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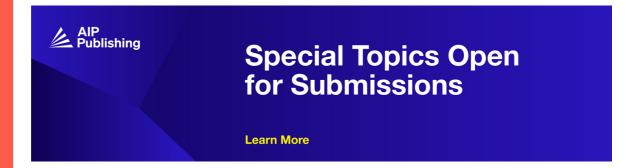
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# Wind tunnel investigation on the two- and three-blade Savonius rotor with central shaft at different gap ratio

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The Savonius rotor seems to be a promising wind turbine as it not only has the simplest and cheapest design but also is capable of yielding a higher annual energy output at low wind speed than the Darrieus rotor. Moreover, the Savonius rotor can also be used in ventilation systems, for local electricity production, as the start-up device for the Darrieus rotor, and small hydrokinetic turbines operating at low velocity. As a two-blade Savonius rotor suffers from negative average static torque coefficient (AC<sub>TS</sub>) at some azimuth angles and large-amplitude variation of AC<sub>TS</sub>, several studies have been conducted in recent years to improve ACTS. The three-blade rotor seems to be a potential candidate for AC<sub>TS</sub> improvement. However, less research has been done on three-blade rotors with a 180° arc and central shaft at different gap ratios (GRs) for different wind speeds. Therefore, the focus of the present work is to compare the two- and three-blade rotor in terms of AC<sub>TS</sub> and power coefficient (C<sub>P</sub>) through a wind tunnel experiment. Results show that the wind speed had a small effect on AC<sub>TS</sub>. However, negative azimuth angle range is narrowed and the negative azimuth angle range is moved upward as GR increased. Hence, the Savonius rotor with three blades could not only eliminate the negative range of AC<sub>TS</sub> but also smooth AC<sub>TS</sub> curves. In terms of the C<sub>P</sub>, the maximum power coefficient of the twoblade configuration was approximately 1.5 times that of the three-blade configuration. The 1/6 GR test data exhibited the attainment of super performance for all wind speed and blade number. © 2016 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4940434]

#### I. INTRODUCTION

The vertical axis wind turbine (VAWT) has been reported as a potential renewable device in the field of construction. There are two types of VAWTs: the Savonius rotor and the Darrieus rotor. The Darrieus rotor is superior to the Savonius rotor in terms of power efficiency. However, the Darrieus rotor features a very small starting torque and may fail to accelerate beyond the "dead band" even when it does begin to run. This drawback has limited the utilization of Darrieus rotor in buildings area to a great extent. Recent researches showed that the Savonius rotor can have a high annual energy output at a relatively low wind speed making these micro wind turbines suitable for application on urban terrain. From this point, the Savonius rotor seems to be a promising wind turbine as it not only has the simplest and cheapest design but also is capable of producing a higher annual energy output at low wind speed than the Darrieus rotor. Moreover, the Savonius rotor can also be used in the ventilation

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system, for local electricity production,<sup>5</sup> as a start-up device<sup>6</sup> for the Darrieus rotor and in small hydrokinetic turbines operating at low velocity.<sup>7</sup>

Numerous numerical and experimental investigations have been conducted on the Savonius rotor recently, with the focus mainly on the blade profile,<sup>8–11</sup> the multi-stage,<sup>12–15</sup> the blade number,<sup>16</sup> the aspect ratio,<sup>17,18</sup> the gap ratio (GR),<sup>19</sup> and the argument (block) device.<sup>4</sup> From these researches, it is known that the optimization of the blade profile will directly increase the C<sub>P</sub> of the rotor;<sup>5</sup> that multi-stage designs have been investigated mainly to unify the static torque coefficient (C<sub>TS</sub>) or eliminate the negative C<sub>TS</sub> range;<sup>20</sup> and that secondary design parameters, such as the aspect ratio and GR, are highly dependent on the blade profile design and the blade number. Among the aforementioned research topics, the literature review revealed that very few published papers have investigated the effect of blade number. The most well-known paper about the blade number was published by Blackwell et al.<sup>21</sup> in 1977, who conducted a comprehensive experimental investigation on one-stage two- and three-bladed Savonius rotors without shaft at wind speeds of 7 m/s and 14 m/s, wherein the blade profile of the three-blade rotor was built with a  $150^{\circ}$  arc, the arc of the blade profile was about  $20^{\circ}$  and  $10^{\circ}$  on the outer and inner edges, respectively, and the GR ranged from 0 to 0.2 and the height ratio from 1 to 1.5. The sweep areas of the tested rotors are different from each other. In 2005, Islam et al.<sup>22</sup> studied the static characteristics of two-, three-, and four-bladed Savonius rotors without shaft when GR was 0.2. Biswas et al.<sup>23</sup> inspected the effects of overlap and blockage on a threeblade Savonius rotor. Morshed et al.<sup>24</sup> conducted an experimental and numerical investigation on three different three-blade Savonius rotors with 0, 0.12, and 0.26 overlap ratios and without central shaft, respectively. Hayashi et al. 25 tested and compared a one-stage three-blade Savonius rotor with a three-stage three-blade Savonius rotor. In fact, researches done by Biswas and Hayashi focused on the overlap effect and the stage effect, respectively.

Different from previous researches, we laid the focus on two- and three-blade Savonius rotors with the same sweep area for all rotors and a shaft at the center of the rotor. The use of center shaft can improve the stability of the whole system. GR values studied in this paper were 0, 1/3, and 2/3. However, the definition of this GR (with shaft) is different from that of the rotor without shaft. This difference will be discussed in Section II C. The blade profile of a three-blade rotor was constructed with a 180° arc, instead of a 150° arc, <sup>21</sup> for the purpose of easy manufacturing and fabrication. Besides, considering the application in building area, a series of tests were also conducted at relatively low wind speeds. Hence, this paper studied the impact of blade number, wind speed and GR on C<sub>P</sub> and C<sub>TS</sub>.

## II. EXPERIMENTAL INSTRUMENTATION AND TESTING MODELS

#### A. Wind tunnel

The wind tunnel shown in Figure 1 is a low speed open-circuit environmental wind tunnel (EWT) consisting of four sections (i.e., contraction section, test section, developed section, and diffuser section). In this wind tunnel, a honeycomb flow straighter is placed at the upstream of the contraction section to coordinate the speed of the oncoming wind and reduce the turbulence intensity; the air flow is then accelerated in the contraction section to gain a desired speed for the test section; and the test section is a square cross section ( $1050 \, \text{mm} \times 1050 \, \text{mm}$ ) and have

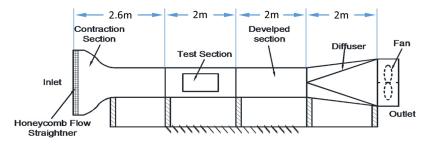


FIG. 1. Wind tunnel.

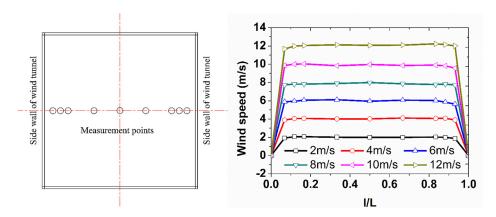


FIG. 2. Wind speed distribution along the central line of the testing section.

two transparent windows at the tunnel side through which the running conditions of the tested rotor can be observed.

A variable-frequency controller is provided to drive the fan and regulate the wind speed within the range of 0-30 m/s. In order to make sure that the rotor is tested by the uniform incoming air flow, the rotor is placed at the central area of the test section of the wind tunnel. The length of the test section is 2 m. In the test section, we set nine measurement points in the middle cross section (left of Figure 2) when wind speed varied from 2 m/s to 12 m/s using a TSI hot wire anemometer with 0.01 m/s accuracy. We placed the TSI hot wire anemometer at the appointed nine points to record the wind speed data lasting for 1 min. We averaged the recorded wind speed data to gain the average wind speed at each point. Figure 2 (right) displays the wind distribution at nine points when the wind speed varied from 2 m/s to 12 m/s. Although a small decay of wind speed was found at points which were close to the wall of the wind tunnel, the wind speed distribution was fairly uniform along the central line of the tunnel when the wind speed varied from 2 m/s to 12 m/s. The recorded wind speed data at the central point of the test section are also used to calculate the standard deviation of the wind speed (Table I). The standard deviation indicates the uniformity of the wind speed at one point. It is found that the standard deviation of the wind speed ranged from 0.32% to 0.47%. This uniform wind speed distribution and small standard deviation at the test section provided a desirable testing condition for the Savonius rotor.

## B. Test rig and procedure

Considering the axis orientation, there are two types of test rigs that are the horizontal test rig<sup>26,27</sup> and the vertical test rig.<sup>12,28,29</sup> Theoretically, these two test rig types can satisfy the testing requirements for any test condition. At the very beginning, we adopted the horizontal test rig as shown on the right side of Figure 3 and placed most part of the test rig outside the wind tunnel to attain and maintain a small blockage ratio. However, as the test went on, it was discovered that the shaft had to be rigid enough to sustain the unbalance force caused by the rotating rotors. As tiny unbalance of the rotating system at high rotational speed will generate astonishingly excessive stress, vibration and noise, it became more and more difficult to control the axiality of each component in the test. In addition, we found that the horizontal test rig (Figure 3) is receivable for the condition in which the test rig is erected completely outside the wind tunnel or the size of the wind tunnel is large enough. Based on our testing experience, the configuration of the Savonius

TABLE I. Standard deviation of wind speed at central point of testing section.

Wind speed	4	6	8	10	12
Standard deviation of wind speed	0.004725	0.00493	0.003752	0.003218	0.003391

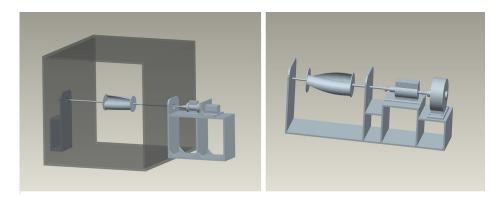


FIG. 3. The horizontal test rig.

rotor is naturally unbalance at no-zero azimuth angel for the horizontal test rig when measuring the static torque coefficient. It means that the Savonius rotor will return from the no-zero azimuth angle state to the zero azimuth angle state without any load in the horizontal test rig. But this unbalance can be easily eliminated in the vertical test rig.

Out of consideration for those problems, a vertical test rig was built showed in Figure 4 (left). This vertical test rig was manufactured using the computerized numerical control (CNC) machine. To attain easy manufacturing and high mechanical strength, aluminum alloy was chosen as the material for the test rig. Each component of the test rig was built to a tolerance of 0.01 mm to ensure the axiality. Components involved in this test included bearings, bearing holds, magnetic bearing, couplings, torque meters, flyer wheel, and motor. All these components are presented on the left side of Figure 4. The basic function of the magnetic bearing was to reduce the transmission of vibration caused by rotating unbalance and minimize the usage of the mechanical bearing in order to reduce the friction force. In the same time, all mechanical bearings were washed using the gasoline to remove the bearing grease which might increase the friction. Under the magnetic bearing, there is a torque meter having a measuring range of 0-2 Nm and an accuracy up to 0.01 Nm. This torque meter will record torque signals and rotational speed signals simultaneously and transmit them to a computer through the RS-232 port. A homemade software is programmed to process those signals and write them into a related file. At the end of the test rig, a motor is provided to drive the torque meter, magnetic bearing, and tested rotor by way of the motor controller and keep the rotor rotate at a specified rotational speed or a specified tip speed ratio (TSR). To ensure minimum blockage, only one

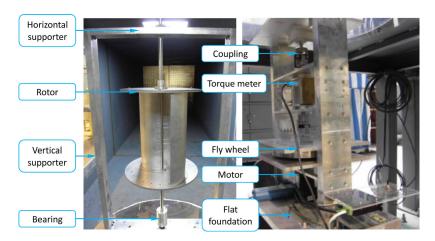


FIG. 4. The vertical test rig.

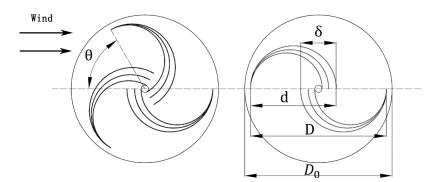


FIG. 5. Two and three blades Savonius rotor.

horizontal and two vertical supports are placed inside the wind tunnel. A flat foundation outside the wind tunnel holds the rest part of the test rig (right side of Figure 4).

In this paper, a frequency controller was used to regulate the wind speed with a fixed value. And we used a motor controller to adjust the rotational speed of the motor to gain different TSRs. TSR is obtained by the following equation:

$$TSR = \frac{\omega r}{V},\tag{1}$$

where  $\omega$  is the rotational speed of the Savonius rotor, r is the radius of the Savonius rotor, and V is the speed of wind pass through the wind tunnel.

The instantaneous dynamic torque was recorded lasting for 3-min at fixed wind speed and fixed TSR value, and recorded values were then averaged to gain the average dynamic torque coefficient ( $C_T$ ). The product of  $C_T$  and TSR was the power coefficient ( $C_P$ ). The instantaneous static torque was recorded for 3 min at a fixed wind speed and a fixed azimuth angle. The average static torque meter ( $AC_{TS}$ ) was gained by averaging the instantaneous static torque. The next  $AC_{TS}$  testing is carried out after an interval of  $5^{\circ}$ .

#### C. Tested models

Main components of the Savonius rotor include two end-plates, two or three blades, and one shaft.  $^{30}$  Generally, the  $C_P$  of the rotor with endplates is higher than that of the rotor without the endplates.  $^{15}$  In the test, most of the components except the shaft were fabricated with aluminum alloy (6061-T6). Two or three semicircular slots and one circular hole were formed using the wire-electrode cutting machine to accommodate, respectively, the semicircular aluminum blades and shaft. Blades were rolled up with a cylinder inside. This cylinder had the same diameter as the designed blade. Based on other researches, the optimal size of endplate ( $D_0$ ) is about 1.1 times the rotor diameter ( $D_0$ ). As  $D_0$  is 250 mm, D should be 227.27 mm. This value is then rounded up to 230 mm to facilitate the measurement. In order to keep D constant, the blade diameter ( $D_0$ ) is adjusted according to different GRs. The diameter of the shaft, which is denoted as  $D_0$  is 1.088.

According to previous researches, the best GR of Savonius rotor without shaft is 1/6 or ranges from 0.20 to 0.30.<sup>17,31</sup> Whether the shaft exists or not is likely to alter this range. Thus, three GRs different from those in other researches were selected in this paper, and were 0, 1/6, and 1/3. The equation for GR is

$$GR = \frac{\delta - a}{d},\tag{2}$$

Blade number	Model designation	Blade diameter	Gap between two blades	GR	Rotor diameter	Rotor height
2	S1B2GR0	121	12	0	230	270
	S1B2GR1/6	132	34	1/6	230	270
	S1B2GR1/3	145	60	1/3	230	270
3	S1B3GR0	121	12	0	230	270
	S1B3GR1/6	132	34	1/6	230	270
	S1B3GR1/3	145	60	1/3	230	270

TABLE II. Detailed geometry information of two- and three-blade Savonius rotors (in mm).

where a is the diameter of the shaft, d is the blade diameter, and  $\delta$  is the gap between two blades. Unlike equations in other researches, this equation takes into account the effect of the shaft. All definitions of design parameters for two- and three-blades rotors can be found in Figure 5. Different from the test conducted by Blackwell  $et\ al.$ , <sup>21</sup> the blade profile of the three-blade rotor in this paper was constructed with a 180° arc, instead of a 150° arc, to facilitate manufacturing and fabrication. Meanwhile, Table II summaries the value of each design parameter and the testing designation of each model.

### III. WIND TUNNEL BLOCKAGE CORRECTION AND MEASUREMENT UNCERTAINTY

#### A. Blockage correction

Considering the increase of local wind speed in the test section, the blockage of the Savonius should be considered.<sup>32</sup> Two wind tunnel blockage correction methods are widely used, i.e., the Pope and Harper<sup>33</sup> and the Maskell<sup>34</sup> methods. Generally, the wind tunnel correction is to ascertain the  $\varepsilon$  and m factor for the Pope's method and Maskell method, respectively. However, it is very difficult to determine these two factors for an unusual shape, such as the Savonius rotor. Alexander<sup>35,36</sup> extended the Maskell's method to make it suitable for the wind tunnel test of the Savonius rotor.

The Alexander's correction method is given as follows:

$$\emptyset = \frac{C_{Du}}{C_{D\infty}} = \frac{q_c}{q_u} = \frac{v_c^2}{v_u^2} = \frac{1}{1 - m(S/C)},\tag{3}$$

where m is determined in the wind tunnel test;  $v_c$  is the corrected wind speed;  $v_u$  is undisturbed wind speed; S is the model frontal area of the test model and rig; and C is the frontal area of the test section.

Figure 6 is the Alexander correction for Savonius rotor tested in the wind tunnel. In addition, Alexander's method can get accurate correction results even when the S/C value reaches up to 0.334. In this test, the swept area of the tested rotor was 0.06256 m² and the frontal area of related supporting components was 0.004 m². Hence, S was equal to 0.06656 m² and the frontal area of the test section was 1.1025. So, the S/C value of this test was about 0.060372 which is far less than the value of 0.334. All the experimental data in this paper were corrected using the Alexander method. The RN is calculated using the following equation:

$$RN = VD/\vartheta,$$
 (4)

where V is wind speed. D is the diameter of the rotor and  $\vartheta$  is Kinematic viscosity.

## B. Measurement uncertainty

The standard deviation was used to estimate the experimental uncertainty associated with the wind velocity, torque, measured RPM, and tip speed ratio and the following equation was used to calculate the standard deviation of variants mentioned above

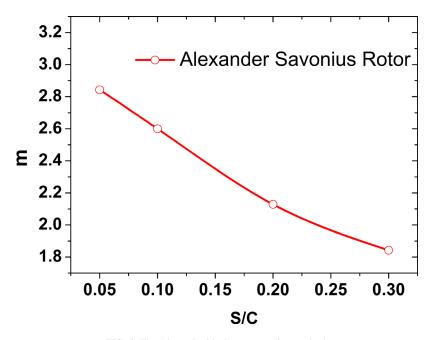


FIG. 6. The Alexander blockage correction method.

$$E_{st} = \sqrt{\frac{(x_1 - x_{mean})^2 + (x_2 - x_{mean})^2 + \dots + (x_n - x_{mean})^2}{n - 1}},$$
 (5)

where x means the measured values and n means the total number of measurements. Some unforeseen results were repeated several times to minimize the measurement error. Table III shows the percentage of the measurement uncertainty of each variant. The uncertainty of the wind velocity, torque, RPM, and TSR ranged, respectively, from 1.8% to 3.61%.

#### **IV. RESULTS**

In this section, the effects of wind speed, GR and Blade number on  $AC_{TS}$  and  $C_P$  were discussed in detail.  $AC_{TS}$  was gained at various azimuth angles ( $\theta=0^{\circ}-180^{\circ}$  with steps of  $5^{\circ}$ ) in respect of the oncoming wind. The definition of  $\theta$  can be found in Figure 5.  $AC_{TS}$ ,  $C_T$ , and  $C_P$  are expressed by the following equations, respectively,

$$AC_{TS} = \frac{TS}{0.5\rho AV^2R},\tag{6}$$

$$C_T = \frac{T}{0.5\rho A V^2 R},\tag{7}$$

TABLE III. Uncertainty percentage of each variant.

Variant	Uncertainty (%)	
Wind velocity	1.8	
Measured torque	3.4	
Measured RPM	3.2	
Measured TSR	3.61	

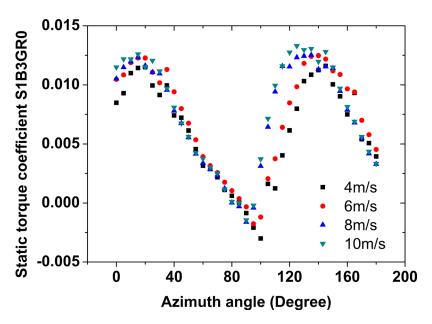


FIG. 7. Wind speed effect on AC<sub>TS</sub> of the Savonius rotor with three blades.

$$C_P = C_T * TSR, \tag{8}$$

where V (m/s) is the oncoming wind speed; A (m<sup>2</sup>) is the swept area of the Savonius rotor; TS (Nm) is the measured static torque; R (m) is the radius of the Savonius rotor; T (Nm) is the measured dynamic torque; TSR is the tip speed ratio;  $\rho$  (kg/m<sup>3</sup>) is the density of wind;  $AC_{TS}$  is the average static torque coefficient;  $C_T$  is the dynamic torque coefficient; and  $C_P$  is the power coefficient. T is gained at various TSRs to calculate the related  $C_T$ .

#### A. Static torque coefficient

### 1. Wind speed effect on $AC_{TS}$

Figure 7 presents the effect of wind speed on  $AC_{TS}$  of the Savonius rotor with three blades at four different wind speed when GR=0. In this three-blade configuration, three peaks appeared within the whole azimuth angle range  $(0^{\circ}-360^{\circ})$ . In theory, the  $AC_{TS}$  curve over the range of  $0^{\circ}-120^{\circ}$  is sufficient to describe the  $AC_{TS}$  curve over the whole azimuth angle range. In order to compare the three-blade rotor with the two-blade rotor, the azimuth angle range in this paper varied from  $0^{\circ}$  to  $180^{\circ}$ . Thus, the  $AC_{TS}$  curve of a three-blade rotor had two peaks within the  $0^{\circ}-180^{\circ}$  azimuth angle range.

It is known from the figure that the  $AC_{TS}$  curve at wind speed 4 m/s is close to the  $AC_{TS}$  curve at wind speed 6 m/s; that the  $AC_{TS}$  curve at wind speed 8 m/s almost coincides with the  $AC_{TS}$  curve at wind speed 10 m/s; and that  $AC_{TS}$  curves at 4 m/s and 6 m/s are lower than  $AC_{TS}$  curves at 8 m/s and 10 m/s. Every case has the same variation pattern with different wind velocities, and which is agreed with the Blackwell's conclusion, that the same change trend of static torque can be obtained under different RN. But with the increase of RN, the difference between the peak and valley value decreased. A relatively large distinction between  $AC_{TS}$  curves at 6 m/s and 8 m/s within azimuth angle ranges of  $0^{\circ}$ – $20^{\circ}$  and  $90^{\circ}$ – $120^{\circ}$  was observed, which might be caused by the initial friction force and specific separation patterns for different wind speeds. It can also be indicated that the wind speed had a slight effect on  $AC_{TS}$  of the Savosnius rotor and that this effect varied regionally. Peaks of four  $AC_{TS}$  curves at different wind speeds were fairly close to each other in terms of location and amplitude and this characteristic can be found in Table IV that presents the  $AC_{TSmax}$  and  $AC_{TSmin}$  with respect to the

	4 m/s	6 m/s	8 m/s	10 m/s
AC <sub>TSmax</sub>	0.0115	0.01228	0.01233	0.01259
Azimuth angle (C <sub>Pmax</sub> )	20	20	15	15
$AC_{TSmin}$	-0.00301	-0.00119	-0.00161	-0.00144
Azimuth angle (C <sub>Pmin</sub> )	100	100	90	90

TABLE IV. The  $AC_{TSmax}$  and  $AC_{TSmin}$  of the rotor with three blades.

related azimuth angle. Due this independence, the GR and Blade Number (BN) effects were discussed at wind speed of 8 m/s.

### 2. GR effect

Figure 8 shows  $AC_{TS}$  varying with the azimuth angle for two-blade Savonius rotor at different gap ratios when the wind speed is 8 m/s. It is found that there were some azimuth positions where the  $AC_{TS}$  was negative at three gap ratios within azimuth angle ranges of  $130^{\circ}-180^{\circ}$  (when gap ratio = 0),  $155^{\circ}-175^{\circ}$  (when GR=1/6), and  $135^{\circ}-160^{\circ}$  (when gap ratio = 1/3).

The two-blade rotor with zero GR had the widest negative range, indicating that with the increase of GR, the negative azimuth angle decreased. An interesting finding is that negative azimuth angle range moved forward as GR increased. In addition, a significant improvement of  $AC_{TS}$  was found for rotor (GR = 1/3) within azimuth angle ranges of  $90^{\circ}$ – $125^{\circ}$  and  $165^{\circ}$ – $180^{\circ}$ , indicating that the existence of the gap will generally increase the  $AC_{TS}$  of the Savonius rotor and improve the rotor's starting ability. The reason behind this phenomenon is that the wind flow passed through the gap and imposed an additional force on the returning blade.

Compared with the results of Blackwell, the same conclusion was that the  $AC_{TS}$  curve moved up with the increase of GR and all the curves have the same rules. Blackwell gained the negative static torque only at the zero GR and the rest cases with different GR all had the positive static torque. However, in our testing, the negative static torque can be obtained in every

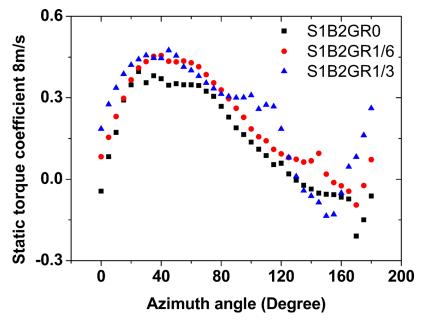


FIG. 8. The effect of GR on AC<sub>TS</sub> for rotor with two blades (8 m/s).

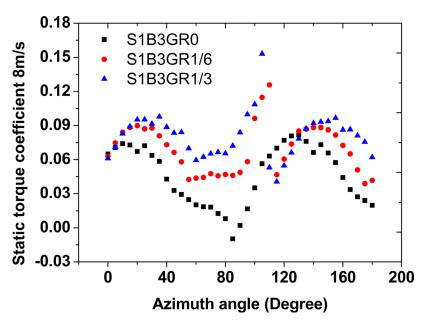


FIG. 9. The effect of GR on the static torque coefficient for rotor with three blades.

GR condition, not only zero GR. And the peak of  $AC_{TS}$  is lower than Blackwell's result, which is 0.7 and ours is 0.55.

The effect of GR on  $AC_{TS}$  of the rotor with three blades at the wind speed of 8 m/s is shown in Figure 9. Generally, increasing GR (from 0.0 to 1/6 and 1/3) for the rotor with three blades will increase the value of  $AC_{TS}$  and smooth the  $AC_{TS}$  curve, which is similar with the Blackwell's curves. However, there is an obvious step at azimuth angle  $120^{\circ}$  in our data, which is absent in Blackwell's curve. Except for the case where GR is zero,  $AC_{TS}$  was positive for all azimuth angles. The only negative  $AC_{TS}$  was found at azimuth angle  $85^{\circ}$  for the three-blade rotor with zero GR, suggesting that the three-blade rotor with zero GR can be started at almost any azimuth angle without friction force or load. While all the data of static torque in Blackwell's paper was positive. It is also found that  $AC_{TSmin}$  of the three-blade rotor with 1/6 and 1/3 GRs can be started to run at any azimuth angle and be used to assist the startup of the Darrieus rotor. The rotor with a 1/3 GR had the highest  $AC_{TSmax}$  (0.15).

#### 3. Blade number effect

The effect of blade number was investigated for rotors with two and three blades at wind speed of 8 m/s. Figure 10 shows the comparison of  $AC_{TS}$  values for the zone spanning from 0 to 180. From this figure, it can be clearly seen that the maximum  $AC_{TS}$  values of rotors with two blades were much higher than the maximum  $AC_{TS}$  value of rotors with three blades, especially within the azimuth angle range of  $0^{\circ}$ – $110^{\circ}$ . However, rotors with two-blade exhibited a very low  $AC_{TS}$  within the range of  $112^{\circ}$ – $180^{\circ}$ . For the three-blade configuration, there was almost no azimuth angle where the static torque coefficient was negative. Moreover, the three-blade configuration exhibited a smaller variation in  $AC_{TS}$  than the two-blade configuration.  $AC_{TS}$  values of the three-blade configuration were normally within the range of 0.03–0.10 for one cycle and were smaller than those of the two-blade configuration ( $AC_{TS}$  values of the two-blade configuration were within the range of -0.25–0.50), all indicating that the three-blade rotor has a good starting ability than the two-blade rotor in terms of smooth curve and positive  $AC_{TS}$ . Overall, increasing the blade number could smoothen the variation of  $AC_{TS}$  curves and eliminate  $AC_{TS}$ 's negative range. The reason behind this phenomenon is that the total drive

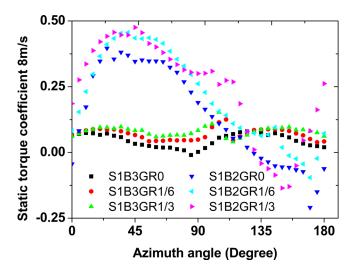


FIG. 10. The effect of blade number on the static torque coefficient.

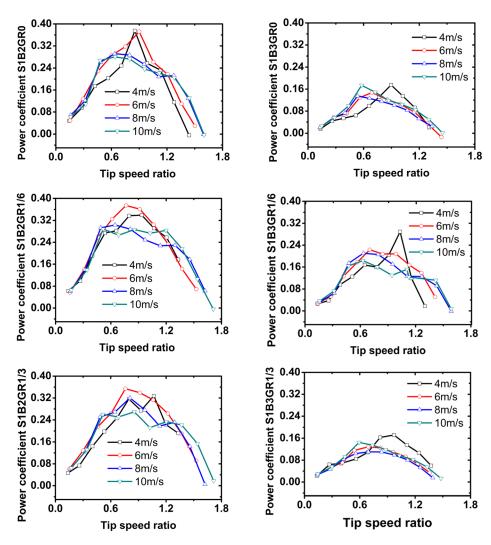


FIG. 11. The Wind speed effect on the power coefficient of the Savonius rotor.

TABLE V. Relationship between wind speed and RN.

RN and wind speed			
Wind speed	RN		
4 m/s	62 162.16		
6 m/s	93 243.24		
8 m/s	124 324.3		
10 m/s	155 405.4		

force is the superposition of drive force on each blade; as each blade has one  $AC_{TS}$  curve and the phase shift angle of  $AC_{TS}$  curve between blades becomes smaller, the superposition of each blade's  $AC_{TS}$  curve will smooth the total  $AC_{TS}$  curve.

#### **B.** Power coefficient

#### 1. Effects of wind speed and blade number

The effects of wind speed and blade number are examined in Figure 11 for both rotor types. The relationship between the RN and wind speed is shown in Table V, where the wind speed effect is displayed for each tested rotor. Generally, there was a slight improvement in performance as wind speed increased from 4 m/s to 6 m/s, and the lower wind speed data performed better within the range from 8 m/s to 10 m/s for the two-blade Savonius rotor. It is speculated that the lower RN, about 10<sup>4</sup> orders, has the better performance. While in Blackwell's plots, there were curves only for high RN, about 10<sup>5</sup> orders, and the results showed slightly different. For the three-blade Savonius rotor, the scenario was different whereas wind speed increased from 4 m/s to 6 m/s, the power coefficient decreased slightly, and the higher wind speed data performed better within the range of 6 m/s–10 m/s. Another finding is that with the increase of wind speed, the C<sub>P</sub> curve became flat at the maximum C<sub>P</sub> area. And it cannot be found so obviously different in Blackwell's results.

Figure 11 also compares the performance between typical two- and three-blade configurations. From the perspective of performance, the two-blade configuration was superior in most respects. The maximum power coefficient of the two-blade configuration was approximately 1.5 times that of the three-blade configuration. The reason for the low power output of the three-blade rotor may be due to the superposition of the instantaneous  $C_P$  of three blades. Another finding is that the working TSR range of the two-blade rotor was wider than that of the three-blade rotor in general. The maximum TSR value was about 1.7 for the two-blade rotor, but only 1.5 for the three-blade rotor. The rotor with a wider TSR range can easily match with the generator's curve. At the position of the maximum  $C_P$ , the TSR decreased when the number of blades went from two to three. For the two-blade configuration, the optimum speed ratio was between 0.7 and 0.8, which, however, was 0.5–0.6 for the three-blade configuration. This conclusion is the same with those obtained by researches without central shaft, suggesting that rotors with three blades had a stronger drag property than rotors with two blades. Thus, rotors with three blades had a better starting ability and weaker power output when compared to rotors with two blades.

#### 2. GR effect

The effect of GR on rotor performance for two-blade configuration is presented in Figure 12 where the performance was evaluated at three GRs ranging from 0.0 to 1/6 and 1/3 as the wind speed increased from 4 m/s to 10 m/s. The 1/6 GR test data in Figure 12 exhibited the attainment of super performance for all wind speed. Both larger and smaller gaps showed a decrease in performance, and the distribution curve was Parabolic. Optimum TSR was within the 0.8-1.0 range when wind speed = 4 m/s, and the maximum  $C_P$  was about 0.3. With the increase of the wind speed, the optimum TSR decreased, so did the maximum  $C_P$ . The maximum  $C_P$  attained 0.25 at

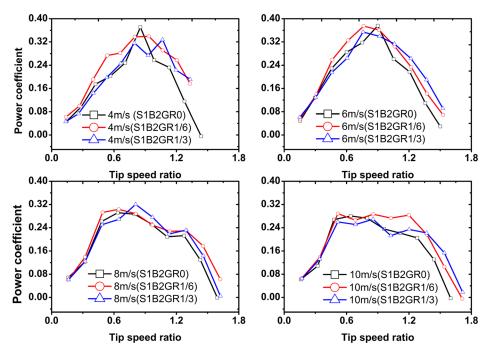


FIG. 12. GR effect on the power coefficient of the Savonius rotor (two-blade rotor).

the wind speed of 8 m/s when the optimum TSR ranged from 0.5 to 0.6. The curve had a quick spike before attaining the best TSR, and then dropped when climbing over the peak. At the wind speed of 10 m/s, there was an obvious flat area for TSR between 0.5 and 1.2, indicating that the high wind speed can provide a broader range of high power work and stable power output.

Figure 13 presents the effect of GR on rotor performance for three-blade configuration within the range from 0.0 to 1/6 and 1/3 GR as the wind speed increases from 4 m/s to 10 m/s. The 1/6 GR test data in Figure 13 also exhibited the attainment of super performance for all

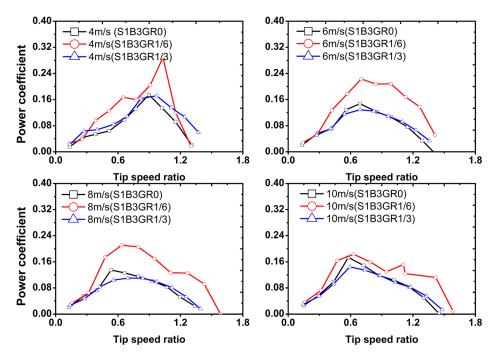


FIG. 13. GR effect on rotor performance (three-blade rotor).

wind velocities. Both larger and smaller gaps showed a decrease in performance, which is agreed with the conclusion of Blackwell. The distribution curve was also Parabolic. The performance difference became most noticeable when the wind speed was  $6\,\text{m/s}$  and  $8\,\text{m/s}$ . The optimum speed ratio was within the  $0.8{\text -}1.0$  range when wind speed  $=4\,\text{m/s}$ , and the maximum  $C_P$  was about 0.25. With the increase of the wind speed, the optimum TSR decreased, so did the maximum  $C_P$ . The maximum  $C_P$  was 0.20 within the  $0.6{\text -}0.8$  optimum TSR range when wind speed  $=8\,\text{m/s}$ . The curve had a quick spike before attaining the best TSR, and then dropped when climbing over the peak. At the wind speed of  $10\,\text{m/s}$ , the maximum value was reduced to about 0.16 within the same optimum TSR range.

#### V. CONCLUSION

A detailed experimental test of two- and three-blade rotors with central shaft was conducted at different wind speeds to offer some directions for the selection of Savonius rotors.

By exploring and discussing the effects of wind speed, GR, and BN on  $AC_{TS}$ , it is found that wind speed has a small effect on  $AC_{TS}$  curves. Test results suggest that with the increase of GR, the azimuth angle range of negative  $AC_{TS}$  decreases, and the negative azimuth angle range moves forward as GR increases; and that increasing BN from two to three,  $AC_{TS}$  curves become smooth and less varied and the negative range of  $AC_{TS}$  is almost eliminated.

In terms of the effects of wind speed, GR, and BN on  $C_P$ , it is known from the 1/6 GR test data that the best performance is observed on rotors with two and three blades. Moreover, the two-blade configuration is superior than the three-blade configuration. The maximum power coefficient of the two-blade configuration is approximately 1.5 times that of the three-blade configuration. Another finding is that with the increase of wind speed, the  $C_P$  curve becomes flat at the maximum  $C_P$  area.

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