

Smart control of the assembly process with a fuzzy control system in the context of Industry 4.0

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Abstract: Assembly line balancing is important for the efficiency of the assembly process, however, a wide range of disruptions can break the current workload balance. Some researchers explored the task assignment plan for the assembly line balancing problem with the assumption that the assembly process is smooth with no disruption. Other researchers considered the impacts of disruptions, but they only explored the task re-assignment solutions for the assembly line re-balancing problem with the assumption that the re-balancing decision has been made already. There is limited literature exploring on-line adjustment solutions (layout adjustment and production rate adjustment) for an assembly line in a dynamic environment. This is because real-time monitoring of an assembly process was impossible in the past, and it is difficult to incorporate uncertainty factors into the balancing process because of the randomness and non-linearity of these factors. However, Industry 4.0 breaks the information barriers between different parts of an assembly line, since smart, connected products, which are enabled by advanced information and communication technology, can intelligently interact and communicate with each other and collect, process and produce information. Smart control of an assembly line becomes possible with the large amounts of real-time production data in the era of Industry 4.0, but there is little literature considering this new context. In this study, a fuzzy control system is developed to analyze the real-time information of an assembly line, with two types of fuzzy controllers in the fuzzy system. Type 1 fuzzy controller is used to determine whether the assembly line should be re-balanced to satisfy the demand, and type 2 fuzzy controller is used to adjust the production rate of each workstation in time to eliminate blockage and starvation, and increase the utilization of machines. Compared with three assembly lines without the proposed fuzzy control system, the assembly line with the fuzzy control system performs better, in terms of blockage ratio, starvation ratio and buffer level. Additionally, with the improvement of information transparency, the performance of an assembly line will be better. The research findings shed light on the smart control of the assembly process, and provide insights into the impacts of Industry 4.0 on assembly line balancing.

Keywords: Assembly line balancing; Re-balancing; Industry 4.0; Fuzzy control system.

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1. Introduction

An assembly line, which is essentially a continuous production line, consists of materials and workstations combined by conveyor belts, contacting workers and machines closely and efficiently [1]. The Assembly Line Balancing Problem (ALBP) focuses on assigning tasks to workstations, with the aim of satisfying the precedence relationships among the tasks and the workload limitations of workstations, with the aim of optimizing performance measures [2].

Most of the existing literature on ALBP assumes an environment that works smoothly without any disruption [3]. However, modifications in the input parameters, such as task adding or moving, changes in precedence relationships, increases and decreases in task times, and changes in the cycle time because of changing demand, necessitate a re-balancing [4]. Thus, an assembly line needs to be re-balanced rather than balanced, in practice [2], and assembly line balancing or the re-balancing problem should be considered in a dynamic environment with disruptions. There is some literature that deals with the re-balancing problem [4-6], however, the problem is still underdeveloped [7]. The existing research is based on the assumption that the re-balancing decision has been made already, and only addresses the task re-assignment problem without discussing how disruptions affect the current assembly plan and how to react to disruptions. Nevertheless, there is a trade-off between re-balancing the assembly line as soon as possible to reduce production losses, and keeping the stability of the assembly line to prevent bigger disruptions to the assembly line. How to make such a tradeoff is a problem faced by practitioners, and assembly planning and control are essential for managing the expanding product ranges, reducing delivery time, reducing costs and increasing profitability [8].

The majority of the literature on ALBP addresses the problem in the traditional context where it is manpower-intensive. Consequently, in a traditional assembly line, on-line monitoring of buffer levels, production performance of each workstation and processing times of tasks is unrealistic in practice. However, with the development of new technologies, automated assembly lines are attracting increasingly more attention, especially since the introduction of Industry 4.0, which is the fourth industrial revolution, in 2013.

Industry 4.0 aims to increase operational effectiveness and provide new definitions of business models, services and products [9, 10]. It introduces Internet technology to make factories more intelligent, improves adaptability, resource efficiency and ergonomics, and integrates customers and business partners into the product definition process and value and logistics chains, respectively [11]. According to ElMaraghy and ElMaraghy [12], Internet of things (IoT), which is a basic premise of Industry 4.0, refers to a networked interconnection of objects aiming to make all things communicable, and enables objects to exchange information on their status and condition. The advanced information and communication technology (e.g. wireless sensor network, and cyber-physical systems) enables the prevailing digital transformation, and enables products to evolve from the usual products to the smart, connected products (SCP) [13, 14]. SCP represents the third wave of IT-driven competition, with IT embedded in the products, and can collect, process and produce information [15].

1 Smart manufacturing resources embedded with IoT technologies (i.e. RFID, barcoding) can
2 interact and communicate with each other intelligently, and smart machines in the era of Industry
3 4.0 have the ability to send their working status to a central cloud-based “manager” in real time
4 [16]. Large amounts of real-time manufacturing data can be obtained, and different parts of an
5 assembly line can communicate with each other and can get access to real-time information
6 easily. Thus, Industry 4.0 will bring new attributes and opportunities for an assembly line, and
7 will create a novel context for an assembly line, with real-time information on an assembly line.
8 Nevertheless, there is sparse literature on on-line planning and control of an assembly line,
9 taking the novel context into account. Furthermore, how to efficiently use the real-time data to
10 make advanced decisions in a smart factory is an urgent problem to be solved [17].

11

12 Accurate analysis of an automotive assembly line is difficult because of the randomness and
13 nonlinearity caused by unpredictable machine failures, asynchronism among various sections
14 in the assembly line, the coupling of sections through finite buffers, and coupling between the
15 production and material handling system [18]. It is challenging to design a control system for a
16 nonlinear system having unexpected events [19], and a mathematical model of such a control
17 system is difficult to obtain. However, fuzzy controllers can provide a systematic and efficient
18 framework for incorporating data obtained by sensors and human judgments, and it is always
19 possible to design a fuzzy controller that is suitable for the nonlinear system by carefully
20 choosing the parameters of the fuzzy controller [20]. Therefore, fuzzy controllers can be used to
21 realize the smart control of an assembly line.

22

23 Although there are some explorations on ALBP with fuzzy theory, fuzzy theory is always used to
24 deal with uncertain processing times, multiple goals, or improve the algorithm to solve ALBP
25 [21-23]. To make balance control of the sewing operations on assembly lines, Hui et al. [24] used
26 a fuzzy system to determine the number of operators to be moved in and out of a sewing section.
27 This is an important exploration in that a fuzzy system is utilized to deal with the balance control
28 of a manufacturing process. However, they restricted the balance control problem to apparel
29 manufacturing and assumed that the machine downtime due to failure was insignificant. Thus,
30 they did not consider possible disruptions in the manufacturing process, and did not discuss
31 when disruptions can lead to assembly plan modifications.

32

33 Therefore, there is little literature that addresses ALBP, considering the novel context brought by
34 Industry 4.0, where real-time information is accessible to workstations, and commands can be
35 easily sent to machines to adjust their production rates to react to disruptions and achieve a better
36 collaboration of workstations. Differing from the traditional production system, assembly lines in
37 the era of Industry 4.0 will be more re-configurable and be re-balanced more frequently, thus, the
38 assembly process to be controlled should be treated from a dynamic perspective. In this study,
39 real-time information of an assembly line is analyzed by a fuzzy control system, and whether and
40 how to re-balance the current assembly line and adjust the production rate of each workstation
41 are determined. The number of open workstations will decrease or increase based on the
42 availability of workstations and the ‘decisions’ of the fuzzy system, and task re-assignments will
43 be implemented after the re-balancing decision is made. Consequently, an assembly line can be
44 adjusted with the proposed fuzzy system to adapt to the dynamic environment, and to the best of

1 our knowledge, this is the first study that deals with the on-line adjustment (layout adjustment
2 and production rates adjustments) of an assembly line with a fuzzy system. The automated
3 balance control of an assembly line is explored in a novel context created by Industry 4.0, and
4 the link between disruptions and the corresponding reactions is created by the proposed fuzzy
5 system. The research findings shed light on the smart control of the assembly process.
6 Additionally, the performance of assembly lines with different levels of information transparency
7 is compared to show the impact of high-level information transparency on the assembly process.
8 Thus, the research findings also provide references for practitioners who are considering the
9 adoption of new technologies involved in Industry 4.0.

10
11 The rest of the paper is structured as follows. The related literature is shown in section 2; The
12 fuzzy control system is introduced in section 3; Section 4 shows the numerical experiments and
13 results; Conclusions of the research findings and suggestions for future research are shown in
14 section 5.

15 16 **2. Literature review**

17 18 **2.1 Assembly line balancing and re-balancing**

19 Assembly Line Balancing (ALB) is important for overall efficiency. Most of the ALB literature
20 assumes an environment that works smoothly without any disruptions, however, manufacturing
21 environments are often prone to disruptions [3]. A wide variety of modifications in the input
22 parameters, such as task adding or moving, changes in precedence relationships, increases and
23 decreases in task times, and changes in the cycle time because of the changing demand,
24 necessitate a re-balancing [4]. Robust solutions can retain the initial task assignment to some
25 extent without modifications, however, at some point, re-balancing of the line becomes
26 inevitable [25]. Not surprisingly, Celik et al. [2] claimed that an assembly line needs to be
27 re-balanced rather than balanced.

28
29 The re-balancing problems are quite different from the balancing problems since the existing
30 configuration has to be taken into account, thus, the methods and solutions developed for line
31 balancing problems cannot be directly used for re-balancing problems [25]. There are some
32 researchers who have explored the re-balancing problems. Based on “Technique for Order
33 Preference by Similarity to Ideal Solution” (TOPSIS), which is an integration of a multi-attribute
34 decision-making procedure, Gamberini et al. [4] dealt with the assembly line re-balancing
35 problem by considering minimizing the unit labor and expected unit incompleteness costs and tasks
36 re-assignment. Yang et al. [5] proposed a multi-objective genetic algorithm to address the
37 re-balancing problem for a mixed-model assembly line with seasonal demands. Celik et al. [2]
38 defined a U-line re-balancing problem with stochastic task times, and proposed a method based
39 on ant colony optimization. Motivated by task improvements during the production process
40 along an assembly line, Li [6] used an algorithm named ENCORE to solve the problem in the
41 context of automatic assembly line systems. Sancı and Azizoğlu [3] considered the re-balancing
42 problem in which tasks at least on the disrupted workstations should be reassigned to other
43 workstations.

1 For the re-balancing problem, a quick resolution is more important than an optimal solution, and
2 the aim is to react quickly to reduce negative impacts of any disturbing events and define a new
3 solution that is close to the initial line balancing [26]. When dealing with the re-balancing
4 problem, Celik et al. [2] proposed an algorithm to minimize the total cost of re-balancing which
5 is the sum of task transposition costs, workstation opening/closing costs and operating costs of
6 workstations for a particular planning horizon. Sancı and Azizoğlu [3] made a trade-off between
7 the efficiency of the new balance and the stability, indicated by the differences between the initial
8 and the new task assignments.

9
10 However, the re-balancing problem is still underdeveloped [7]. As discussed above, there are
11 many factors resulting in re-balancing, but monitoring all these factors and combining them
12 together to make a decision is difficult. Consequently, the re-assignment solutions are searched
13 for with the assumption that the re-balancing decision has been made, however, there is sparse
14 literature on when the re-balancing decision should be made, although this problem is faced by
15 all practitioners. Because of the uncertainties, exact parameters of the production process are
16 difficult to obtain before the process begins [27]. Thus, on-line solutions are needed to deal with
17 uncertainties effectively.

18 19 **2.2 Industry 4.0**

20 Industry 4.0, as an industrial revolution, will reshape the ways things are made. Optimized cells
21 will be integrated, automated and optimized to improve the efficiency and change the
22 relationships among suppliers, producers and customers, and redefine the relationship between
23 humans and machines [10]. Apart from providing great opportunities to reshape the future,
24 Industry 4.0 aims to increase the operational effectiveness and new definitions of business
25 models, services and products [9, 10]. With the latest advanced technologies, the smart factory in
26 the context of Industry 4.0 is becoming a new manufacturing pattern [28].

27
28 According to Jazdi [29], we are experiencing Industry 4.0 in terms of Cyber-Physical Systems
29 (CPS). With cyber technology, automated systems and equipment, internal logistics systems and
30 operating supplies are connected, which enables direct access to the higher-level processes and
31 services, optimal resource utilization and smart control [29].

32
33 The CPS connected to the Internet is often referred to as the Internet of Things (IoT), which is an
34 information network that consists of physical objects which allows interaction and cooperation to
35 reach common goals [30]. IoT is the basic premise for the implementation of Industry 4.0 [31]. It
36 provides a version for the future Internet where physical things (such as Radio-Frequency
37 Identification (RFID) tags, sensors, actuators and mobile phones) are connected [32]. What is
38 more, its basic idea is the pervasive presence of large amounts and kinds of things or objects,
39 allowing it to gain ground in the scenario of modern wireless telecommunications [30]. It gives
40 access to information about the physical world and promotes innovative services to increase
41 efficiency and productivity [32]. With the real-time data obtained by IoT, big data analysis can be
42 used to make logistic decisions [33], and smart production [28], smart logistics [34] and smart
43 cities [35] are possible. Meanwhile, advanced technologies enable better implementation of
44 automated guided vehicles [36, 37], which supports smart warehouse. Additionally, big data

1 analysis can be used to improve the speed and accuracy in maintenance decision making [38].

2
3 In the era of Industry 4.0, there will be vast changes in the assembly process. Different parts of
4 an assembly line can communicate with each other, and with more easily accessible real-time
5 information, it is expected to realize better collaboration between different parts. Smart assembly
6 systems are needed to achieve more autonomy in communication between entities in the system
7 and more adaptable control of assembly flow and better performance [12]. However, there are
8 few studies dealing with assembly process control with the new attributes of an assembly line in
9 the context of Industry 4.0 considered.

10 11 **2.3 Fuzzy logic system**

12 Researchers have used fuzzy logic when dealing with ALBP. Some use fuzzy logic to define the
13 processing time of one task. For example, Zacharia and Nearchou [23] presented a fuzzy
14 extension of the type 2 ALBP with fuzzy job processing times, and the processing times were
15 formulated by triangular fuzzy membership functions. Some researchers use fuzzy theory to deal
16 with multiple goals and heuristic algorithms improvements in ALBP. For example, fuzzy goal
17 programming was used, and an appropriate genetic algorithm was developed by Cheshmehgaz et
18 al. [21], to consider three criteria during the balancing: cycle time, overall workload and
19 assembly worker postures. To solve a multi-objective ALBP, Simona [22] utilized a fuzzy
20 controller for tuning inertia weight in particle swarm optimization.

21
22 There are few studies exploring the application of fuzzy controllers in workload balancing
23 control of assembly lines, and real-time production rate adjustment in each workstation to
24 decrease inventory and improve the overall production rate when there are uncertainties.
25 However, fuzzy controllers are always applied in decision making. Tsourveloudis et al. [39]
26 developed a line, assembly, and disassembly controller to adjust the processing rate of each
27 production stage so that the workflow is balanced, and the extreme events of machine starving or
28 blocking are reduced, and simulation results showed that the proposed approach outranks other
29 control policies in keeping the WIP inventory low. Nakandala et al. [40] proposed a fuzzy-based
30 decision support model for determining the chance of meeting on-time delivery in a complex
31 supply chain environment. Fuzzy logic principles and a unitary structure-based supply chain
32 model were integrated, and uncertainties associated with key inputs of on-time delivery
33 performance for effective decision-making process were addressed, to minimize of business
34 losses that result from penalties and customer dissatisfaction and the consequently reduced
35 market share. Al-Ebbini et al. [41] presented a fuzzy lung allocation system to determine which
36 potential recipients would receive a lung for transplantation in order to deal with the vagueness
37 and fuzziness of the decision making of the medical experts, and the proposed decision process
38 provided a more effective, time-efficient, and systematic decision support tool.

39
40 Thus, although there are some explorations on ALBP with fuzzy theory, there are few
41 publications considering the impacts of Industry 4.0 on the assembly process, exploring the
42 fuzzy control system to utilize the real-time information which is accessible to all workstations
43 and adjusting the assembly line when necessary. In our study, a fuzzy control system is
44 developed to deal with the disruptions to an assembly line and to adjust the assembly line to

1 achieve better performance.

2

3 **3. Problem statements and assumptions**

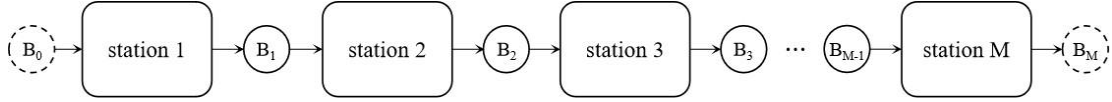
4

5 Figure 1 shows the structure of an assembly line consisting of M workstations and $M - 1$

6 buffers between these workstations, and this is the assembly line considered in this study. B_i

7 denotes buffer i ($i = 0, 1, 2, \dots, M$).

8



9

10 **Figure 1.** An assembly line with M workstations

11

12 The whole assembly process is divided into production cycles by assembly line re-balancing.

13 After the preparation for assembly line re-balancing is completed, a new production cycle will

14 begin, and P_i denotes the cumulative production in the i^{th} production cycle. Figures 2a and

15 2b are used to illustrate the related variables for two scenarios. Let P , D and T_d denote the

16 cumulative production, the demand quantity of products and the delivery time left for the current

17 production cycle, respectively. Let t_i ($i > 0$, $t_0 = 0$) denote the time when the preparation for

18 the i^{th} re-balancing is completed and a new production cycle will begin. At t_i , D and T_d

19 will be updated, and P will be initialized to be 0.

20

21 At first, $D = D_0$, and $T_d = T_{total}$. If there is no re-balancing since t_0 , D and T_d will not

22 be updated, and P is the cumulative production since t_0 (see Figure 2a). Let T_i ($i > 0$)

23 denote the duration between t_{i-1} and the beginning of the i^{th} re-balancing, and let T_{r_i} denote

24 the preparation time for the i^{th} re-balancing. If assembly line re-balancing has been

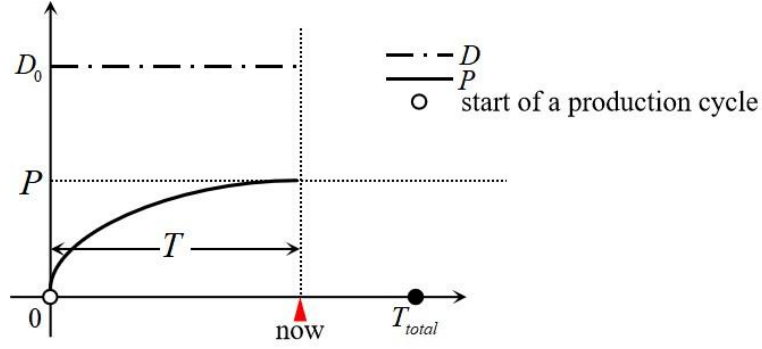
25 implemented for k times ($k > 0$),

$$26 \quad D = D_0 - \sum_{i=1}^k P_k, \quad (1)$$

$$27 \quad T_d = T_{total} - \sum_{i=1}^k (T_i + T_{r_i}), \quad (2)$$

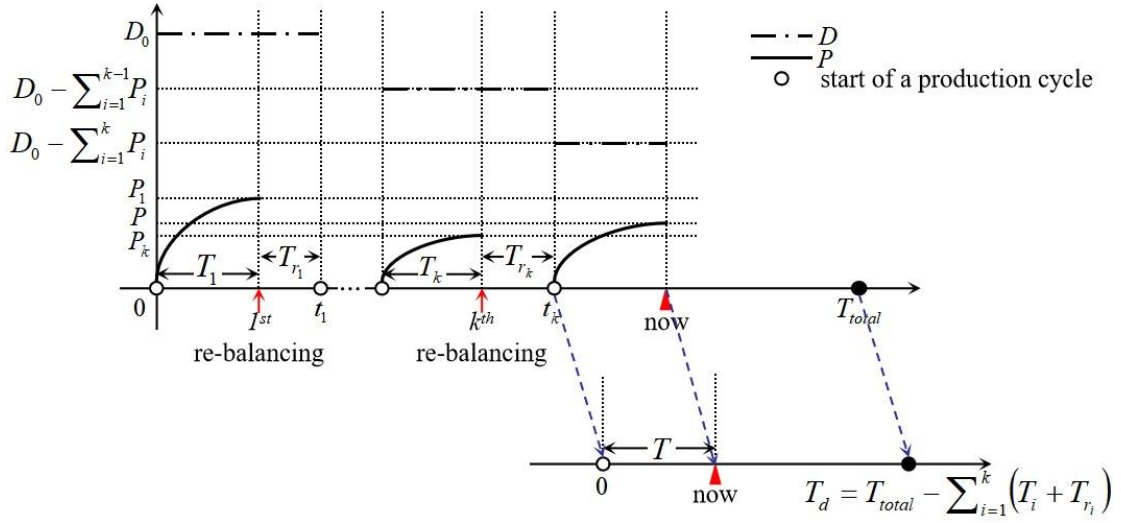
28 and P is the cumulative production since t_k (see Figure 2b).

29



1
2
3

Figure 2a. Illustration of variables when no re-balancing has been conducted



4
5
6

Figure 2b. Illustration of variables after an assembly line has been re-balanced

7 The main assumptions in this study are as follows:

8 (1) Let pr_i denote the production rate of workstation i ($pr_i \leq pr_{\max}^i$), and pr_{\max}^i is the
9 largest production rate of workstation i . Thus, workstation i can operate at a minimum
10 processing time $\frac{1}{pr_{\max}^i}$.

11 (2) $B_i (1 \leq i \leq M-1)$ has finite capacity. B_0 is infinite source of raw material so that station
12 1 is never starved. B_M has infinite storage capacity so that station M is never blocked.

13 (3) D_0 is the demand quantity of products given at t_0 .

14 (4) The financial cost for assembly line re-balancing is ignored in this study, but the time cost
15 due to the preparation for all the re-assigned tasks is considered.

16 (5) Machines break down and are repaired randomly with different probabilities. The failure rates
17 of all machines are λ , and the repair rates of all machines are μ . The uptimes and downtimes

1 of machines follow exponential distributions with the mean of $\frac{1}{\lambda}$ and $\frac{1}{\mu}$, respectively.

2 (6) The automated assembly line, where more automated technologies are adopted and the
3 assembly tasks are done by robots rather than human workers, is considered in this study.
4 According to Li [6], there are two characteristics of the automated assembly line in which robots
5 are the primary agents in assembly tasks: learning automata, and control architecture and
6 collaborative learning. The first characteristic means manufacturing techniques can be refined
7 based on the prior manufacturing experience and this leads to task time reductions. As to the
8 second characteristic, task time reductions of one robot can be realized by the other robots since
9 the learned skills can be transferred to the other robots. In this study, the above learning effect is
10 considered, and after the learning effect occurs, the processing ability of each workstation is
11 improved. The processing time reductions of all tasks are assumed to occur simultaneously. The
12 task time reduction rate of the task i is defined in equation (3):

$$13 \quad r_i = \frac{t_i - t'_i}{t_i} \quad (3)$$

14 where t_i is the initial processing time of the task i , and t'_i is the decreased processing time
15 of task i after a learning effect occurs.

16 (7) Blockage of workstation i occurs when it finishes one workpiece, but buffer i is full.
17 Workstation i will be blocked until there is space in buffer i . Starvation of workstation i
18 occurs when it is idle, but buffer $i-1$ is empty. The starvation will end when there is inventory
19 in buffer $i-1$.

20

21 **4. Fuzzy control model**

22

23 **4.1 Fuzzy control system**

24 Figure 3 shows the fuzzy control system for the assembly line shown in Figure 1. FC_i denotes

25 the i^{th} fuzzy controller. There are two types of fuzzy controllers in the fuzzy control system.

26 Fuzzy controller FC_1 is used to deal with global information and make a decision on whether

27 to re-balance the assembly line. Fuzzy controllers FC_2 to FC_{M+1} are used to process the

28 local information and make decisions on how to adjust the production rate of each workstation
29 when re-balancing is not needed.

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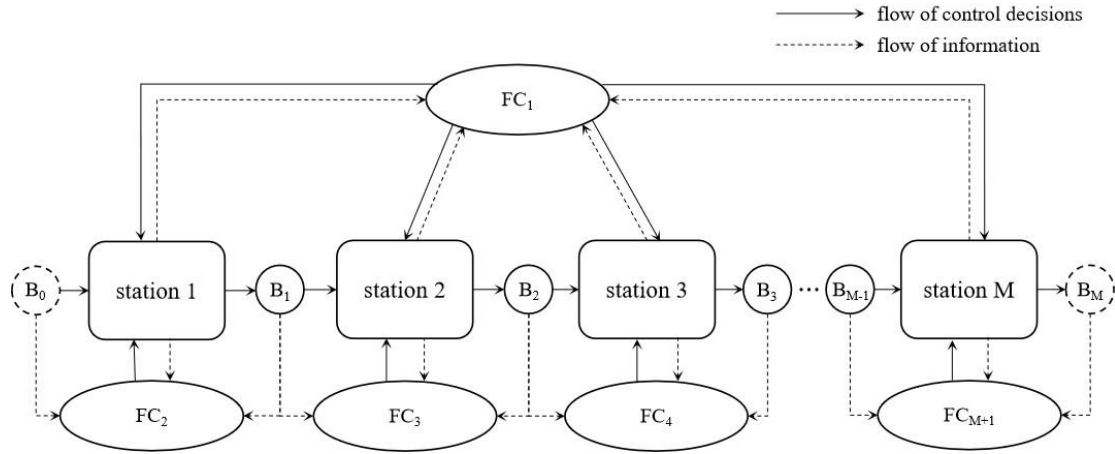


Figure 3. The framework of the fuzzy control system

4.2 Structures of two types of fuzzy controllers

A fuzzy controller is an inference system to mimic human thinking, which consists of a fuzzifier, some fuzzy IF-THEN rules, a fuzzy inference engine and a defuzzifier [41].

4.2.1 Fuzzification

In the fuzzification process, the input data set is converted into fuzzy sets by fuzzy membership functions. Each of the fuzzy subsets represents one linguistic term that allows its members to have different grades of membership.

4.2.2 Fuzzy inference engine and fuzzy rule base of type 1 fuzzy controller

Two factors, which are important in determining whether to re-balance the assembly line, are the inputs of the fuzzy controller, and the output is the necessity of assembly line re-balancing.

(1) Urgency of the assembly job, urg

To keep the stability of an assembly line and prevent overacting to disruptions, urgency of the assembly job is considered before a re-balancing decision is made. The assembly job urgency is defined in equation (4) as follows:

$$urg = \begin{cases} \frac{D \cdot \frac{T}{T_d} - P}{D \cdot \frac{T}{T_d}}, & D \cdot \frac{T}{T_d} \geq \frac{P}{2} \\ -1, & D \cdot \frac{T}{T_d} < \frac{P}{2} \end{cases} \quad (4)$$

where T is the assembly time used in the current production cycle. $D \cdot \frac{T}{T_d}$ is the amount of

production that should be finished at present, and if it is larger than P , there is a risk that the demand cannot be satisfied. urg ranges from -1 to 1, and the fuzzy term set is {very small, small, medium, large, very large}.

1 (2) Time cost to re-balance the assembly line, T_c

2 Assembly line re-balancing should not be considered when there is not a large possibility that the
3 production after re-balancing is more than that without re-balancing, even though it is quite
4 urgent to increase production The cost of re-balancing is defined in equation (5):

$$5 \quad T_c = \frac{pr_{ini} \cdot (T_{total} - T - T_m) - pr_{new} \cdot \left(T_{total} - T - T_r - \frac{1}{pr_{new}} \cdot n_{avail} \right)}{pr_{max} \cdot (T_{total} - T)} \quad (5)$$

6 where T_m denotes the maintenance time of the assembly line, and is defined as

$$7 \quad T_m = \max_{i \in T_A} \{T_{m_i}\}. \quad (6)$$

8 T_A is a set consisting of the stations involved in the current assembly plan (some workstations

9 may be closed for maintenance), and T_{m_i} is the maintenance time needed by station i . T_r

10 designates the preparation time for re-balancing the assembly line and is defined as the sum of

11 the preparation times of all the re-assigned tasks. The term pr_{ini} denotes the largest production

12 ability according to the current assembly plan, defined as

$$13 \quad pr_{ini} = \min_{i \in T_A} \{pr_{max}^i\}. \quad (7)$$

14 Besides, pr_{new} is the production rate after re-balancing, and pr_{max} designates the largest

15 production rate that can be achieved by the current assembly line with all stations operative.

16 n_{avail} denotes the number of stations used in the re-balancing plan. $T_r + \frac{1}{pr_{new}} \cdot n_{avail}$ denotes

17 the shortest time from the beginning of the preparation for the re-balancing to obtaining one

18 finished product. A small T_c less than 0 indicates that there is some possibility that the

19 production, after re-balancing during the simulation time remaining, is increased. The smaller

20 T_c is, the larger the possibility becomes. The fuzzy term set is {very small, small, medium, large,

21 very large}.

22

23 (3) Output variable: the necessity of re-balancing, N

1 The set of fuzzy terms is {very small, small, medium, large, very large}. The necessity is
 2 between 0% and 100%, and the fuzzy terms of ‘very small’ and ‘very large’ indicate the range
 3 from 0% to 100%. Assembly line re-balancing is conducted when N is larger than a
 4 predetermined threshold.

6 Fuzzy rules are the base of the fuzzy inference engine, and they can be utilized to make decisions
 7 and generate control actions. The rules are in the form of if-then statements. There are 25 fuzzy
 8 rules for type 1 fuzzy controller (see Table 1). When there is a risk that the demand cannot be
 9 satisfied and T_c is smaller than 0, assembly line re-balancing may take place. Otherwise,
 10 re-balancing will not take place. Therefore, assembly line re-balancing takes place only when the
 11 necessity is large enough, so as to adjust the assembly line in time and prevent overreaction.

13 **Table 1**

14 Fuzzy rule base for the type 1 fuzzy controller

| | T_c | | | | |
|-------|-------|----|----|----|----|
| urg | VS | S | ME | L | VL |
| VS | S | S | S | VS | VS |
| S | L | ME | ME | VS | VS |
| ME | VL | VL | L | VS | VS |
| L | VL | VL | L | S | VS |
| VL | VL | VL | L | S | VS |

15 Note: VS, S, ME, L and VL denote very small, small, medium, large and very large, respectively.

17 4.2.3 Fuzzy inference engine and fuzzy rule base of type 2 fuzzy controller

18 Three factors, which affect decision making on the production rate adjustment of a workstation,
 19 are the inputs of type 2 fuzzy controllers, and the output is the production rate adjustment of the
 20 corresponding workstation.

22 (1) Upstream buffer level BL_{i-1} and downstream buffer level BL_i of workstation i

23 The upstream buffer of workstation i is B_{i-1} , and the downstream buffer is B_i . The buffer
 24 level of buffer i is defined in equation (8):

$$25 \quad BL_i = \frac{w_i}{C_i}, \quad i = 0, 1, 2, \dots, M \quad (8)$$

26 where w_i is the inventory of buffer i , and C_i is the capacity of buffer i . Buffer levels range
 27 from 0 to 1. The set of fuzzy terms is {very small, small, medium, large, very large}.

29 (2) Production surplus rate, S_i

30 The third factor that affects the production rate adjustment is the production surplus rate, which
 31 is defined in equation (9) as follows:

$$S_i = \begin{cases} \frac{P_{S_i} - d}{T} - d, & P_{S_i} \geq d \cdot T \\ pr_{\max}^i - d, & \\ \frac{P_{S_i} - d}{T}, & P_{S_i} < d \cdot T \\ d, & \end{cases} \quad (9)$$

where P_{S_i} is the cumulative production of workstation i . d denotes the demand production rate that is updated at the beginning of each production cycle. The production rate of workstation i should be around d to satisfy the demand.

If the percentage of the operative time of a workstation is $\frac{1}{\frac{1}{\lambda} + \frac{1}{\mu}}$, the operative time of the

whole assembly line is no larger than $T_{total} \cdot \frac{\mu}{\lambda + \mu}$. Thus, a relatively safe demand rate d at

t_0 should be at least $\frac{D_0}{T_{total} \cdot \frac{\mu}{\lambda + \mu}}$. In addition, the re-balancing decision is made only when

there is a risk that the demand cannot be satisfied, thus, after re-balancing, d is set to be a small value (it is 10^{-6} in this study) smaller than pr_{ini} in order to make up for the production loss due to assembly plan modification as soon as possible.

The surplus rate ranges from -1 to 1. When it is larger than 0, there is more inventory; Otherwise, there are backlogs. The fuzzy set of production surplus rate is {very small, small, medium, large, very large}.

(3) Output variable: production rate adjustment of workstation i , adj_pr_i

The output adj_pr_i is the adjustment suggestion for pr_i , and ranges from -1 to 1. The fuzzy terms set is {very small, small, medium, large, very large}. When adj_pr_i is larger than 0,

pr_i should be increased toward pr_{\max}^i . Otherwise, pr_i should be decreased toward 0. The production rate after adjustment is defined in equation (10) as follows:

$$pr_i' = \begin{cases} pr_i + adj_pr_i \cdot (pr_{\max}^i - pr_i), & adj_pr_i \geq 0 \\ pr_i + adj_pr_i \cdot (pr_i - 0), & adj_pr_i < 0 \end{cases} \quad (10)$$

1 There are 125 rules for the type 2 fuzzy controllers (see Table 2). When there is no risk of
2 starvation or blockage, pr_i should be adjusted mainly based on S_i . Otherwise, since the
3 adverse impact of starvation and blockage propagates throughout the assembly line, pr_i should
4 be adjusted to eliminate starvation and blockage.

1 **Table 2**

2 Fuzzy rule base for type 2 fuzzy controllers

| $S_i=VS$ | | | | | |
|------------|--------|----|----|----|----|
| | BL_i | | | | |
| BL_{i-1} | VS | S | ME | L | VL |
| VS | L | S | S | S | VS |
| S | VL | VL | VL | L | VS |
| ME | VL | VL | VL | VL | S |
| L | VL | VL | VL | VL | S |
| VL | VL | VL | VL | VL | ME |
| $S_i=S$ | | | | | |
| | BL_i | | | | |
| BL_{i-1} | VS | S | ME | L | VL |
| VS | L | S | S | VS | VS |
| S | VL | VL | L | L | VS |
| ME | VL | VL | VL | L | S |
| L | VL | VL | VL | L | S |
| VL | VL | VL | VL | L | ME |
| $S_i=ME$ | | | | | |
| | BL_i | | | | |
| BL_{i-1} | VS | S | ME | L | VL |
| VS | ME | S | VS | VS | VS |
| S | VL | ME | ME | ME | VS |
| ME | VL | L | ME | ME | S |
| L | VL | VL | ME | ME | S |
| VL | VL | VL | L | ME | ME |
| $S_i=L$ | | | | | |
| | BL_i | | | | |
| BL_{i-1} | VS | S | ME | L | VL |
| VS | S | VS | VS | VS | VS |
| S | ME | S | S | S | VS |
| ME | ME | S | S | S | VS |
| L | L | ME | S | S | S |
| VL | VL | L | L | ME | ME |
| $S_i=VL$ | | | | | |
| | BL_i | | | | |
| BL_{i-1} | VS | S | ME | L | VL |
| VS | VS | VS | VS | VS | VS |
| S | S | VS | VS | VS | VS |
| ME | ME | VS | VS | VS | VS |
| L | L | ME | VS | VS | VS |
| VL | VL | L | L | ME | ME |

3

4 **4.2.4 Defuzzification**

5 The output generated by the fuzzy inference engine is a set of fuzzy membership values [40].

6 Fuzziness helps rule evaluation during the intermediate steps. However, the final desired output

7 is generally a single number. Therefore, all the outputs are transferred into the final crisp value

8 by a widely used defuzzification method: the centroid method, which assesses the center of

1 gravity of the possible distribution of the fuzzy output [40], and is defined in equation (11) as
 2 follows [41]:

$$3 \quad y = \frac{\sum_{r=1}^{R_l} A^{cr} C_{A^{cr}}}{\sum_{r=1}^{R_l} A^{cr}} \quad (11)$$

4 where A^{cr} denotes the area of consequent's fuzzy subset, which is obtained by α
 5 membership determined by the r^{th} rule. $C_{A^{cr}}$ is the center of area A^{cr} . R_l designates the
 6 number of fuzzy rules.

7

8 **5. Numerical experiments**

9 **5.1 Numerical experiments design**

10 The assembly line used to test the fuzzy control system is defined by KILBRID (45 tasks), and
 11 the task times and precedence relationship information can be found in the SALBP data sets
 12 shown on <https://assembly-line-balancing.de/salbp/benchmark-data-sets-1993/>. Table 3 shows
 13 the original information of the task times and the precedence graph of the chosen instance.
 14 However, the total simulation time is set to be 1000, and in order to be consistent with this
 15 setting, all the task times in this study are made to be 100 times smaller so that t_{\min} , t_{\max} and
 16 t_{avg} become to 0.03, 0.55 and 0.12267. The first column is the total number of tasks, and the
 17 second to the fifth columns are the minimal, maximal, total and average task times, respectively.
 18 The sixth column shows the order strength of the precedence graph, which is calculated by the
 19 ratio of the number of all precedence relations to $n \cdot (n - 1)$. TV is the time variability ratio
 20 defined by $\frac{t_{\max}}{t_{\min}}$, and div and $conv$ are the degrees of divergence and convergence of the
 21 precedence graph.

22

23 **Table 3**

24 Original information of task times and the precedence graph of KILBRID

| n | t_{\min} | t_{\max} | t_{sum} | t_{avg} | OS | TV | div | $conv$ |
|-----|------------|------------|-----------|-----------|-------|-------|-------|--------|
| 45 | 3 | 55 | 552 | 12.267 | 44.55 | 18.33 | 0.67 | 0.69 |

25

26 There are 8 workstations in total, and the assembly line is balanced with all tasks assigned to
 27 these 8 workstations. Some workstations which need excessively long maintenance may be
 28 closed, and after the maintenance work is completed, whether a closed workstation should be
 29 opened again is based on the fuzzy control system. Although we only chose one instance from
 30 the SALBP data set, different characteristics of machine states and different production rates
 31 required by the demand will be considered to examine the effectiveness of the proposed fuzzy
 32 system. For each combination of parameters, there are ten random runs, and different seeds are

1 used to guarantee the independent states of the machines.
2
3 Since the problem defined in this study is novel, there are no benchmark instances in the existing
4 literature. In order to model different levels of information transparency and make comparisons,
5 we set three kinds of comparative assembly lines. Table 4 shows the characteristics of the four
6 kinds of assembly lines discussed in this study. The length of the time from the breakdown of the
7 machine in station i to the recognition of the breakdown follows a normal distribution with a
8 mean which is a multiple of T_{S_i} , which denotes the sum of the processing times of tasks
9 assigned to station i . Since the real-time information is not only collected but also analyzed, the
10 assembly line with the proposed fuzzy system (AS₁) achieves higher-level information
11 transparency compared with the other three assembly lines. From AS₂ to AS₄, the level of
12 information transparency decreases.

13
14 **Table 4**
15 Assembly lines to be compared in this study

| Name | There is a fuzzy system | Production rate | Is there a maintenance delay | Description of the delay when it is applicable |
|-----------------|-------------------------|--------------------------------|---|---|
| AS ₁ | Yes | $0 \leq pr_i \leq pr_{\max}^i$ | No | - |
| AS ₂ | No | $pr_i = pr_{\max}^i$ | No | - |
| AS ₃ | No | $pr_i = pr_{\max}^i$ | Yes, and it follows a normal distribution | the mean is $5T_{S_i}$ and the standard deviation is 3 |
| AS ₄ | No | $pr_i = pr_{\max}^i$ | Yes, and it follows a normal distribution | the mean is $10T_{S_i}$ and the standard deviation is 5 |

16
17 Figure 4 shows the assembly process with the proposed fuzzy system. FC_1 is used to
18 determine whether to re-balance the assembly line. If it is decided to re-balance the assembly line,
19 then the re-balancing solution is prepared and undertaken. Otherwise, FC_2 to FC_9 are
20 activated to adjust the production rate of each workstation.
21

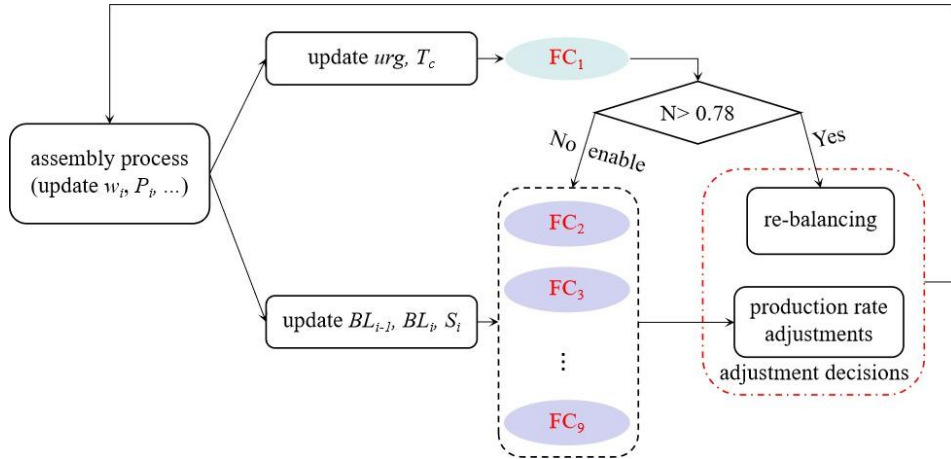


Figure 4. Assembly process with the proposed fuzzy system

As solution development for the assembly line re-balancing problem is not the main contribution of this study, the algorithm of ACO-BS developed by Huo et al. [42] to solve ALBP is used iteratively to generate the re-balancing solution, given the number of available workstations and the initial assembly plan. The framework of this method is shown in Figure 5. LB denotes the lower bound of cycle time, given the number of available workstations m^* , and is initialized to

be $\max\left\{t_{\max}, \frac{t_{sum}}{m^*}\right\}$. tr_i denotes the sum of the preparation times of all the reassigned tasks

for the solution s_i . The given cycle time is increased by 1 step by step to find all the possible cycle times, with all the available stations utilized. Finally, the re-balancing solution is obtained by considering both the cycle time and the corresponding preparation time for re-balancing.

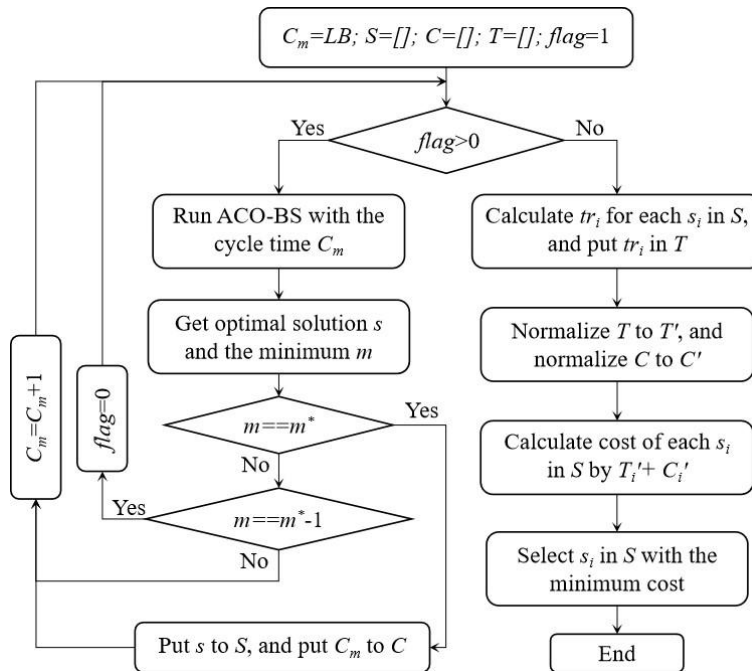


Figure 5. Framework of the method to generate the re-balancing solution

1 **5.2 Numerical results**

2 The numerical experiments were done with Simulink in MATLAB (R2016a). The learning effect
3 was set to occur at a simulation time of 500. The task time reduction rate r_i was generated
4 following the uniform distribution in the interval (0, 0.1), with mean 0.050, and standard
5 deviation 0.027. For comparison reasons, the same setting related to the learning effect was used
6 for all the cases. Additionally, all the buffer capacity of the buffer between workstations was set
7 to be 25 units, and the preparation time for each task was set to be 0.01. The experiment stops
8 when the simulation time is used up or the demand is satisfied.

9
10 There are 5 different combinations of λ and μ , 3 levels of d_0 (measured by $\frac{D_0}{T_{total}}$), and 4
11 different assembly lines. For each assembly line, there are 15 different cases to test, and for each
12 case, the average values and the standard deviations of the ten random runs are calculated and
13 shown in Tables 5a and 5b. For each experiment, six indicators are shown, that is, blockage ratio
14 (ratio of the length of blockage to the total simulation time), average buffer level, starvation ratio
15 (ratio of the length of starvation to the total simulation time), simulation time used, total
16 production and number of times of assembly line re-balancing.

1 **Table 5a**

2 Results of the numerical experiments

| λ | μ | μ/λ | No. | Mean and std | $d_0=1$ | | | | | | $d_0=0.7$ | | | | | | $d_0=0.3$ | | | | | |
|-----------|-------|---------------|-----------------|-----------------|---------|-------|-------|---------|---------|-------|-----------|-------|-------|---------|---------|-------|-----------|-------|-------|---------|---------|-------|
| | | | | | b_r | BL | st_r | t | P | no_r | b_r | BL | st_r | t | P | no_r | b_r | BL | st_r | t | P | no_r |
| 0.1 | 0.5 | 5 | AS ₁ | mean | 0.000 | 0.347 | 0.047 | 949.409 | 1000.00 | 0.000 | 0.000 | 0.123 | 0.062 | 803.144 | 700.000 | 0.000 | 0.000 | 0.089 | 0.031 | 559.940 | 300.000 | 0.000 |
| | | | | std | 0.000 | 0.064 | 0.008 | 21.739 | 0.000 | 0.000 | 0.000 | 0.018 | 0.012 | 9.844 | 0.000 | 0.000 | 0.000 | 0.002 | 0.004 | 5.607 | 0.000 | 0.000 |
| | | | AS ₂ | mean | 0.016 | 0.362 | 0.071 | 918.023 | 1000.00 | 0.000 | 0.011 | 0.327 | 0.083 | 671.585 | 700.000 | 0.000 | 0.007 | 0.244 | 0.119 | 315.004 | 300.000 | 0.000 |
| | | | | std | 0.010 | 0.085 | 0.023 | 22.647 | 0.000 | 0.000 | 0.006 | 0.085 | 0.026 | 17.781 | 0.000 | 0.000 | 0.006 | 0.065 | 0.023 | 15.842 | 0.000 | 0.000 |
| | | | AS ₃ | mean | 0.053 | 0.428 | 0.118 | 1000.00 | 725.900 | 0.000 | 0.053 | 0.428 | 0.117 | 964.831 | 699.600 | 0.000 | 0.039 | 0.363 | 0.153 | 466.546 | 300.000 | 0.000 |
| | | | | std | 0.017 | 0.075 | 0.035 | 0.000 | 31.370 | 0.000 | 0.017 | 0.078 | 0.029 | 22.982 | 1.265 | 0.000 | 0.020 | 0.086 | 0.032 | 30.299 | 0.000 | 0.000 |
| | | | AS ₄ | mean | 0.087 | 0.444 | 0.155 | 1000.00 | 512.900 | 0.000 | 0.079 | 0.430 | 0.153 | 1000.00 | 525.000 | 0.000 | 0.063 | 0.384 | 0.184 | 639.721 | 300.000 | 0.000 |
| | | | | std | 0.032 | 0.077 | 0.036 | 0.000 | 39.159 | 0.000 | 0.023 | 0.057 | 0.032 | 0.000 | 27.793 | 0.000 | 0.025 | 0.062 | 0.026 | 29.157 | 0.000 | 0.000 |
| 0.01 | 0.1 | 10 | AS ₁ | mean | 0.003 | 0.285 | 0.090 | 967.039 | 999.200 | 0.333 | 0.000 | 0.126 | 0.062 | 863.241 | 700.000 | 0.000 | 0.000 | 0.095 | 0.041 | 594.412 | 300.000 | 0.000 |
| | | | | std | 0.011 | 0.051 | 0.025 | 34.312 | 1.751 | 0.707 | 0.000 | 0.016 | 0.028 | 29.816 | 0.000 | 0.000 | 0.000 | 0.003 | 0.016 | 16.654 | 0.000 | 0.000 |
| | | | AS ₂ | mean | 0.067 | 0.435 | 0.098 | 911.229 | 1000.00 | 0.000 | 0.066 | 0.429 | 0.103 | 652.414 | 700.000 | 0.000 | 0.032 | 0.307 | 0.136 | 295.451 | 300.000 | 0.000 |
| | | | | std | 0.024 | 0.089 | 0.032 | 44.328 | 0.000 | 0.000 | 0.022 | 0.080 | 0.029 | 26.334 | 0.000 | 0.000 | 0.036 | 0.123 | 0.036 | 25.368 | 0.000 | 0.000 |
| | | | AS ₃ | mean | 0.092 | 0.462 | 0.120 | 976.718 | 982.600 | 0.000 | 0.092 | 0.440 | 0.134 | 724.977 | 700.000 | 0.000 | 0.054 | 0.332 | 0.160 | 325.486 | 300.000 | 0.000 |
| | | | | std | 0.029 | 0.101 | 0.036 | 27.294 | 33.662 | 0.000 | 0.030 | 0.094 | 0.034 | 37.823 | 0.000 | 0.000 | 0.050 | 0.139 | 0.038 | 37.421 | 0.000 | 0.000 |
| | | | AS ₄ | mean | 0.114 | 0.460 | 0.154 | 1000.00 | 904.400 | 0.000 | 0.111 | 0.454 | 0.145 | 777.045 | 700.000 | 0.000 | 0.088 | 0.367 | 0.186 | 372.435 | 300.000 | 0.000 |
| | | | | std | 0.023 | 0.078 | 0.042 | 0.000 | 59.024 | 0.000 | 0.029 | 0.074 | 0.032 | 52.693 | 0.000 | 0.000 | 0.073 | 0.140 | 0.039 | 47.908 | 0.000 | 0.000 |
| 0.01 | 0.5 | 50 | AS ₁ | mean | 0.000 | 0.082 | 0.017 | 924.738 | 1000.00 | 0.000 | 0.000 | 0.088 | 0.017 | 835.108 | 700.000 | 0.000 | 0.000 | 0.085 | 0.022 | 590.860 | 300.000 | 0.000 |
| | | | | std | 0.000 | 0.001 | 0.001 | 2.036 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 3.102 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.544 | 0.000 | 0.000 |
| | | | AS ₂ | mean | 0.000 | 0.138 | 0.029 | 727.136 | 1000.00 | 0.000 | 0.000 | 0.107 | 0.031 | 519.023 | 700.000 | 0.000 | 0.000 | 0.054 | 0.045 | 228.329 | 300.000 | 0.000 |
| | | | | std | 0.001 | 0.027 | 0.006 | 3.864 | 0.000 | 0.000 | 0.000 | 0.028 | 0.006 | 6.212 | 0.000 | 0.000 | 0.000 | 0.027 | 0.014 | 5.763 | 0.000 | 0.000 |
| | | | AS ₃ | mean | 0.011 | 0.324 | 0.051 | 787.344 | 1000.00 | 0.000 | 0.009 | 0.265 | 0.067 | 572.001 | 700.000 | 0.000 | 0.001 | 0.143 | 0.088 | 254.766 | 300.000 | 0.000 |
| | | | | std | 0.005 | 0.046 | 0.009 | 15.836 | 0.000 | 0.000 | 0.006 | 0.055 | 0.016 | 14.634 | 0.000 | 0.000 | 0.002 | 0.042 | 0.022 | 8.706 | 0.000 | 0.000 |
| | | | AS ₄ | mean | 0.041 | 0.408 | 0.077 | 861.475 | 1000.00 | 0.000 | 0.031 | 0.350 | 0.089 | 621.326 | 700.000 | 0.000 | 0.014 | 0.237 | 0.117 | 286.753 | 300.000 | 0.000 |
| | | | | std | 0.015 | 0.056 | 0.015 | 22.755 | 0.000 | 0.000 | 0.013 | 0.072 | 0.020 | 18.745 | 0.000 | 0.000 | 0.011 | 0.065 | 0.027 | 12.734 | 0.000 | 0.000 |

1 **Table 5b**

2 Results of the numerical experiments

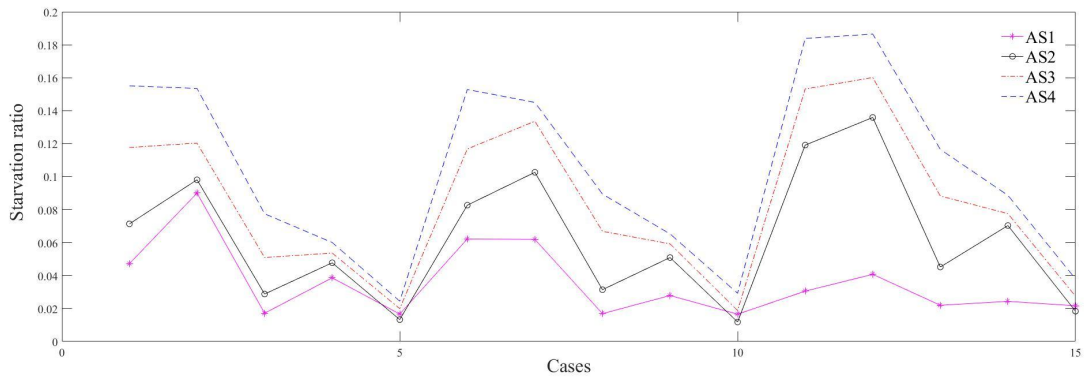
| λ | μ | μ/λ | No. | Mean and std | $d_0=1$ | | | | | | $d_0=0.7$ | | | | | | $d_0=0.3$ | | | | | | |
|-----------|-------|---------------|-----------------|-----------------|---------|-------|-------|---------|---------|-------|-----------|-------|-------|---------|---------|-------|-----------|-------|-------|---------|---------|-------|-------|
| | | | | | b_r | BL | st_r | t | P | no_r | b_r | BL | st_r | t | P | no_r | b_r | BL | st_r | t | P | no_r | |
| 0.001 | 0.1 | 100 | AS ₁ | mean | 0.000 | 0.093 | 0.039 | 938.273 | 1000.00 | 0.000 | 0.000 | 0.091 | 0.028 | 840.511 | 700.000 | 0.000 | 0.000 | 0.086 | 0.024 | 594.759 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.000 | 0.015 | 0.022 | 11.883 | 0.000 | 0.000 | 0.000 | 0.005 | 0.014 | 2.664 | 0.000 | 0.000 | 0.000 | 0.002 | 0.008 | 4.481 | 0.000 | 0.000 | 0.000 |
| | | | AS ₂ | mean | 0.011 | 0.203 | 0.048 | 750.031 | 1000.00 | 0.000 | 0.013 | 0.163 | 0.051 | 540.471 | 700.000 | 0.000 | 0.012 | 0.099 | 0.070 | 240.230 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.010 | 0.097 | 0.024 | 29.281 | 0.000 | 0.000 | 0.013 | 0.080 | 0.034 | 31.280 | 0.000 | 0.000 | 0.022 | 0.088 | 0.066 | 29.834 | 0.000 | 0.000 | |
| | | | AS ₃ | mean | 0.015 | 0.238 | 0.054 | 763.129 | 1000.00 | 0.000 | 0.016 | 0.182 | 0.059 | 553.254 | 700.000 | 0.000 | 0.014 | 0.113 | 0.078 | 243.959 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.013 | 0.089 | 0.028 | 31.488 | 0.000 | 0.000 | 0.015 | 0.070 | 0.036 | 32.275 | 0.000 | 0.000 | 0.023 | 0.084 | 0.066 | 29.451 | 0.000 | 0.000 | |
| | | | AS ₄ | mean | 0.023 | 0.280 | 0.060 | 781.053 | 1000.00 | 0.000 | 0.021 | 0.200 | 0.065 | 562.290 | 700.000 | 0.000 | 0.018 | 0.128 | 0.089 | 251.713 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.015 | 0.092 | 0.033 | 34.417 | 0.000 | 0.000 | 0.017 | 0.067 | 0.038 | 32.991 | 0.000 | 0.000 | 0.031 | 0.084 | 0.077 | 36.822 | 0.000 | 0.000 | |
| 0.001 | 0.3 | 300 | AS ₁ | mean | 0.000 | 0.081 | 0.017 | 933.622 | 1000.00 | 0.000 | 0.000 | 0.087 | 0.017 | 842.267 | 700.000 | 0.000 | 0.000 | 0.085 | 0.022 | 594.838 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.000 | 0.000 | 0.001 | 2.134 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.353 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.095 | 0.000 | 0.000 | |
| | | | AS ₂ | mean | 0.000 | 0.036 | 0.013 | 697.191 | 1000.00 | 0.000 | 0.000 | 0.026 | 0.012 | 494.844 | 700.000 | 0.000 | 0.000 | 0.013 | 0.018 | 214.962 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.000 | 0.021 | 0.003 | 3.281 | 0.000 | 0.000 | 0.000 | 0.023 | 0.005 | 3.809 | 0.000 | 0.000 | 0.000 | 0.016 | 0.005 | 3.626 | 0.000 | 0.000 | |
| | | | AS ₃ | mean | 0.000 | 0.090 | 0.020 | 709.865 | 1000.00 | 0.000 | 0.000 | 0.060 | 0.019 | 503.267 | 700.000 | 0.000 | 0.000 | 0.034 | 0.028 | 219.521 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.000 | 0.051 | 0.004 | 6.178 | 0.000 | 0.000 | 0.000 | 0.038 | 0.007 | 5.083 | 0.000 | 0.000 | 0.000 | 0.031 | 0.011 | 6.124 | 0.000 | 0.000 | |
| | | | AS ₄ | mean | 0.001 | 0.130 | 0.024 | 721.407 | 1000.00 | 0.000 | 0.001 | 0.108 | 0.029 | 516.427 | 700.000 | 0.000 | 0.001 | 0.061 | 0.038 | 225.219 | 300.000 | 0.000 | 0.000 |
| | | | | std | 0.003 | 0.081 | 0.006 | 10.219 | 0.000 | 0.000 | 0.001 | 0.088 | 0.012 | 13.785 | 0.000 | 0.000 | 0.002 | 0.058 | 0.019 | 10.527 | 0.000 | 0.000 | |

3

1 To show the findings of this study, the numerical results clustered by the performance indicators
 2 are shown in Figures 6a to 8. For each kind of assembly line, the performance of fifteen cases is
 3 shown. The demand rates are 1, 0.7 and 0.3 for cases 1 to 5, cases 6 to 10 and cases 11 to 15,
 4 respectively.

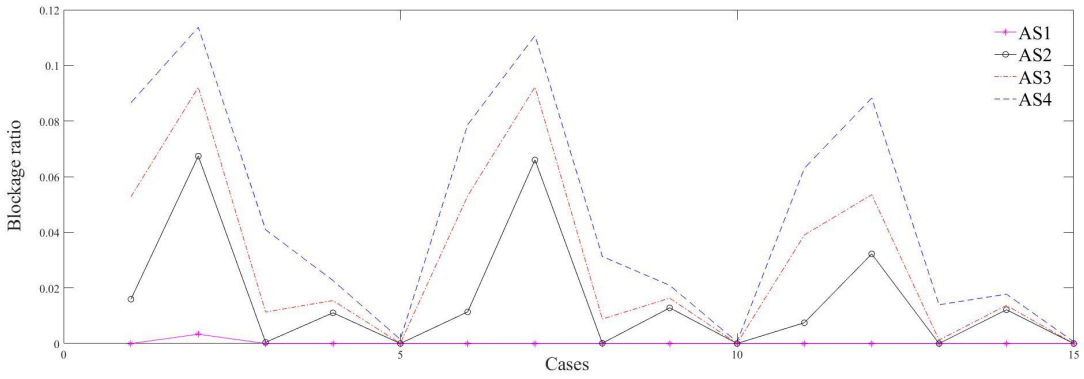
5
 6 Figures 6a to 6c shows the average starvation ratio, blockage ratio and idle ratio (the sum of
 7 starvation ratio and blockage ratio). As these three figures (6a-6c) show, the assembly line with
 8 the proposed fuzzy system has significantly less blockage, less starvation and a higher level of
 9 machine utilization, and there is almost no blockage for all the cases. When machine breakdown
 10 is recognized more slowly, there is more idle time for an assembly line. Additionally, the idle
 11 time for AS₁ is the least, which indicates that the idle time is reduced further when actions are
 12 taken in time to deal with disruptions. Thus, there is less blockage, less starvation and a higher
 13 level of machine utilization when the level of information transparency is higher.

14



15

16 **Figure 6a.** Average starvation ratio for the four assembly lines



17

18 **Figure 6b.** Average blockage ratio for the four assembly lines

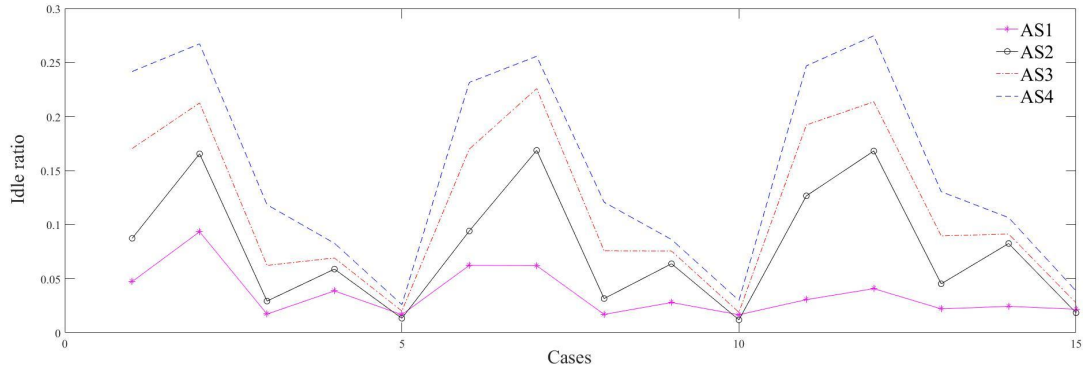


Figure 6c. Average idle ratio for the four assembly lines

Figure 7 shows the results related to the buffer level. For AS₁, except for the first two cases, the buffer levels are about 0.1. In general, the buffer level of AS₁ is significantly lower than that of the other three assembly lines, and stays at a stable level. Not surprisingly, the buffer levels of AS₂, AS₃ and AS₄ rank the second, third and fourth, which indicates that the buffer level decreases significantly with the increase of information transparency level. Therefore, timely recognition of the disruptions and in-time adjustment of the assembly line are helpful to keep the WIP at a low level.

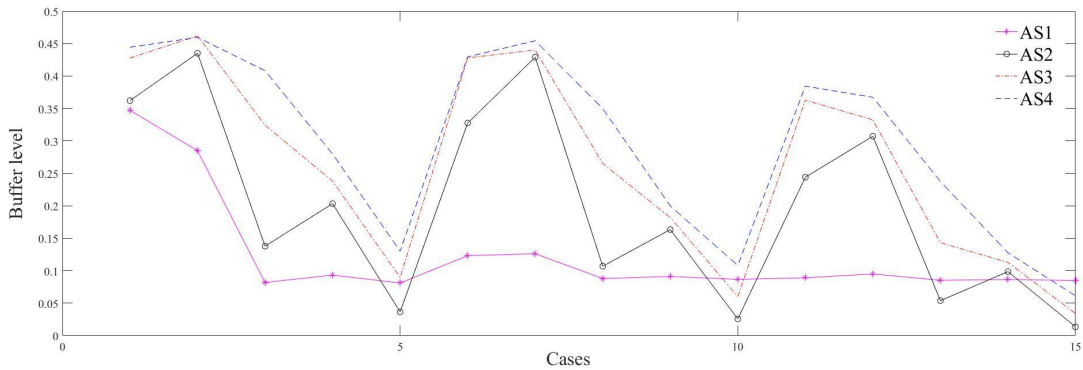


Figure 7. Average buffer levels for the four assembly lines

Figure 8 shows the total production information for the four assembly lines. For cases 1 to 5, the demand quantity is 1000 units, and there is a large backlog for AS₃ and AS₄. For cases 6 to 10, the demand quantity is 700 units, and there is a large backlog for only AS₄. For cases 11 to 15, production of the four assembly lines satisfies the demand (300 units). AS₃ and AS₄ show worse production ability, which suggests that the information transparency positively affects the production ability of an assembly line. When disruptions are recognized and dealt with in time, production losses caused by disruptions can be reduced.

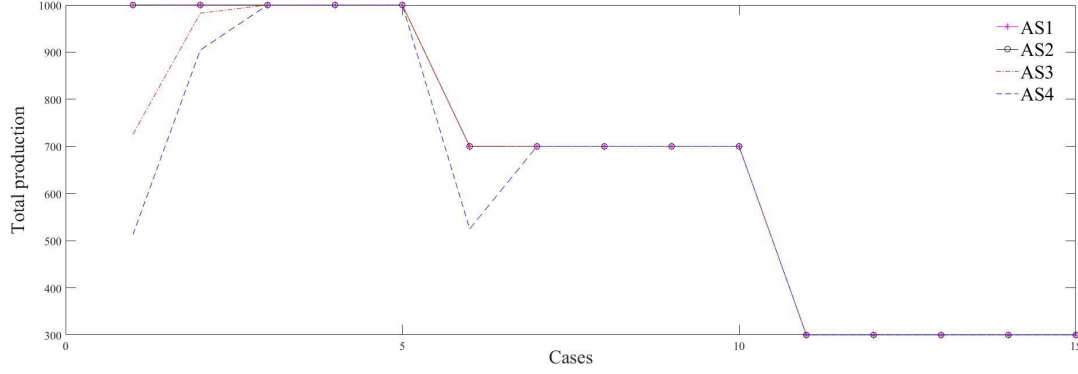


Figure 8. Average total production for the four assembly lines

Thus, the higher the information transparency level is, the better the performance of an assembly line becomes. For an assembly line with the proposed fuzzy system, real-time information can be analyzed, and in-time adjustments are undertaken accordingly. The performance is better due to the right decisions made by the proposed fuzzy system.

It can be seen from Tables 5a and 5b that assembly line re-balancing is conducted only for one case ($\lambda = 0.01$, $\mu = 0.1$, $d_0 = 1$). For ten runs in that case, assembly line re-balancing takes place in two runs. In order to explore the impact of the preparation time of each task when it is reassigned to another workstation, the preparation time is increased to 0.10 from 0.01, and the numerical results are shown in Table 6. This change does not affect the results of those cases without assembly line re-balancing, thus, only the results for the two special cases are discussed further. For AS₁ without FC₁, the production rates of the workstations are adjusted in time, but whether assembly line re-balancing is necessary is not examined.

Table 6

Numerical results of the two random cases where re-balancing are taken place

| No. | random cases | Avg. b_r | Avg. BL | Avg. st_r | t | P | no_r |
|-----|--|----------|---------|-----------|----------|------|------|
| 1 | AS ₁ | 0.000 | 0.314 | 0.074 | 999.620 | 997 | 2 |
| | AS ₁ (with increased T_r) | 0.000 | 0.315 | 0.072 | 997.530 | 994 | 1 |
| | AS ₁ (without FC ₁) | 0.000 | 0.326 | 0.067 | 1000.000 | 986 | 0 |
| | AS ₂ | 0.105 | 0.482 | 0.060 | 902.590 | 1000 | |
| | AS ₃ | 0.124 | 0.517 | 0.074 | 979.800 | 1000 | |
| | AS ₄ | 0.131 | 0.561 | 0.085 | 1000.000 | 982 | |
| 2 | AS ₁ | 0.033 | 0.294 | 0.094 | 996.870 | 1000 | 1 |
| | AS ₁ (with increased T_r) | 0.033 | 0.294 | 0.094 | 996.870 | 1000 | 1 |
| | AS ₁ (without FC ₁) | 0.000 | 0.260 | 0.127 | 1000.000 | 963 | 0 |
| | AS ₂ | 0.077 | 0.379 | 0.145 | 969.670 | 1000 | |
| | AS ₃ | 0.093 | 0.402 | 0.170 | 1000.000 | 945 | |
| | AS ₄ | 0.106 | 0.390 | 0.235 | 1000.000 | 799 | |

1 As seen in Table 6, when the preparation time for each task is increased to 0.10 from 0.01, there
2 are no significant changes in the performance of AS₁. For the first special case, the total
3 production is 986 units when there are production rate adjustments but no assembly line
4 re-balancing, and the production increases to 997 units when both production rate adjustments
5 and re-balancing are allowed. There is a relatively large difference between the total production
6 of AS₄ and the demand quantity. Although the production for AS₂ and AS₃ can satisfy the
7 demand within the simulation time, the buffer levels are 153.503% and 164.650% of the buffer
8 level of AS₁, and the utilization of the machines for AS₂ and AS₃ are also significantly smaller
9 than for AS₁. Similar rules are found for the second special case.

11 **6. Conclusions**

12 Disruptions break the initial balance of an assembly line, and negatively affect the collaboration
13 between workstations and lead to worsening performance. In this study, the assembly process is
14 discussed in a dynamic environment, where there are task time reductions due to the learning
15 effect, maintenance due to machine failures, starvation and blockage. A fuzzy control system is
16 developed to deal with the unpredictable disruptions. Based on the results of the fuzzy control
17 system proposed in this study, an assembly line is re-balanced with tasks re-assigned to the
18 available workstations so as to decrease the adverse impact of failed workstations on the whole
19 assembly line. Meanwhile, since starvation and blockage can propagate throughout the assembly
20 line, the production rate of each workstation is monitored and controlled by a fuzzy controller.
21 Consequently, the production rate of each workstation tends to be maximum when there is no
22 risk of blockage or starvation, and is adjusted when it is necessary.

23
24 To examine the effectiveness of the proposed fuzzy control system, the performance of four
25 kinds of assembly lines (AS₁, AS₂, AS₃ and AS₄) are compared. We can see from the numerical
26 results that with the increase of information transparency level, the performance of an assembly
27 line is better. Not surprisingly, AS₁ performs much better in terms of blockage ratio, starvation
28 ratio and the buffer level, with the satisfaction of demand considered. Thus, information
29 transparency positively affects the performance of an assembly line, and Industry 4.0 will lead us
30 to a more intelligent and efficient era. Practitioners should devote more effort to the adoption and
31 application of new advanced technologies to improve the information transparency level and the
32 intelligence level of the assembly process.

33
34 There are some limitations in this study. Although a promising fuzzy control system is used to
35 deal with the disruptions of an assembly line, only a straight assembly line is considered. The
36 more complex assembly lines will be discussed in the next stage. Besides, it is assumed that the
37 production rates of the workstations do not change without adjustment. However, the production
38 rate of one workstation will not remain constant even without adjustment, since the health state
39 of machines will not be always the same. This will be considered in future research.

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