

1     **Sustainability Prioritization of Energy Storage Technologies for Promoting the Development**  
2     **of Renewable Energy: A Novel Intuitionistic Fuzzy Combinative Distance-based Assessment**  
3    **Approach**

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24 **Abstract:** Energy storage technology plays an important role for promoting the development of  
25 renewable energy sources due to their highly erratic and intermittent characteristics. However, it is  
26 usually difficult for the decision-makers/stakeholders to select the most sustainable scenario among  
27 multiple energy storage technologies. This study aims at developing a novel multi-criteria decision  
28 making method by combining the interval analytic hierarchy process (IAHP) and the intuitionistic  
29 fuzzy combinative distance-based assessment method for prioritizing the alternative energy storage  
30 technologies. Four alternative energy storage technologies including pumped hydro, compressed air,  
31 lithium-ion, and flywheel were studied by the proposed method, the sustainability sequence of the  
32 four energy storage technologies from the most sustainable to the least is pumped hydro, flywheel,  
33 lithium-ion, and compressed air. Sensitivity analysis was also carried out to investigate the effects  
34 of the weights of the metrics on the sustainability ranking of the four alternative energy storage  
35 technologies, and the results reveal that altering the preferences/willingness of the decision-  
36 makers/stakeholders and the relative importance of the metrics will change the sustainability  
37 ranking of the four energy storage technologies.

38  
39 **Keywords:** Energy storage technologies; sustainability; intuitionistic fuzzy set; Combinative  
40 Distance-based Assessment Method

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## 48        **1. Introduction**

49        The development of the power based on renewable energy sources (i.e. wind power, solar energy,  
50        and tidal energy, etc.) has been recognized as a promising way for energy security improvement and  
51        emissions mitigation all over the world (Ren and Sovacool, 2015). However, the integration of  
52        renewable energy sources into grid is often faced with reluctance by the utility operators due to the  
53        intermittent and stochastic features of renewable energy sources (Hall and Bain, 2008; Kuravi *et al.*,  
54        2013). With the increase of the share of intermittent renewable energy sources in the power industry  
55        in many countries, energy storage technology for creating smart grid with a better utilization of  
56        fluctuating renewable energy sources becomes more and more important.

57        As discussed above, energy storage technology for facilitating the large-scale integration of  
58        variable renewable electricity sources, plays an important role in promoting the integration of  
59        renewable energy sources into grid through capturing immediate resources and keeping until they  
60        are required as renewable energy sources are usually highly erratic and intermittent (Satkin *et al.*,  
61        2014). However, it is usually difficult for the decision-makers/stakeholders to select the most  
62        sustainable or the most suitable energy storage technology, because the decision-makers usually  
63        face multiple alternative choices for energy storage, i.e. mechanical (pumped hydro, compressed air  
64        and flywheel), electrochemical, thermochemical, thermal, chemical, and electrical energy storage  
65        technologies (Luo *et al.*, 2015). Meanwhile, the decision-making process also involves multiple  
66        conflict criteria when selecting the most suitable/sustainable scenario among multiple energy  
67        storage technologies.

68        According to literature reviews (Hadjipaschalis *et al.*, 2009; Divyaand Østergaard, 2009; Koohi-  
69        Kamali *et al.*, 2013), it is apparent that different energy storage technologies have different  
70        performances on economic, environmental and social aspects. For instance, the capital costs of  
71        pumped hydro energy storage and lithium-ion energy storage are different; they also have different

72 environmental impacts and technological characteristics; in addition, the social impacts of these two  
73 technologies are also different because of their different performances on economic, environmental  
74 and technological aspects. Therefore, the decision-making on energy storage technology selection is  
75 of vital importance for the decision-makers/stakeholders to select the best scenario among multiple  
76 alternatives.

77 There are many studies focusing on multi-criteria decision making on the selection of energy  
78 storage technologies. For instance, Vo *et al.* (2017) employed cost, position flexibility, storage  
79 capacity/discharge time, efficiency, environmental issues, and energy carrier vector to compare  
80 three energy storage technologies, i.e. power to gas (methane), pumped hydroelectric storage and  
81 compressed air energy storage. Barin *et al.* (2009) combined Analytic Hierarchy Process (AHP) and  
82 fuzzy logic to evaluate the energy storage systems. Lee and Ho (2016) developed a technology  
83 evaluation technique to analyze the promising electricity storage technologies by considering  
84 multiple criteria (i.e. operation cost, safety, and deep-cycle life, etc.). All these studies are beneficial  
85 for the decision-makers/stakeholders to select the best energy storage technologies; however, there  
86 are still two research gaps:

87 (1) The lack of the methods for multi-criteria decision making under uncertainties, most of the  
88 previously published works have to know the exact data of the alternative energy storage  
89 technologies with respect to the metrics, while it is usually difficult to obtain all the data,  
90 and the methods for decision-making under uncertainties are of vital importance;

91 (2) The lack of the methods for accurately determining the weights of the metrics which  
92 represent the preferences/willingness of the decision-makers/stakeholders; AHP is the most  
93 widely used method for weights determination in the multi-criteria decision making on the  
94 selection of the alternative energy storage technologies, while this method relies on the  
95 scales from 1 to 9 and their reciprocals to establish the comparison matrix, it is usually

96 difficult for the users to use a crisp number to depict the relative preference of one metric  
97 over another.

98 The objective of this study is to overcome the above-mentioned two research gaps and develop a  
99 generic sustainability assessment method for prioritizing the alternative energy storage technologies  
100 comprehensively with the considerations of multiple sustainability criteria under uncertainties  
101 according to the actual conditions and the preferences of the decision-makers/stakeholders for the  
102 integration of renewable energy sources into grid, and to achieve scientific and democracy decisions  
103 for adapting the increased renewable energy penetration. The results obtained by the proposed  
104 method highlight the development roadmap of energy storage technology for promoting the  
105 development of renewable energy.

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## 107 **2. Methods**

108 There are three parts in this section. The criteria for sustainability assessment of energy storage  
109 technology were firstly presented in section 2.1; fuzzy set and intuitionistic fuzzy set were  
110 subsequently introduced in section 2.2; The intuitionistic fuzzy Multi-criteria decision making  
111 method was then developed by combining the Interval Analytic Hierarchy Process (IAHP) and the  
112 developed the Intuitionistic Fuzzy Combinative Distance-based Assessment Method (IFCODAS) in  
113 section 2.3.

### 114 2.1 Criteria for sustainability assessment of energy storage technology

115 Sustainability or sustainable development refers to achieve economy booming, environmental  
116 protection and social responsibility simultaneously (Ren et al., 2016). Thus, economic,  
117 environmental, and social issues are the three pillars of sustainability, and the criteria/metrics in  
118 these three aspects are widely used for sustainability assessment. A total of nine metrics in four  
119 aspects including economic, environmental, technological, and social aspects are summarized for

120 sustainability assessment of energy storage technology, and they are capital cost (EC<sub>1</sub>), life (EC<sub>2</sub>),  
 121 and operating cost (EC<sub>3</sub>) in economic aspect (EC), CO<sub>2</sub> density (EN<sub>1</sub>) and integrated environmental  
 122 impact (EN<sub>2</sub>) in environmental aspect (EN), energy efficiency (T<sub>1</sub>), energy density (T<sub>2</sub>), and  
 123 technology maturity (T<sub>3</sub>) in technological aspect (T) , and social acceptability (S<sub>1</sub>) in social aspect  
 124 (S) based on literature review (Ren and Ren, 2017) and focus group meetings.

## 125 2.2 Fuzzy set and intuitionistic fuzzy set

126 **Definition 1.** Fuzzy sets (FS) (Zadeh, 1965)

127 The set  $X$  is an universe of discourse composed by  $x$ , and a fuzz set  $\tilde{\alpha}$  can be characterized by a  
 128 membership function  $\mu_{\tilde{\alpha}}(x)$  which can measure the degree of  $x$  belonging to  $\alpha$ .  $\mu_{\tilde{\alpha}}(x)$  represents  
 129 the membership of  $x$  in  $\tilde{\alpha}$

$$130 \quad \alpha = \{(x, \mu_{\tilde{\alpha}}(x)) \mid x \in X\} \quad (1)$$

131 **Definition 2.** Intuitionistic fuzzy set (IFS)

132 Assuming that  $X$  is an object collection of  $x$  and  $\beta \in X$  is a fixed set, the intuitionistic fuzzy set  
 133  $\beta$  on  $X$  can be defined as (Atanassov, 1986):

$$134 \quad \beta = \{(x, \mu_{\beta}(x), \nu_{\beta}(x)) \mid x \in X\} \quad (2)$$

135 where  $\mu_{\beta}(x): X \rightarrow [0,1], x \in X \rightarrow \mu_{\beta}(x) \in [0,1]$  represents the degree of membership of the  
 136 element  $x \in X$  to the set  $\beta$ , and  $\nu_{\beta}(x): X \rightarrow [0,1], x \in X \rightarrow \nu_{\beta}(x) \in [0,1]$  is the degree of  
 137 non-membership of the element  $x \in X$  to the set  $\beta$ .

138  $\mu_{\beta}$  and  $\nu_{\beta}(x)$  usually satisfies  $0 \leq \mu_{\beta}(x) + \nu_{\beta}(x) \leq 1$  for all  $x \in X$ . Besides the degree of  
 139 membership and non-membership, an indeterminacy degree, so-called “hesitancy degree” of  $x$  to  
 140 the set  $\beta$  which is different from the numbers  $\mu_{\beta}(x)$  and  $\nu_{\beta}(x)$  representing the degree of  
 141 membership and the degree of non-membership of the element  $x \in X$  to the set  $\beta$ , can measure

142 the degree of indeterminacy of  $x \in X$  to the set  $\beta$  is defined as:

$$143 \quad \pi_\beta(x) = 1 - \mu_\beta(x) - \nu_\beta(x), x \in X \quad (3)$$

144 Accordingly, an intuitionistic fuzzy number  $\beta$  can usually be represented by  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$

145 which included the degree of membership, non-membership, and indeterminacy degree.

146 **Definition 3.** Arithmetic operations (Xu and Yager, 2006)

147 Let  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  and  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$  be two intuitionistic fuzzy numbers, and the  
148 arithmetic operations between these two intuitionistic fuzzy numbers were presented as follows:

149 **Addition**

$$150 \quad \gamma \oplus \beta = (\mu_\gamma, \nu_\gamma, \pi_\gamma) \oplus (\mu_\beta, \nu_\beta, \pi_\beta) = (\mu_\gamma + \mu_\beta - \mu_\gamma \mu_\beta, \nu_\gamma \nu_\beta, 1 + \mu_\gamma \mu_\beta - \mu_\gamma - \mu_\beta - \nu_\gamma \nu_\beta)$$

151 (4)

$$152 \quad \bigoplus_{j=1}^n \gamma_j = \bigoplus_{j=1}^n (\mu_{\gamma_j}, \nu_{\gamma_j}, \pi_{\gamma_j}) = \left( 1 - \prod_{j=1}^n (1 - \mu_{\gamma_j}), \prod_{j=1}^n \nu_{\gamma_j}, \prod_{j=1}^n (1 - \mu_{\gamma_j}) - \prod_{j=1}^n \nu_{\gamma_j} \right) \quad (5)$$

153 **Multiplication**

$$154 \quad \gamma \otimes \beta = (\mu_\gamma, \nu_\gamma, \pi_\gamma) \otimes (\mu_\beta, \nu_\beta, \pi_\beta) = (\mu_\gamma \mu_\beta, \nu_\gamma + \nu_\beta - \nu_\gamma \nu_\beta, 1 + \nu_\gamma \nu_\beta - \mu_\gamma \mu_\beta - \nu_\gamma - \nu_\beta) \quad (6)$$

$$155 \quad \bigotimes_{j=1}^n \gamma_j = \bigotimes_{j=1}^n (\mu_{\gamma_j}, \nu_{\gamma_j}, \pi_{\gamma_j}) = \left( \prod_{j=1}^n \mu_{\gamma_j}, \prod_{j=1}^n (1 - \nu_{\gamma_j}), 1 - \prod_{j=1}^n \mu_{\gamma_j} - \prod_{j=1}^n (1 - \nu_{\gamma_j}) \right) \quad (7)$$

156 **Scale multiplication**

$$157 \quad \lambda \gamma = \left( 1 - (1 - \mu_\gamma)^\lambda, (\nu_\gamma)^\lambda, (1 - \mu_\gamma)^\lambda - (\nu_\gamma)^\lambda \right) \quad (8)$$

158 where  $\lambda$  is a crisp number.

159 **Definition 4.** Geometric distance (Szmidt and Kacprzyk, 2000).

160 The distance between two intuitionistic fuzzy sets  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  and  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$  can

161 be determined by Eqs.9-10.

162 The Hamming distance:

$$163 \quad d(\gamma, \beta) = \frac{1}{2} \sum_{j=1}^n \left( \left| \mu_{\gamma}(x_j) - \mu_{\beta}(x_j) \right| + \left| \nu_{\gamma}(x_j) - \nu_{\beta}(x_j) \right| + \left| \pi_{\gamma}(x_j) - \pi_{\beta}(x_j) \right| \right) \quad (9)$$

164 The Euclidean distance:

$$165 \quad d(\gamma, \beta) = \sqrt{\frac{1}{2} \sum_{j=1}^n \left[ \left( \mu_{\gamma}(x_j) - \mu_{\beta}(x_j) \right)^2 + \left( \nu_{\gamma}(x_j) - \nu_{\beta}(x_j) \right)^2 + \left( \pi_{\gamma}(x_j) - \pi_{\beta}(x_j) \right)^2 \right]} \quad (10)$$

166 **Definition 5.** Score and accuracy degree of an intuitionistic fuzzy set (Hong and Choi, 2000). The  
167 score and the accuracy degree of the intuitionistic fuzzy set  $\gamma = (\mu_{\gamma}, \nu_{\gamma}, \pi_{\gamma})$  can be determined by  
168 Eq.11 and Eq.12, respectively.

$$169 \quad S_{\gamma} = \mu_{\gamma} - \nu_{\gamma} \quad (11)$$

$$170 \quad H_{\gamma} = \mu_{\gamma} + \nu_{\gamma} \quad (12)$$

171 where  $S_{\gamma}$  and  $H_{\gamma}$  are the score and the accuracy degree of the intuitionistic fuzzy set

$$172 \quad \gamma = (\mu_{\gamma}, \nu_{\gamma}, \pi_{\gamma}).$$

### 173 2.3 Intuitionistic fuzzy Multi-criteria decision making method

174 A novel multi-criteria decision making (MCDM) method was developed for sustainability  
175 ranking of the alternative energy storage technologies by combining the IAHP and IFCODAS, the  
176 framework of the developed MCDM method was proposed in Figure 1. The IAHP which allows the  
177 decision-makers to use interval numbers rather than the crisp numbers to determine the comparison  
178 matrix was employed to determine the weights of the criteria for sustainability assessment of energy  
179 storage technologies. The IFCODAS method by combining the Intuitionistic Fuzzy Set (IFS) theory  
180 and the Combinative Distance-based Assessment Method (CODAS) method which allows the  
181 decision-makers/stakeholders using intuitionistic fuzzy numbers to rate the alternative energy



182 storage technologies with respect to each criterion was used to prioritize the alternative energy  
 183 storage technologies.

### 184 2.3.1 Interval Analytic Hierarchy Process

185 The interval Analytic Hierarchy Process (IAHP) consists of four steps (Xu and Da,2003):

186 **Step 1:** Determining the interval pair-wise comparison matrix.

187 Assuming that there a total of  $n$  metrics ( $M_1, M_2, \dots, M_n$ ) which need the decision-makers to  
 188 determine the relative weights, the decision-makers were asked to use the nine-scale system  
 189 developed by Saaty (2008) to establish the pair-wise comparison matrix (see Table 1). The  
 190 traditional AHP method usually used the numbers from 1 to 9 and their reciprocals for comparing  
 191 each pair of factors for establishing the pair-wise comparison matrix; however, a single number  
 192 sometime cannot depict the relative weight/priority of each pair metrics accurately. For example,  
 193 there is not any single number can depict the relative weight/priority of a metric over another when  
 194 the decision-makers held the view that the relative importance of a metric over another is between  
 195 ‘equal importance’ (corresponding to number a) and ‘moderate importance’ (corresponding to  
 196 number 3). Accordingly, the interval number  $[1, 3]$  can be used to depict this situation. In this way,  
 197 the interval comparison matrix for the  $n$  metrics can be determined:

$$\begin{matrix}
 & M_1 & M_2 & \cdots & M_n \\
 M_1 & 1 & [q_{12}^L, q_{12}^U] & \cdots & [q_{1n}^L, q_{1n}^U] \\
 198 \quad Q^\pm = M_2 & [q_{21}^L, q_{21}^U] & 1 & \cdots & [q_{2n}^L, q_{2n}^U] \\
 & \vdots & \vdots & \ddots & \vdots \\
 M_n & [q_{n1}^L, q_{n1}^U] & [q_{n2}^L, q_{n2}^U] & \cdots & 1
 \end{matrix} \quad (13)$$

199 where  $Q^\pm$  represents the interval pair-wise matrix,  $[q_{ij}^L, q_{ij}^U]$  is an interval number and denotes the  
 200 relative importance of the  $i$ -th metric over the  $j$ -th metric, and  $a_{ij}^L$  and  $a_{ij}^U$  are the lower and upper  
 201 boundary of the interval number  $[q_{ij}^L, q_{ij}^U]$ .

202 The relative importance of the  $j$ -th metric comparing to  $i$ -th metric can be determiend by Eq.14.

203 
$$\frac{1}{[q_{ij}^L, q_{ij}^U]} = \left[ \frac{1}{q_{ij}^U}, \frac{1}{q_{ij}^L} \right], i, j = 1, 2, \dots, n \quad (14)$$

204 **Step 2:** Decomposing the interval pair-wise comparison matrix into two crisp nonnegative matrices.

205 The interval pair-wise comparison matrix in Eq. 14 can be decomposed into two crisp nonnegative  
 206 matrices, as presented in Eqs. 15-16.

207 
$$Q_L = \begin{bmatrix} 1 & q_{12}^L & \cdots & q_{1n}^L \\ 1/q_{21}^U & 1 & \cdots & q_{2n}^L \\ \vdots & \vdots & \ddots & \vdots \\ 1/q_{n1}^U & 1/q_{n2}^U & \cdots & 1 \end{bmatrix} \quad (15)$$

208 
$$Q_U = \begin{bmatrix} 1 & q_{12}^U & \cdots & q_{1n}^U \\ 1/q_{21}^L & 1 & \cdots & q_{2n}^U \\ \vdots & \vdots & \ddots & \vdots \\ 1/q_{n1}^L & 1/q_{n2}^L & \cdots & 1 \end{bmatrix} \quad (16)$$

209 The geometric mean method (Ren *et al.*, 2017) can be used to determine the weights according to  
 210 the matrices presented in Eqs.15-16, and the weight vectors determined by these two matrices were  
 211 presented in Eq.17 and Eq.18, respectively.

212 
$$W_L = [\omega_1^L \quad \omega_2^L \quad \cdots \quad \omega_n^L] \quad (17)$$

213 
$$W_U = [\omega_1^U \quad \omega_2^U \quad \cdots \quad \omega_n^U] \quad (18)$$

214 where  $W_L$  and  $W_U$  represent the weight vectors determined by the matrices presented in Eq.15 and  
 215 Eq.16, respectively.  $\omega_j^L$  and  $\omega_j^U$  are the weights of the j-th metric in  $W_L$  and  $W_U$ , respectively.

216 **Step 3:** Determining the interval weights. The interval weights of each metric can be determined by  
 217 Eqs.19-21.

218 
$$k = \sqrt{\frac{\sum_{j=1}^n 1}{\sum_{i=1}^n q_{ij}^+}} \quad (19)$$

219 
$$m = \sqrt{\frac{\sum_{j=1}^n 1}{\sum_{i=1}^n q_{ij}^-}} \quad (20)$$

220 It is worth pointing out that if  $k$  and  $m$  satisfy  $0 < k \leq 1 \leq m$ , then, the users can use Eq.21 to  
 221 determine the interval weight of the  $j$ -th metric, or the users should modify the interval pair-wise  
 222 comparison matrix to make  $k$  and  $m$  satisfy this condition.

223 
$$\omega_j^\pm = [k\omega_j^L \quad m\omega_j^U] \quad (21)$$

224 where  $\omega_j^\pm$  represents the interval weight of the  $j$ -th metric.

225 **Step 4:** Determining the crisp weights of the metrics. The possibility of  $\omega_j^\pm$  be greater than  $\omega_r^\pm$  can  
 226 be determined by Eq.22 according to Xu and Da (2003).

227 
$$p_{jr} = P(\omega_j^\pm \geq \omega_r^\pm) = \max \left\{ 1 - \max \left[ \frac{m\omega_r^U - k\omega_j^L}{m\omega_r^U - k\omega_r^L + m\omega_j^U - k\omega_j^L}, 0 \right], 0 \right\} \quad (22)$$

228 where  $p_{jr} = P(\omega_j^\pm \geq \omega_r^\pm)$  represents the possibility of  $\omega_j^\pm$  be greater than  $\omega_r^\pm$ .

229 After comparing each pair of weights, the possibility matrix can be determined by Eq.23.

230 
$$P = \begin{pmatrix} p_{11} & p_{12} & \cdots & p_{1n} \\ p_{21} & p_{22} & \cdots & p_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ p_{n1} & p_{n2} & \cdots & p_{nn} \end{pmatrix} \quad (23)$$

231 Then, the crisp of each metric can be determined by Eq.24.

232 
$$\omega_j = \frac{\sum_{r=1}^n p_{jr} + \frac{n}{2} - 1}{n(n-1)} \quad (24)$$

233 where  $\omega_j$  represents the crisp weight of the  $j$ -th metric.

### 234 2.3.2 Intuitionistic Fuzzy Combinative Distance-based Assessment Method

235 The Combinative Distance-based Assessment Method (CODAS) developed by Keshavarz  
 236 Ghorabae et al. (2016) which can measure the overall performances of the alternatives by the  
 237 Euclidean and Taxicab distance from the native-ideal solutions. However, the traditional CODAS  
 238 method cannot address the vagueness and ambiguity existing human judgements. Accordingly, the  
 239 IFCODAS was developed by combining the intuitionistic fuzzy set theory and CODAS method.  
 240 The IFCODAS developed in this study was specified as follows:

241 **Step 1:** Determining the intuitionistic fuzzy decision-making matrix. Assuming that there are  $m$   
 242 alternatives  $(A_1, A_2, \dots, A_m)$  to be evaluated by  $n$  metrics  $(M_1, M_2, \dots, M_n)$ , the decision-makers  
 243 were firstly asked to rate the alternatives with respect to each metric by using the linguistic  
 244 variables including extreme good (EG), very good (VG), good (G), medium good (MG), fair (F),  
 245 medium poor (MP), poor (P), very poor (VP), and extreme poor (EP). In other words, these  
 246 linguistic terms were used to describe the relative performances of the  $m$  alternatives with respect to  
 247 each of the  $n$  metrics. Subsequently, these linguistic variables can be transformed into intuitionistic  
 248 fuzzy numbers according to Table 2. Then, the intuitionistic fuzzy decision-making matrix can be  
 249 determined, as presented in Eq.13.

$$\begin{array}{ccccc}
 & M_1 & M_2 & \cdots & M_n \\
 250 \quad D = \begin{array}{c} A_1 \\ A_2 \\ \vdots \\ A_m \end{array} & \begin{array}{c} (\mu_{11}^x, \nu_{11}^x, \pi_{11}^x) \\ (\mu_{21}^x, \nu_{21}^x, \pi_{21}^x) \\ \vdots \\ (\mu_{m1}^x, \nu_{m1}^x, \pi_{m1}^x) \end{array} & \begin{array}{c} (\mu_{12}^x, \nu_{12}^x, \pi_{12}^x) \\ (\mu_{22}^x, \nu_{22}^x, \pi_{22}^x) \\ \vdots \\ (\mu_{m2}^x, \nu_{m2}^x, \pi_{m2}^x) \end{array} & \begin{array}{c} \cdots \\ \cdots \\ \ddots \\ \cdots \end{array} & \begin{array}{c} (\mu_{1n}^x, \nu_{1n}^x, \pi_{1n}^x) \\ (\mu_{2n}^x, \nu_{2n}^x, \pi_{2n}^x) \\ \vdots \\ (\mu_{mn}^x, \nu_{mn}^x, \pi_{mn}^x) \end{array}
 \end{array} \quad (13)$$

251 where  $D$  is the decision-making matrix, and  $(\mu_{ij}^x, \nu_{ij}^x, \pi_{ij}^x)$  represents the relative performance of  
 252 the  $i$ -th alternative with respect to the  $j$ -th metric.

253 **Step 2:** Determining the weighted intuitionistic fuzzy decision-making matrix. The weighted  
 254 intuitionistic fuzzy decision-making matrix can be determined by Eqs.14-15. Note that the weights  
 255 of the metrics in this study will be obtained by the IAHP method.

$$\begin{array}{ccccccc}
 & & M_1 & & M_2 & & M_n \\
 & A_1 & \omega_1(\mu_{11}^x, \nu_{11}^x, \pi_{11}^x) & \omega_2(\mu_{12}^x, \nu_{12}^x, \pi_{12}^x) & \cdots & \omega_n(\mu_{1n}^x, \nu_{1n}^x, \pi_{1n}^x) & \\
 WD = & A_2 & \omega_1(\mu_{21}^x, \nu_{21}^x, \pi_{21}^x) & \omega_2(\mu_{22}^x, \nu_{22}^x, \pi_{22}^x) & \cdots & \omega_n(\mu_{2n}^x, \nu_{2n}^x, \pi_{2n}^x) & \\
 & \vdots & \vdots & \vdots & \ddots & \vdots & \\
 & A_m & \omega_1(\mu_{m1}^x, \nu_{m1}^x, \pi_{m1}^x) & \omega_2(\mu_{m2}^x, \nu_{m2}^x, \pi_{m2}^x) & \cdots & \omega_n(\mu_{mn}^x, \nu_{mn}^x, \pi_{mn}^x) & \\
 & & M_1 & & M_2 & & M_n \\
 & A_1 & (\mu_{11}, \nu_{11}, \pi_{11}) & (\mu_{12}, \nu_{12}, \pi_{12}) & \cdots & (\mu_{1n}, \nu_{1n}, \pi_{1n}) & \\
 = & A_2 & (\mu_{21}, \nu_{21}, \pi_{21}) & (\mu_{22}, \nu_{22}, \pi_{22}) & \cdots & (\mu_{2n}, \nu_{2n}, \pi_{2n}) & \\
 & \vdots & \vdots & \vdots & \ddots & \vdots & \\
 & A_m & (\mu_{m1}, \nu_{m1}, \pi_{m1}) & (\mu_{m2}, \nu_{m2}, \pi_{m2}) & \cdots & (\mu_{mn}, \nu_{mn}, \pi_{mn}) & 
 \end{array} \tag{14}$$

$$257 \quad wd_{ij} = (\mu_{ij}, \nu_{ij}, \pi_{ij}) = \omega_j(\mu_{ij}^x, \nu_{ij}^x, \pi_{ij}^x) = (1 - (1 - \mu_{ij}^x)^{\omega_j}, (\nu_{ij}^x)^{\omega_j}, (1 - \mu_{ij}^x)^{\omega_j} - (\nu_{ij}^x)^{\omega_j}) \tag{15}$$

258 where  $WD$  represents the weighted intuitionistic fuzzy decision-making matrix,  $\omega_j$  represents the  
 259 weight of the  $j$ -th criterion, and  $wd_{ij} = (\mu_{ij}, \nu_{ij}, \pi_{ij})$  is the element of cell (i, j) in the weighted  
 260 intuitionistic fuzzy decision-making matrix.

261 **Step 3:** Determining the negative-ideal solutions (NIS). The negative-ideal solutions can be  
 262 determined by Eqs.16-20.

$$263 \quad NIS_j = (\mu_j, \nu_j, \pi_j), j = 1, 2, \dots, n \tag{16}$$

$$264 \quad t = \arg \min_i (\mu_{ij}) \tag{17}$$

$$265 \quad \mu_j = \mu_{jt} \tag{18}$$

$$266 \quad \nu_j = \nu_{jt} \tag{19}$$

$$267 \quad \pi_j = 1 - \mu_{jt} - \nu_{jt} \tag{20}$$

268 **Step 4:** Determining the Euclidean distance and the Hamming distances of the alternatives to the  
 269 negative-ideal solutions.

270 The Euclidean distance:

$$271 \quad E(wd_{ij}, NIS_j) = \sqrt{\frac{1}{2} \sum_{j=1}^n \left[ (\mu_{ij} - \mu_j)^2 + (\nu_{ij} - \nu_j)^2 + (\pi_{ij} - \pi_j)^2 \right]} \quad (21)$$

272 The Hamming distance:

$$273 \quad H(wd_{ij}, NIS_j) = \frac{1}{2} \sum_{j=1}^n (|\mu_{ij} - \mu_j| + |\nu_{ij} - \nu_j| + |\pi_{ij} - \pi_j|) \quad (22)$$

274 **Step 5:** Establishing the relative assessment matrix. The relative assessment matrix can be  
 275 determined by Eqs.23-24.

$$276 \quad R = \{r_{ik}\}_{m \times m} \quad (23)$$

$$277 \quad r_{ik} = \left[ E(wd_{ij}, NIS_j) - E(wd_{kj}, NIS_j) \right] + \Phi \left[ E(wd_{ij}, NIS_j) - E(wd_{kj}, NIS_j) \right] \times \left[ H(wd_{ij}, NIS_j) - H(wd_{kj}, NIS_j) \right] \quad (22)$$

$$279 \quad \Phi \left[ E(wd_{ij}, NIS_j) - E(wd_{kj}, NIS_j) \right] = \begin{cases} 1 & \text{if } -\tau \leq E(wd_{ij}, NIS_j) - E(wd_{kj}, NIS_j) \leq \tau \\ 0 & \text{if } \text{others} \end{cases} \quad (24)$$

280 where  $\Phi$  represents the threshold function to recognize the equality of the Euclidean distance of  
 281 two alternatives,  $\tau$  is the threshold value set by the users according to their judgments, and  $r_{ik}$   
 282 represent the priority difference of the  $i$ -th alternative to the  $k$ -th alternative.

283 **Step 6:** Determining the final assessment score of each alternative and ranking the alternatives. The  
 284 final score of each alternative can be determined by Eq.25.

$$285 \quad F_i = \sum_{k=1}^m r_{ik} \quad (25)$$

286 where  $F_i$  represent the final assessment score of the  $i$ -th alternative.

287 After determining the final assessment score of each alternative, the alternatives can be ranked

288 according to the rule that the greater the value of the final assessment score, the more superior the  
289 alternative will be.

290

### 291 3. Case study

292 Four energy storage technologies including pumped hydro storage (A<sub>1</sub>), compressed air energy  
293 storage (A<sub>2</sub>), Lithium-ion battery (A<sub>3</sub>), and flywheel energy storage system (A<sub>4</sub>) were studied by the  
294 proposed intuitionistic fuzzy multi-criteria decision making method. These four energy storage  
295 technologies have been specified as follows:

296 **Pumped hydro:** pumped hydro storage is a kind of large scale system for energy storage by  
297 controlling the gravitational potential energy of water. The water will be pumped from a lower  
298 reservoir to an upper reservoir when the power demand is low, and it will flow from the upper  
299 reservoir to the lower reservoir to activate the turbines to generate electricity during the periods of  
300 higher energy demand (Díaz-González *et al.*, 2012);

301 **Compressed air:** compressed air energy storage system is based on the conventional gas turbine  
302 technology in which the energy is stored in form of compressed air in an underground storage  
303 cavern. The energy in the form of compressed air will be transformed into rotational kinetic energy  
304 through a set of high and low pressure turbines(Díaz-González *et al.*, 2012);

305 **Lithium-ion:** Li-ion batteries is one of the battery energy storage systems, which can store the  
306 energy in the form of electrochemical energy, and Li-ion batteries is based on the electrochemical  
307 reactions between positive lithium ions (Li<sup>+</sup>) with anolytic and catholytic active materials  
308 (Wakihara, 2011).

309 **Flywheel:** The flywheel energy storage system is an electromechanical system that stores energy in  
310 form of kinetic energy. Energy is transferred to the flywheel through the flywheel accelerates, and  
311 the system is discharged when the electric machine regenerates through the drive (slowing the

312 flywheel) (Díaz-González *et al.*, 2012).

313 A total of nine criteria in four categories (economic, environmental, technological and social  
 314 aspects) have been employed for sustainability assessment , and there are capital cost (EC<sub>1</sub>), life  
 315 (EC<sub>2</sub>), and operating cost (EC<sub>3</sub>) in economic aspect (EC), CO<sub>2</sub> density (EN<sub>1</sub>) and integrated  
 316 environmental impact (EN<sub>2</sub>) in environmental aspect (EN), energy efficiency (T<sub>1</sub>), energy density  
 317 (T<sub>2</sub>), and technology maturity (T<sub>3</sub>) in technological aspect (T) , and social acceptability (S<sub>1</sub>) in  
 318 social aspect (S). The IAHP was firstly used to determine the weights of the four categories and the  
 319 weights of the criteria in each aspect. Taking the calculation of the weights of the four categories as  
 320 an example, the four steps of IAHP were specified as follows:

321 **Step 1:** The interval pair-wise comparison matrix (see Table 3) can be firstly determined for  
 322 determining the weights of the four categories.

323 **Step 2:** The two crisp nonnegative matrices can be then determined according to Table 1, and the  
 324 results were presented in Eq.26 and Eq.27, respectively.

$$325 \quad Q_L = \begin{vmatrix} 1 & 1 & 1/3 & 5 \\ 1/2 & 1 & 1/5 & 3 \\ 1 & 3 & 1 & 7 \\ 1/7 & 1/5 & 1/9 & 1 \end{vmatrix} = \begin{vmatrix} q_{11}^- & q_{12}^- & q_{13}^- & q_{14}^- \\ q_{21}^- & q_{22}^- & q_{23}^- & q_{24}^- \\ q_{31}^- & q_{32}^- & q_{33}^- & q_{34}^- \\ q_{41}^- & q_{42}^- & q_{43}^- & q_{44}^- \end{vmatrix} \quad (26)$$

$$326 \quad Q_U = \begin{vmatrix} 1 & 2 & 1 & 7 \\ 1 & 1 & 1/3 & 5 \\ 3 & 5 & 1 & 9 \\ 1/5 & 1/3 & 1/7 & 1 \end{vmatrix} = \begin{vmatrix} q_{11}^+ & q_{12}^+ & q_{13}^+ & q_{14}^+ \\ q_{21}^+ & q_{22}^+ & q_{23}^+ & q_{24}^+ \\ q_{31}^+ & q_{32}^+ & q_{33}^+ & q_{34}^+ \\ q_{41}^+ & q_{42}^+ & q_{43}^+ & q_{44}^+ \end{vmatrix} \quad (27)$$

327 Then,  $W_L$  and  $W_U$  can be determined by the geometric-method, and the result were presented in  
 328 Eq.28 and Eq.29, respectively.

$$329 \quad W_L = [0.2671 \quad 0.1740 \quad 0.5032 \quad 0.0558] \quad (28)$$



330  $W_U = [0.2848 \quad 0.1673 \quad 0.5019 \quad 0.0460]$  (29)

331 **Step 3:** The parameters  $k$  and  $m$  can be determined by Eq.30 and Eq.31, respectively.

332  $k = \sqrt{\frac{\sum_{j=1}^4 1}{\sum_{i=1}^4 q_{ij}^+}} = 0.8727$  (30)

333  $m = \sqrt{\frac{\sum_{j=1}^4 1}{\sum_{i=1}^4 q_{ij}^-}} = 1.1141$  (31)

334 According to Eq.21, the interval weights of the four categories for sustainability assessment of  
335 energy storage technologies can be determined, and the results were presented in Eqs.32-35.

336  $\omega_{EC}^\pm = [0.8727 \times 0.2671 \quad 1.1141 \times 0.2848] = [0.2331 \quad 0.3173]$  (32)

337  $\omega_{EN}^\pm = [0.8727 \times 0.1740 \quad 1.1141 \times 0.1673] = [0.1518 \quad 0.1864]$  (33)

338  $\omega_T^\pm = [0.8727 \times 0.5032 \quad 1.1141 \times 0.5019] = [0.4391 \quad 0.5592]$  (34)

339  $\omega_S^\pm = [0.8727 \times 0.0558 \quad 1.1141 \times 0.0460] = [0.0487 \quad 0.0512]$  (35)

340 **Step 4:** The elements in the possibility matrix can be determined by comparing the weights of each  
341 pair of categories according to Eq.22. Taking the possibility of  $\omega_{EC}^\pm$  be greater than  $\omega_{EN}^\pm$  as an  
342 example:

343 
$$P(\omega_{EC}^\pm \geq \omega_{EN}^\pm) = \max \left\{ 1 - \max \left[ \frac{\omega_{EN}^U - \omega_{EC}^L}{\omega_{EN}^U - \omega_{EN}^L + \omega_{EC}^U - \omega_{EC}^L}, 0 \right], 0 \right\}$$

$$= \max \left\{ 1 - \max \left[ \frac{0.1864 - 0.2331}{0.1864 - 0.1518 + 0.3173 - 0.2331}, 0 \right], 0 \right\}$$

$$= 1.0000$$
 (36)

344 In a similar way, all the elements in the possibility matrix can be determined, and the results were  
345 presented in Eq.37.

		<i>EC</i>	<i>EN</i>	<i>T</i>	<i>S</i>	
	<i>EC</i>	0.5000	1.0000	0	1.0000	
346	<i>P = EN</i>	0	0.5000	0	1.0000	(37)
	<i>T</i>	1.0000	1.0000	0.5000	1.0000	
	<i>S</i>	0	0	0	0.5000	

347 Then, the crisp weight of each metric can be determined according to Eq.38, and the results were  
 348 presented in Eqs.38-41.

$$349 \quad \omega_{EC} = \frac{\sum_{r=1}^4 p_{1r} + \frac{4}{2} - 1}{4(4-1)} = \frac{0.5000 + 1.0000 + 0 + 1.0000 + \frac{4}{2} - 1}{4(4-1)} = 0.2917 \quad (38)$$

$$350 \quad \omega_{EN} = \frac{\sum_{r=1}^4 p_{2r} + \frac{4}{2} - 1}{4(4-1)} = \frac{0 + 0.5000 + 0 + 1.0000 + \frac{4}{2} - 1}{4(4-1)} = 0.2083 \quad (39)$$

$$351 \quad \omega_T = \frac{\sum_{r=1}^4 p_{3r} + \frac{4}{2} - 1}{4(4-1)} = \frac{1.0000 + 1.0000 + 0.5000 + 1.0000 + \frac{4}{2} - 1}{4(4-1)} = 0.3750 \quad (40)$$

$$352 \quad \omega_S = \frac{\sum_{r=1}^4 p_{4r} + \frac{4}{2} - 1}{4(4-1)} = \frac{0 + 0 + 0 + 0.5000 + \frac{4}{2} - 1}{4(4-1)} = 0.1250 \quad (41)$$

353 Therefore, the weights of the economic, environmental, technological and social categories are  
 354 0.2917, 0.2083, 0.3750, and 0.1250, respectively.

355 In a similar way, the weights of the criteria in each category for sustainability assessment of  
 356 energy storage technologies can also be determined, and the results were presented in Tables 4-6.

357 After determining the weights of the four categories and that of the metrics in each category, and  
 358 the global weights of the nine metrics can be determined, and the results were presented in Table 7.

359 Then, the linguistic variables were firstly used by the decision-makers to rate the four alternative  
 360 energy storage technologies with respect to each of the metrics for sustainability assessment, and  
 361 there are eight experts including two professor who focuses on energy storage technologies, three

362 senior researchers of renewable energy, and two PhD students from Chinese universities who  
 363 majored in power system engineering participating in rating the four energy storage technologies.  
 364 The results were summarized in Table 8.

365 The linguistic variables can be transformed into intuitionistic fuzzy numbers according to Table 1.  
 366 For instance, “VG” in Table 7 can be transformed into (0.85, 0.10, 0.05). In a similar way, all the  
 367 elements in Table 1 can be transformed into intuitionistic fuzzy numbers, and the results were  
 368 summarized in Table 9.

369 According to Eq.15, the element in the weighted intuitionistic fuzzy decision-making matrix can  
 370 be determined. Taking the element “(0.65, 0.25, 0.10)” in cell (1,1) which represents the value of  
 371 pumped hydro ( $A_1$ ) with respect to capital cost ( $EC_1$ ) as an example:

$$\begin{aligned}
 wd_{11} &= (\mu_{11}, \nu_{11}, \pi_{11}) = \omega_1(\mu_{11}^x, \nu_{11}^x, \pi_{11}^x) = (1 - (1 - \mu_{11}^x)^{\omega_1}, (\nu_{11}^x)^{\omega_1}, (1 - \mu_{11}^x)^{\omega_1} - (\nu_{11}^x)^{\omega_1}) \\
 &= (1 - (1 - 0.65)^{0.0972}, (0.25)^{0.0972}, (1 - 0.65)^{0.0972} - (0.25)^{0.0972}) \quad (42) \\
 &= (0.0970, 0.8739, 0.0291)
 \end{aligned}$$

373 where  $wd_{11}$  represents the value of the element in cell (1,1) of the weighted intuitionistic fuzzy  
 374 decision-making matrix.

375 In a similar way, all the elements in the weighted intuitionistic fuzzy decision-making matrix can  
 376 be then determined, and the results were summarized in Table 10.

377 According to Eqs.16-20, the negative-ideal solutions can be determined. Taking the negative-  
 378 ideal solution with respect to  $EC_1$  as an example:

379 The relative performances of these four alternatives ( $A_1$ ,  $A_2$ ,  $A_3$ , and  $A_4$ ) with respect to  $EC_1$  are  
 380 (0.0970, 0.8739, 0.0291), (0.1684, 0.7995, 0.0321), (0.0276, 0.9590, 0.0134), and (0.0410, 0.9435,  
 381 0.0154), respectively. According to Eq.16, it could be obtained that

$$t = \arg \min_{i=1,2,3,4} (0.0970, 0.1684, 0.0276, 0.0410) = 3 \quad (43)$$

383 Then, the three elements in the negative-ideal solution with respect to  $EC_1$  can be determined:

384  $\mu_j = \mu_{3j} = 0.0276$  (44)

385  $\nu_j = \nu_{3j} = 0.9590$  (45)

386  $\pi_j = 1 - \mu_{3j} - \nu_{3j} = 1 - 0.0276 - 0.9590 = 0.0134$  (46)

387 In a similar way, all the negative-ideal solutions can be determined, and the results were presented  
388 in Table 11.

389 The Euclidean and Hamming distance from each energy storage technology to the negative-ideal  
390 solutions can be determined according to Eq.21 and Eq.22, respectively, and the results were  
391 presented in Table 12.

392 The threshold value set  $\tau$  was set as 0.05, and the relative assessment matrix can be determined  
393 according to Eqs.23-24, and the results were presented in Eq.47.

$$\begin{array}{cc}
 & \begin{array}{cccc} A_1 & A_2 & A_3 & A_4 \end{array} \\
 \begin{array}{c} A_1 \\ A_2 \\ A_3 \\ A_4 \end{array} & R = \begin{array}{cccc}
 0 & 0.0973 & 0.0514 & 0 \\
 -0.0973 & 0 & -0.0459 & -0.0841 \\
 -0.0514 & 0.0459 & 0 & -0.0382 \\
 0 & 0.0841 & 0.0382 & 0
 \end{array}
 \end{array} \quad (47)$$

394

395 Then, the final assessment score of each alternative energy storage technology can be determined  
396 by Eq.25. For instance, the final assessment score of the four alternative energy storage  
397 technologies can be determined by Eqs.48-51 respectively.

398  $F_1 = 0 + 0.0973 + 0.0514 + 0 = 0.1487$  (48)

399  $F_2 = -0.0973 + 0 + (-0.0459) + (-0.0841) = -0.2272$  (49)

400  $F_3 = -0.0514 + 0.0459 + 0 + (-0.0382) = -0.0437$  (50)

401  $F_4 = 0 + 0.0841 + 0.0382 + 0 = 0.1223$  (51)

402 According to the final assessment scores of the four energy storage technologies, pumped hydro  
403 (A<sub>1</sub>) was recognized as the most sustainable one, followed by flywheel (A<sub>4</sub>), lithium-ion (A<sub>3</sub>), and

404 compressed air (A<sub>2</sub>) from the most sustainable to the least. The result of recognizing pumped hydro  
 405 as the most sustainable was reasonable, because this technology has the longest life, lowest CO<sub>2</sub>  
 406 emission, relatively lower capital cost and higher technology maturity. However, it is worth  
 407 pointing out that the sustainability order of the four energy storage technologies may change when  
 408 the weights of the metrics change.

409

#### 410 **4. Discussions**

411 The single-criterion analysis method was also employed to rank these four alternative energy  
 412 storage technologies according to the relative performances on each of the nine metrics. The single-  
 413 criterion analysis method was specified as follows:

414 Suppose  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  and  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$  are two intuitionistic fuzzy numbers to  
 415 describe the relative performances of two alternative energy storage technologies A and B on an  
 416 evaluation criterion, respectively. The more superior energy storage technology between these two  
 417 alternatives can be determined according to the following rules (Xu, 2007):

418 (1) If  $S_\gamma = \mu_\gamma - \nu_\gamma < S_\beta = \mu_\beta - \nu_\beta$  , then,  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  is smaller than  
 419  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , and A is inferior to B;

420 (2) If  $S_\gamma = \mu_\gamma - \nu_\gamma < S_\beta = \mu_\beta - \nu_\beta$ , then:

421 I.  $H_\gamma = \mu_\gamma + \nu_\gamma = H_\beta = \mu_\beta + \nu_\beta$  , then,  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  is equal to  
 422  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , and A is indifferent to B;

423 II.  $H_\gamma = \mu_\gamma + \nu_\gamma < H_\beta = \mu_\beta + \nu_\beta$  , then,  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  is smaller than  
 424  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , and A is inferior to B;

425 III.  $H_\gamma = \mu_\gamma + \nu_\gamma > H_\beta = \mu_\beta + \nu_\beta$  , then,  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  is bigger than  
 426  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , and A is superior to B;

427 where  $S_\gamma$  and  $S_\beta$  represent the scores of the intuitionistic fuzzy sets  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  and  
 428  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , respectively.  $H_\gamma$  and  $H_\beta$  are the accuracy degrees of the intuitionistic fuzzy  
 429 sets  $\gamma = (\mu_\gamma, \nu_\gamma, \pi_\gamma)$  and  $\beta = (\mu_\beta, \nu_\beta, \pi_\beta)$ , respectively.

430 The results of using the single-criterion analysis method to rank these four alternative energy  
 431 storage technologies were presented in Table 13. It is apparent that the rankings of these four  
 432 alternative energy storage technologies based on different criteria are different. Thus, the decision-  
 433 makers/stakeholders need a unique sustainability order of these four alternative energy storage  
 434 technologies by aggregating the performances of each alternative on the nine evaluation criteria into  
 435 a generic index. The developed intuitionistic fuzzy multi-criteria decision making model facilitate  
 436 the decision-makers/stakeholders to achieve this objective.

437 In order to analyze the influences of the threshold value  $\tau$  on the final ranking, the value of  $\tau$  has  
 438 been altered to investigate the change of the sustainability ranking of the four alternative energy  
 439 storage technologies, and the results were presented in Table 14.

440 The results reveal the results were robust to the threshold value in this case, but it is worth pointing  
 441 out that the threshold value may have significant effects on the final priority ranking of the  
 442 alternatives in some other cases.

443 In order to investigate the weights of the nine metrics for sustainability assessment of energy  
 444 storage technologies (set  $\tau = 0.05$ ), the following cases have been studied:

445 **Case 0:** the weights determined by the IAHP method;

446 **Case 1:** equal weights-all the nine metrics was assigned to be equal  $\omega_{EC_1} = \omega_{EC_2} = \dots = \omega_{S_1} = \frac{1}{9}$ ;

447 **Case 2-10:** a dominant weight 0.36 was assigned to each of the nine metrics (capital cost ( $EC_1$ ), life  
448 ( $EC_2$ ), and operating cost ( $EC_3$ ), CO<sub>2</sub> density ( $EN_1$ ) and integrated environmental impact ( $EN_2$ ),  
449 energy efficiency ( $T_1$ ), energy density ( $T_2$ ), and technology maturity ( $T_3$ ), and social acceptability  
450 ( $S_1$  in social aspect (S)) one by one, and the other metrics were assigned an equal weight 0.08. For  
451 instance, 0.36 was assigned to capital cost ( $EC_1$ ), and 0.08 was assigned to the other eight metrics.

452 The rankings of the four alternative energy storage technologies when changing the weights of  
453 the evaluation criteria were presented in Figure 2. It is apparent that the final assessment scores of  
454 the four energy storage technologies which represent their relative priorities vary with the change of  
455 the weights of the metrics for sustainability assessment. The energy storage technology-flywheel  
456 ( $A_4$ ) was ranked as the most sustainable energy storage technology in most of the cases, pumped  
457 hydro ( $A_1$ ) and lithium-ion ( $A_3$ ) located in the middle, and compressed air ( $A_2$ ) was recognized as  
458 the worst according to its sustainability. The results of sensitivity analysis reveal that the  
459 sustainability ranking is highly sensitive to the weights of the metrics for sustainability assessment  
460 of energy storage technologies. Therefore, the accurate determination of the weights of the metrics  
461 for sustainability assessment of energy storage technologies is critical for determining the  
462 sustainability order.

463 Moreover, it is worth pointing out that the final sustainability rankings of these four alternative  
464 energy storage technologies may change with the progress in technological aspects, because the  
465 factors in technological aspects usually have significant effects on the criteria in economic,  
466 environmental and social aspects (Ren *et al.*, 2016a).

467

## 468 **5. Conclusion**

469 This objective of this study is to develop an intuitionistic fuzzy multi-criteria decision making  
470 model for sustainability assessment of energy storage technologies, an intuitionistic fuzzy multi-

471 criteria decision making model was developed by combing the interval analytic hierarchy  
472 process method and the intuitionistic fuzzy combinative distance-based assessment method.  
473 The interval analytic hierarchy process which allows the decision-makers/stakeholders to use  
474 interval numbers which can address the vagueness and ambiguity in human judgments to  
475 establish the pair-wise comparison matrices for determining the weights of the metrics. The  
476 intuitionistic fuzzy combinative distance-based assessment method which allows the decision-  
477 makers/stakeholders to use the intuitionistic fuzzy numbers to rate the alternative energy storage  
478 technologies with respect to each metric for sustainability assessment was developed to  
479 determine the sustainability order of the alternative energy storage technologies. Four  
480 alternative energy storage technologies including pumped hydro, compressed air, lithium-ion,  
481 and flywheel were studied by the proposed method, the sustainability order of the four  
482 technologies from the most sustainable to the least is pumped hydro, flywheel, lithium-ion, and  
483 compressed air according to the weights determined by the decision-makers; however, the  
484 weights of the metrics have significant impacts on the final sustainability ranking of the  
485 alternative energy storage technologies according to the results of sensitivity analysis. All in all,  
486 the developed intuitionistic fuzzy multi-criteria decision making model for sustainability  
487 assessment of energy storage technologies has the following advantages:

- 488 (1) Interval numbers which are more suitable for the decision-makers/stakeholders to express  
489 the opinions on the relative importance of one metric over another were adopted to establish  
490 the pair-wise comparison matrices for determining the weights of the metrics;
- 491 (2) Linguistic terms corresponding to intuitionistic fuzzy numbers were used to rate the energy  
492 storage technologies, and the decision-makers/stakeholders do not need to know the exact  
493 data of the alternative energy storage technologies when selecting the most sustainable  
494 energy storage technology among multiple alternatives.



495 The developed intuitionistic fuzzy multi-criteria decision making method can not only be used  
496 for selecting the most sustainable energy storage technology, but also for determining the best or the  
497 most sustainable energy scenario among multiple alternatives in some other cases. In other words,  
498 the developed intuitionistic fuzzy multi-criteria decision making method can be popularized to some  
499 other cases in energy sector.

500 Besides the advantages of the proposed intuitionistic fuzzy multi-criteria decision making  
501 method, there is also a severe weak point-it cannot effectively use the known data even the data of  
502 some alternatives with respect to some evaluation criteria can be described with units  
503 quantitatively., and the performances of all the alternatives were described subjectively by using the  
504 intuitionistic fuzzy numbers in the proposed method. The future work of the authors is to develop a  
505 multi-criteria decision making method which can handle the decision-making matrix composed by  
506 the hybrid numbers (i.e. the mixture of intuitionistic fuzzy numbers, crisp numbers and interval  
507 numbers) to help the decision-makers/stakeholders to select the most sustainable energy storage  
508 technology.

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### Figure captions

593 **Figure 1:** The framework of the MCDM method based on the interval analytic hierarchy process  
594 and the CODAS method

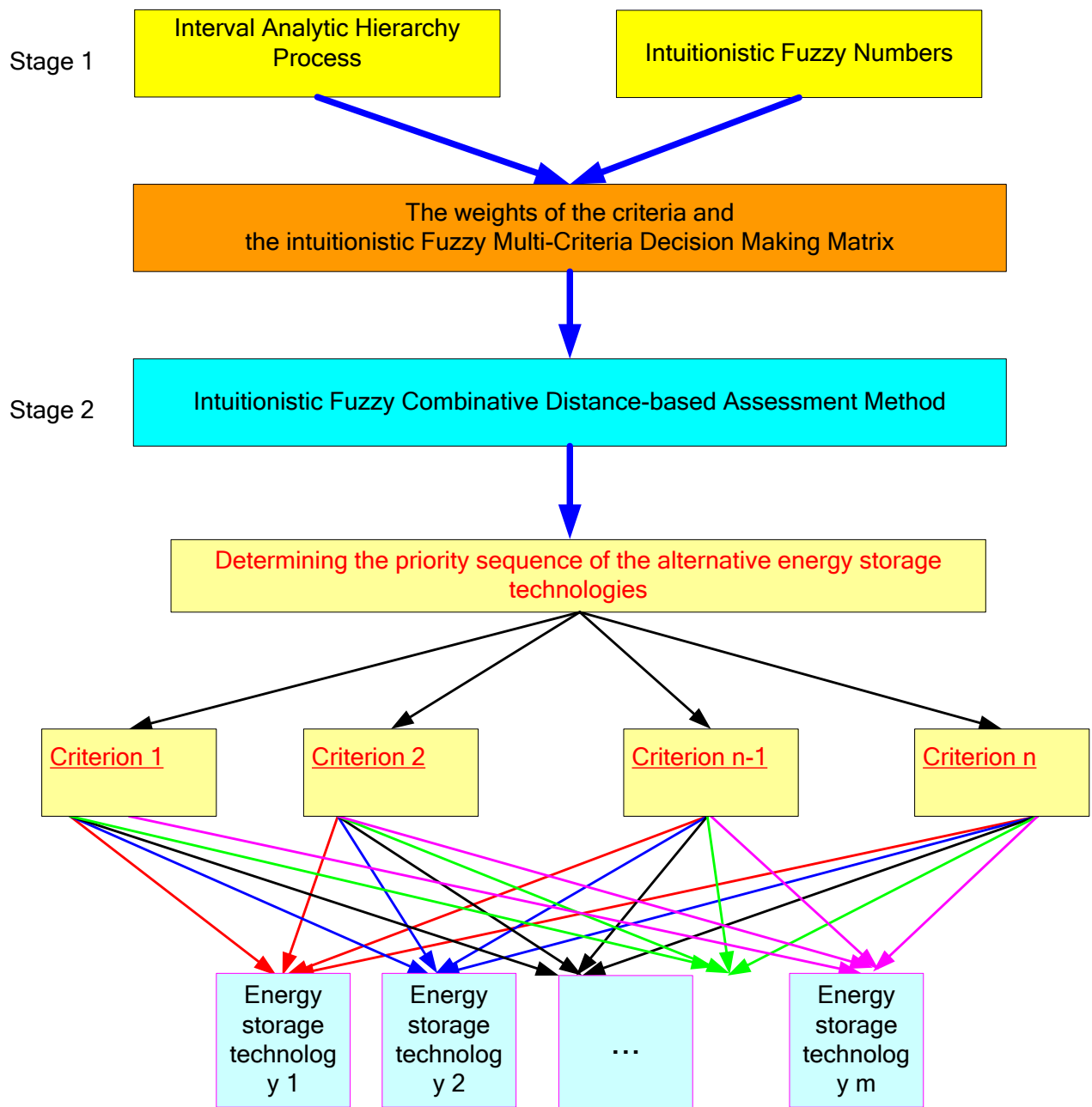
595 **Figure 2:** The results of sensitivity analysis

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**Figure 1:** The framework of the MCDM method based on the interval analytic hierarchy process

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and the CODAS method

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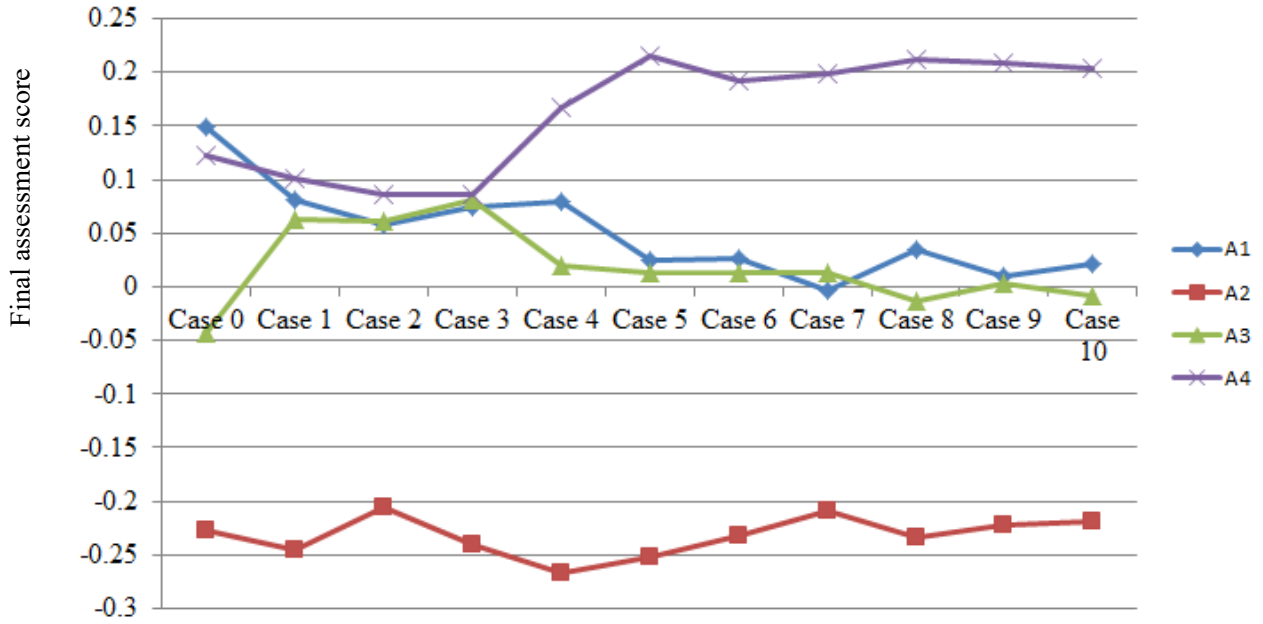
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613 **Figure 2:** The rankings of the four alternative energy storage technologies when changing the  
614 weights of the evaluation criteria

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## Tables

**Table 1:** Saaty scales for establishing the pair-wise comparison matrix

Scales	Definition	Explanation
1	Equal importance	Two elements perform equally
3	Moderate importance	Experience and judgement slightly favour one element over another
5	Essential importance	Experience and judgement strongly favour one element over another
7	Very Strong importance	An element is favoured very strongly over another; its dominance demonstrated in practice
9	Absolute importance	The evidence favouring one element over another is of the highest possible order of affirmation
2,4,6,8	Intermediate value	Intermediate value

631 **Reference:** Saaty (2008)

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**Table 2:** Linguistic variables and their corresponding intuitionistic fuzzy numbers

Linguistic variables	Abbreviation	Intuitionistic fuzzy numbers
Extreme good	EG	(0.95, 0.05, 0)
Very good	VG	(0.85, 0.10, 0.05)
Good	G	(0.75, 0.15, 0.10)
Medium good	MG	(0.65, 0.25, 0.10)
Fair	F	(0.50, 0.40, 0.10)
Medium poor	MP	(0.35, 0.55, 0.10)
Poor	P	(0.25, 0.65, 0.10)
Very Poor	VP	(0.15, 0.80, 0.05)
Extreme poor	EP	(0.05, 0.95, 0)

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**Reference:** Pramanik and Mukhopadhyaya, 2011

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**Table 3:** The interval pair-wise comparison matrix for determining the weights of the four categories

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	Economic	Environmental	Technological	Social
Economic (EC)	1	[1 2]	[1/3 1]	[5 7]
Environmental (EN)	[1/2 1]	1	[1/5 1/3]	[3 5]
Technological (T)	[1 3]	[3 5]	1	[7 9]
Social (S)	[1/7 1/5]	[1/5 1/3]	[1/9 1/7]	1

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665 **Table 4:** The interval pair-wise comparison matrix for determining the weights of the three criteria  
 666 in economic category

	Capital cost (EC <sub>1</sub> )	Life (EC <sub>2</sub> )	Operating cost (EC <sub>3</sub> )
Capital cost (EC <sub>1</sub> )	1	[1 3]	[1/2 1]
Life (EC <sub>2</sub> )	[1/3 1]	1	[1/4 1/2]
Operating cost (EC <sub>3</sub> )	[1 2]	[2 4]	1
Weights	0.3333	0.1667	0.5000

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684 **Table 5:** The interval pair-wise comparison matrix for determining the weights of the three criteria  
 685 in environmental category

	CO <sub>2</sub> density (EN <sub>1</sub> )	Integrated environmental impact (EN <sub>2</sub> )
CO <sub>2</sub> density (EN <sub>1</sub> )	1	[1/4 1/2]
Integrated environmental impact (EN <sub>2</sub> )	[2 4]	1
Weights	0.2500	0.7500

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703 **Table 6:** The interval pair-wise comparison matrix for determining the weights of the three criteria  
 704 in technological category

	Energy efficiency (T <sub>1</sub> )	Energy density (T <sub>2</sub> )	Technology maturity(T <sub>3</sub> )
Energy efficiency (T <sub>1</sub> )	1	[1/3 1]	[1/4 1/2]
Energy density (T <sub>2</sub> )	[1 3]	1	[1/4 1]
Technology maturity (T <sub>3</sub> )	[2 4]	[1 4]	1
Weights	0.1667	0.3333	0.5000

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**Table 7:** The global weights of the nine metrics

Metrics	EC <sub>1</sub>	EC <sub>2</sub>	EC <sub>3</sub>	EN <sub>1</sub>	EN <sub>2</sub>	T <sub>1</sub>	T <sub>2</sub>	T <sub>3</sub>	S <sub>1</sub>
Weights	0.0972	0.0486	0.1459	0.0521	0.1562	0.0625	0.1250	0.1875	0.1250

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**Table 8:** The performances of the four energy storage technologies using linguistic variables

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
EC <sub>1</sub>	MG	VG	P	MP
EC <sub>2</sub>	VG	G	VP	F
EC <sub>3</sub>	P	F	MG	VP
EN <sub>1</sub>	G	EG	F	EP
EN <sub>2</sub>	VP	MP	F	G
T <sub>1</sub>	MG	MP	G	VG
T <sub>2</sub>	VP	F	VG	MP
T <sub>3</sub>	MG	G	P	F
S <sub>1</sub>	MP	G	VG	MG

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**Table 9:** The performances of the four energy storage technologies using intuitionistic fuzzy

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numbers

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
EC <sub>1</sub>	(0.65, 0.25, 0.10)	(0.85, 0.10, 0.05)	(0.25, 0.65, 0.10)	(0.35, 0.55, 0.10)
EC <sub>2</sub>	(0.85, 0.10, 0.05)	(0.75, 0.15, 0.10)	(0.15, 0.80, 0.05)	(0.50, 0.40, 0.10)
EC <sub>3</sub>	(0.25, 0.65, 0.10)	(0.50, 0.40, 0.10)	(0.65, 0.25, 0.10)	(0.15, 0.80, 0.05)
EN <sub>1</sub>	(0.75, 0.15, 0.10)	(0.95, 0.05, 0)	(0.50, 0.40, 0.10)	(0.05, 0.95, 0)
EN <sub>2</sub>	(0.15, 0.80, 0.05)	(0.35, 0.55, 0.10)	(0.50, 0.40, 0.10)	(0.75, 0.15, 0.10)
T <sub>1</sub>	(0.65, 0.25, 0.10)	(0.35, 0.55, 0.10)	(0.75, 0.15, 0.10)	(0.85, 0.10, 0.05)
T <sub>2</sub>	(0.15, 0.80, 0.05)	(0.50, 0.40, 0.10)	(0.85, 0.10, 0.05)	(0.35, 0.55, 0.10)
T <sub>3</sub>	(0.65, 0.25, 0.10)	(0.75, 0.15, 0.10)	(0.25, 0.65, 0.10)	(0.50, 0.40, 0.10)
S <sub>1</sub>	(0.35, 0.55, 0.10)	(0.75, 0.15, 0.10)	(0.85, 0.10, 0.05)	(0.65, 0.25, 0.10)

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**Table 10:** The weighted intuitionistic fuzzy decision-making matrix

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
EC <sub>1</sub>	(0.0970, 0.8739, 0.0291)	(0.1684, 0.7995, 0.0321)	(0.0276, 0.9590, 0.0134)	(0.0410, 0.9435, 0.0154)
EC <sub>2</sub>	(0.0881, 0.8941, 0.0178)	(0.0652, 0.9119, 0.0229)	(0.0079, 0.9892, 0.0029)	(0.0331, 0.9564, 0.0104)
EC <sub>3</sub>	(0.0411, 0.9391, 0.0198)	(0.0962, 0.8749, 0.0290)	(0.1420, 0.8169, 0.0411)	(0.0234, 0.9680, 0.0086)
EN <sub>1</sub>	(0.0697, 0.9059, 0.0244)	(0.1445, 0.8555, 0)	(0.0355, 0.9534, 0.0111)	(0.0027, 0.9973, 0)
EN <sub>2</sub>	(0.0251, 0.9657, 0.0092)	(0.0651, 0.9108, 0.0241)	(0.1026, 0.8666, 0.0307)	(0.1947, 0.7435, 0.0618)
T <sub>1</sub>	(0.0635, 0.9170, 0.0195)	(0.0266, 0.9633, 0.0101)	(0.0830, 0.8882, 0.0288)	(0.1118, 0.8660, 0.0222)
T <sub>2</sub>	(0.0201, 0.9725, 0.0074)	(0.0830, 0.8918, 0.0252)	(0.2111, 0.7499, 0.0390)	(0.0524, 0.9280, 0.0196)
T <sub>3</sub>	(0.1787, 0.7711, 0.0502)	(0.2289, 0.7007, 0.0704)	(0.0525, 0.9224, 0.0251)	(0.1219, 0.8421, 0.0360)
S <sub>1</sub>	(0.0524, 0.9280, 0.0196)	(0.1591, 0.7889, 0.0520)	(0.2111, 0.7499, 0.0390)	(0.1230, 0.8409, 0.0361)

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**Table 11:** The negative-ideal solutions

Metrics	NIS
EC <sub>1</sub>	(0.0276, 0.9590, 0.0134)
EC <sub>2</sub>	(0.0079, 0.9892, 0.0029)
EC <sub>3</sub>	(0.0234, 0.9680, 0.0086)
EN <sub>1</sub>	(0.0027, 0.9973, 0)
EN <sub>2</sub>	(0.0251, 0.9657, 0.0092)
T <sub>1</sub>	(0.0266, 0.9633, 0.0101)
T <sub>2</sub>	(0.0201, 0.9725, 0.0074)
T <sub>3</sub>	(0.0525, 0.9224, 0.0251)
S <sub>1</sub>	(0.0524, 0.9280, 0.0196)

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**Table 12:** The Euclidean and Hamming distance from each energy storage technology to the

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negative-ideal solutions

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
Euclidean distance	1.8787	1.7814	1.8273	1.8655
Hamming distance	4.2170	4.1632	4.2026	4.2099



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827 **Table 13:** The ranking of the four energy storage technologies using the single-criterion analysis

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method

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
EC <sub>1</sub>	2	1	4	3
EC <sub>2</sub>	1	2	4	3
EC <sub>3</sub>	3	2	1	4
EN <sub>1</sub>	2	1	3	4
EN <sub>2</sub>	4	3	2	1
T <sub>1</sub>	3	4	2	1
T <sub>2</sub>	4	2	1	3
T <sub>3</sub>	2	1	4	3
S <sub>1</sub>	4	2	1	3

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841 **Table 14:** The results of the analysis of the threshold value on the sustainability ranking of the four  
 842 energy storage technologies

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
Final assessment score	0.1618	-0.2272	-0.0437	0.1091
( $\tau = 0.01, 0.02, 0.03, 0.04$ )				
Ranking	1	4	3	2

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