in capturing fine local geometric details. IFMatch [15] proposes an efficient matching approach based on signed distance fields (SDFs) [16]. An SDF-based method utilizes volumetric representations to encode shape information but may face challenges with symmetric objects [17], where different locations can share the same distance value despite distinct geometric meanings, a situation frequently observed in anatomical structures.

Addressing the challenge of data acquisition, we present a comprehensive dataset featuring detailed internal structures of human heads derived from high-fidelity CT scans. This dataset, covering a demographic spread of 100 adults aged 18 to 65, is designed to provide a wide range of anatomical accuracy. Accompanied by precisely designed template models, including the skull, mandible, brain, and head surface, this resource aims to overcome the prevalent issues of noise and alignment common in medical imaging data. The inclusion of high-resolution imagery and detailed templates makes this dataset a critical source for enhancing the accuracy of internal structure modeling.

In response to the challenge in modeling, we propose a novel approach, DDF-ISM, which leverages a probabilistic directed distance field (DDF) [18] for modeling the anatomical internal structures of human heads. The DDF-ISM framework consists of two primary components: 1) a conditioned deformation network trained to learn deformations on a template model and 2) a probabilistic DDF network that implicitly represents the target model and provides crucial local geometric information to the deformation network. By integrating *directed* distance fields and *conditioning* mechanism, our method enables efficient deformation of various symmetric components of the head while maintaining anatomical accuracy. Furthermore, through rigorous evaluations of the proposed dataset, we demonstrate the superior performance of our method compared to existing point-based and SDF-based modeling methods, both in terms of modeling quality and computational efficiency.

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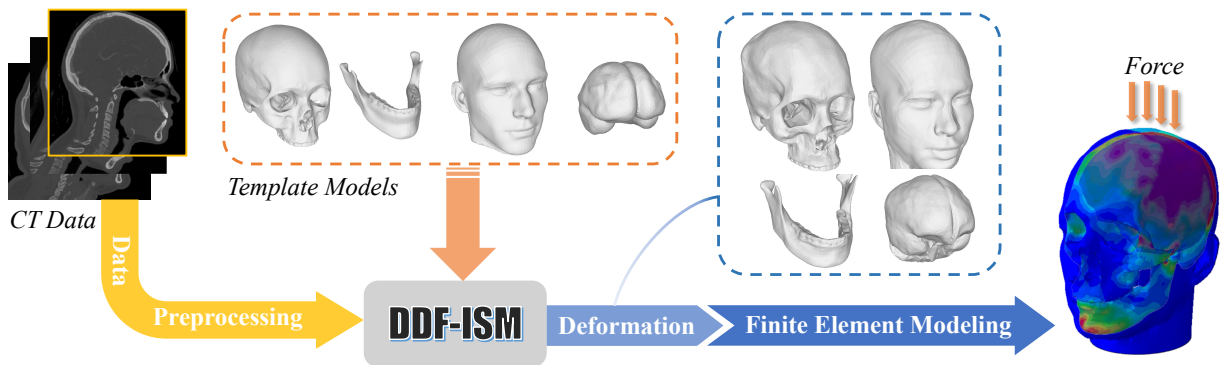


Fig. 1: **Internal structure modeling workflow.** This diagram outlines the key stages from CT data acquisition to deformation and simulation, highlighting the integration of DDF-ISM and finite element modeling for precise biomechanical analysis.

Our main contributions are summarized as follows:

- We propose DDF-ISM, a novel modeling framework for accurately modeling the internal structures of human heads with geometric guidance.
- We integrate the directed distance field (DDF) to capture geometry features that are robust to symmetry, enabling efficient and anatomically accurate deformations.
- We construct a comprehensive dataset of human heads with internal structures derived from CT scans, along with well-designed template models for benchmarking.
- Extensive experiments show the superior performance of DDF-ISM over existing point-based and SDF-based modeling methods. We also conduct the application of finite element modeling based on our deformed head models to show the effectiveness of the proposed method.

II. RELATED WORK

A. Data Sources for 3D Head Modeling

The foundation of 3D human head modeling resides in the meticulous acquisition of precise data. Traditional methodologies have predominantly focused on external detail capture through advanced techniques such as laser scanning, structured light systems, and photogrammetry. The most esteemed human head datasets [19, 20, 21, 22] in the literature, constructed utilizing multi-camera stereo systems, offer comprehensive variations in pose, shape, and expression. However, these approaches often do not adequately address the capture of internal anatomical features essential for a broad range of applications, including detailed medical analyses and the generation of realistic digital human avatars.

Recent developments have prompted a shift toward the integration of medical imaging technologies, such as Computed Tomography (CT) and Magnetic Resonance Imaging (MRI), for the acquisition of intricate internal anatomical details. CT scans, distinguished by their superior spatial resolution, have emerged as invaluable for their precise differentiation between bone and soft tissue, offering remarkable clarity. This advancement in data collection methods represents a notable transition from mere surface capture to the acquisition of detailed internal structures, broadening the utility of models across diverse fields, from medical diagnostics to the animation of digital humans. Notably, [23] introduces a human

head dataset integrating full-head CT and facial scans, aimed at advancing craniofacial reconstruction techniques. Besides, SCULPTOR [12] presents the LUCY dataset, a unique collection of shape and skeleton-correlated facial data derived from pre- and post-surgery CT scans, designed to support further facial editing applications.

In addition, template models of human head for parameterization have a profound impact on the functionality of subsequent simulation applications. The design strategy of template models significantly varies, directly influencing the scope and precision of the model’s applicability. Specifically, methods focusing on facial features [19, 24] tend to only parameterize the facial area, potentially overlooking the overall representation necessary for comprehensive applications. Moreover, current approaches that consider internal anatomical structures [7, 11, 12] employ overly simplified template models for parameterization, lacking in detail. Such simplifications can limit the effectiveness of the model in simulations, which require high fidelity to real-world anatomical complexities.

B. 3D Morphable Models

3D Morphable Models (3DMMs) have emerged as a key technique in computer vision and graphics, enabling the representation and manipulation of 3D shapes and textures from limited data inputs. Traditional 3DMMs [25] create a statistical model of 3D facial shape and texture, allowing for the generation of novel faces by altering model parameters. The integration of deep learning with 3DMMs has revolutionized the field. [26] proposed a deep convolutional neural network to learn 3DMM parameters directly from images, bypassing the traditional optimization-based fitting methods. This approach, termed Deep 3DMMs, demonstrated superior performance in terms of speed and accuracy, facilitating real-time applications.

Recent works have extended 3DMMs to encompass additional anatomical structures. For instance, FLAME [19] incorporates facial expressions, enhancing the dynamic representation of facial movements. A combined model of the scalp and skull [11] offers a more comprehensive head model, essential for medical and forensic applications. Addressing the variability in scalp shape under hair, a parametric head model considering scalp shape under hair was proposed [24]. SCULPTOR [12] integrates internal skull and mandible structures, ensuring anatomical consistency in generated faces. A

head geometry model accounting for variations in brain structures among different age groups has been introduced [7], beneficial for developmental biology and characterized medicine.

Despite these advancements, a comprehensive model that includes more internal anatomical structures of the head is still evolving. Our approach aims to address this gap by developing a morphable model that includes more detailed head internal structures. By integrating features of the head surface, skull, mandible, and brain, our model enhances accuracy and utility across various applications.

C. 3D Head Deformation

In the process of parametric modeling, vertices are sampled on meshes for matching with the template model, followed by the deformation of the template. Traditional methods typically involve point-based optimization during modeling. A classic non-rigid deformation method focused on points is the Coherent Point Drift (CPD) [27], which also has a variant guided by landmarks, known as LGCPD [13]. However, when the number of vertices to be modeled is large or the deformation is significant, these methods require substantial computational memory and suffer from reduced processing speed, leading to less accurate deformation results.

To address these challenges, some approaches utilize hierarchical structures to reduce computational memory while simultaneously improving modeling precision. For instance, Neural Deformation Pyramid (NDP) [14] utilizes a pyramid structure with Multi-Layer Perceptrons (MLPs) [28] at each level to process sinusoidally encoded 3D points, enabling incremental non-rigid deformations. Similarly, SCULPTOR [12] utilizes control nodes to accelerate deformation, incorporating landmarks for more precise guidance. Besides, attention mechanisms have been employed to enhance shape deformation accuracy by capturing geometric relationships. [29] is the first to apply an attention module for shape deformation, showcasing its potential in non-rigid transformations.

Despite these advancements, point-based modeling approaches continue to be encumbered by their computational speed. Leveraging advancements in implicit functions, IF-Match [15] introduces a paradigm shift by utilizing Signed Distance Functions (SDFs) [16] for geometrically representing target objects, coupled with the deployment of an MLP-based network for learning deformations, thus significantly enhancing computational efficiency. Nonetheless, the application of SDF-based matching to anatomical head modeling can benefit from enhancements in capturing geometric features. While SDF effectively encodes shape information, incorporating directional information (*i.e.*, DDF [18]) alongside point queries may offer advantages in better representing the intricate geometry of symmetrical structures [17]. This approach could provide a more detailed representation of anatomical features compared to traditional SDF-based methods.

III. OVERVIEW

In this work, we introduce DDF-ISM, a novel parametric anatomical head model that integrates comprehensive internal

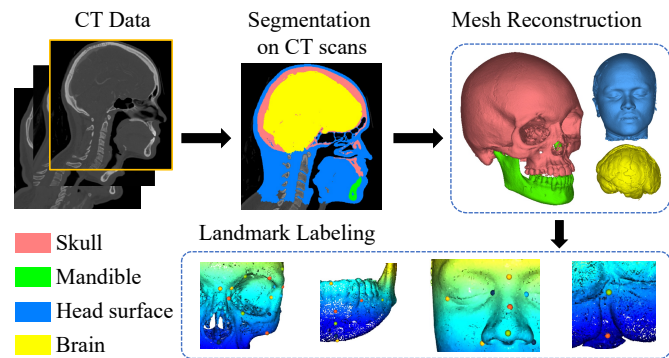


Fig. 2: Overall workflow of data preprocessing of CT scans.

structures to enhance medical imaging simulations and diagnostics. Our approach includes the development of a large-scale anatomical head dataset comprising CT scans, segmented meshes, labeled landmarks, and meticulously designed template models. We propose the utilization of a directed distance field (DDF) to innovatively guide the mesh deformation. This methodology aims to tackle significant challenges in data construction and parametric modeling, particularly those related to anatomical accuracy and computational efficiency. The structure of this paper is organized as follows: we begin with a detailed description of the data acquisition and processing, proceed to elaborate on the network architectures, the training and inference processes, and conclude with experimental results and analyses.

IV. DATA CONSTRUCTION

A. Data Acquisition of CT Scans

In collaboration with experts from a Malaysian hospital, we ethically collected CT data following approval from the university’s ethics committee (HSEARS20210804001). This dataset encompasses all parts of the human head, clearly capturing the necessary anatomical details that are essential for subsequent 3D model fitting. Specifically, this dataset includes scans from 100 Malaysian adults, whose ages range from 18 to 65. To facilitate robust analysis and minimize biases associated with age and gender, we organized the participants into five age groups (*i.e.*, 18-25, 26-35, 36-45, 46-55, and 56-65), collecting 20 CT scans for each category. Each group maintains an equal distribution of male and female participants, thereby reducing potential analytical discrepancies due to age and gender differences. These scans were captured at a resolution of $0.54 \times 0.54 \times 1 \text{ mm}^3$, providing the high-resolution data necessary for precise anatomical modeling and the accurate depiction of complex structures in subsequent parametric modeling. This high level of detail is crucial for the effective segmentation and modeling processes that follow.

B. Data Preprocessing

The preprocessing of the collected CT scans involves two critical steps: segmentation and downsampling. In the segmentation phase, we employ Materialise Mimics¹ to delineate

¹www.materialise.com/en/healthcare/mimics-innovation-suite/mimics

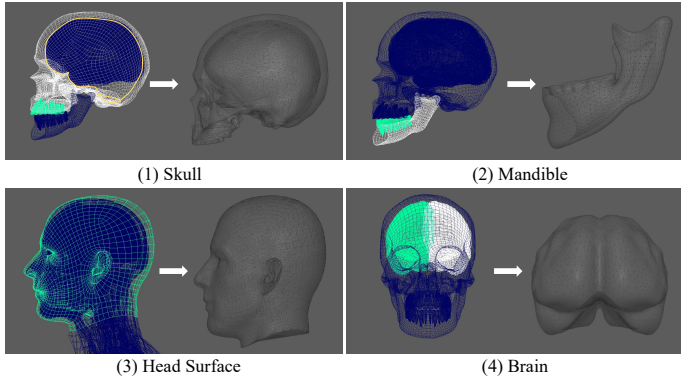


Fig. 3: Template construction from source models.

four key anatomical parts of the human head (*i.e.*, skull, mandible, head surface, and brain) from a series of 2D CT images, subsequently reconstructing individual 3D meshes for each part. Initially, we apply predefined thresholds within the software to automatically extract masks for bone and soft tissue structures. Following this, as illustrated in Fig. 2, the bone is further segmented into two distinct components: the skull (shown in pink) and the mandible (shown in green), through manual labeling of multiple masks across three views, *i.e.*, axial, coronal, and sagittal. In a similar manner, the soft tissue is divided into the head surface (shown in blue) and the brain (shown in yellow). Once segmentation is complete, the software calculates the meshes for these four structures.

Given that the original meshes are overly dense for effective 3D registration, a downsampling process is implemented. This involves using a uniform sampling filter to reduce mesh density according to a specified percentage, denoted by σ . Specifically, we set $\sigma = 0.8$ for the skull and head surface, and $\sigma = 1.5$ for the mandible and brain, corresponding to a downsampling factor of approximately 100. This adjustment ensures that the meshes are optimized for subsequent computational tasks without compromising the structural integrity and detail required for accurate modeling and analysis.

C. Template Model Construction

Prior to exploring the approach for 3D mesh deformation, it is imperative to develop template models for the four key anatomical components of the human head. We acquired a detailed 3D human model, including comprehensive anatomical structures, from TurboSquid. Using Autodesk Maya, we extracted and refined key components for template construction: the skull with upper teeth, the mandible with bottom teeth, the head surface, and the brain, as shown in Fig. 3. Refinements included merging and cleaning intersections, closing open surfaces, aligning the brain with the skull’s inner surface, and resampling and smoothing meshes. These processes ensured the templates retained sufficient detail for comprehensive biomechanical analyses.

The refined template models are characterized by their intricate structures and are depicted in Fig. 4, which provides both a visual representation and detailed geometric data under X-Ray rendering. We denote the template model as $\bar{\mathbf{T}} =$

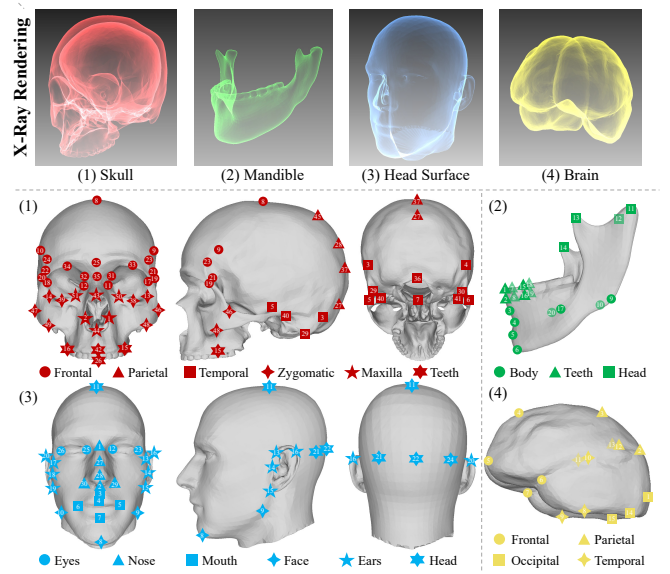


Fig. 4: Anatomical template models with regional landmarks of four key parts of human head.

$\{\bar{\mathbf{T}}_{skl}, \bar{\mathbf{T}}_{mdb}, \bar{\mathbf{T}}_{surf}, \bar{\mathbf{T}}_{brn}\}$, including skull, mandible, head surface, and brain. Specifically, the skull model comprises $N_{skl} = 21,294$ vertices with 42,597 polygons; the mandible model includes $N_{mdb} = 4,000$ vertices with 8,008 polygons; the head surface is detailed with $N_{surf} = 20,234$ vertices and 40,464 polygons; and the brain includes $N_{brn} = 4,838$ vertices with 9,672 polygons. Additionally, we build an internal structure of the skull closely matching the brain’s surface to facilitate realistic simulations.

D. Landmark Labeling

In conjunction with the development of templates and subsequent preprocessing of meshes, we define and label anatomical landmarks to facilitate semantic information for modeling. As illustrated in Fig. 4, we define $K_{skl} = 51$ landmarks for the skull, $K_{mdb} = 14$ for the mandible, $K_{surf} = 30$ for the head surface, and $K_{brn} = 15$ for the brain. The definitions of these landmarks are guided by the anatomy of each part, drawing from established standards in the field. Specifically, the landmark definitions for the skull and mandible models are adapted from [30]. Specifically, we separate the skull into six anatomical regions, including frontal, parietal, temporal, zygomatic, maxilla, and teeth, while mandible is divided into three regions, *i.e.*, body, teeth, and head. Similarly, we separate the head surface into six regions, *i.e.*, eyes, nose, mouth, face, ears, and head, while brain is divided into four regions, including frontal, parietal, occipital, and temporal. We split out these anatomical regions to further analyze the modeling errors of each region. For the landmarks annotated for templates, we denote them as $\bar{\mathbf{x}}_{lmk} = \{\bar{\mathbf{x}}_{lmk}^{skl}, \bar{\mathbf{x}}_{lmk}^{mdb}, \bar{\mathbf{x}}_{lmk}^{surf}, \bar{\mathbf{x}}_{lmk}^{brn}\}$. For the landmarks labeled for the target meshes, we denote them as $\mathbf{x}_{lmk} = \{\mathbf{x}_{lmk}^{skl}, \mathbf{x}_{lmk}^{mdb}, \mathbf{x}_{lmk}^{surf}, \mathbf{x}_{lmk}^{brn}\}$.

Besides, before internal structure modeling, we apply rigid alignment using iterative closest point (ICP) algorithm [31] to coarsely align the preprocessed target meshes to the templates.

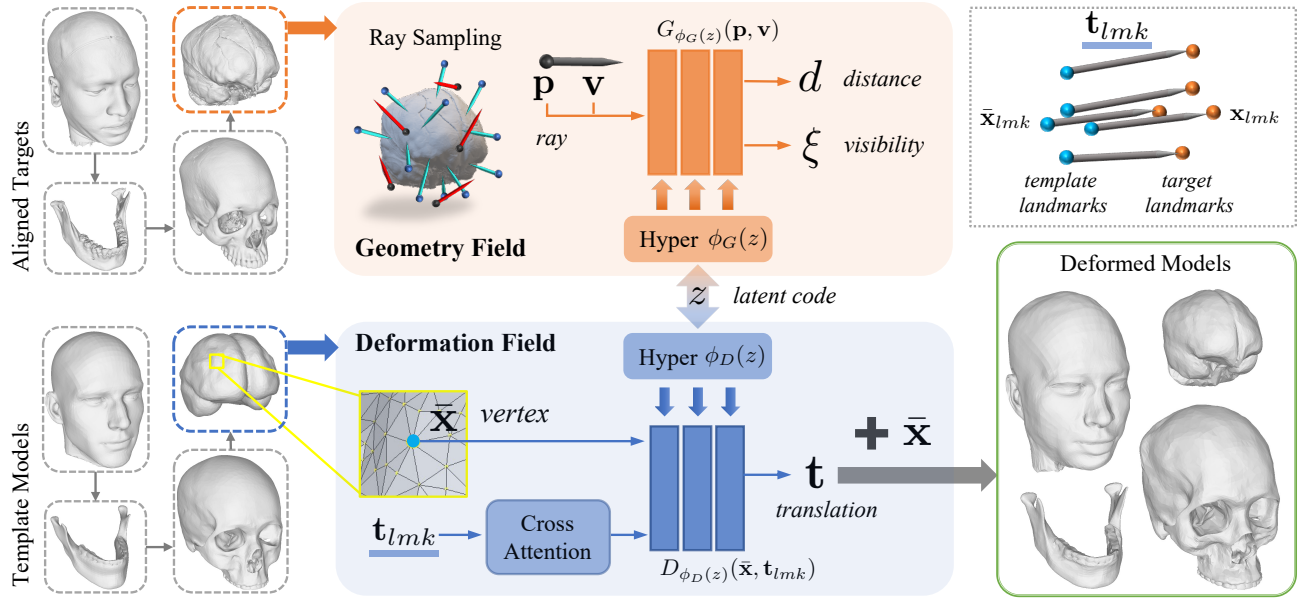


Fig. 5: The overall pipeline of DDF-ISM. Starting with the alignment of target and template models, the pipeline proceeds through the stages of ray sampling, distance computation, and visibility assessment. It then leverages the geometry and deformation fields, guided by latent codes, to achieve precise deformation of the template model. The cross-attention mechanism ensures the accurate translation of vertices, resulting in a deformed model that closely matches the target’s anatomical features.

342 We select 5 landmarks from $\bar{\mathbf{x}}_{lmk}^{surf}$ and \mathbf{x}_{lmk}^{surf} (label 8, 11, 22, 23, 26 in Fig. 4 (3)), respectively. With the paired landmarks, we compute the coarse transformation and scale and perform them on the four anatomical parts of target meshes to obtain aligned targets $\bar{\mathbf{M}} = \{\bar{\mathbf{M}}_{skl}, \bar{\mathbf{M}}_{mdb}, \bar{\mathbf{M}}_{surf}, \bar{\mathbf{M}}_{brn}\}$. With the template models $\bar{\mathbf{T}}$ and aligned targets $\bar{\mathbf{M}}$, we discuss how to model these internal structures of human head in next section.

349 V. INTERNAL STRUCTURE MODELING

350 The process of internal structure modeling is crucial for creating an accurate and comprehensive 3D representation of the human head. Our approach meticulously integrates various anatomical details, including the skull, mandible, head surface, and brain, to enhance both the accuracy and utility of the model. We develop a **geometry field** to capture local geometric features of each anatomical part and propose a **deformation field** to learn the deformation on vertices from templates to targets. A *latent code* is then introduced to transfer geometric information from the geometry field and as the *condition* for the deformation field. The overall pipeline of our method is shown in Fig. 5.

362 A. Geometry Field

363 The geometry field G is a probabilistic directed distance field (DDF) [18], which takes a ray originated at point \mathbf{p} with a view direction \mathbf{v} as input and predicts the distance value d and binary visibility ξ . The visibility $\xi = 1$ indicates the surface is visible from the ray viewpoint. When the surface is visible, we have distance value $d \geq 0$, which is the distance from \mathbf{p} to the surface along \mathbf{v} . To transmit the geometric information to the subsequent deformation field, we introduce a latent code $z \in \mathbb{R}^{C_z}$ and a hypernetwork [32] $\phi_G(z)$. Since the DDF requires

372 only one query to obtain the surface distance, it is efficient to provide geometric information. Meanwhile, the query here is directional, so the geometric information provided by the DDF is not ambiguous for the approximately symmetric internal structure of the human head.

373 **Ray sampling.** We sample multiple rays in free space according to some criteria to learn the whole geometry of the target mesh. Following [18], we apply three data types for ray sampling, *i.e.*, *Uniform (U)*, *Bounding (B)*, and *Surface (S)*. We visualize the sampled rays in Fig. 5, with rays that successfully hit the surface colored in green ($\xi = 1$) and rays that miss the surface colored in red ($\xi = 0$). More details of ray sampling are in Sec. VII-A.

374 **Loss terms.** During ray sampling, it is intuitive to acquire the ground-truth distance d and visibility ξ . Therefore, we have distance loss \mathcal{L}_d using ℓ_1 loss and visibility loss \mathcal{L}_ξ using binary cross entropy as follows: 375 376 377 378 379 380 381 382 383 384 385 386 387 388

$$\mathcal{L}_d = \xi |\hat{d} - d|, \text{ where } \hat{d} = \hat{d}_{i^*}, i^* = \arg \max_i w_i \quad (1)$$

$$\mathcal{L}_\xi = BCE(\hat{\xi}, \xi) \quad (2)$$

389 In the paper, we set $K = 2$, which means the geometry network outputs two distance values with weights w_0, w_1 and $\sum_i w_i = 1$ to handle the discontinuity of vanilla DDF. Besides, we adopt the proposed weight field regularizations in [18], *i.e.*, weight variance loss $\mathcal{L}_V = \prod_i w_i$ and weight transition loss $\mathcal{L}_T = \max(0, \varepsilon_T - |\nabla_{\mathbf{p}} w_0 \hat{\mathbf{n}}|)$. Specifically, $\hat{\mathbf{n}}$ is the surface normals computed from the derivative of predicted distance \hat{d} w.r.t. the ray view point \mathbf{p} , *i.e.*, $\hat{\mathbf{n}} = \tau \nabla_{\mathbf{p}} \hat{d} / \|\nabla_{\mathbf{p}} \hat{d}\|^2$, where $\tau \in \{-1, 1\}$ is the sign to make sure $\hat{\mathbf{n}}^T \mathbf{v} < 0$.

390 Moreover, according to the geometric properties of DDF [18], we have constraints on distance, visibility, and 391 392 393 394 395 396 397 398 399 400

401 surface normals. We adopt the directed Eikonal regularization
402 \mathcal{L}_{DE} and first-order normals loss \mathcal{L}_n from [18] as follows:

$$\mathcal{L}_{DE} = \lambda_{E,d} \sum_{i=0}^K \xi(\nabla_{\mathbf{p}} \hat{d}_i \mathbf{v} + 1)^2 + \lambda_{E,\xi} (\nabla_{\mathbf{p}} \hat{\xi} \mathbf{v}) \quad (3)$$

$$\mathcal{L}_n = -\xi |\mathbf{n}^T \hat{\mathbf{n}}_{i^*}| \quad (4)$$

404 In summary, we have a geometry loss $\mathcal{L}_G = \lambda_d \mathcal{L}_d + \lambda_\xi \mathcal{L}_\xi +$
405 $\lambda_V \mathcal{L}_V + \lambda_T \mathcal{L}_T + \lambda_{DE} \mathcal{L}_{DE} + \lambda_n \mathcal{L}_n$.

406 B. Deformation Field

407 Mesh deformation is a critical component of fitting the
408 morphable model to the target data. The deformation field
409 $D_{\phi_D}(z)(\bar{\mathbf{x}}, \mathbf{t}_{lmk})$ operates on the vertex $\bar{\mathbf{x}}$ from template model
410 with the landmark translations $\mathbf{t}_{lmk} = \mathbf{x}_{lmk} - \bar{\mathbf{x}}_{lmk}$, then learn
411 the translation \mathbf{t} from the template to target. By applying the
412 predicted translation on the template vertex, we can obtain
413 the deformed mesh with new vertex $\hat{\mathbf{x}} = \bar{\mathbf{x}} + \hat{\mathbf{t}}$. It is noted
414 that \mathbf{t}_{lmk} is fed into a cross-attention module [33] to extract
415 the potential geometric relationship between the template and
416 targets. Then the landmark translation features are concate-
417 nated with $\bar{\mathbf{x}}$ as inputs of D . Similar to the geometry field,
418 we introduce a hypernetwork $\phi_D(z)$ for the deformation field.
419 The latent code z passes geometric features through ϕ_D
420 to the deformation network D . Therefore, this field allows for
421 the precise translation of vertices, ensuring that the deformed
422 models accurately represent the target anatomical structures.
423 The cross-attention mechanism facilitates the refinement of
424 these deformations by considering the relationship between
425 the template and target landmarks.

426 **Loss terms.** After deformation, we have a new set of vertices
427 of each part, denoted as $\hat{\mathbf{X}}_{part} \in \mathbb{R}^{N_{part} \times 3}$, where $part \in$
428 $\{skl, mdb, surf, brn\}$. With the vertices $\mathbf{X}_{part} \in \mathbb{R}^{N \times 3}$ from
429 target \mathbf{M}_{part} (N is the number of vertices of target mesh), we
430 minimize ℓ_2 Chamfer-Distance [34] for shape fitting.

$$\mathcal{L}_{CD} = CD(\hat{\mathbf{X}}_{part}, \mathbf{X}_{part}) \quad (5)$$

431 In addition, we minimize the ℓ_2 distances between deformed
432 landmarks and target landmarks using a landmark loss \mathcal{L}_{lmk} .
433 To preserve the smoothness of deformed surface, we add a
434 smoothness regularization \mathcal{L}_{smooth} by controlling the gradi-
435 ents of deformation field.

$$\mathcal{L}_{lmk} = \|\hat{\mathbf{x}}_{lmk} - \mathbf{x}_{lmk}\|_2 \quad (6)$$

$$\mathcal{L}_{smooth} = \|\nabla_{\bar{\mathbf{x}}} \mathbf{t}\|_2 \quad (7)$$

437 In summary, we have a deformation loss $\mathcal{L}_D = \lambda_{CD} \mathcal{L}_{CD} +$
438 $\lambda_{lmk} \mathcal{L}_{lmk} + \lambda_{smooth} \mathcal{L}_{smooth}$.

439 C. Training

440 When training both the geometry field and deformation
441 field, we introduce a regularization $\mathcal{L}_z = \|z\|_2$ on latent
442 code. Therefore, when learning the morphable model of one
443 of the anatomical parts, we minimize the total loss $\mathcal{L} =$
444 $\mathcal{L}_G + \mathcal{L}_D + \mathcal{L}_z$. Furthermore, as shown in Fig. 5, to reduce
445 collisions among the four anatomical parts, we learn the
446 morphable models in the order of brain, skull, mandible, then

447 head surface. For collision detection, we convert the DDF
448 values to signed distances [18] and eliminate intersections by
449 pushing vertices out of the volume.

450 D. Inferencing

451 Our method employs an optimization-based strategy, lever-
452 aging hypernetworks to dynamically generate parameters for
453 shape deformation during fitting. To infer deformed models of
454 new subjects, we first load the pre-trained geometry field G
455 and minimize \mathcal{L}_G to obtain initial latent code \hat{z} . Subsequently,
456 we load the pre-trained deformation field D and minimize
457 \mathcal{L}_{CD} and \mathcal{L}_{lmk} to obtain the optimized latent code \tilde{z} (ex-
458 cluding the smoothness term to reduce gradient computation
459 time). With \tilde{z} , we can infer the deformation field D to obtain
460 translations and then get the morphable model.

461 VI. APPLICATION

462 Finite Element Analysis (FEA) is a critical application of
463 our anatomical head model. By providing accurate represen-
464 tations of the skull, mandible, head surface, and brain, it
465 is straightforward to use our model for precise simulation
466 of physical forces and their effects on human head. This is
467 particularly valuable in medical fields such as neurosurgery,
468 orthodontics, and craniofacial surgery, where understanding
469 the impact of surgical interventions on the entire head anatomy
470 is crucial. In this study, we use a software called ABAQUS
471 for FEA, and the pipeline of FEA is as follows:

- 472 1) **Mesh Generation:** We first randomly select one participant
473 from our dataset, then by applying our DDF-ISM on the CT
474 data, we can obtain the morphed models of skull, mandible,
475 head surface, and brain. Before performing FEA, we add
476 ligaments between skull and mandible (label 40 of \mathbf{x}_{lmk}^{skl}
477 and label 11 of \mathbf{x}_{lmk}^{mdb} , label 41 of \mathbf{x}_{lmk}^{skl} and label 12 of \mathbf{x}_{lmk}^{mdb})
478 as constraints. Besides, a boolean operation is conducted
479 on the bone (including both skull and mandible) and head
480 surface to obtain the mesh of soft tissue. Then, the skull,
481 mandible, soft tissue, and brain can be assembled to form a
482 Parasolid file of the human head as a finite element model.
- 483 2) **Material Properties:** After loading the above finite el-
484 ement model in ABAQUS, we set appropriate material
485 properties [35] for different head regions as shown in Table
486 I, where ρ is density, E is elastic modulus, and ν is poisson
487 ratio. The material properties are assigned to corresponding
488 parts respectively.
- 489 3) **Impact Force and Boundary Condition:** To simulate the
490 impacts of an external force on different parts of the human
491 head, we apply an impact force of 100N directed along the
492 negative Y-axis at the head vertex, over an area of $50 \times$
493 50 mm^2 , as shown in Fig. 6 (a). The bottom of the soft
494 tissue (neck) is constrained as a fixed boundary condition
495 throughout the simulation process.
- 496 4) **Simulation and Analysis:** In Fig. 6 (b) and (c), we show
497 the simulation results at two scales after applying the
498 impact force on the head vertex. For visualization, the
499 maximum von Mises stress is 0.2 MPa for the soft tissue
500 scale and 50 MPa for bone scale. The top of soft tissue,

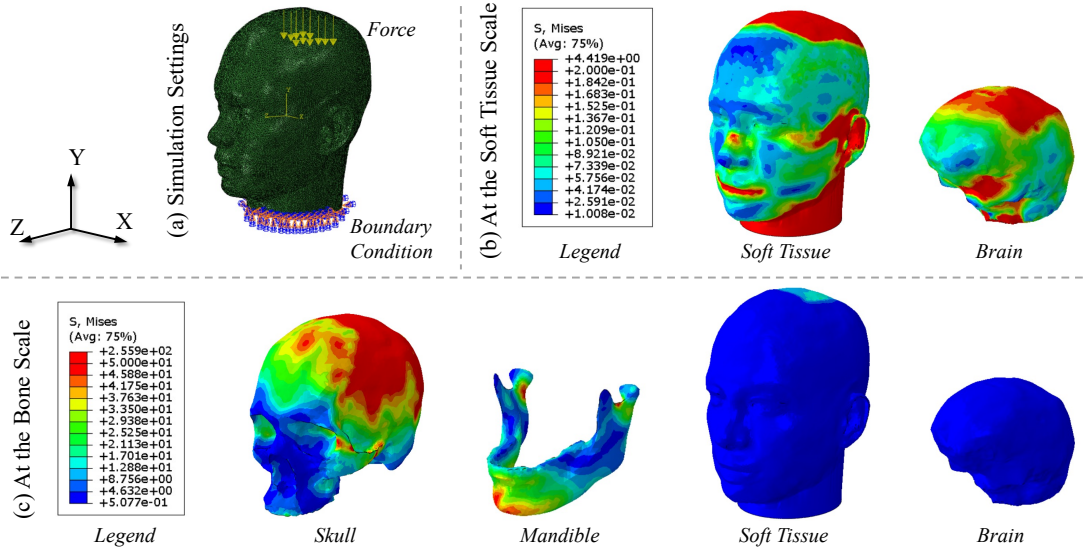


Fig. 6: Illustration of simulation settings and FEA results of different parts. This illustration presents the Von Mises stress distribution across various components within a biomechanical model. The legend provides a guide to the stress values, indicating the structural integrity and potential areas of concern within the model.

TABLE I: Material properties for different anatomical parts in a biomechanical model.

Part	$\rho \times 10^{-8}$ (kg/mm ³)	E (MPa)	ν	Material Type	Element Type
Bone and ligament	193.5	4096.8	0.22	Elastic	C3D4
Soft tissue	140.0	0.7	0.45	Elastic	C3D4
Brain	104	1.58	0.5	Viscoelastic	C3D4H

direction are selected randomly from the surface of a sphere. To optimize the geometry field, the geometry loss includes distance loss \mathcal{L}_d , visibility loss \mathcal{L}_ξ , weight variance loss \mathcal{L}_V , and weight transition loss \mathcal{L}_T , with specific regularizations (*i.e.*, \mathcal{L}_{DE} and \mathcal{L}_n) to handle the symmetry and discontinuities of the human head’s internal structures.

brain, and skull are in red, indicating the highest stress. It is noted that the bottom of soft tissue, *i.e.*, the neck part, and the bottom of mandible are also in red, it is because the constraints when applying impact force are set at the neck, therefore, the bottom of soft tissue takes counterforce and squeezes the bottom of mandible. The results show accurate stress of the four anatomical parts according to the force, demonstrating that our DDF-ISM is feasible to work for precise simulations.

VII. EXPERIMENTS

A. Implementation Details

Our implementation leverages a multi-stage process for training the geometry and deformation fields. The training process begins with the acquisition of CT scans, followed by segmentation and mesh reconstruction of the skull, mandible, head surface, and brain. These segmented meshes serve as the basis for training our DDF-ISM.

For the **geometry field**, we utilize a combination of *Uniform (U)*, *Bounding (B)*, and *Surface (S)* ray sampling strategies [18] to train, ensuring comprehensive coverage of the target mesh’s geometry. In the Uniform way, a point is sampled randomly from within a specified boundary, and a direction is chosen randomly from the surface of a sphere. In the Bounding way, the point is selected randomly from the boundary itself, and the direction is also chosen from the surface of the sphere, but with the restriction that it points toward the interior of the boundary. In the Surface way, both the point and the

For the **deformation field**, we implement the cross-attention module following [33]. The cross-attention module captures the geometric relationship between the template and target models by processing the landmark translations. This helps to enhance the accuracy of the deformation process by allowing the model to better understand how the template should be adjusted to match the target. The deformation loss incorporates Chamfer Distance loss \mathcal{L}_{CD} , landmark loss \mathcal{L}_{lmk} , and smoothness regularization \mathcal{L}_{smooth} , balancing shape-fitting accuracy with smooth surface transitions.

To train the two fields for each internal structure of the human head, we use SIREN (MLPs using Sine activation) [36]. The geometry field $G_{\phi_G(z)}$ is modeled using three hidden layers with 256 hidden units, while the deformation field $D_{\phi_D(z)}$ employs five hidden layers to incorporate the cross-attention features, with 512 hidden units. The latent dimension is set to 512. DDF-ISM is implemented by PyTorch and the network is optimized using the Adam optimizer [37] with a learning rate of 0.0001 over 50 iterations on a single NVIDIA RTX 3090 GPU.

The inference phase involves loading the pre-trained geometry and deformation fields and optimizing the latent codes to fit new subject data with the same settings as the above training phase. The operation of latent code optimization in the inference phase ensures that the deformed models accurately represent the anatomical structures of new subjects while maintaining computational efficiency.

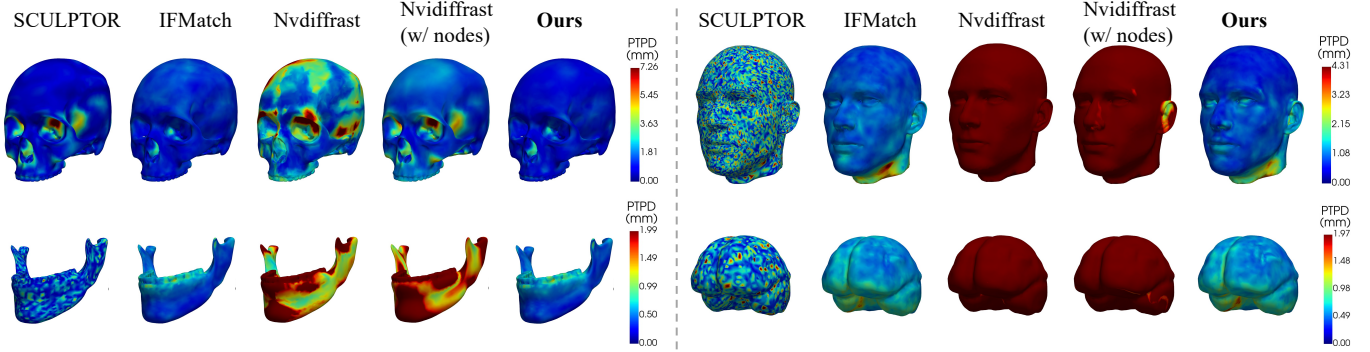


Fig. 7: Comparison of PTPD between different methods on the four anatomical parts. The lower the PTPD value (blue), the closer the deformed mesh is to the target mesh, indicating better performance.

TABLE II: PTPD (mm) ↓ and $RMSE_{lmk}$ (mm) ↓ (mean ± std. dev.) for different methods on four anatomical parts.

	Head Surface		Brain		Skull		Mandible		Avg.	
	PTPD	$RMSE_{lmk}$	PTPD	$RMSE_{lmk}$	PTPD	$RMSE_{lmk}$	PTPD	$RMSE_{lmk}$	PTPD	$RMSE_{lmk}$
SCULPTOR [12]	1.41	6.46 ± 2.78	0.61	6.73 ± 3.68	1.50	6.21 ± 3.63	0.42	2.86 ± 1.72	0.99	5.57 ± 2.95
IFMatch [15]	1.16	8.47 ± 4.11	0.68	23.02 ± 10.63	1.27	7.42 ± 4.87	0.51	4.40 ± 2.60	0.91	10.83 ± 5.55
Ours	0.95	4.33 ± 2.34	<u>0.66</u>	3.78 ± 2.15	1.06	3.92 ± 2.48	<u>0.46</u>	2.39 ± 1.31	0.78	3.61 ± 2.07
Nvdiffrast [38]	14.21	23.83 ± 10.14	7.64	29.62 ± 10.71	3.19	13.68 ± 7.76	2.33	10.86 ± 5.56	6.84	19.50 ± 8.54
Nvdiffrast [38] (w/ nodes)	6.48	13.28 ± 18.79	13.08	28.63 ± 16.63	2.10	6.77 ± 4.37	2.11	7.06 ± 3.27	5.94	13.94 ± 10.77
Ours (w/o CA, dim=512)	<u>0.97</u>	7.27 ± 5.39	0.70	17.37 ± 8.52	<u>1.11</u>	<u>5.94 ± 4.27</u>	0.48	4.13 ± 2.27	<u>0.82</u>	8.67 ± 5.11
Ours (w/o CA, dim=256)	1.05	7.41 ± 5.47	0.71	17.83 ± 8.75	1.15	6.07 ± 4.28	0.51	4.29 ± 2.37	0.86	8.90 ± 5.22

TABLE III: Region-specific errors $RMSE_{reg}$ (mm) ↓ (mean ± std. dev.) for different methods on *head surface*.

	Eyes	Nose	Mouth	Face	Ears	Head	Avg.
SCULPTOR [12]	5.43 ± 2.36	4.26 ± 1.55	4.61 ± 2.12	15.31 ± 6.50	6.80 ± 2.98	5.77 ± 2.66	6.46 ± 2.78
IFMatch [15]	6.19 ± 3.11	4.06 ± 2.07	7.13 ± 3.87	11.59 ± 5.50	9.18 ± 4.69	15.29 ± 6.27	8.47 ± 4.11
Ours	3.85 ± 1.90	2.97 ± 1.51	3.41 ± 1.68	5.85 ± 3.07	4.70 ± 2.86	<u>6.11 ± 3.22</u>	4.33 ± 2.34

TABLE IV: Region-specific errors $RMSE_{reg}$ (mm) ↓ (mean ± std. dev.) for different methods on *brain*.

	Frontal	Parietal	Occipital	Temporal	Avg.
SCULPTOR [12]	5.16 ± 2.19	5.02 ± 1.90	7.17 ± 2.27	9.71 ± 2.31	6.73 ± 3.68
IFMatch [15]	16.35 ± 6.37	24.53 ± 8.19	22.26 ± 5.15	28.76 ± 5.80	23.02 ± 10.63
Ours	3.57 ± 2.10	4.01 ± 2.22	3.55 ± 2.22	3.94 ± 2.05	3.78 ± 2.15

561 **B. Evaluations**

562 **Comparing methods.** In our experiments, we compare the
 563 performance of our DDF-ISM with existing state-of-the-art
 564 methods SCULPTOR [12] and IFMatch [15], as well as
 565 differentiable rendering-based shape fitting method (*i.e.*, Nvd-
 566 iffrast [38]). SCULPTOR models not only the head surface but
 567 also the internal structures of the skull and mandible. However,
 568 SCULPTOR is developed on explicit mesh geometric repre-
 569 sentation, making it significantly slower. IFMatch introduces
 570 the use of implicit geometric representation combined with
 571 deformation to enhance speed. This approach contrasts with
 572 SCULPTOR and aligns more closely with our method’s goals
 573 of efficiency and effectiveness. To evaluate Nvdiffrast with
 574 multi-view L_2 loss on mesh normals, we optimize vertex
 575 deformations over 500 random viewpoints for 200 iterations.
 576 Additionally, we implement a version with control nodes
 577 (*w/ control nodes*) based on SCULPTOR’s strategy. For a
 578 fair comparison, all baselines are supervised with the same

579 sampled rays and points as ours, validated through 5-fold
 580 cross-validation. The 100 scans were randomized and divided
 581 into five groups (20 scans each), with one group used as the
 582 test set and the remaining four as the training set, repeated
 583 across five iterations.

584 **Evaluation metrics.** The evaluation metrics include: 1) point-
 585 to-point distance (PTPD) [39, 40] between deformed mesh
 586 and target mesh, 2) root mean square error ($RMSE_{lmk}$) for
 587 landmarks, and 3) root mean square error for specific regions
 588 ($RMSE_{reg}$). All the above metrics are in millimeters (mm)
 589 averaged across testing meshes.

590 Our results, as detailed in Table II, highlight the superior
 591 performance of our DDF-ISM over conventional point-based
 592 and Signed Distance Function (SDF)-based methods in terms
 593 of both PTPD and $RMSE_{lmk}$. The directed distance field
 594 approach facilitates an accurate representation of internal
 595 structures, while the cross-attention mechanism ensures pre-
 596 cise alignment of template and target landmarks.

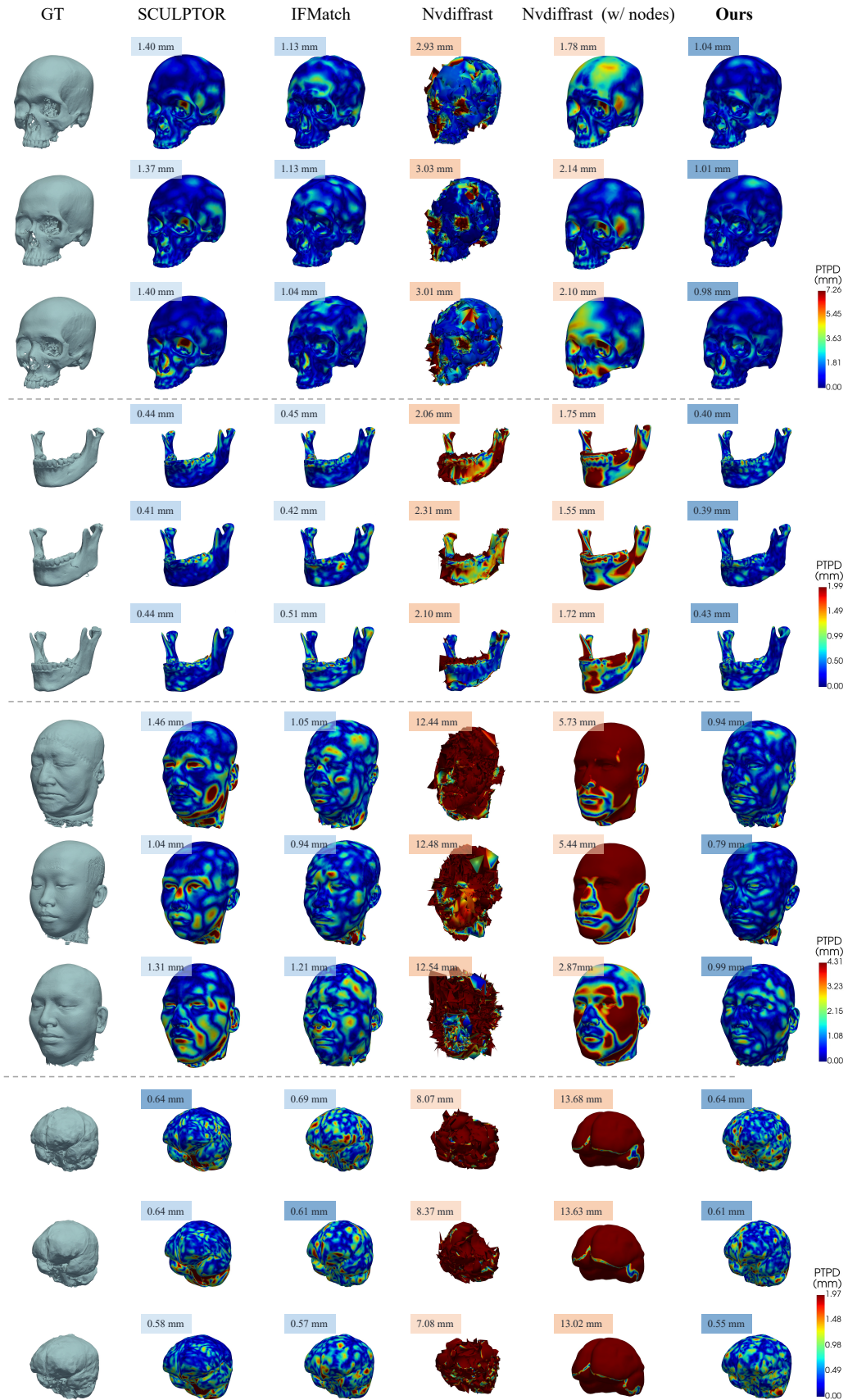


Fig. 8: Deformation result comparisons of our method and baselines. The visual representation of the deformations highlights the differences in accuracy and alignment between the methods.

TABLE V: Region-specific errors \mathbf{RMSE}_{reg} (mm) \downarrow (mean \pm std. dev.) for different methods on *skull*.

	Frontal	Parietal	Temporal	Zygomatic	Maxilla	Teeth	Avg.
SCULPTOR [12]	5.09 \pm 2.28	8.52 \pm 3.52	6.22 \pm 2.58	7.16 \pm 2.56	6.87 \pm 1.87	5.33 \pm 3.18	6.21 \pm 3.63
IFMatch [15]	7.70 \pm 3.50	12.99 \pm 5.70	6.99 \pm 3.48	5.90 \pm 3.16	7.10 \pm 2.77	5.39 \pm 3.71	7.42 \pm 4.87
Ours	3.95 \pm 2.00	5.48 \pm 2.67	3.92 \pm 2.23	3.37 \pm 2.07	3.65 \pm 1.65	3.93 \pm 2.30	3.92 \pm 2.48

TABLE VI: Region-specific errors \mathbf{RMSE}_{reg} (mm) \downarrow (mean \pm std. dev.) for different methods on *mandible*.

	Body	Teeth	Head	Avg.
SCULPTOR [12]	2.46 \pm 1.31	3.54 \pm 1.38	2.58 \pm 2.47	2.86 \pm 1.72
IFMatch [15]	4.12 \pm 2.21	5.30 \pm 2.24	3.78 \pm 3.35	4.40 \pm 2.60
Ours	2.41 \pm 1.29	2.45 \pm 1.34	2.31 \pm 1.30	2.39 \pm 1.31

TABLE VII: Runtime comparisons (in minutes).

	Head	Surface	Brain	Skull	Mandible	Total
SCULPTOR [12]	0.99	1.36	4.07	0.66		7.08
IFMatch [15]	0.26	0.09	0.33	0.09		0.77
Ours	0.31	0.12	0.48	0.12		1.03
Nvdiffrast [38]	2.89	2.66	2.98	2.66		2.80
Nvdiffrast [38] (w/ nodes)	6.11	7.07	9.01	5.64		6.96
Ours (w/o CA, dim=512)	<u>0.30</u>	<u>0.10</u>	<u>0.38</u>	<u>0.10</u>		<u>0.88</u>
Ours (w/o CA, dim=256)	0.26	0.09	0.33	0.09		0.77

597 Furthermore, we conduct a detailed comparison of errors in
 598 specific anatomical regions, including the eyes, nose, mouth,
 599 and various parts of the brain, skull, and mandible. To quantify
 600 the deformation error corresponding to each anatomical region,
 601 we select landmarks within these regions and calculate their
 602 respective errors. The experiment results are presented in
 603 Tables III, IV, V, and VI.

604 Beyond quantitative assessments, we also perform qualita-
 605 tive experiments to visually evaluate the anatomical fidelity of
 606 the models. Fig. 7 and 8 provide a comprehensive evaluation
 607 of the deformation accuracy of baselines and our DDF-ISM
 608 on anatomical meshes. The PTPD values in Fig. 7 reveal that
 609 our method consistently achieves lower distances, indicating
 610 a closer match to the target mesh across all anatomical
 611 parts. This suggests a higher precision in modeling complex
 612 anatomical structures. The visual comparison in Fig. 8 cor-
 613 roborates these findings, showcasing the superior alignment
 614 and structural fidelity of our method’s deformation results.
 615 Notably, our method outperforms the baselines, particularly
 616 in regions critical for biomechanical relevance, such as the
 617 eyes, nose, and mouth. Additionally, differentiable rendering-
 618 based methods yield unsmooth results (without control nodes)
 619 or minimal deformation (with control nodes), failing to match
 620 target shapes effectively compared to direct 3D geometry
 621 methods (*e.g.*, the baseline methods and ours).

622 The lower PTPD values and enhanced visual accuracy in
 623 our method can be attributed to the effective cross-attention
 624 mechanism and the directed distance field approach, which
 625 facilitates precise landmark alignment and internal structure
 626 modeling. In summary, our experimental results underscore the
 627 efficacy of our method in delivering high-fidelity deformations,
 628 essential for reliable biomechanical analysis.

629 *C. Computational Efficiency*

630 We report the runtime comparisons in Table VII, highlight-
 631 ing the efficiency of different methods in processing anatom-
 632 ical meshes. SCULPTOR shows the longest total runtime at
 633 7.08 minutes, indicating it may require more computational
 634 resources or time for processing. Conversely, IFMatch has the
 635 shortest total runtime of 0.59 minutes, suggesting it is highly
 636 optimized for speed, which is beneficial for time-sensitive
 637 applications. The total runtime of our method is much lower

638 than that of SCULPTOR while is closer to that of IFMatch,
 639 potentially balancing computational efficiency with the quality
 640 of deformation results.

641 Compared to SCULPTOR, our method processes N vertices
 642 directly through the network layers to compute deformations,
 643 ensuring computational efficiency. In contrast, SCULPTOR
 644 samples K control nodes from N vertices based on predefined
 645 intervals σ , followed by vertex deformation optimization. In
 646 Table VIII, SCULPTOR evaluates intervals of decreasing size
 647 (A: $\sigma_{surf} = 512, \sigma_{brn} = 16, \sigma_{skl} = 128, \sigma_{mdb} = 16$;
 648 B: $\sigma_{surf} = 256, \sigma_{brn} = 8, \sigma_{skl} = 64, \sigma_{mdb} = 8$; C:
 649 $\sigma_{surf} = 128, \sigma_{brn} = 4, \sigma_{skl} = 32, \sigma_{mdb} = 4$; D: $\sigma_{surf} =$
 650 $64, \sigma_{brn} = 2, \sigma_{skl} = 32, \sigma_{mdb} = 2$). Smaller intervals increase
 651 runtime but improve performance, especially when sampling
 652 iteratively from large to small intervals (A to D) in a coarse-to-
 653 fine manner, compared to single-interval sampling. In contrast,
 654 our method eliminates iterative sampling, offering a more
 655 efficient and effective solution for deformation.

656 Compared to IFMatch, our design introduces two key im-
 657 provements. First, we integrate a cross-attention (CA) module
 658 to capture landmark translation features, requiring five hidden
 659 layers in the deformation field, compared to IFMatch’s three
 660 layers without CA. Second, we increase the hidden units in
 661 both the deformation field and latent codes from 256 to 512,
 662 enhancing representational capacity. As shown in Table VII,
 663 our method without CA and with 256 hidden units matches
 664 IFMatch’s runtime. However, the full model, incorporating CA
 665 and larger hidden dimensions, outperforms IFMatch and the
 666 simplified variants of our method (Table II), demonstrating the
 667 benefits of these design choices.

668 *D. Ablation Studies*

669 We conducted ablation studies to understand the contribu-
 670 tion of different components in DDF-ISM on both original
 671 and noisy data. Noise is introduced by randomly adding small
 672 outlier structures to the original mesh, simulating a low-quality
 673 scan. We train on the noisy data and test on the original data.

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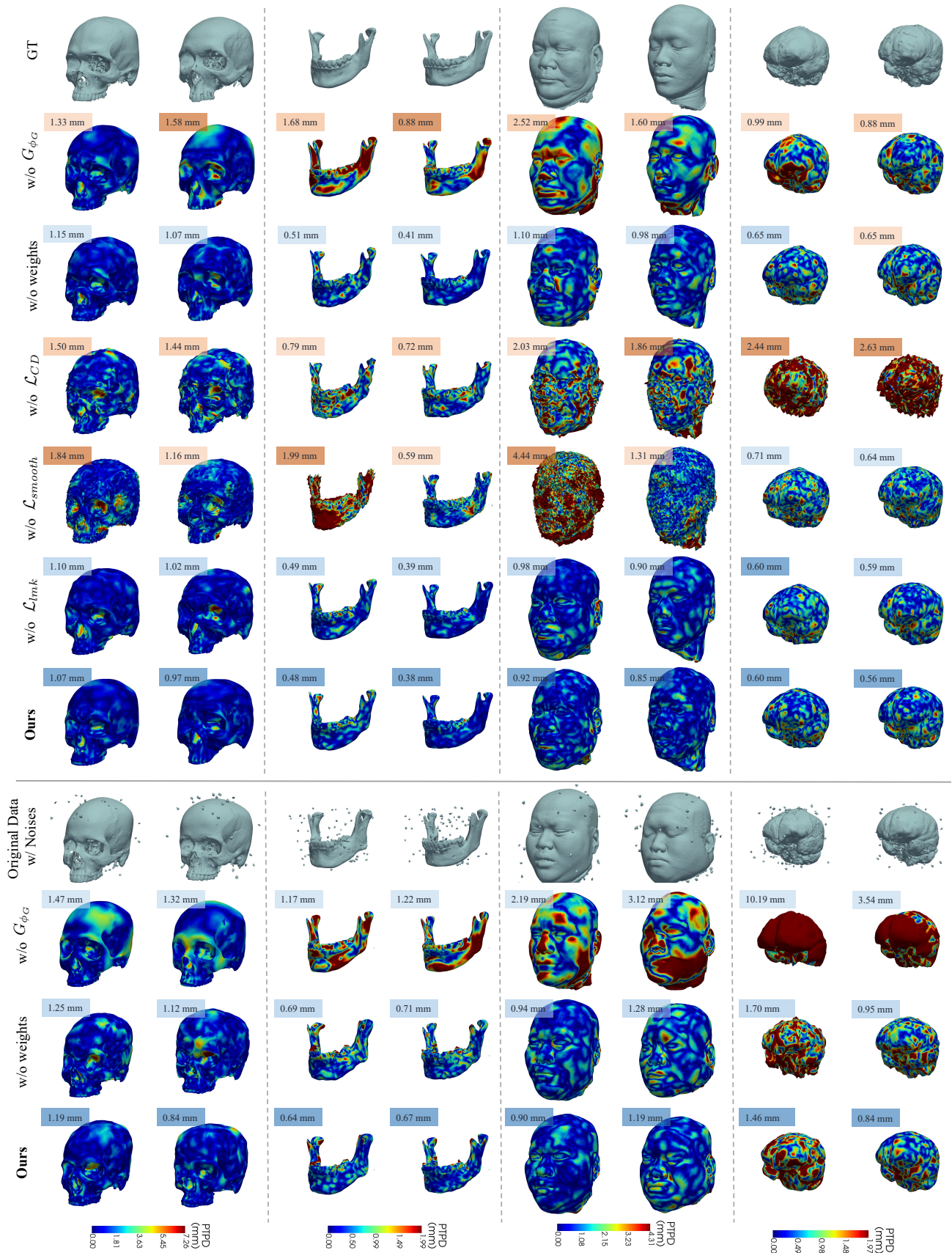


Fig. 9: Deformation result comparisons for ablation study. The values represent the magnitude of deformation, with lower values indicating closer alignment to the target mesh.

TABLE VIII: PTPD (mm) ↓, $\text{RMSE}_{l_{mk}}$ (mm) ↓ (mean ± std. dev.), and Time (mins) ↓ for SCULPTOR.

	Head Surface			Brain			Skull			Mandible			Avg.		Sum
	PTPD	$\text{RMSE}_{l_{mk}}$	Time	PTPD	$\text{RMSE}_{l_{mk}}$	Time	PTPD	$\text{RMSE}_{l_{mk}}$	Time	PTPD	$\text{RMSE}_{l_{mk}}$	Time	PTPD	$\text{RMSE}_{l_{mk}}$	Time
SCULPTOR	1.41	6.46 ± 2.78	0.99	0.61	6.73 ± 3.68	1.36	1.50	6.21 ± 3.63	4.07	0.42	2.86 ± 1.72	0.66	0.99	5.57 ± 2.95	7.08
SCULPTOR-A	1.80	7.73 ± 5.26	0.08	0.72	9.44 ± 6.88	0.10	1.55	6.67 ± 4.07	0.35	0.53	3.35 ± 1.90	0.09	1.15	6.80 ± 4.53	0.62
SCULPTOR-B	1.68	7.33 ± 5.16	0.14	0.72	9.36 ± 7.01	0.18	1.56	6.72 ± 4.07	0.59	0.50	3.23 ± 1.83	0.11	1.12	6.66 ± 4.52	1.02
SCULPTOR-C	1.70	7.43 ± 5.11	0.24	0.84	11.05 ± 9.67	0.38	1.58	6.80 ± 4.16	1.05	0.49	3.25 ± 1.90	0.17	1.15	7.13 ± 5.21	1.84
SCULPTOR-D	1.68	7.43 ± 5.16	0.53	1.15	12.99 ± 11.45	0.70	1.62	7.01 ± 4.27	2.08	0.52	3.33 ± 1.98	0.29	1.24	7.69 ± 5.72	3.60

TABLE IX: PTPD (mm) ↓ and $\text{RMSE}_{l_{mk}}$ (mm) ↓ (mean ± std. dev.) for ablation studies on four anatomical parts.

	Head Surface		Brain		Skull		Mandible		Avg.	
	PTPD	$\text{RMSE}_{l_{mk}}$	PTPD	$\text{RMSE}_{l_{mk}}$	PTPD	$\text{RMSE}_{l_{mk}}$	PTPD	$\text{RMSE}_{l_{mk}}$	PTPD	$\text{RMSE}_{l_{mk}}$
<i>Original Data</i>										
w/o G_{ϕ_G}	2.01	6.82 ± 4.40	1.18	7.78 ± 4.95	1.39	4.56 ± 3.17	1.56	4.75 ± 2.48	1.54	5.98 ± 3.75
w/o weights	1.02	5.46 ± 3.91	0.70	6.56 ± 3.71	1.10	4.78 ± 3.33	0.51	2.97 ± 1.63	0.83	4.61 ± 2.97
w/o \mathcal{L}_{CD}	1.77	7.27 ± 3.75	2.44	9.06 ± 4.41	1.40	5.49 ± 2.77	0.86	3.88 ± 2.10	1.62	6.43 ± 3.26
w/o \mathcal{L}_{smooth}	2.15	6.61 ± 5.71	0.77	3.95 ± 2.10	1.63	5.74 ± 4.05	1.37	4.41 ± 3.11	1.48	5.18 ± 3.74
w/o $\mathcal{L}_{l_{mk}}$	0.93	7.67 ± 5.83	0.61	21.98 ± 10.46	<u>1.08</u>	6.42 ± 4.71	0.45	4.48 ± 2.68	0.77	10.14 ± 5.97
Ours	<u>0.95</u>	4.33 ± 2.34	<u>0.66</u>	3.78 ± 2.15	1.06	3.92 ± 2.48	<u>0.46</u>	2.39 ± 1.31	<u>0.78</u>	3.61 ± 2.07
<i>Original Data with Noises</i>										
w/o G_{ϕ_G}	2.64	10.24 ± 6.67	7.06	24.95 ± 11.90	1.51	7.09 ± 4.50	1.45	5.62 ± 2.74	3.17	11.98 ± 6.45
w/o weights	<u>1.12</u>	8.07 ± 5.93	1.21	6.77 ± 3.73	<u>1.14</u>	6.12 ± 4.25	<u>0.66</u>	4.28 ± 2.30	<u>1.03</u>	6.31 ± 4.05
Ours	1.06	7.63 ± 5.74	1.21	4.91 ± 2.70	1.13	6.04 ± 4.22	0.63	4.12 ± 2.27	1.01	5.68 ± 3.73

Fig. 9 presents deformation magnitudes in millimeters, with lower values indicating better alignment with the target. The variation in values across the board underscores the impact of different factors on the deformation process. Table IX complements this visual assessment with quantitative data, reporting both PTPD and $\text{RMSE}_{l_{mk}}$ for four anatomical parts under different conditions.

For our DDF-ISM without $\mathcal{L}_{G_{\phi_G}}$ or without \mathcal{L}_{CD} , the increase in PTPD and $\text{RMSE}_{l_{mk}}$ values suggests that these components are necessary for enhancing the accuracy of the deformations. The notable increase in error metrics for DDF-ISM without \mathcal{L}_{smooth} or without $\mathcal{L}_{l_{mk}}$ highlights the importance of landmarks in guiding the deformation process to achieve higher fidelity. A comparison of our DDF-ISM without $\mathcal{L}_{G_{\phi_G}}$ and weights reveals that excluding either the DDF or its probabilistic component markedly decreases shape-matching accuracy, especially for noisy scans. Therefore, each part contributes to the overall accuracy, and their combined use yields the best results, as shown by the lowest metric values.

VIII. CONCLUSION

In conclusion, the proposed DDF-ISM is a novel approach for modeling the internal structures of the human head with high anatomical accuracy and computational efficiency. Our DDF-ISM leverages probabilistic directed distance fields to overcome the limitations of traditional mesh and point cloud-based models, providing superior performance in both quality and speed. The results demonstrate its potential for enhancing applications in biomechanical simulations, medical imaging, and surgical planning. Future work will explore adapting DDF-ISM to model other anatomical regions and integrating it into wearable product design, broadening its impact in various areas including clinical practice and application research.

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