

1 **Drying Behavior Modeling of Bitumen Emulsion-based Cold In-place Recycling Pavement**
2 **Considering Heat-moisture Coupling Effects**

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11 **ABSTRACT**

12 Bitumen Emulsion-based Cold In-place Recycling (BE-CIR) pavement has been widely applied for its
13 energy-saving and environmental friendliness. BE-CIR is manufactured at ambient temperature and
14 requires a specific drying duration to develop sufficient strength before overlay placement. However, it is
15 challenging to characterize the drying behavior of BE-CIR pavement due to the complex field curing
16 environments and strength formation process. Hence, this research aims to develop a drying behavior
17 model of BE-CIR pavement considering the heat-moisture coupling effects, which can help optimize the
18 timing for overlay placement under different curing environments. Numerical models of mixture and
19 pavement were established based on the heat and mass transfer theories. Actual temperature and humidity
20 data obtained from laboratory tests and field monitoring were used for model calibration and validation.
21 Time-variable coefficient and depth correction coefficient developed based on functional relationships of
22 physical parameters were proposed to calibrate the model. The finite element calculation results indicated
23 that the calibrated model could effectively simulate the drying behavior of BE-CIR pavement under
24 natural curing environments. Two typical working conditions based on natural pavement curing
25 environments were simulated. The calculation results suggested that the curing time required to reach
26 moisture equilibrium was 120 hours at medium temperature and high humidity and 50 hours at low
27 temperature and medium humidity, both higher than the measured 30 hours at high temperature and low
28 humidity.

29 **Keywords:** Bitumen emulsion; Cold in-place recycling; Drying behavior; Numerical simulation; Heat-
30 moisture coupling effects

1 INTRODUCTION

Bitumen Emulsion-based Cold In-place Recycling (BE-CIR) pavement is a green technology for asphalt pavement recycling (Xiao et al., 2018). In the BE-CIR pavement recycling process, crushed old pavement, i.e., aggregates coated with old asphalt, are used as the aggregate source (Gu et al., 2019). Bitumen emulsion is used as the main binder, while non-organic additives, such as Portland cement, are incorporated to obtain high early-stage strength, which allows traffic to be opened earlier (Modarres et al., 2014). Compared to hot recycling pavement, BE-CIR pavement offers significant advantages in terms of energy consumption, economic costs, and environmental protection (Alkins et al., 2008). This is attributed to the 100% utilization of reclaimed asphalt pavement (RAP) and the elimination of heating processes during construction. Nonetheless, BE-CIR is commonly used as a base course material with an additional overlay placed on top due to its relatively weak mechanical properties.

BE-CIR mixture is a visco-elasto-plastic material with complex composition. After rehabilitation and compaction, the BE-CIR mixture is cured under the environmental contexts of ambient temperature and relative humidity (RH). The development of bitumen films containing fine aggregates, non-organic additives, and hydration products during curing is the main contributor to the strength formation of the mixture, resulting from multiple physical and chemical interactions, including emulsion breaking and non-organic additives hydration. Bitumen droplets dispersed in emulsion gradually flocculate and coalesce as the moisture evaporates. This process may continue for more than 28 days and contributes to the long-term mechanical properties of BE-CIR pavement (Miljković and Radenberg, 2015). Hydration reaction between non-organic additives and water can increase alkalinity to change the chemical stability of bitumen emulsion, while hydration products dispersed in bitumen film can increase the viscosity and deformation resistance of BE-CIR (Du, 2014). The curing process can be characterized by water content, which decreases until reaching equilibrium with the environment, with a final water content of approximately 1% by mass of the mixture (Graziani et al., 2016). A portion of this water is trapped in the bitumen film, deteriorating the mixture's cohesive and adhesive properties (Khan et al., 2016). To evaluate the effect of initial water content on pavement performance and the curing degree characterized by mechanical properties, a series of strength indexes or stiffness indexes, including indirect tensile strength, failure tensile strain, and stiffness modulus, were tested (Ouyang et al., 2019). In fact, the effect of water on the mechanical properties and performance of BE-CIR pavement starts from compaction (Gao et al., 2014). Evidently, the presence and transfer of moisture are strongly related to the development of the mechanical properties of the mixture.

Water in newly constructed BE-CIR pavement mainly comes from bitumen emulsion, which contains 25-60% water, and extra water, which accounts for around 2% by mass of the mixture (Flores et al., 2020). Water in bitumen emulsion is used to disperse bitumen droplets for long-term preservation. Due to the lubricating effect, extra water is added in the recycling process to pave and compact the BE-CIR mixture instead of heating and to ensure that bitumen film can coat the aggregate surface entirely and uniformly. To predict the development pattern of mechanical properties and to clarify the strength formation process, research on drying behavior in BE-CIR pavement is essential. As the essential feature of drying behavior, moisture migration is a process of water transfer and phase transition in porous media under the heat-moisture coupling interaction. Fig. 1 illustrates the process of moisture migration in BE-CIR pavement. The mechanism of moisture migration in asphalt pavement includes surface infiltration, capillary rise, and diffusion (Arambula et al., 2010). In the initial curing phase of BE-CIR pavement, diffusion dominates the moisture migration, consisting of gaseous water molecules diffusion and the liquid water molecules evaporation, a phase transition process in which water molecules move away from the surface of the liquid under the action of Brownian motion. After compaction, liquid water evaporates into the gaseous phase, which moves to a lower RH environment following Fick's law. Ultimately, the water content in the BE-CIR mixture is reduced to equilibrium. This process is affected by a combination of internal factors and environmental factors. Internal factors include bitumen emulsion breaking rate, ionic properties of bitumen emulsion, additives interference, micro-void structure, and so on. External factors include ambient temperature, RH, wind speed, solar irradiance, layer thickness, and so on.

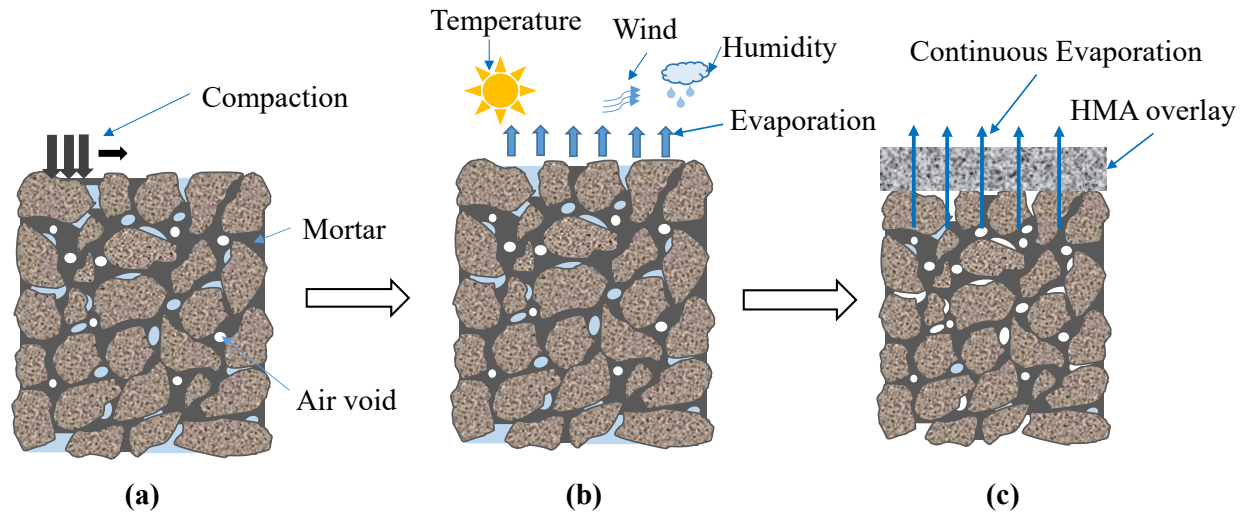


Fig. 1. Moisture migration in BE-CIR pavement: (a) initial full-depth CR mixture after the compaction stage; (b) evaporation during the curing stage; (c) continuous evaporation during the in-service stage.

Many pieces of research have been done to characterize the drying behavior of the BE-CIR mixture. Evaporation dynamics of the BE-CIR curing process were investigated by evaporation tests and hydraulic conductivity tests, using water loss and evaporation rate as indicators (Saadoon et al., 2017). Based on this, an evaporation depth prediction model was proposed and related to the mechanical properties. In-situ tests were conducted to investigate the moisture behavior inside the pavement structure. Ground-penetrating radar, nuclear density and moisture gauge, time-domain reflectometer, and capacitance moisture sensors were used to monitor and predict the evolution of the water content inside the BE-CIR pavement (Kim et al., 2011; Ogbo et al., 2022; Zhao et al., 2022). The study of water vapor movement inside the mixture primarily aims at hot-mix asphalt pavement and its moisture damage resistance. Based on Fick's first law, researchers developed simple devices to measure the effective diffusion coefficient of mixtures, a material property affecting the moisture diffusion behavior (Arambula et al., 2010). Devices based on Fick's second law and thermocouple psychrometers can also measure the effective diffusion coefficient of mixtures, but the method is complicated (Apegyei et al., 2014). It is worth noting that the aforementioned drying behavior studies were conducted under specific constant environments, and the humidity inside the pavement was assumed to be uniformly distributed. Although some patterns have been derived from the existing studies, theoretical analyses based on heat and mass transfer are still lacking, making it difficult to explicate the BE-CIR drying behavior in a field pavement curing environment with real-time variations in temperature and RH. In addition, the overlay placement timing of BE-CIR pavement after compaction in construction mainly relies on experience and lacks theoretical guidance for different curing environments the contractors may encounter in practice.

To fill this gap, the primary objectives of this research are to 1) establish a drying behavior model of BE-CIR pavement under the effect of the moisture-heat coupling before overlay placement; 2) predict moisture equilibrium timing under natural curing environments based on the model.

2 METHODS

2.1 Governing Equations

The drying behavior of BE-CIR pavement is a result of combined mass and heat transfer, and the energy and continuity equations govern the migration of heat and moisture. Ambient temperature and RH are critical factors affecting the drying behavior. To model the drying behavior inside the BE-CIR pavement, following assumptions were taken based on the properties of the curing phase of BE-CIR

118 pavement: (1) ignoring capillary; (2) ignoring liquid water convection; (3) no chemical reactions; (4)
 119 constant geometry.

120

121 2.1.1 Heat Transfer

122 Heat transfer includes three components: heat conduction, heat convection, and heat radiation
 123 (Sun and Sheng, 2020). Heat conduction inside the mixture was calculated using the energy conservation
 124 equation, as shown in Eq. (1) (M. L. Hoang et al., 2003).

125

$$126 (\rho C_p)_{eff} \frac{\partial T}{\partial t} - \nabla \cdot (k_{eff} \nabla T + L_v \delta_p \nabla(\varphi p_{sat})) = Q \quad (1)$$

127

128 Where $(\rho C_p)_{eff}$ = effective volumetric heat capacity at constant pressure; T = temperature; k_{eff}
 129 = effective thermal conductivity; L_v = latent heat of evaporation; δ_p = vapor permeability; φ = relative
 130 humidity; p_{sat} = vapor saturation pressure; Q = heat source.

131 Heat flux at the pavement surface was calculated by Newton's cooling equation shown in Eq. (2)
 132 (Winterton, 1999). Heat transfer coefficient was obtained based on ambient wind speed and width of the
 133 pavement surface.

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$$135 Q_c = h(T_{amb} - T) = \frac{Nu \times \beta}{L} (T_{amb} - T) \quad (2)$$

136

137 Where Q_c = heat flux by convection; h = heat transfer coefficient; T_{amb} = ambient temperature;
 138 Nu = Nusselt number; β = air thermal conductivity; L = characteristic length.

139 Radiative heat transfer included radiation from the environment to the pavement and from the
 140 pavement to the environment. The radiation from the pavement to the environment is calculated by the
 141 Stephan-Boltzmann law shown in Eq. (3) (Nuijten and Høyland, 2017).

142

$$143 Q_F = \varepsilon \sigma (T^4 - T_{amb}^4) \quad (3)$$

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145 Where Q_F = effective radiation rate; ε = surface emissivity; σ = Stefan-Boltzmann constant.

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147 2.1.2 Moisture Migration

148 Moisture migration in the BE-CIR pavement structure consists of diffusion only. According to the
 149 continuity equation and the assumptions mentioned above, Eq. (4) demonstrates governing equation for
 150 moisture (Welty et al., 1976).

151

$$152 \xi \frac{\partial \varphi}{\partial t} + \nabla \cdot g_w = G \quad (4)$$

$$153 \xi = \frac{\partial w(\varphi)}{\partial \varphi} \quad (5)$$

154

155 Where ξ = moisture storage capacity; g_w = diffusive flux for vapor; G = moisture source; $w(\varphi)$ =
 156 water content.

157 Fick's law was employed to describe the moisture flux. The effective diffusion coefficient
 158 expressed in terms of concentration was rewritten as the vapor permeability expressed in terms of
 159 pressure, as shown in Eq. (6) (Paul et al., 2014).

160

$$161 g_w = -\rho_g D_{eff} \nabla \omega_v = -\frac{M_v D_{eff}}{R_{H_2O}} \frac{M_a}{(x_a M_a + x_v M_v)^2} \nabla p_v = -\delta_p \nabla(\varphi p_{sat}) \quad (6)$$

162

163 Where ρ_g = vapor density; D_{eff} = effective diffusion coefficient of BE-CIR mixture; ω_v = vapor
164 mass fraction; M_v = molar mass of water vapor; M_a = molar mass of dry air; R_{H_2O} = universal gas
165 constant of water vapor; p_v = water vapor partial pressure.

166 Wide variations in the temperature of the pavement structure can significantly affect the
167 magnitude of vapor permeability, so the Arrhenius equation was adopted, which proved to be suitable for
168 expressing temperature-dependent reaction rates (Ma et al., 2022).

$$169 D_{eff} = Ae^{-\frac{E_a}{R_{H_2O}T}} \quad (7)$$

170
171 Where A = preexponential factor; E_a = activation energy.

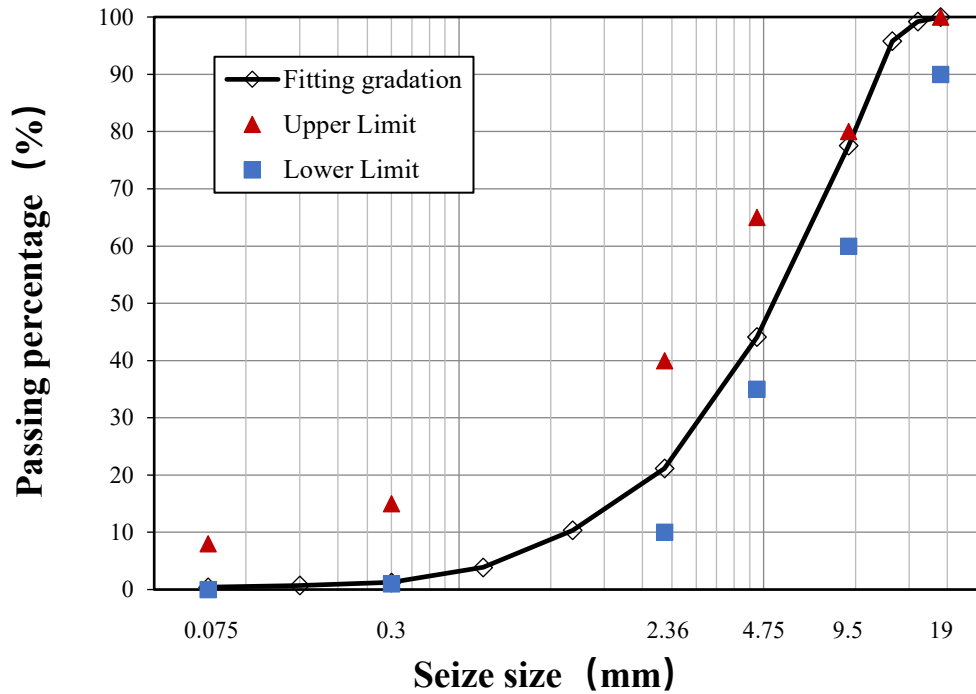
174 2.2 Experimental Study

175 Field and laboratory measurements were implemented to clarify the drying behavior of BE-CIR
176 pavement after compaction and obtain the physical parameters of materials.

177 2.2.1 Field Monitoring for BE-CIR Pavement

178 Field monitoring for the BE-CIR pavement after compaction was executed in a pavement
179 maintenance project at Fenguan Highway (G15) in Lianyungang, Jiangsu Province of China. A trial
180 section with a total length of more than 4 km was treated by the BE-CIR technology, which recycled the
181 original top and middle layer into the BE-CIR layer. During construction, 3.3% cationic slow-setting
182 emulsified asphalt, 2.2% Ordinary Portland Cement (P.O 42.5), 2.8% extra water, and 100% old
183 pavement were recycled into the new BE-CIR layer. Gradation of the BE-CIR layer is shown in Fig. 2,
184 and the properties of the emulsified asphalt are presented in Table 1. The maximum dry density method
185 (MOT, 2019), Marshall Stability Test, and Indirect Tensile Strength Test were employed to determine the
186 optimum moisture content and the optimum bitumen emulsion content. After recycling, the BE-CIR layer
187 must be cured for a period before the overlay is placed. Sensors were buried at road pile number
188 K795+500, located in the construction section from K794+636 to K796+372, with a total length of 1.736
189 km. Four different depths were chosen to embed sensors to record the gradient variation characteristics of
190 temperature and humidity in the BE-CIR layer. The recording lasted 163 hours, from the recycle
191 completion to the overlay placement. Depths 1 to 4 corresponded to 5, 35, 65, and 95 mm from the BE-
192 CIR layer upper surface and were denoted as D1, D2, D3, and D4. Two humidity sensors and one
193 temperature sensor were buried at each depth. The humidity sensor measured the moisture condition of
194 solid using the Frequency Domain Reflectance method, and the output was defined as the humidity index
195 (HI), which varied between 0 and 1. Laboratory tests were implemented to obtain the relationship
196 between water content and HI. A functional equation between RH and water content was determined as
197 well. Based on this, the relationship between HI and RH was obtained. Considering the influence of the
198 curing environment on moisture and temperature distribution inside the BE-CIR layer, ambient
199 temperature, RH, wind speed, and solar radiation during the monitoring were collected from local weather
200 stations. More specific information can be found in the authors' previous study (Zhao et al., 2022).

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Fig. 2. Aggregate gradation of BE-CIR mixture.

Table 1

Properties of emulsified bitumen.

Properties	Value
Residual content (%)	63.8
Penetration (25 °C; 0.1 mm)	62.1
Softening point (°C)	50.6
Ductility (15 °C; cm)	110
Sieve residue (1.18 mm; %)	0.03
Storage stability (5 d, 25 °C; %)	0.18
Storage stability (1 d, 25 °C; %)	0.06

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2.2.2 Indoor monitoring for BE-CIR mixture

Considering the inconvenience of modeling due to the complex field conditions, laboratory mixture tests were implemented as well. 150 mm diameter and 100 mm high mixture specimens were prepared by 30 times gyratory compaction. The RAP was sourced entirely from the trial section field, the gradation was not adjusted, and the material composition was designed to be the same as in the field. A special curing procedure was adopted to simulate the drying behavior in the field condition. Waterproofing membranes were covered on the bottom and sides of the mixtures to achieve unidirectional evaporation (Zhao et al., 2023). The mixtures were cured at a constant temperature and humidity chamber for 28 days at 45% RH, with curing temperatures at 25°C, 30°C, 35°C, 40°C, and 45°C, respectively. On day 1, 3, 7, 14, and 28, the mixtures were taken out and measured for mass, which were combined with the initial mass to calculate water loss. Michaelis-Menten model is commonly used to describe the tendency of material properties to increase rapidly over time and then stabilize, as in Eq. (8) (Graziani et al., 2018). Hence, this model was used to define the relationship between curing time and water loss.

223

$$224 \quad y(t) = \frac{y_A \cdot t}{h_y + t} \quad (8)$$

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226 Where $y(t)$ = water loss; y_A , h_y = fitting parameters with physical meaning, y_A is stabilized value,
227 and h_y is the required curing time to reach half of the stabilized value.

228 Another fully cured mixture slice was prepared, and the effective diffusion coefficient was tested
229 at different temperatures according to ASTM E96 (ASTM, 2014). The effective diffusion coefficient was
230 converted to vapor permeability according to Eq. (6).

231 Due to the difficulty of embedding sensors in the mixture specimens to obtain variations of
232 internal moisture distribution, X-ray computed tomography (X-CT) was implemented. Two mixture
233 specimens 100 mm in diameter and 100 mm in height were prepared with the same material composition
234 as the abovementioned mixture. The curing temperature of these two specimens was 25°C and 40°C.
235 Specimens were scanned on day 0, 3, and 7 after compaction. Scan parameters were set as voltage 240 kV
236 and scanning current 0.72 mA. Body pixels of images were set to 60.1 μm with 1747*1747 pixels per
237 slice. Noise reduction and grayscale transformation were implemented to obtain clearer images. The voids
238 at different moments were extracted by the OTSU method and reconstructed. Scanned images of different
239 curing days were rotated and panned for alignment adjustment. Define the earlier scanned image as the
240 base image and the later scanned image as the processed image. Boolean operations were performed on
241 the processed image and the base image. The portions that were void in the base image and non-void in
242 the processed image were extracted. This portion represented the void change during the curing time,
243 which was the location of dispersed water. The value obtained by dividing the portion's area by the slice's
244 area was defined as the water loss C_{wl} . More specific information can be found in the authors' previous
245 study (Jiang et al., 2023).

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247 **2.3 Model Establishment**

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249 *2.3.1 Laboratory Mixture Model*

250 According to the laboratory mixture test's specimen dimension and curing conditions, a numerical
251 model was established, as shown in Fig. 3(a).

252 Material parameters: Heat and mass transfer parameters of the BE-CIR mixture, including
253 thermal conductivity, heat capacity at constant pressure, vapor permeability, and moisture storage
254 function, were determined from laboratory tests.

255 Boundary conditions: The bottom and sides of the model were moisture and heat insulated, with
256 only the upper surface allowing exchange of moisture and heat flux with the environment.

257 Initial conditions: Initial HI of the whole model was set to be 0.75 according to the initial water
258 content of the mixture, and the initial temperature was set to be 35°C.

259 Environmental conditions: The ambient RH was kept at 30% consistently, while the ambient
260 temperatures were set to 25°C, 30°C, 35°C, 40°C, and 45°C, respectively.

261 Calculation settings: The simulation duration was 28 days; the step size was varied over time to
262 improve the stability and efficiency of the simulation.

263 Observation points were assigned at 10mm intervals at the cylinder center, except for the upper
264 and lower surfaces, with nine observation points employed for data analysis.

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266 *2.3.2 Field Pavement Model*

267 As shown in Fig. 3(b), a model consistent with the field pavement structure was built. The model
268 was 10.76m in depth with five structural layers. The overlay was not built up as it only simulated the
269 situation before it overlaid. The length and width were 3.75m, which means one lane width. In order to
270 ensure simulation accuracy, temperature variations were calculated for each structural layer. Due to the
271 insensitivity of the remaining layers to moisture and computational efficiency, only the moisture
272 distribution inside the BE-CIR layer was simulated.

273 Material parameters: The heat and mass transfer parameters for the BE-CIR layer were identical
 274 to those used in the laboratory mixture model. Material parameters for the remaining structural layers
 275 were collected from literature.

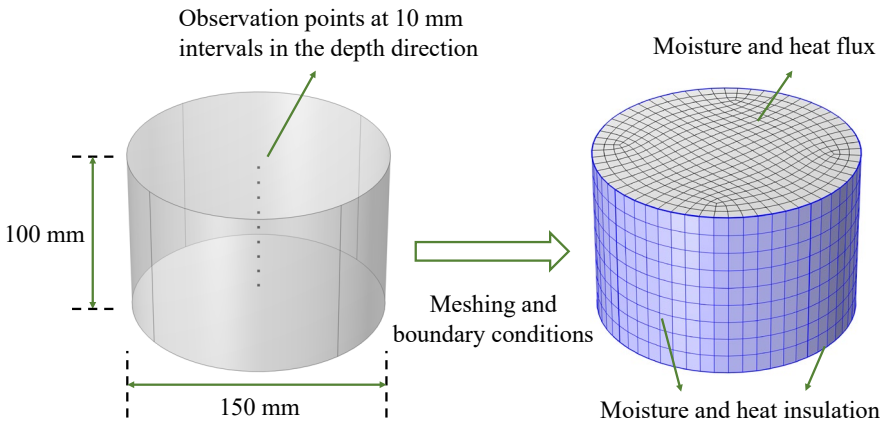
276 Boundary conditions: For the temperature simulation, corresponding to the constant temperature
 277 layer in geography, the temperature at the bottom of the subgrade was constant at 15°C. The sides of the
 278 model were thermally insulated. Heat exchange with the environment existed at the model's upper surface.
 279 For the moisture simulation, the bottom and sides of the BE-CIR layer were set as moisture insulation.
 280 Moisture exchange with the environment existed at the model's upper surface.

281 Initial conditions: Initial HI and temperature at each depth of the BE-CIR layer were obtained
 282 from field-measured data.

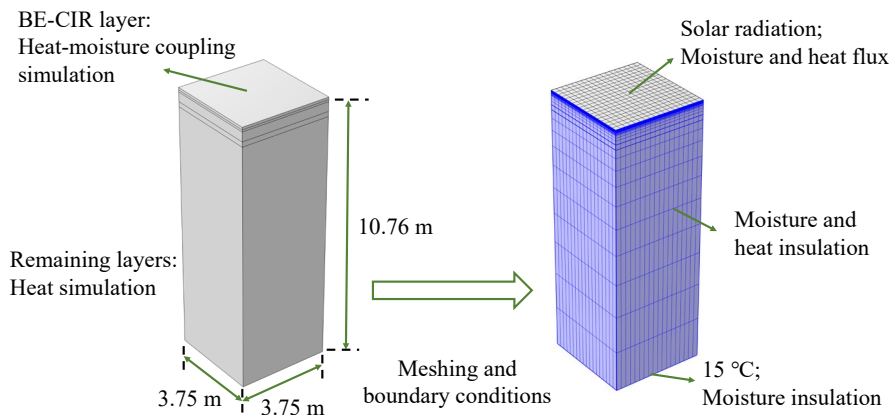
283 Environmental conditions: The ambient temperature, RH, wind speed, solar irradiance, and other
 284 data were collected from the weather station where the field section is located.

285 Calculation settings: The simulation duration was seven days. Starting time was 16:00 on May 23,
 286 2021, corresponding to the sensors' burial time. The maximum solution step was 1 hour to ensure
 287 simulation accuracy.

288 Corresponding to the burial depths of the sensors, four observation points were assigned to
 289 monitor temperature and moisture variations inside the BE-CIR layer.
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(a) Laboratory mixture model schematic



(b) Field pavement model schematic

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 292 **Fig. 3. Numerical simulation model.**

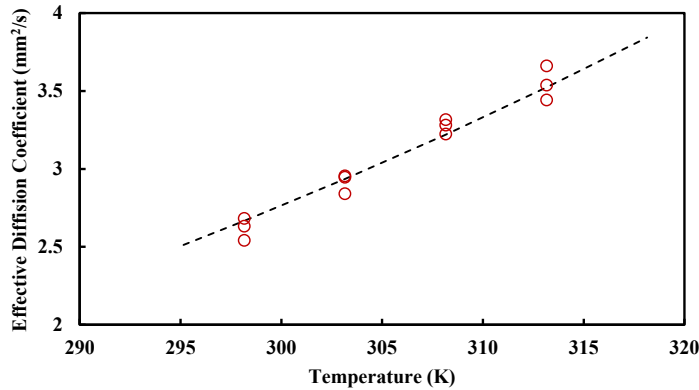
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 294 **3 RESULTS AND DISCUSSION**

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296 **3.1 Drying Behavior Model**

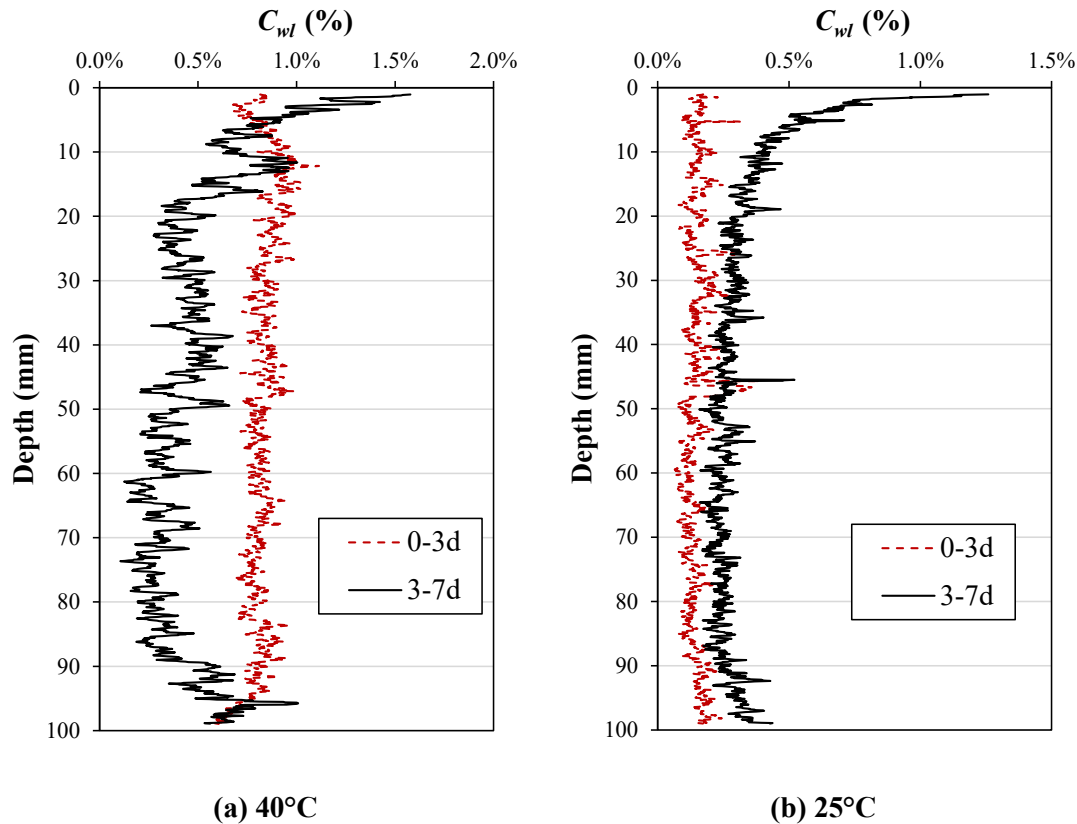
297 Based on Fick's first law, the effective diffusion coefficients were tested at different temperatures,
298 as shown in Fig. 4. The Arrhenius equation was used to fit the effective diffusion coefficient to
299 temperature as in Eq. (9).

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$$D_{eff} = 89.8 \times e^{-\frac{14426}{8.3147T}}$$
 (9)
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305 **Fig. 4.** Fitting model for the effective diffusion coefficient and temperature.
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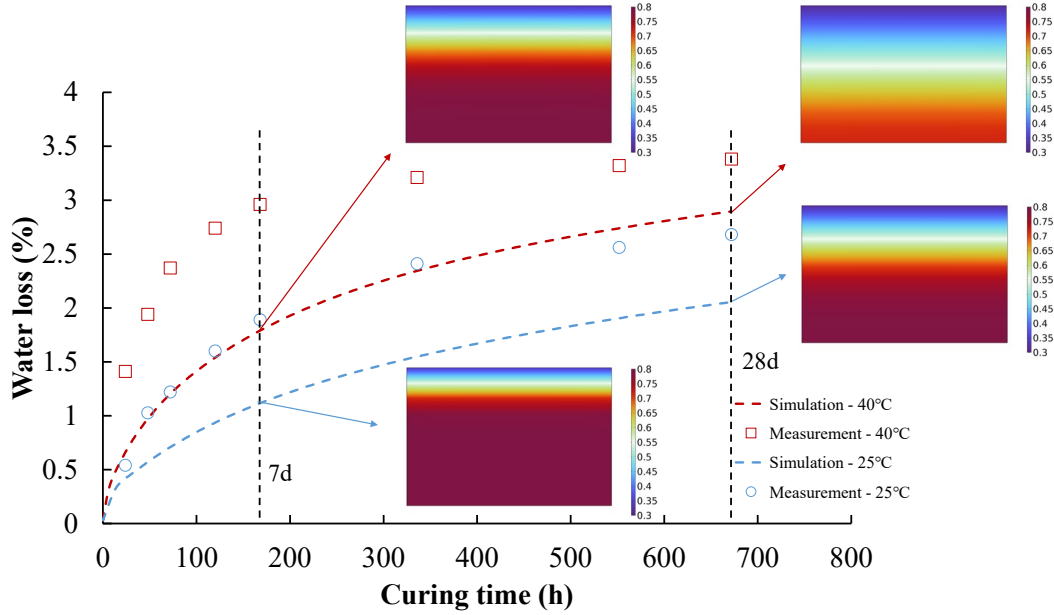
307 Fig. 5 shows the X-CT test results. On the third day, the BE-CIR mixtures with different curing
308 temperatures had no significant gradient characteristics in the depth direction. On the seventh day, the
309 moisture gradient characteristics exhibited in the upper 90 mm for the curing temperature of 40°C and in
310 the upper 45 mm for the curing temperature of 25°C.
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 313 **Fig. 5.** Variation of C_{wl} in depth.(Jiang et al., 2023)
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315 *3.1.1 Time-variable Coefficient Calibration*
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317 The laboratory mixture model was calculated, and the result is shown in Fig. 6. In the first seven
 318 days, the measured water loss increased rapidly while the simulated water loss grew slowly, and the
 319 difference between the simulated and measured values was more evident with higher curing temperatures.
 320 After the seventh day, the difference between the measured and simulated values were gradually
 321 stabilized. It indicated that the effective diffusion coefficient used in the simulation was smaller than the
 322 actual value at the beginning of curing. This phenomenon could be attributed to the different strength
 323 formation mechanisms of BE-CIR and hot-mix asphalt mixture. At the early stage of curing, non-organic
 324 additives such as cement in the BE-CIR mixture had not formed a dense mesh structure, asphalt droplets
 325 were dispersed in the emulsion, and the channel for moisture diffusion was unrestricted, so moisture
 326 evaporated fast. With the increasing curing time, the non-organic additives were gradually hydrated. At
 327 the same time, the asphalt droplets aggregated to form the film. The channels for moisture diffusion were
 328 gradually blocked, which decreased the effective diffusion coefficient with the curing time. According to
 329 the analysis, the effective diffusion coefficient obtained from the laboratory tests was a physical property
 330 of the BE-CIR mixture that had already developed strength, which was much smaller than that in the early
 331 curing stage. Therefore, it is necessary to introduce a time-variable coefficient to correct the effective
 332 diffusion coefficient to reflect the time-dependence of the effective diffusion coefficient of the BE-CIR
 333 mixture (Apegyei et al., 2015).



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Fig. 6. Simulation results of model uncorrected by the time-variable coefficient.

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A time-variable effective diffusion coefficient relationship was constructed to clarify the decay pattern of the effective diffusion coefficient during the curing process. It has been demonstrated that the effective diffusion coefficient exhibited a tendency to decrease with increasing modulus in the asphalt mixture. For the BE-CIR mixture, the relationship between strength and residual water content during the curing process could be described by a linear function (Graziani et al., 2018). The residual water content was defined as the water content of the mixture at the initial moment minus water loss at the current moment, while the relationship between water loss and the curing time can be described by the Michaelis-Menten model (Graziani et al., 2018). Based on the relationship between the curing time, water loss, residual water content, strength, and effective diffusion coefficient, Eq. (10) defined an expression for the time-variable coefficient $\varphi(t)$. When $t = 0$, $\varphi(t) = e^{ky_A}$, and when $t = +\infty$, $\varphi(t) = 1$, which corresponds to the return of $\varphi(t)$ to the measured effective diffusion coefficient after a period of curing.

According to the laboratory tests results, y_A and h_y were temperature dependent and could be fitted by linear and exponential functions, respectively, as in Eq. (11) and Eq. (12).

$$\varphi(t) = e^{k\left(y_A - \frac{y_A \cdot t}{h_y + t}\right)} \quad (10)$$

$$y_A = 0.0268T + 2.428 \quad (11)$$

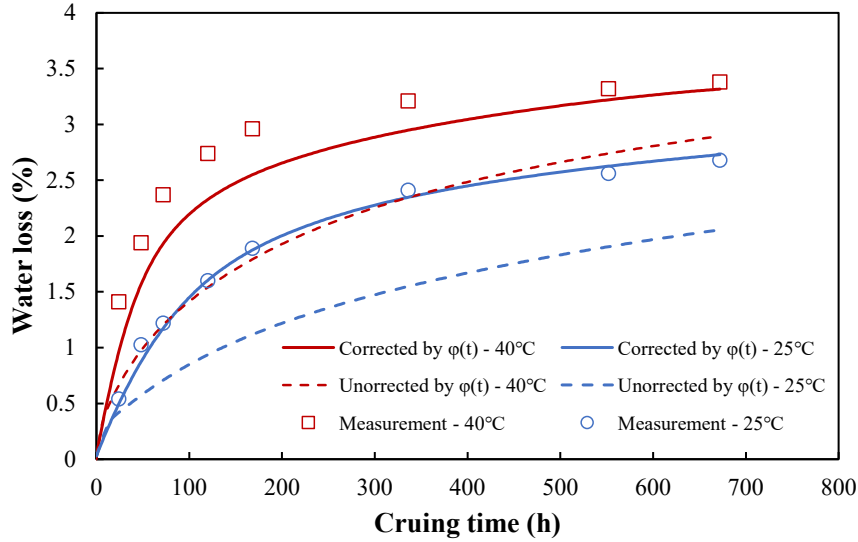
$$h_y = 27.007e^{-0.072T} \quad (12)$$

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Where k = adjustment coefficient to correct the effective diffusion coefficient at the initial moment of curing.

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The adjustment coefficient was set to 1. The calculation results of the modified model with the time-variable coefficient are shown in Fig. 7. The relationship curves between water loss and curing time changed significantly after introducing the time-variable coefficient. The simulated results, closer to the measured values, indicated that adopting the time-variable coefficient was effective.



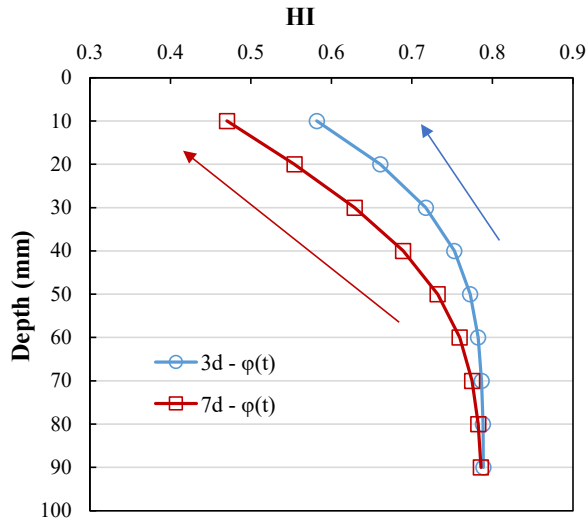
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364 **Fig. 7.** Comparison of simulation results after introducing the time-variable coefficient.
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366 3.1.2 Depth Correction Coefficient Calibration

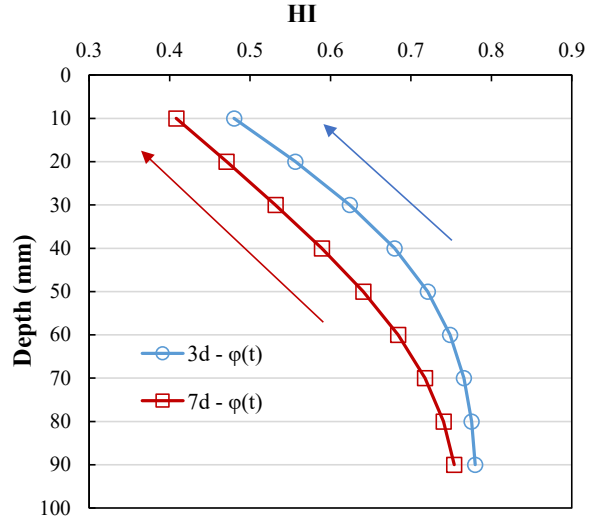
367 Fig. 8 shows the humidity distribution inside the mixture in depth on the third day and the
368 seventh day of curing. On the third day of curing, significant gradient characteristics were present
369 between 0-50 mm depth for both mixtures at two curing temperatures. On the seventh day of curing, the
370 mixture cured at 40°C demonstrated a moisture gradient over almost the entire depth, whereas the mixture
371 cured at 25°C was characterized by a moisture gradient only between 0-60 mm at depth. By comparing
372 Fig. 5 and Fig. 6, the simulated and measured values showed different patterns in depth, which was
373 attributed to the same effective diffusion coefficient of the model over the depth. With the BE-CIR
374 material losing moisture, the combined effect of bitumen emulsion breaking and cement hydration formed
375 the material's strength while at the same time blocking the channels for moisture diffusion and decreasing
376 the effective diffusion coefficient. Measured and simulated results demonstrated that the moisture
377 evaporated from the upper surface of the mixture and gradually dried the whole mixture downward along
378 the depth direction. This indicated that the top-to-bottom moisture drying process of the material during
379 the actual curing process resulted in a similar top-to-bottom gradient in the effective diffusion coefficient
380 of the material. A drier depth position implied a lower effective diffusion coefficient. A depth correction
381 coefficient ω was proposed to characterize this phenomenon. This coefficient was affected by φ , with
382 high φ leading to high effective diffusion coefficient. Meanwhile, the strength formation was an
383 irreversible process, and the strength would not vary remarkably in a short time due to variations in φ .
384 Consequently, the depth correction coefficient ω should decrease gradually with increasing curing time
385 and eventually to 1. In summary, the depth correction coefficient should be expressed as a function
386 affected by φ and time t , denoted as $\omega(\varphi, t)$. The depth correction coefficient was essentially a time-
387 variable coefficient in depth, so the same exponential relationship was employed to describe the depth
388 correction coefficient, as shown in Eq. (13).
389

$$390 \omega(\varphi, t) = e^{\left(\frac{\varphi}{t+m}\right)} \quad (13)$$

391
392 Where m = adjustment coefficient that controls the timing of the depth correction coefficient
393 taking effect. m can be preset to 0.01 to ensure $\omega(\varphi, t)$ makes sense at $t = 0$.
394



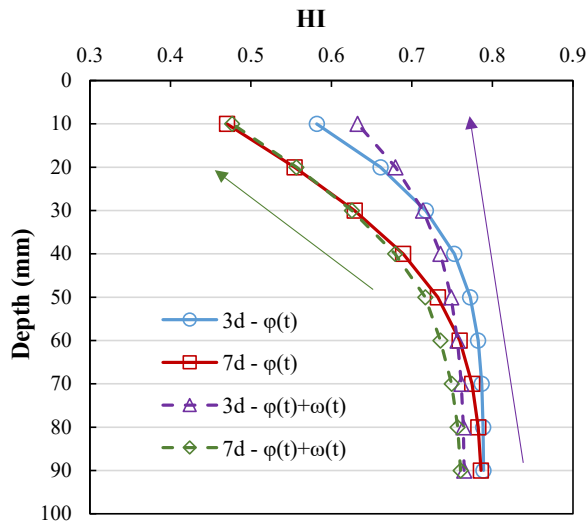
(a) 25°C



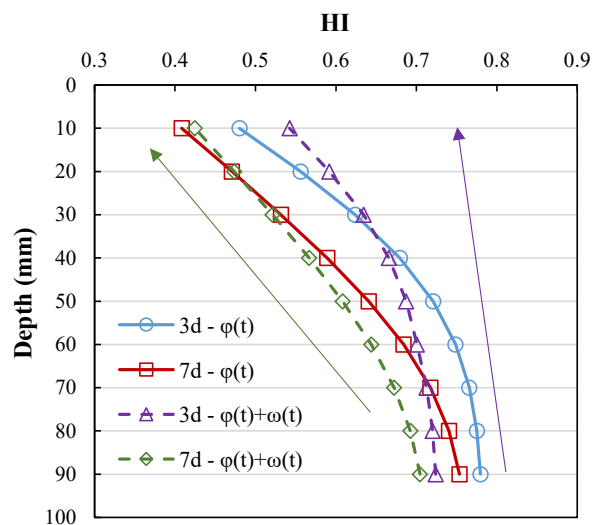
(b) 40°C

395
396 **Fig. 8.** Moisture distribution in depth.
397

398 The model modified by the time-variable coefficient and depth correction coefficient was
399 calculated, and m was finally determined to be 0.6. Calculation results are shown in Fig. 9. The results
400 indicated that the difference in moisture distribution at each depth was reduced and close to the measured
401 results.
402



(a) 25°C



(b) 40°C

403
404 **Fig. 9.** Effect of depth correction coefficient on the moisture distribution in depth.
405

406 The final form of the effective diffusion coefficient after modification by the time-variable
407 coefficient and depth correction coefficient is shown in Eq. (14) and Eq. (15). In order to verify the

408 accuracy of the model after the modification of two coefficients, the model was employed to calculate the
 409 water loss of the mixture at curing temperatures of 25°C, 30°C, 35°C, 40°C, and 45°C, respectively.
 410 coefficient of determination (R^2 , Eq. (16)) and Root Mean Square Error (RMSE, Eq. (17)) were adopted
 411 to evaluate the simulation results. Fig. 10 demonstrates the comparison results between simulated and
 412 measured values for different curing days and different curing temperature. The results showed that all
 413 points were close to the line of equality, and the R^2 reached 0.956, meaning that the simulation was
 414 accurate.
 415

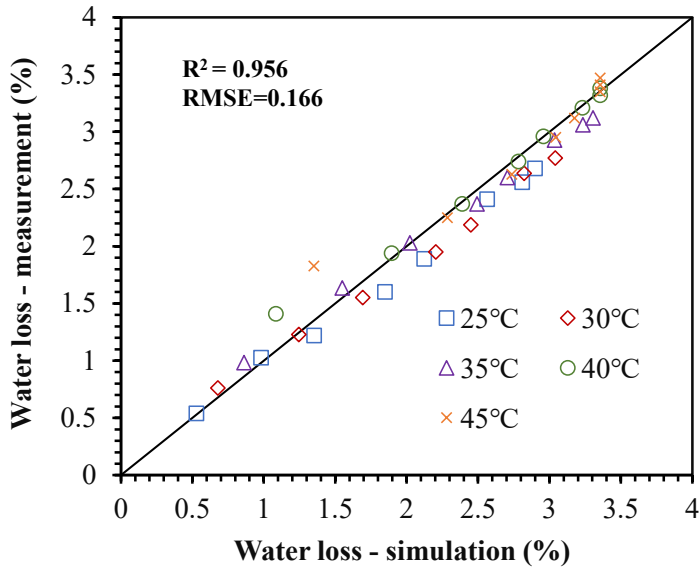
$$416 \quad D_{eff} = Ae^{-\frac{E_a}{RH_2O T}} \cdot \varphi(t, T) \cdot \omega(\phi_w, t) \quad (14)$$

$$417 \quad D_{eff} = 89.8e^{-\frac{1735}{T}} \times e^{\left(0.0268T + 2.428 - \frac{(0.0268T + 2.428) \cdot t}{27.007e^{-0.072T} + t} + \frac{\varphi}{t + 0.6}\right)} \quad (15)$$

$$418 \quad R^2 = 1 - \frac{\sum_{i=1}^m (\hat{y}_i - y_i)^2}{\sum_{i=1}^m (y_i - \bar{y})^2} \quad (16)$$

$$419 \quad RMSE = \sqrt{\frac{1}{m} \sum_{i=1}^m (y_i - \hat{y}_i)^2} \quad (17)$$

420 Where \hat{y}_i = simulated value; y_i = measured value; \bar{y} = mean of the measured value.
 421

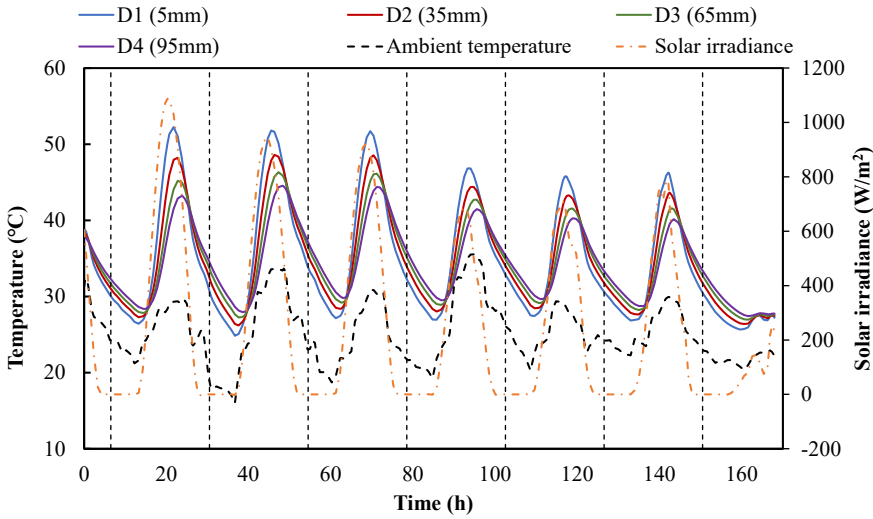


422
 423
 424 **Fig. 10.** Evaluation of model corrected by two coefficients.
 425

426 3.1.3 Model Validation

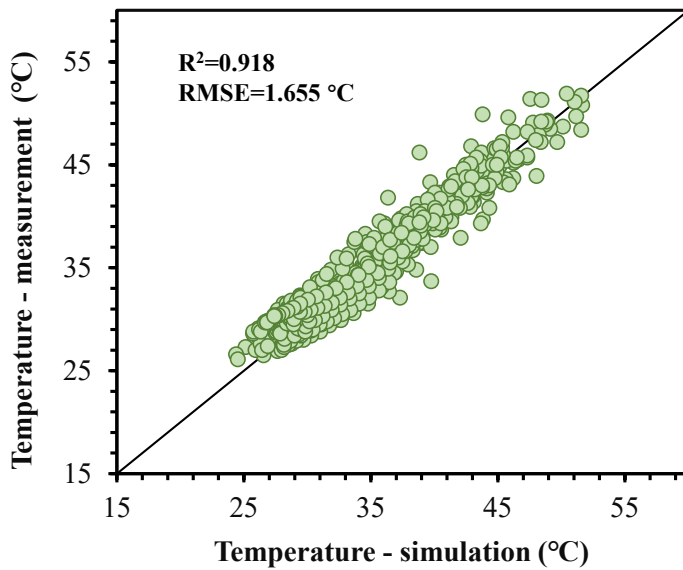
427 The two correction coefficients obtained from the laboratory mixture model were applied to the
 428 field pavement model calculations to validate the accuracy of the model parameters.

429 Fig. 11 illustrates the results of temperature field simulation for the BE-CIR layer. Fig. 12
 430 compares the simulated and measured results of the temperature field. The comparison results showed
 431 that the simulated the R^2 reached 0.93 and the RMSE was only 1.655 °C. The model could accurately
 432 simulate pavement temperature changes.
 433



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437

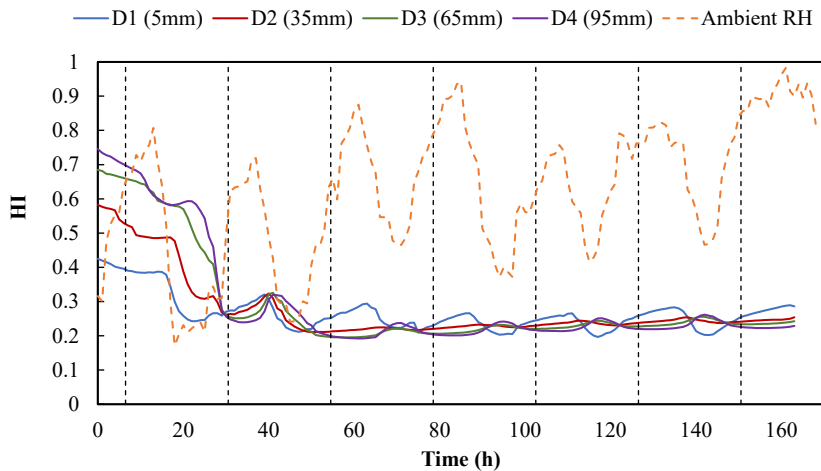
Fig. 11. Simulation result of temperature field.



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Fig. 12. Evaluation of temperature field simulation results.

Fig. 13 illustrates the HI simulation results for the BE-CIR layer. Unlike the uniform initial humidity distribution of the laboratory mixture model, a humidity gradient distribution had been characterized inside the pavement after compaction. There were different degrees of delay in humidity decline at each depth. After about 30 hours of humidity decrease, the moisture movement inside the BE-CIR layer stabilized and only slightly fluctuated with ambient RH variation. The simulated results showed a consistent trend with the measured results.



449
450

451 **Fig. 13.** Simulation results of HI at each depth.

452

453 Fig. 14 demonstrates the simulated values of HI at each depth compared to the measured values.

454 The corrected and uncorrected models were computed separately to validate the two correction

455 coefficients. For the uncorrected model, the HI of D2 and D3 were constantly higher than the measured

456 values, and the HI of D4 was also higher than the measured values after the 11th hour. This phenomenon

457 indicated that the effective diffusion coefficient uncorrected by the time-variable coefficient was too

458 small in the early curing stage. This resulted in a slow moisture diffusion inside the pavement and

459 moisture accumulation. The large fluctuations in HI at D1 indicated that the effective diffusion coefficient

460 uncorrected by the depth correction coefficient was large at that depth, making HI susceptible to ambient

461 RH. The computational results of the uncorrected model verified the necessity of correcting the effective

462 diffusion coefficients for time and depth. The calculated results of the corrected model fitted the measured

463 data better than those of the uncorrected model, but there were still gaps. The decrease rate of HI was

464 faster for the measured values. On the one hand, this might be related to the complex curing conditions of

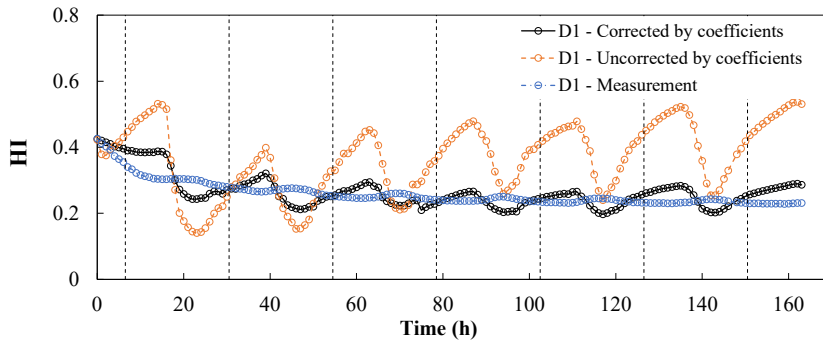
465 the actual pavement, where pavement compaction by vehicles after recycling might result in accelerated

466 moisture migration. On the other hand, both sides and bottom of the field pavement model were set to be

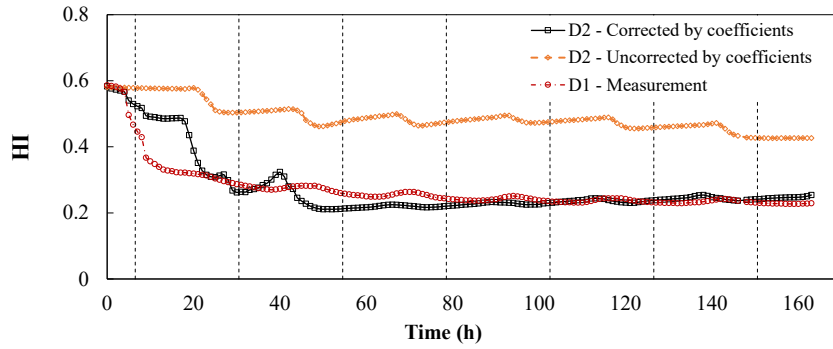
467 moisture insulated, whereas they were permeable to moisture in the actual pavement curing environment,

468 which led to a rapid drop in humidity.

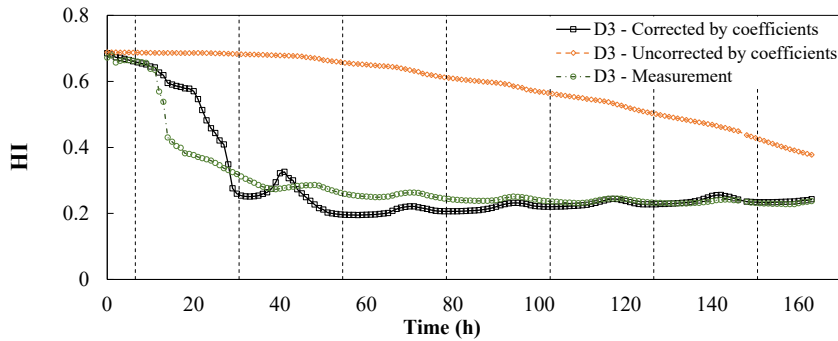
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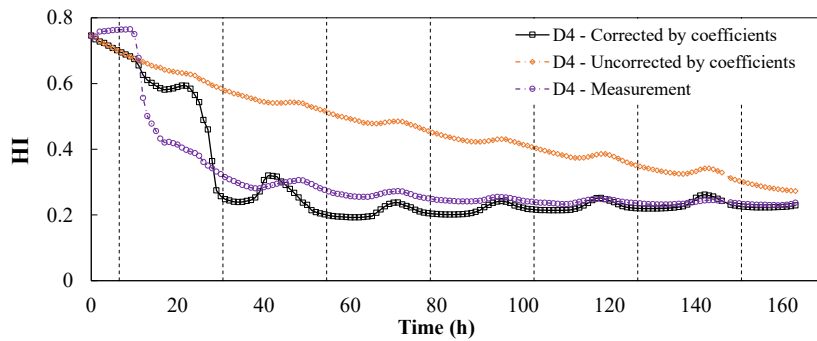
(a) Depth1 - 5mm



(b) Depth2 - 35mm



(c) Depth3 - 65mm

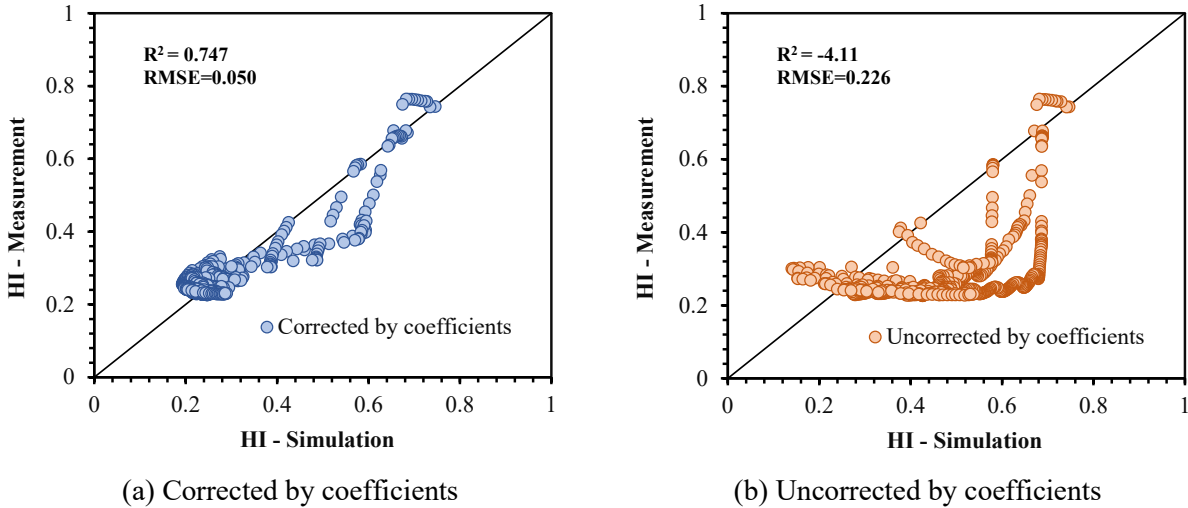


(d) Depth4 - 95mm

470
471 **Fig. 14.** Humidity comparison between simulation and measurement at each depth.
472

473 Fig. 15 evaluated the difference between the calculated results of the corrected and uncorrected
474 models and the measured values, respectively. The results suggested that the difference between the
475 calculated results of the uncorrected model and the measured values was significant, with the R^2 less than
476 0. Most of the simulated values were significantly greater than the measured values. The calculated
477 results of the corrected model were closer to the measured values, with the R^2 up to 0.747 and the RMSE
478 was only 0.05. The comparison indicated that the correction of the two coefficients can greatly improve
479 the accuracy of humidity field simulation results.

480



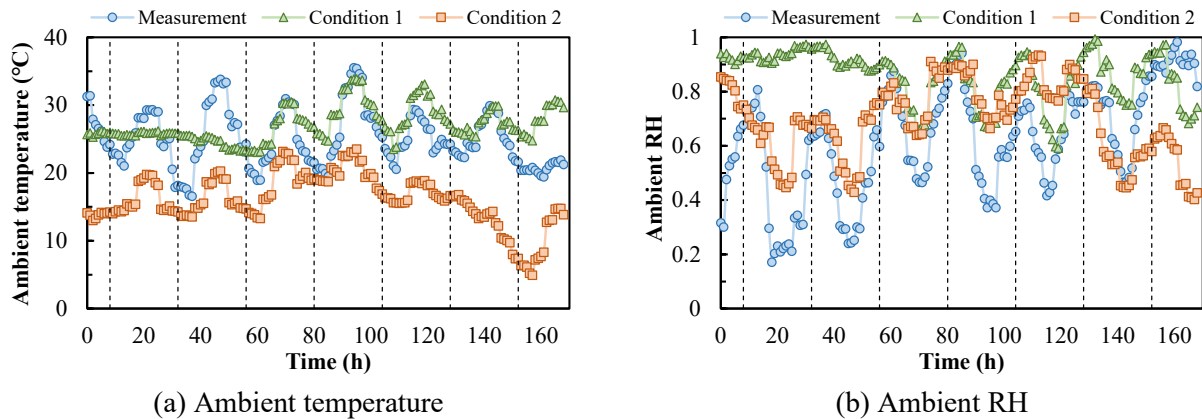
481
482 **Fig. 15.** Evaluation of simulation results.
483

484 By combining with the temperature field simulation results, it was observed that the model
485 corrected by the two coefficients could accurately simulate and predict the temperature field and humidity
486 field under a natural pavement curing environment. The validity of the drying behavior model was
487 verified.
488

489 **3.2 Effect of Curing Environment on Drying Behavior**

490 The duration between compaction and overlay placement on BE-CIR pavement significantly
491 impacts construction economics. Early overlay placement and traffic opening reduce the impact of
492 construction on community transportation capacity. The moisture distribution inside the BE-CIR
493 pavement is an important factor influencing the timing of overlay placement. Generally, a higher moisture
494 evaporation degree corresponds to a stronger pavement strength. Nevertheless, due to the difficulty of
495 real-time monitoring of the moisture inside pavement, constructors often determine the overlay placement
496 timing through coring tests and empirical judgment, which raises the economic expense to some extent
497 and is detrimental to long-term healthy pavement service. The drying behavior prediction model based on
498 two correction coefficients can calculate the moisture distribution of the BE-CIR layer under different
499 natural curing environments in real-time, which is vital to guide the placement timing of the overlay.

500 Two typical working conditions were selected to clarify the effect of the curing environment on
501 the drying behavior of BE-CIR pavement. The different working conditions were distinguished based on
502 temperature and RH, which were categorized into three classes, i.e., low, medium, and high. The grade
503 thresholds for temperature were 17°C and 25°C, and for RH were 55% and 90%. Condition 1 was rainy
504 summer days with medium temperature and high humidity, and condition 2 was regular fall days with low
505 temperature and medium humidity. Meteorological data of Lianyungang, Jiangsu Province, China, where
506 the trial section is located, from 2021/7/27 16:00 to 2021/8/3 16:00 and from 2021/10/10 16:00 to
507 2021/10/17 16:00 were collected to serve as curing environments for the two conditions. As a comparison,
508 the curing environment for the trial section was dry summer days with high temperature and low humidity.
509 These three conditions represented the relatively extreme environments encountered during construction.
510 The cure duration required for moisture equilibrium for the remaining six conditions was almost
511 exclusively between these three conditions. Fig. 16 illustrates the ambient temperature and RH of these
512 three curing environments. The measured humidity distribution used for model validation was employed
513 as the initial value for this simulation, and the temperature distribution at the initial moment was set to be
514 the same as the ambient temperature. The remaining simulation settings were consistent with those of the
515 field pavement model.



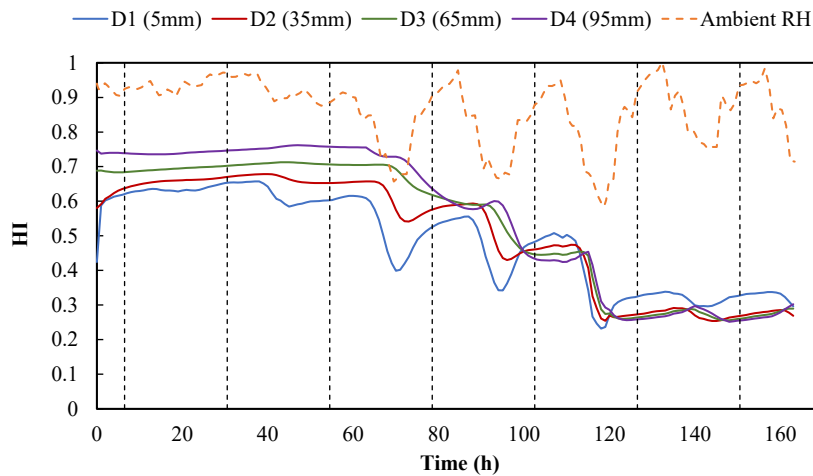
517

518 **Fig. 16.** Ambient temperature and RH for different working conditions.

519

520 Fig. 17 shows the HI calculation result of the BE-CIR layer for condition 1. It could be observed
 521 that the moisture variation inside the BE-CIR layer was in three stages. In the first stage, the HI remains
 522 constant at all depths. Corresponding to the summer rainy days, the ambient RH was higher than 0.9 for
 523 the first 38 hours of this condition, while the ambient temperature was kept around 25°C. The HI at each
 524 depth increased slowly with time during the first 38 hours and generally remained at a high level. In the
 525 second stage, the HI decline at all depths decreased in the order of depth. After the 38th hour, rainfall
 526 weakened, and ambient RH fluctuated periodically. Between the 38th and 120th hour, the HI at all depths
 527 showed an overall decreasing trend with increasing time, which was attributed to the declining ambient
 528 RH and increasing temperature, implying the evaporation of moisture inside the pavement. In the
 529 third stage, the HI decline ended and remained stable. After the 120th hour, the HI fluctuated around 0.26 at all
 530 depths. Although ambient RH remained at a high level, benefiting from the correction of the time-variable
 531 and depth correction coefficients, the fluctuation of HI was slight. According to the trial section's test
 532 results, HI dropping to 0.3 meant a general end of drying and overlay placement. For condition 1, which
 533 represented a hot rainy day, 120 curing hours were required for moisture evaporation, implying up to the
 534 standard of overlay placement. From the 40th to the 120th hour at the end of the rainfall, it took 80 hours
 535 for the BE-CIR layer to reach a moisture equilibrium state, much larger than the 30 hours in the trial
 536 section. The results suggested that rainfall had a detrimental effect on the drying of BE-CIR pavement. If
 537 it was rainy at the end of construction, the timing of overlay placement should be delayed to ensure the
 538 drying of the BE-CIR layer.

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542 **Fig. 17.** HI calculation results for condition 1.

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Fig. 18 illustrates the result of HI calculation of the BE-CIR layer for condition 2. From 0 to the 50th hour, the HI at each depth decreased with the ambient RH fluctuation. The rate of decrease was faster in the 40th to the 50th hour than in the 0 to the 40th hour. After the 50th hour, the overall HI at all depths stabilized at about 0.3. From the 50th to the 90th hour, the HI of BE-CIR increased slightly corresponding to the overall increase in ambient RH. After 90 hours, the BE-CIR dryness declined with the overall decrease in ambient RH. The results suggested that for the condition 2, representing low-temperature normal days, 50 curing hours were required to reach the moisture equilibrium state for the BE-CIR layer. The drying time for condition 2 was longer than that measured in the trial section with high temperature and low humidity due to the reduction of the effective diffusion coefficient caused by temperature drop. However, the drying time for condition 2 was shorter than that for condition 1, which was a rainy day after compaction.

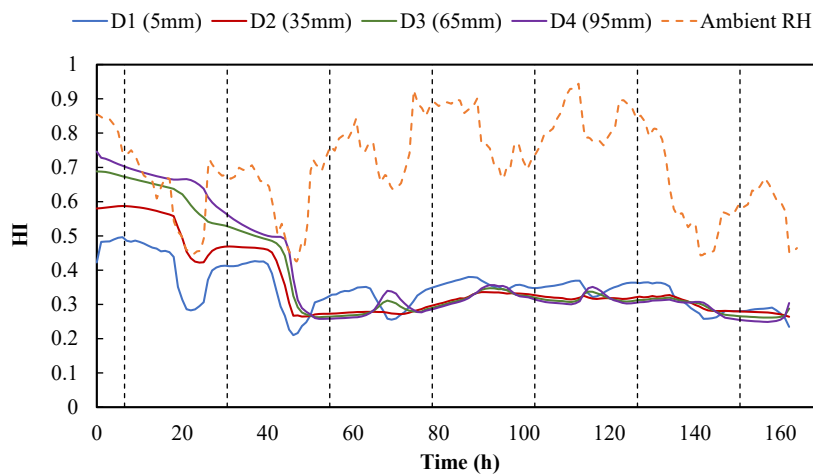
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The simulation results of the two working conditions indicated that the curing environment after compaction could significantly affect the drying behavior of the BE-CIR layer, mainly in terms of the time duration of curing to the moisture equilibrium state as influenced by ambient temperature and RH.



559

560

561 **Fig. 18.** HI calculation results for condition 2.

562

563 **4 CONCLUSIONS**

564 In this research, drying behavior models of BE-CIR were developed for laboratory mixture and
565 field pavement, respectively. Heat-moisture coupling effect was considered to ensure the modeling
566 accuracy. A model of laboratory mixture was established, and the model parameters were calibrated by
567 comparing the simulation results with the measured data. A field pavement model was developed based
568 on actual environmental conditions, corrected material parameters, and pavement structural layer
569 information. Monitoring data obtained from the sensors were used to define the initial temperature and
570 humidity conditions and to validate the simulation. The validated model simulated the pavement drying
571 behavior under two natural curing environments different from the field pavement. The calculations could
572 provide a guide to the curing duration before overlay placement in different natural environments. A
573 complete process of model establishment, parameters calibration, model validation, and model application
574 of BE-CIR pavement drying behavior was determined. The primary results and conclusions can be
575 summarized as follows:

576 (1) A time-variable coefficient was introduced for the unique strength formation process of BE-
577 CIR. Laboratory model calculations showed that water loss in the first three curing days was much less
578 than the measured value, indicating that the effective diffusion coefficient of BE-CIR was not a constant
579 value but decreased with the strength formation during the curing process. Based on laboratory test results,
580 relationships between several physical parameters were established to determine the form of the time-
581 variable coefficient and fitting parameters.

582 (2) A depth correction coefficient was introduced to characterize the unidirectional moisture
583 evaporation of BE-CIR. Mixture model calculations corrected by the time-variable coefficient indicated
584 that the moisture gradient distribution pattern in depth was inconsistent with the measurements. The depth
585 correction coefficient was proposed by combining the relationship between moisture evaporation, strength
586 formation, and effective diffusion coefficient.

587 (3) With testing of the BE-CIR mixture's basic material parameters after curing and the
588 introduction of two correction coefficients, the pavement model with insulation on the sides and bottom
589 can accurately predict the drying behavior of BE-CIR pavements under the heat-moisture coupling effects.
590 The gradient characteristics and variation patterns of the temperature and moisture fields of the BE-CIR
591 pavement under natural curing environments were precisely calculated.

592 (4) Curing environments with low temperatures and high humidity extended the time it took to
593 reach moisture equilibrium for the BE-CIR pavement, implying a delay in overlay placement. The curing
594 time to moisture equilibrium was calculated to be 120 hours for condition 1, representing medium
595 temperature and high humidity, 50 hours for condition 2, representing low temperature and medium
596 humidity, and greater than 30 hours for the trial section, representing high temperature and low humidity.

597 Based on the finite element model proposed in this research, it is necessary to establish a strength
598 prediction model for BE-CIR pavement in the future to calculate the al mechanical response under the
599 multi-physical field coupling effects. This appears to have a significant potential to study the development
600 and deterioration mechanisms of BE-CIR material properties under complex curing conditions and to
601 establish a real-time responsive digital twin model.

602

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