

1 **Severe plastic deformation-produced gradient nanostructured copper with a**
2 **strengthening-softening transition**

3 Bo Wu^{a1}, Hui Fu^{a1}, Xiaoye Zhou^{c1}, Lei Qian^a, Jiasi Luo^a, Jiaming Zhu^d, Wing Bun Lee^a, and
4 Xu-Sheng Yang^{a,b*}

5 *^aState Key Laboratory of Ultra-precision Machining Technology, Department of Industrial*
6 *and Systems Engineering, The Hong Kong Polytechnic University, Hung Hom, Kowloon,*
7 *Hong Kong, China (E-mail: xsyang@polyu.edu.hk)*

8
9 *^bHong Kong Polytechnic University Shenzhen Research Institute, Shenzhen, China*

10
11 *^cGuangdong Province Key Laboratory of Durability for Marine Civil Engineering, School of*
12 *Civil Engineering, Shenzhen University, Shenzhen, Guangdong 518060, PR China*

13
14 *^dSchool of Civil Engineering, Shandong University, Jinan 250061, China*

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¹ These authors contributed equally to this work.

* Corresponding author. xsyang@polyu.edu.hk (X.-S Yang). Tel: +852-2766 6604

1 **Abstract**

2 Low-excess energy twin boundary can effectively stabilize the conventional grain
3 boundary. It has been reported that deformation-activated nanotwins in nanograined metals
4 produced by severe plastic deformation techniques can significantly enhance mechanical-
5 thermal stability. However, fabrication, structural evolution and the effect of grain size and twin
6 thickness on the mechanical stability of nanograined-nanotwinned metals, where both the grain
7 size and twin thickness reach the nanometer scale (especially grain size is lower than 40 nm),
8 remain unclear. In this study, a gradient nanostructured layer containing a nanograined-
9 nanotwinned sub-layer region and an extremely refined twin-free nanograined top surface layer
10 with grain size as small as ~ 10 nm is achieved on copper by using an ultrahigh-strain rate
11 single point diamond turning technique. High-resolution transmission electron microscope
12 observations, atomistic molecular dynamic simulations, and nanoindentation tests were
13 performed to reveal the size-dependent mechanisms of grain refinement and hardness along
14 the gradient direction. The propensity of deformation multifold twinning is increased firstly in
15 large-size nanograins and then decreased once grain size is below ~ 48 nm, finally replaced by
16 detwinning to form extremely fine twin-free nanograins at the topmost surface layer. In other
17 words, both the zero-macrostrain-induced deformation multifold twinning and symmetry-
18 breaking-based detwinning processes can continuously refine nanograins along the gradient
19 direction. Critical grain sizes for deformation multifold twinning and detwinning are discussed.
20 Interestingly, a Hall-Petch strengthening-softening transition is discovered at a critical grain
21 size of ~ 30 nm in the gradient nanostructured layer. The softening mechanisms are elucidated
22 to be attributed to the twin thickness effect on deformation mode in nanograined-nanotwinned
23 structures and the pure grain boundary-mediated plasticity in extremely fine twin-free
24 nanograins. A series of critical twin thicknesses for softening in nanograins with different grain
25 sizes are discussed; that is, the smaller the grain size is, the smaller the critical twin thickness
26 will be. This study offers the potential for understanding and developing stable nanostructured
27 metals.

28 **Keywords:** Nanograined-nanotwinned Cu; ultra-precision machining technique; multifold
29 twinning; strengthening-softening transition; high-resolution transition electron microscopy.

1 **1 Introduction**

2 “Smaller is stronger” is generally recognized following the empirical Hall-Petch effect.
3 [1, 2]. Unfortunately, “smaller grain size, less stable” has also been proved in homogeneous
4 nanograined (NG) metals by experiments and simulations [3]. On one hand, multiplication and
5 motion of dislocations are severely inhibited in NG metals via significantly reduced grain size
6 and increased density of grain boundaries (GBs), resulting in high strength but poor tensile
7 ductility [4, 5]. On the other hand, grain coarsening and softening can be triggered in NG metals
8 by mechanical and thermal stimulus, especially when the grain sizes are below certain critical
9 values [6, 7]. This inherent instability of NG metals originates from the conventional GBs with
10 high mobility. Interestingly, numerous investigations have indicated that the special twin
11 boundary (TB) with obviously lower excess energy (usually smaller by an order of magnitude
12 than the conventional GB) can effectively act as a thermally-mechanically stable interface for
13 strengthening metals. For example, heterogeneous nanotwinned (NT) metals have shown the
14 strengthening effects with comparable tensile uniform elongation [8-11]. In addition, ultra-
15 hardness/strength and superior thermal stability have also been surprisingly discovered in
16 nanograined-nanotwinned (NNT) materials, such as cubic boron nitride [12], diamond [13], Ni
17 [14], and Ag-Cu alloy [15], etc., in which NGs (ranging from several to tens nanometers)
18 contain thinner NTs. The relaxation of the GBs into lower-energy states by NTs has been
19 proposed to increase the stability of NG metals under mechanical and/or thermally activations
20 [6].

21 Similar to that in twin-free NG metals, a strengthening-softening transition has also been
22 reported in NT metals once the twin thickness (λ) decreases below a critical value. For example,
23 Lu et al. [16] reported the critical twin thickness is $\lambda = 15$ nm in ultrafine-grained (UFG) Cu
24 containing NTs, contributing to a maximum strength and then a strengthening-softening
25 transition if λ is reduced. A series of critical twin thickness ($\lambda = 12-37$ nm) was also
26 experimentally observed in UFG Cu (400-600 nm) [17]. More recently, experiments,
27 simulations, and theories have been consistently to show that the critical twin thickness for the
28 softening initiation depends on the grain size of metals; that is, the smaller the grain size d is,
29 the smaller the critical twin thickness λ will be [15, 18, 19]. It implies that, in other words, the

1 strengthening-softening transition would also happen in NNT metals. For instance, Ke et al.
2 [15] successfully fabricated a series of NNT Cu-Ag specimens, observing the corresponding
3 softening transition at critical twin thicknesses $\lambda = 3.6\text{-}5.2$ nm for the grain sizes $d = 49\text{-}55$ nm.
4 Wang et al [18] reported statistically the critical values of λ and detailed deformation mode
5 transition in NNT platinum (Pt) with various d and λ by in situ atomic-scale observations. In
6 addition, atomistic molecular dynamics (MD) and theoretically modelling are also known to
7 reveal the critical twin thicknesses and corresponding plastic deformation mechanisms for
8 strengthening-softening transition behavior in NNT Cu [19]. To name a few, Zhu et al. [20] the
9 large-scale MD simulations and quantitative continuum mechanism-based plasticity model to
10 investigate the coupled effects of grain size and twin thickness on the strength and ductility of
11 NT metals, predicting a critical twin thickness λ for the maximum strength is 13 nm when the
12 grain size is 500 nm in NT Cu. Based on the twin thickness-dependent plasticity model, Wei
13 [21] found that the critical twin thickness is proportional to square root of grain size for
14 achieving the corresponding maximum strength. These twin-dependence on grain size
15 activities may rise a question/challenge in NNT metals; that is, how to tailor the NTs (e.g.
16 distribution and size) to persistently stabilize the GBs, especially for the multi-scale NGs (from
17 several tens of nanometers to tens of nanometers).

18 Heterogeneous gradient nanostructured (GNS) metals (e.g. gradient phase, composition,
19 and grain size) have been widely fabricated by various surface severe plastic deformation
20 (SSPD) techniques. This type of structure can have the high strength-ductility by combining
21 the strain/stress partitioning between the multi-scale domains along the gradient direction [22-
22 24]. Noticeably, deformation twinning might be easily activated in low/medium-stacking fault
23 energy (SFE) metals during the SSPD process. In this regard, the SSPD technique might be
24 developed to achieve the stable gradient NNT structure (i.e., the twin thickness gradually
25 reduces with decreasing grain size) by tailoring the morphologies of grain size and twin
26 thickness simultaneously. For example, NNT structural regions were reported in GNS Ag, Cu,
27 Ni and steel produced by SSPD techniques [6, 7, 25]. It was verified that the deformation NTs
28 can stabilize the GBs by diminishing the mechanical loading-driven GB migration in the top
29 surface region with the grain size between 40-75 nm in GNS Cu specimen, while the range of

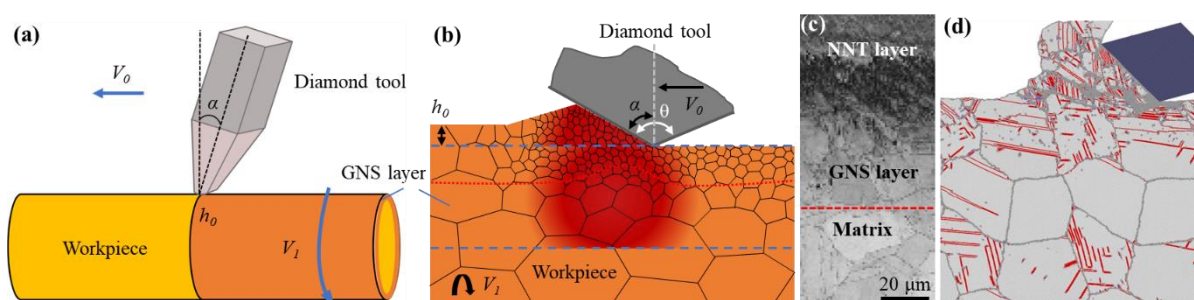
1 twin thickness was not considered [6]. However, it has been a challenge to experimentally
2 verify the stability of TB-GB activities in smaller NGs due to the technological difficulty of
3 synthesizing NNT materials. To date, the stability of TB activities of NG materials with $d \approx 10$ -
4 20 nm was only be garnered by MD simulations [19]. More recently, Li et al [26] developed a
5 two-step severe plastic deformation (SPD) process, i.e. SMGT and subsequent high-pressure
6 torsion (HPT) in liquid nitrogen, obtained the extremely refined NGs that contained three-
7 dimensional (3D) minimal-interface structures stabilized with TB networks. This special
8 interfacial structure can effectively restrain the grain growth even near the melting point and
9 exhibit an ultra-hardness close to the theoretical value. To the best of our knowledge, however,
10 it is still quite limited literature to interrogate the structural evolution and stability of the
11 extremely refined NGs in GNS metals produced by the single SSPD technique, especially the
12 top surface region with the grain size $d < 40$ nm. This might be due to the technological
13 difficulty in synthesizing by SSPD techniques, as the mechanical driven-grain coarsening and
14 deformation detwinning would happen easily in NGs with too small grain sizes [23].

15 Increasing strain rate in the SPD process has been suggested to promote the dislocation
16 multiplication and suppress the dislocation annihilation kinetics, thus effectively facilitating
17 the grain refinement by forming more GBs or dislocation boundaries [27]. In this study, the
18 single point diamond turning (SPDT), a high-speed ultraprecision surface machining method
19 is developed to produce GNS Cu model material for achieving the extremely refined surface
20 region. Cu is a medium SFE metal (~ 45 mJ/m²) and known to form copious deformation NTs
21 during the SPD process [28]. The ultra-precision SPDT technique in this work can achieve
22 ultrahigh strain rate (up to 10^6 s⁻¹) with large strain (typically 2-10) on the workpiece, thus
23 denoting many advantages, e.g. high efficiency and controllability, cost-effectiveness, and
24 excellent surface quality [29]. Accordingly, the GNS Cu possessing both gradient NNT sub-
25 layer region and extremely refined NG with grain size of ~ 10 nm at topmost surface layer is
26 successfully prepared by the SPDT technique. Grain refinement process and related grain size-
27 dependent plastic mechanisms of the SPDT-induced GNS layer, especially the NNT layer has
28 been atomically explored by means of high-resolution transmission electron microscopy
29 (HRTEM) observations and MD simulations. Noticeably, we confirm the twinning and

1 detwinning of multifold NTs play a key role in the grain refinement process in NGs. Moreover,
 2 when the grain size is below 30 nm, a softening transition was observed. This softening
 3 mechanism is attributed to detwinning and twinning softening caused by the reduced grain size
 4 and twin thickness. Our results shed light on origin of softening transition in the fine NGs,
 5 which is critical to the development of mechanical stable nanostructured alloys.

6 2 Experiments and simulations

7 2.1 GNS layer fabricated by SPDT



9
 10 Fig. 1 (a) Schematic of SPDT technique. (b) Surface profile compression during the SPDT process. V_1 , V_0 , h_0
 11 and α are the rotation velocity of the sample, the moving velocity of the diamond tool, the turning depth and
 12 the rake angle, respectively. (c) The cross-sectional SEM image of the SPDT Cu showing the formation of
 13 GNS layer. (d) MD simulation of SPDT process consistently showing the generation of GNS layer (atoms
 14 are colored by common neighbor analysis).

15 Commercial pure Cu (99.97 wt.%) rods consisting of well-annealed equiaxed coarse grains
 16 (CGs) ($\sim 23 \mu\text{m}$) were first machined into cylindrical samples with length of 15 mm and
 17 diameter of 10 mm. The cylindrical workpieces were then subjected to SPDT treatment, as
 18 schematically shown in Fig. 1(a). As shown in Fig. 1(b), this high-speed machining process
 19 compress the deformation surface and thus result in gradient refinement, the detailed process
 20 described in Ref [30]. The high-speed SPDT parameters are listed as follows: cutting speed V_1
 21 of 500 rpm, turning depth h_0 of $30 \mu\text{m}$, rake angle α of 30° and feed rate V_0 of 5 mm/min, and
 22 the cooling media is paraffin lubricant. The SPDT process was repeated 20 passes to
 23 accumulate the SSPD effect for achieving a thick and uniform GNS layer.

24 2.2 Molecular dynamics simulations

25 In addition to the experiments, the MD simulations (Fig. 1(d)) by the LAMMPS software

1 was assisted to understand of the formation of GNS Cu layer during the SPDT process. In
2 particular, atomic microstructure evolution, especially the deformation twinning or/and
3 detwinning mechanisms, will be dissected at the atomic level. The embedded-atom method
4 (EAM) [31] was used to describe the interaction potential between Cu atoms. The simulated
5 cell was built to have an average grain size of 24 nm and 10 nm in-plane and out-of-plane,
6 respectively. After that, the model was first annealed to 700 K for 1 ns and then cooled down
7 to 300 K in 0.3 ns, achieving the equilibrium status. A rigid body diamond quadrangular was
8 modeled as the cutting tool. The cutting depth, cutting speed, cutting cycle and rake angle are
9 10 nm, 500 m/s and 30° and 10 cycles in this model.

10 **2.3 Microstructure and mechanical properties characterizations**

11 The longitudinal sections of the SPDT Cu samples were observed by scanning electron
12 microscopy (SEM, TESCAM MIRA3). Electron backscatter imaging under SEM was used to
13 investigate the microstructure of the GNS layer. The SEM specimens were prepared via both
14 mechanical polishing and vibration polishing. The plane-view TEM observations were
15 performed using the field emission JEM-2100F at 200 kV. The TEM samples were taken at
16 different depth of the GNS layer by mechanically polishing. Then, mechanically polish was
17 continued from the side away from the observation layer, obtaining the ~25 μm-thick TEM
18 slices. Then, the TEM slices were further thinned on the Gatan 691 precision ion polishing
19 system through the single-side ion milling mode.

20 The nanoindentation tests along the depth direction of the SPDT samples were conducted
21 on a Hysitron TI-900 Triboindenter. The max load and holding time are 8 mN and 5 s,
22 respectively. The loading rate and unloaded rate is the same, 0.4 mN/s. The nanoindentation
23 test was repeated 10 times at each sample.

24 **3 Results**

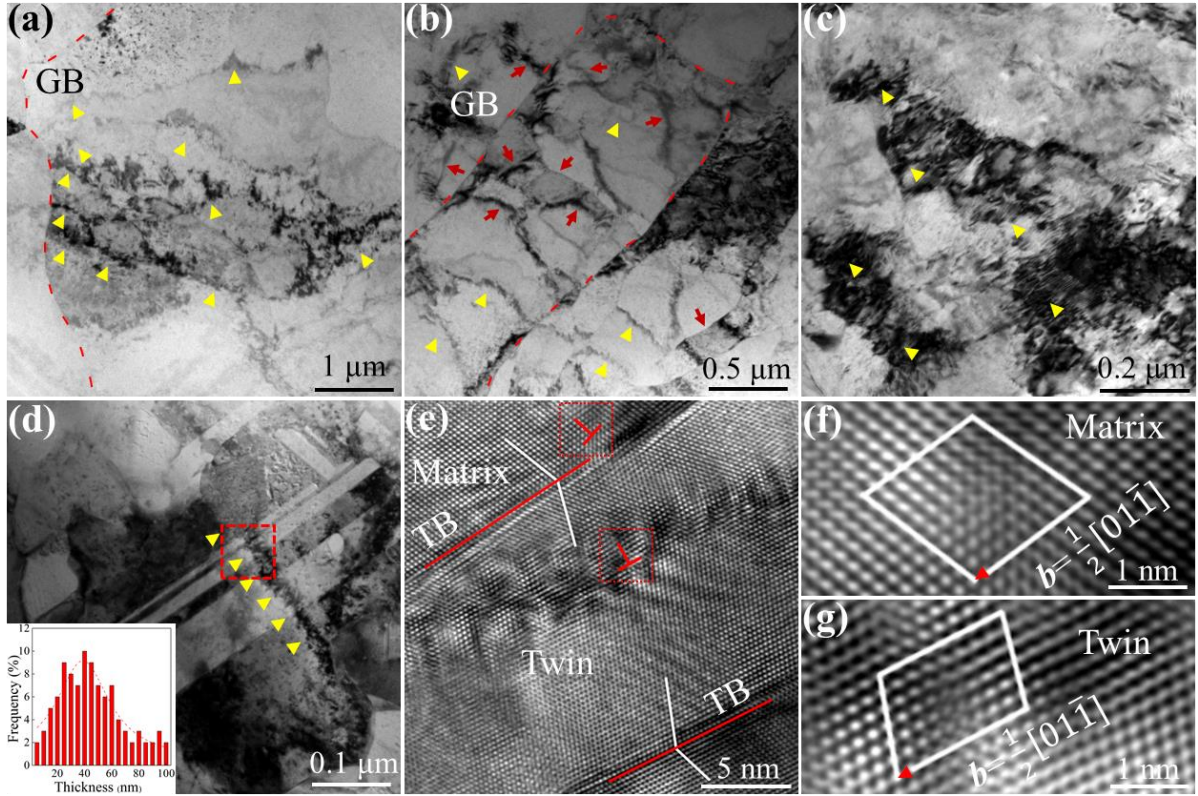
25 **3.1 Grain refinement in GNS layer during the SPDT process**

26 The cross-sectional image of the SPDT Cu sample characterized by SEM is shown in Fig.
27 1(c). It shows that a GNS surface layer with a depth of ~80 μm is successfully prepared. Due
28 to the intensive plastic deformation and refined NGs near the top surface layer, GBs are difficult

1 to identify in this region compared with that of the matrix region. Therefore, detailed HRTEM
2 characterizations at various depth layers along the gradient direction has been carried out to
3 uncover the underlying grain refinement mechanism in GNS layer, where two characteristic
4 regions are defined according to the grain size range. The first one is the deformed sub-layer
5 region deeper than $\sim 20 \mu\text{m}$, where the grain size ranges from tens of microns to hundreds of
6 nanometers, and grain refinement is primarily achieved via full dislocation activities. The
7 second one is the NNT region between $\sim 20 \mu\text{m}$ depth and topmost surface layer, where the
8 grain sizes refine from $\sim 100 \text{ nm}$ to $\sim 10 \text{ nm}$. Detailed microstructural evolution for the grain
9 refinement processes in these two regions are described as follows.

10 **3.1.1 Grain refinement in the deformed sub-surface region**

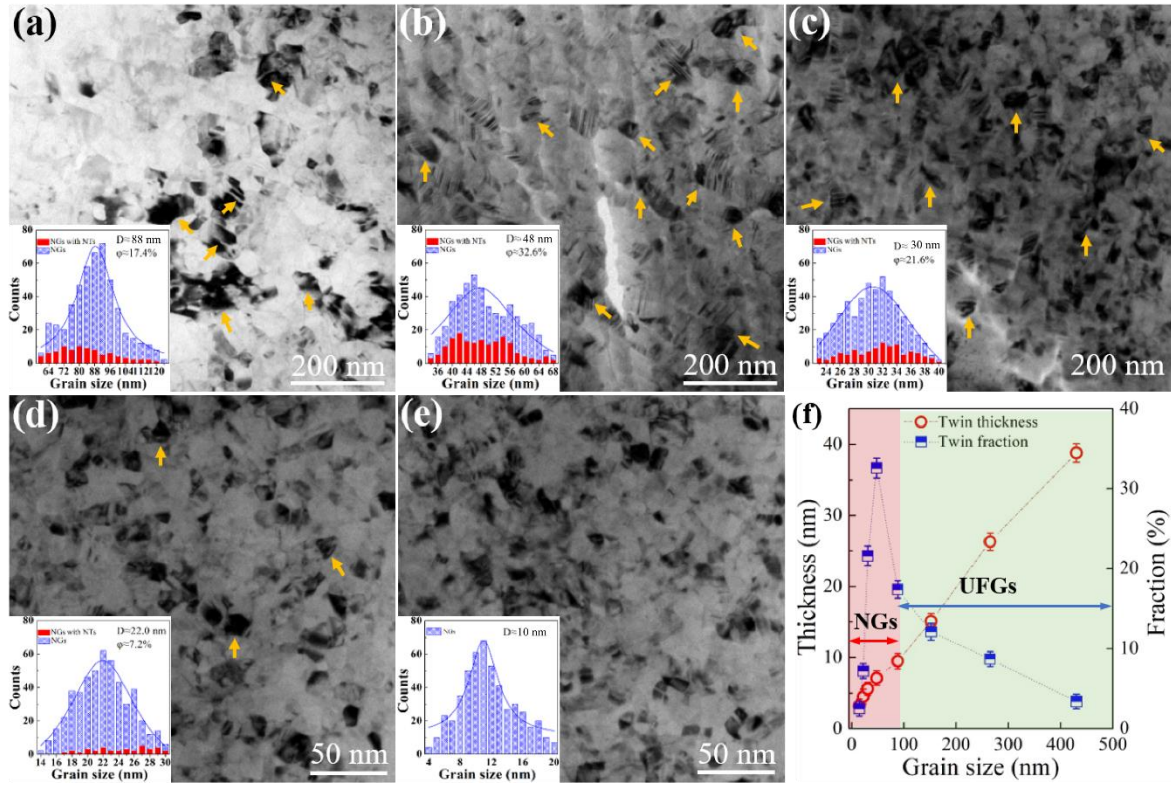
11 Fig. 2(a-d) presents a series of TEM bright-field (BF) images taken from deformed sub-
12 surface layer region deeper than $\sim 20 \mu\text{m}$. Fig. 2(a) is the BF TEM image in the region $\sim 60 \mu\text{m}$
13 depth, near the strain-free matrix, which the grain size is smaller than $\sim 10 \mu\text{m}$. High-density
14 dislocations (labelled as yellow triangles) are generated by plastic deformation as shown in Fig.
15 2(a). When the depth reaches $\sim 40 \mu\text{m}$, the grain size is refined to several micrometers, as
16 shown in Fig. 2(b), in which lamellar structures/sub-grains (labelled as red arrows) are formed
17 to contain large dislocation clusters, dislocation walls and dislocation cells. Furthermore, a
18 typical microstructure of the $25 \mu\text{m}$ -depth region is presented in Fig. 2(c). The equiaxed UFGs
19 with grain size down to several hundreds of nanometers are formed, and dislocation clusters
20 can be found in the interior of these UFGs. Noticeably, deformation twins with average λ about
21 tens of nanometers are started to be found in some UFGs in this depth layer, as shown in Fig.
22 2(d) and corresponding inset. Fig. 2(d)-(e) also show that numerous inclined perfect
23 dislocations are accumulated to cut through TBs, as evidenced by Fourier filtered images in
24 Fig. 2(f-g). Dislocations piled up at $\Sigma 3\{111\}$ TBs may result in the formation of large-angle
25 GBs by gradually losing the coherency, thus leading to the further refinement of NTs into NGs.
26 This refinement mechanism has been verified in SPD Cu [32].



1
2 Fig. 2 Detailed microstructural evolution of the deformed sub-surface region deeper than ~20 μm . Typical
3 BF TEM images showing the microstructures at different depths: (a) ~60 μm , (b) ~40 μm , (c) ~25 μm . (d)
4 TEM image showing the deformation twins in the region of ~25 μm depth, where the inset gives the twin
5 thickness distribution. (e) HRTEM image of T/M lamellar taken from the region outlined in (d). (e-f)
6 Corresponding Fourier-filtered images of perfect dislocations in matrix and twin, respectively.

7 3.1.2 Grain refinement in the gradient NNT region

8 TEM images for the detailed microstructures across the depth span of 0-20 μm in the GNS
9 layer are given in Fig. 3(a-e), showing the equiaxed NGs with random crystallographic
10 orientations and gradient grain size. It is noted that dense deformation NTs including multifold
11 NTs (marked by yellow arrows) are found to embed in these NGs, thereby forming a gradient
12 NNT structural region. Different from the NTs in UFGs, the λ values of NTs in these NNT
13 grains are significantly thinner (below 10 nm) and keeps dropping with decreasing d . However,
14 the twin fraction (ϕ) is increased first and then decreased with decreasing d as shown in Fig.
15 3(f). For example, the value of ϕ is ~17.4% at depth of ~20 μm ($d \approx 88$ nm), which is increased
16 to the peak about 32.6% at depth of ~15 μm ($d \approx 47.6$ nm), and subsequently decreased to be
17 only ~2.5% at depth of ~10 μm ($d \approx 10.5$ nm). Lastly, NTs are hardly observed in the topmost
18 surface ($d \approx 10$ nm), as shown in Fig. 3(e).



1
2 Fig. 3 Detailed microstructural evolution of the gradient NNT region across the depth span of 0-20 μm .
3 Typical TEM images at different depth layers: (a) $\sim 20 \mu\text{m}$ depth. (b) $\sim 15 \mu\text{m}$ depth. (c) $\sim 10 \mu\text{m}$ depth. (d)
4 $\sim 5 \mu\text{m}$ depth. (e) Topmost surface. Insets are the size statistics of the NGs and the corresponding fraction of
5 NGs contained deformation NTs. (f) Statistical diagram of twin thickness and twin fraction dependence on
6 grain size in GNS Cu.

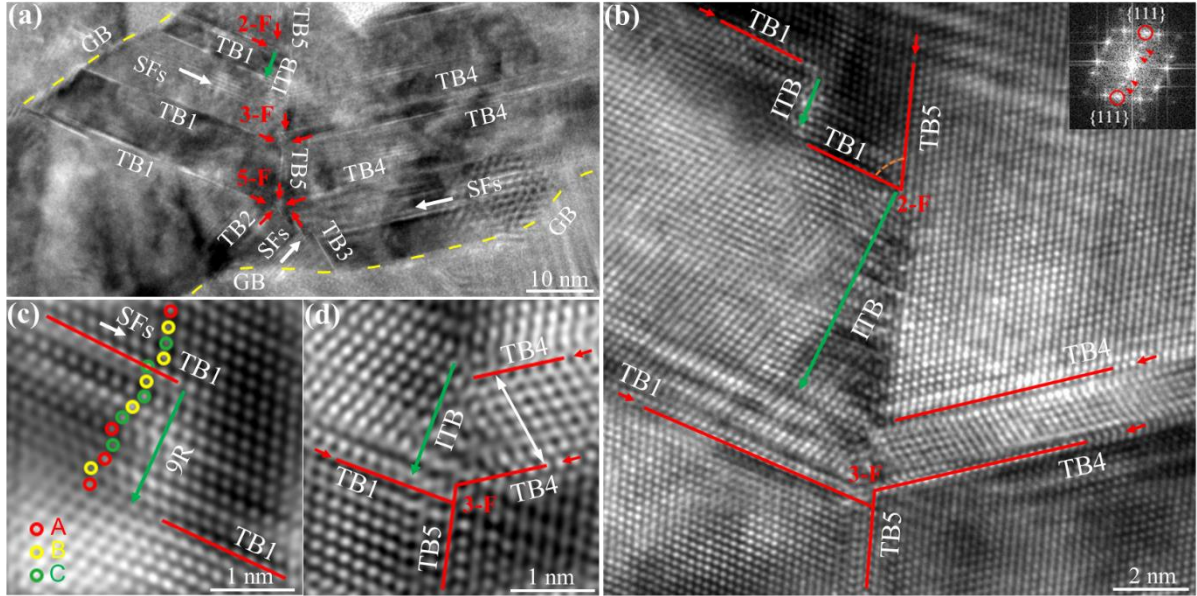
7 The above microstructural evolution observations evidence that a gradient NNT region
8 with extremely refined NGs ($d \approx 10 \text{ nm}$) in the topmost surface has been successfully achieved
9 in GNS Cu by the SPDT technique. It is no doubt that deformation twinning can effectively
10 refine the UFGs into the NGs. However, it is noted that the deformation twinning becomes
11 more difficult when the grain size refines too small. Therefore, one may ask why NGs can be
12 continuously refined with the decrease of the fraction of deformation NTs. It may be related to
13 the existence of deformation multifold NTs [33, 34]. In contrast to the conventional NT metals
14 with parallel TBs, multifold NTs in NGs contain the intersectant TBs, which is similar with the
15 hierarchical NTs [35, 36]. Relative to the parallel NTs, on one hand, multifold and hierarchical
16 NTs with different orientations are more effective in refining the grain, due to the enhanced
17 TB-dislocation interactions [35, 36]. On the other hand, excess dislocations pile up in TBs
18 would lead to the symmetry-forming and -breaking processes of multifold NTs, which play a
19 crucial role in the further grain refinement process of NGs [37, 38]. The formation mechanisms

1 and corresponding grain refinement function of multifold NTs will be dissected by the HRTEM
2 observations and MD simulations.

3 **3.2 HRTEM characterization for deformation multifold NTs in NGs**

4 HRTEM observations were conducted to atomic-level characterize the deformation
5 multifold NTs in NGs with different grain sizes in NNT region. Fig. 4 is the typical HRTEM
6 image of NG ($d \approx 80$ nm) which contained various kinds of deformation multifold NTs
7 (including 2-F, 3-F, and 5-F NTs). It is noted that the parallel NTs and crossed multifold NTs
8 are coexisted in NG. These deformation NTs prefer to nucleate and grow via Shockley partial
9 dislocations emission from GBs. As marked by white arrows in Fig. 4(a), dense SFs are also
10 resulted from the emission of the Shockley partial dislocations from GBs. Fig. 4(b) presents
11 the enlarged image in upper region of the NG in Fig. 4(a). The NTs originated from the left
12 (TB1) and top (TB5) boundaries of the NG are intersected to form 2-F NT, while the 3-F NT
13 is formed by intersecting NTs from the left (TB1), right (TB4) and top (TB5) boundaries. In
14 addition to the SFs along the TBs, $\sum 3\{112\}$ incoherent TBs (ITBs) are found to link with
15 intersection nodes or incomplete multifold NTs, as indicated by green arrows in Fig. 4(b).
16 Specifically, $\sum 3\{112\}$ ITBs may have the 9R phase structures, as evidenced by the extra
17 diffraction spots with three times interplanar spacing of Cu $\{111\}$ from the fast Fourier
18 transform (FFT) patterns inserted in Fig. 4(b). The 9R phase structure with stacking order of
19 BCBCACABA is also well-indexed in Fourier-filtered atomic image for 2-F ITB region
20 enlarged in Fig. 4(c). Previous report has verified that deformation twinning in NG metals can
21 be accomplished by the migration of 9R $\sum 3\{112\}$ ITBs by cooperative passage of a
22 repeatable sequence $b_1:b_2:b_3$ Shockley partial dislocations on every (111) plane [39]. In contrast
23 to the common deformation twinning in CG and UFG regimes, this twinning mechanism in
24 NG regime yields zero-net macrostrain because the sum of their Burgers vectors equal zero. In
25 other words, the 9R structural $\sum 3\{112\}$ ITBs can also provide the nucleation sites to form
26 deformation multifold NTs in NGs, which is similar to the role of GBs in NGs [33]. The
27 Fourier-filtered image of 3-F NT shows twin pole migration in Fig. 4(d). For this 3-F NT, the

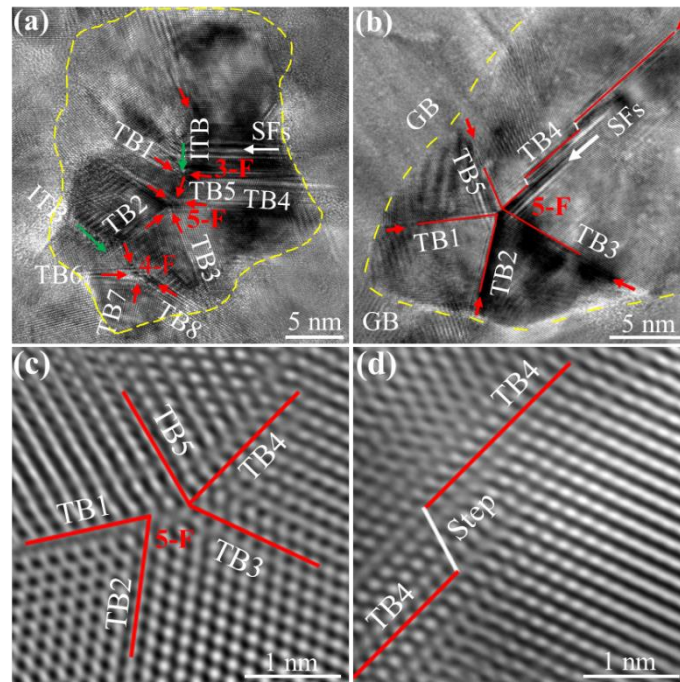
1 intersection acute angles between TB1 and TB5, TB5 and TB4 are 76.04° and 70.20° ,
 2 respectively. In addition, TB migration is observed in this 3-F NT, where TB4 migrates to form
 3 a seven atomic-layers twin lamella.



4
 5 Fig. 4 (a) HRTEM image of the deformation multifold NTs in NG with grain size of ~ 80 nm. Yellow dash
 6 line represents GB, while red, green and white arrows represent TB, ITB and SFs, respectively. Twofold,
 7 threefold, fourfold and fivefold NTs are abbreviated as 2-F, 3-F, 4-F and 5-F, respectively. (b) Enlarged image
 8 for 2-F and 3-F NTs in (a). (c-d) Corresponding Fourier-filtered atomic images of ITBs and 3-F NTs,
 9 respectively.

10 Fig. 5(a-b) give the HRTEM images about the deformation multifold NTs in two typical
 11 NGs with $d \approx 20$ nm in the NNT region. In comparison with that in the relatively larger NGs,
 12 there are also some ITBs formed at the intersection nodes by the parallel and crossed multifold
 13 NTs, as shown in Fig.5 (a). However, no 9R structural $\sum 3\{112\}$ ITBs are obviously observed
 14 to assist the deformation multifold NTs in the smaller NGs. This might be due to that the large
 15 area for forming the 9R structure cannot be provided sufficiently when decreasing the grain
 16 sizes of NGs. Alternatively, synergy-pole twinning mechanism would dominate the
 17 deformation multifold NTs process in the smaller NGs. Specifically, each TB would be formed
 18 by the random activation of partials (RAP) emitted from GBs, which has three Shockley
 19 partials with equal numbers and also yield a zero-net macrostrain [40]. It is evidenced by the
 20 smooth GB segments that intersect with the TBs (Fig. 5(a-b)). For example, complete 3-F, 4-F,
 21 and 5-F NTs in Fig. 5(a) should be formed by intersection of three, four and five single NTs,

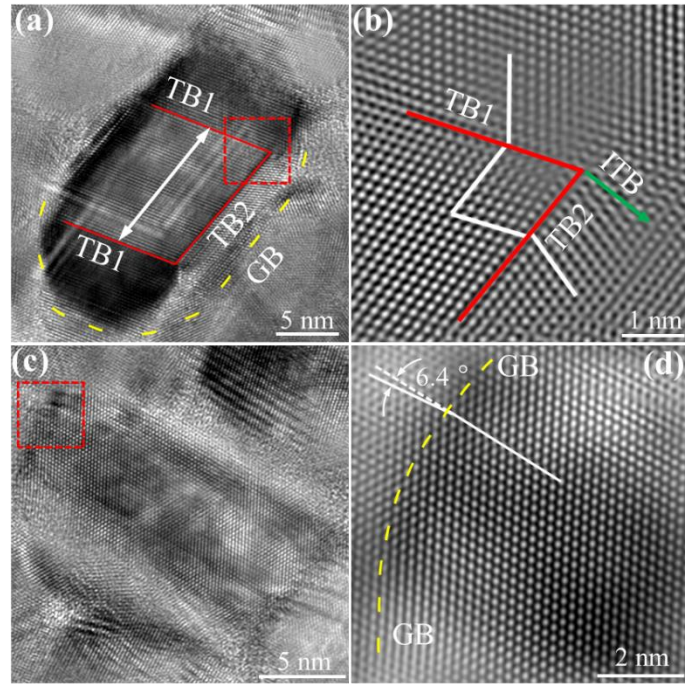
1 respectively, all of which would be formed by the RAP emitted from GBs. The transition
 2 between these two zero-macrostrain 9R and RAP deformation twinning mechanisms has also
 3 been reported in NG Cu with reduction in grain size in NNT region [41]. Noticeably, a twinning
 4 pole splitting and TB migration of TB4 are observed for 5-F NT in another smaller NG,
 5 resulting in the symmetry breaking of the deformation multifold NTs and releasing of
 6 intersectant CTBs self-locking state as shown in Fig. 5(c). In addition, there exist successive
 7 steps in the TB4 (Fig. 5(d)), where the four atomic-layer step leads to the migration and
 8 detwinning of TB4 towards GB. TB Combined with the statistical analysis in the decrease of
 9 NTs in Fig. 3, the twin pole splitting/migration (Fig. 5(c)), TB migration (Fig. 4(d))and steps
 10 (Fig. 5(d) would be incorporated to induce the detwinning process with the reduced grain sizes
 11 of NGs in NNT region [37].



12
 13 Fig. 5 (a-b) HRTEM images of the deformation multifold NTs in two typical NGs with grain sizes of ~ 20
 14 nm. Fourier-filtered atomic image of 5-F NTs (c) and step (d) enlarged from (b).

15 Fig. 6(a) presents the typical TEM image of the NG with $d \approx 16$ nm. Only twofold NT
 16 (marked as TB1 and TB2) is found in this grain. Crossed twin interfaces with an angle of $\sim 109^\circ$
 17 between TB1 and TB2 are shown in Fig. 6(b). The node of this twofold NT lies on the GB and
 18 the node is also linked with the ITBs. In addition, the TB1 is broadened by tens of atomic-layer
 19 migration. Considering the higher stability of twofold NT among the multifold NTs, it can be
 20 inferred that the occurrence of this twofold is caused by the detwinning process of multifold

1 NTs [42]. In addition, the migration of the twin pole from grain interior to GBs as well as TBs
 2 broadening indicate the detwinning process is overwhelming in NGs with reduced grain sizes.
 3 This result is consistent with the results from Fig. 3(f) that the number of NTs is significantly
 4 decreased when the grain sizes reduce to tens of nanometers. At last, there are no NTs observed
 5 interior of the grain when then grain size reduces to ~ 12 nm as shown in Fig. 6(c). From the
 6 Fourier-filtered image as shown in Fig. 6(d), one can see that the closely packed $\{111\}$ planes
 7 of grain interior are inclined by 6.4° to that of grain outside. It can be inferred that a deformation
 8 mode transition from deformation twinning/detwinning to GB mediated-plasticity when the
 9 grain size is below 12 nm.

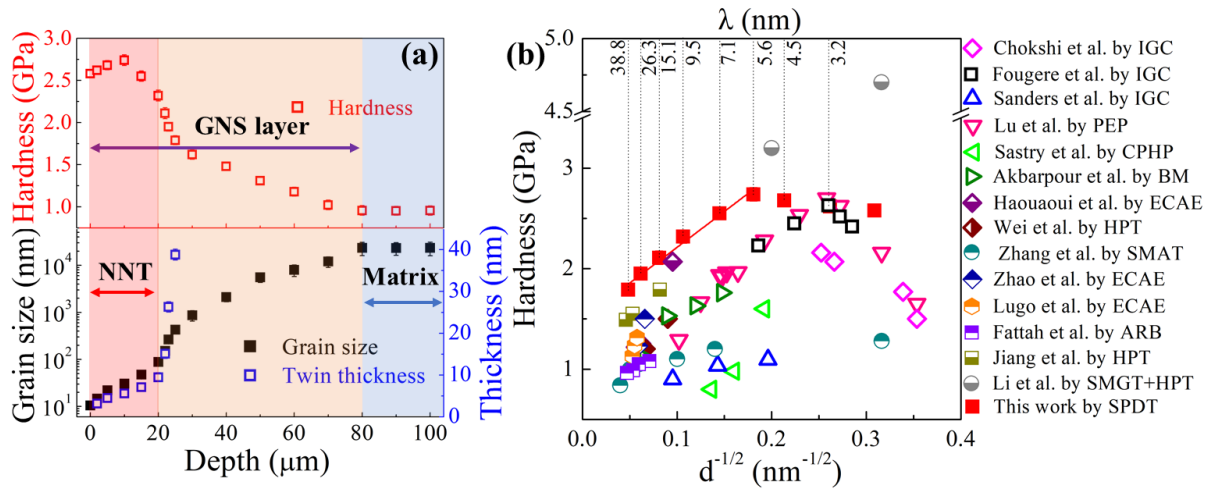


10
 11 Fig. 6 (a) Typical HRTEM image of the twofold NTs in NG ($d \approx 16$ nm) and (b) related Fourier-filtered image
 12 of pole. (c) Typical HRTEM image of NG ($d \approx 12$ nm) and (d) related Fourier-filtered image of GBs.

13 **3.3 Strengthening-softening transition in GNS layer**

14 According to the microstructure observations and nanoindentation tests, Fig. 7(a)
 15 summarizes the varying average grain size, twin thickness and hardness along the depth
 16 direction from the top surface to undeformed matrix in the SPDT Cu sample. It shows that the
 17 average grain size is gradually refined from $\sim 23 \mu\text{m}$ in the matrix region (depth of $\sim 80 \mu\text{m}$) to
 18 ~ 10 nm in the top surface layer. Correspondingly, the twin thickness is also reduced from ~ 38.8
 19 nm (depth of $\sim 25 \mu\text{m}$) to ~ 3.2 nm (depth of $\sim 2 \mu\text{m}$). However, corresponding hardness is

1 firstly increased from ~ 0.95 GPa in the matrix to a maximum value of ~ 2.76 GPa at the ~ 10
 2 μm -depth layer ($d \sim 30$ nm), which is then gradually reduced to 2.58 GPa at the topmost surface
 3 layer. Obviously, there is a strengthening-softening transition in the GNS layer. Fig. 7(b)
 4 displays the Hall-Petch plot with the hardness as a function of $d^{-1/2}$ along the gradient direction
 5 in the NNT region of the SPDT Cu, in which the corresponding twin thickness is also given.
 6 Consistently, the measured hardness in Fig. 7(b) initially follows a traditional positive Hall-
 7 Petch relationship, achieving a peak point (~ 2.76 GPa) at a critical grain size of ~ 30 nm. After
 8 that, such a relationship is broken down when $d < \sim 30$ nm, namely, a negative Hall-Petch slope
 9 with the sign of softening. Note that concurrently gradient reduction in the sizes of GBs and
 10 TBs might lead to the cooperative strengthening effects in the Hall-Petch relationship.
 11 Therefore, the hardness achieved in the NNT layer in our SPDT Cu in Fig. 7(b) surpasses the
 12 hardness reported from some referenced nanostructured Cu, such as NT Cu prepared by pulsed
 13 electrodeposition (PEP) [11]. In addition, there have been several experimental reports about
 14 grain size softening [43, 44] and hardening [45-48] when the grain sizes reduce to tens of
 15 nanometers.



16
 17 Fig. 7 (a) Variation of average grain size, twin thickness and hardness along the depth direction from the
 18 treated top surface to unformed matrix in the SPDT Cu sample. (b) Hall-Petch plot in the NNT region of
 19 SPDT Cu. The hardness values (H) from some literature are calculated from yield strength (σ_y) by Tabor
 20 relation, i.e., $\sigma_y \approx H/3$ [49].

21 Some experimentally data of Cu from literature is added in Fig. 7(b) for comparison [16,
 22 43-48, 50-55]. Hall-Petch softening behaviors have been normally observed in NG Cu prepared
 23 by some bottom-up methods, such as Inert gas condensation (IGC), ball milling (BM), cold
 24 pressing and hot pressing (CPHP) shown in Fig. 7(b). However, it has been suggested that the

1 incomplete densification-induced residual porosity during the above fabrication methods may
2 result in the poor bonding between particles and thus be responsible for the softening. In
3 contrast, conventional SPD methods, including accumulative roll bonding (ARB), equal-
4 channel angular extrusion (ECAE) and HPT, etc., are hard to achieve NGs with grain sizes
5 down to tens nanometers for checking the availability of the strengthening-softening transition.
6 If only increasing the plastic strain during these SPD processes, grain coarsening-induced
7 softening would happen frequently, rather than the continual grain refinement [23].
8 Surprisingly, SMGT and HPT were recently developed to prepare several nanometer-sized NG
9 Cu with 3D minimal-interface structures stabilized by TB networks [26]. This NNT structure
10 can suppress the grain coarsening and exhibit an ultra-hardness, as shown in Fig. 7(b), in lieu
11 of the softening transition. By employing the SPDT technique with a high strain rate, for the
12 first time, we report the strengthening-softening transition involved in the GNS NNT Cu layer
13 with continual grain refinement to ~ 10 nm-grain size at the topmost surface.

14 **4 Discussion**

15 The above experimental results indicate that a high-speed SPDT technique has been
16 validated to successfully fabricate a gradient GNS Cu layer, in which grain size is continually
17 and significantly refined to ~ 10 nm at the topmost surface layer. Noticeably, a gradient NNT
18 surface region across the depth of ~ 20 μm is refined by two main plastic mechanisms, i.e.,
19 gradually transiting from multifold twinning-dominated plasticity in UFGs and relatively larger
20 NGs to multifold detwinning-mediated plasticity in relatively smaller NGs once $d < \sim 48$ nm
21 along the gradient direction. Accordingly, a strengthening-softening transition is confirmed at
22 a critical d of ~ 30 nm. Thus, three critical issues, i.e., (i) grain size effect on the twinning and
23 detwinning of multifold NTs, (ii) their atomic movement mechanisms in grain refinement
24 processes, and (iii) strengthening-softening transition mechanisms in NNT region, will be
25 systematically discussed in this section.

26 **4.1 Grain size effect on the multifold twinning and detwinning in NNT region**

27 Consistent with numerous experiment and simulation results, our observations have
28 testified that the deformation NTs in NGs are corresponding to the partial dislocations emitted

1 from GBs [56-58]. During the high-strain rate SPDT process, the stress for a twinning partial
 2 dislocation nucleation, τ_p , can be expressed as [28, 59]:

$$3 \quad \tau_p = \frac{2\alpha G b_p}{d} + \frac{\gamma}{b_p} \quad (1)$$

4 where α is the dislocation parameter (i.e. edge dislocations with $\alpha = 0.5$, while $\alpha = 1.5$ for screw
 5 ones [60]) representing the scaling factor between the dislocation source length and grain size,
 6 G is the shear modulus of Cu (54.6 GPa[61]), γ is the SFE of Cu (45 mJ/m² [61]), b_p is the
 7 Burgers vector of partial dislocation, and d is the grain size. If consider the localized stress
 8 concentration for the activation of deformation twinning, Eq. (1) can be described as [62]:

$$9 \quad n \cdot \tau_p = \frac{2\alpha G b_p}{d} + \frac{\gamma}{b_p} \quad (2)$$

10 where n is a stress concentration factor. In addition, the stress required to trigger the perfect
 11 dislocation is:

$$12 \quad \tau_N = \frac{2\alpha G b_N}{d} \quad (3)$$

13 where b_N is the Burgers vector of perfect dislocation. For Cu, b_p and b_N are 0.148 nm and 0.256
 14 nm, respectively. According to Eq. (2) and (3), there exists a critical grain size d_c , below which
 15 the stress for the activation of the partial dislocations is lower than that of perfect dislocations

$$16 \quad d_c = \frac{2\alpha G (n b_N - b_p) b_p}{\gamma} \quad (4)$$

17 Accordingly, d_c is determined as ~ 131 nm. As a result, deformation twinning caused by partial
 18 dislocation emission tends to trigger when $d < \sim 131$ nm in Cu. These predictions are verified
 19 by our experiments results, i.e., multifold NTs domain the grain refinement when grain size
 20 lower than one hundred nanometers, as shown in Fig. 3.

21 In contrast to the twinning process, the detwinning process might be happened via the TB
 22 migration by the trailing partial dislocations gliding. Therefore, a simplified equation has been
 23 proposed to evaluate the optimum grain size (d_m) for deformation NTs, which can be written
 24 as [61]:

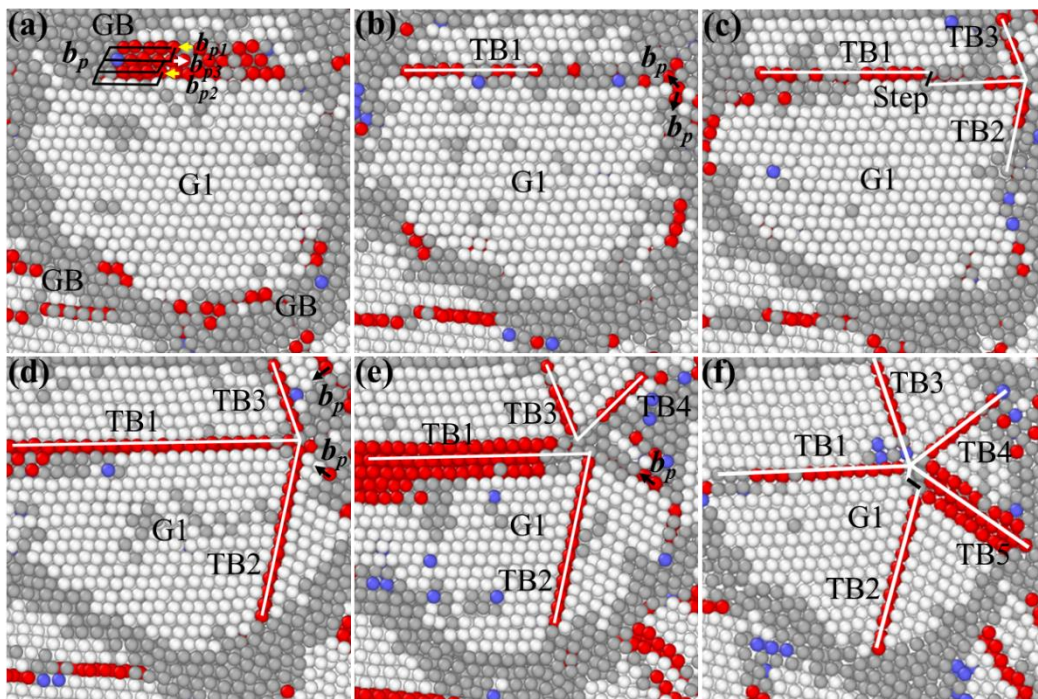
$$25 \quad \frac{d_m}{\ln(\sqrt{2}d_m/a)} = \frac{9.69-v}{253.66(1-v)} \frac{G a^2}{\gamma} \quad (5)$$

26 where v and a is the Poisson's ratio and lattice parameter, respectively. The calculated d_m for
 27 deformation NTs in Cu is ~ 46 nm [61]. This d_m value is consistent with the size of the NGs (\sim
 28 48 nm) with the most profuse NTs in NNT region. When the grain size is smaller than d_m ,

1 twinning will be suppressed and detwinning will be overwhelming in NGs along the gradient
2 direction.

3 4.2 Atomic mechanisms of multifold twinning and detwinning in NNT region

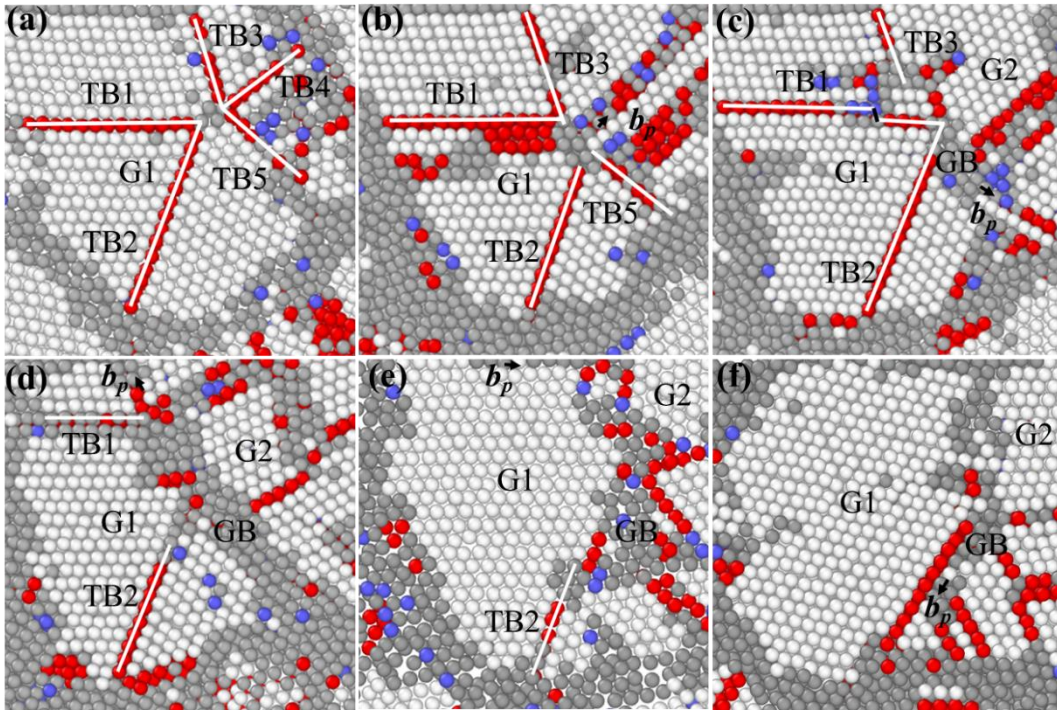
4 According to HRTEM observations in Fig. 4-6, we have identified the zero-macrostrain
5 multifold twinning mechanisms, either through the immigration of 9R structural ITBs by
6 cooperative activation of partials or RAP from GBs. Meanwhile, multifold detwinning process
7 dominated by symmetry breaking, including twin pole splitting/migration and TB migration,
8 is proposed to realize the further grain refinement. In addition, the grain refinement process by
9 multifold twinning and detwinning is also observed during the atomistic MD simulated SPDT
10 process. Herein, we dissect the dynamic atomic-scale microstructural evolution of of
11 representative 5-F NT twinning and detwinning processes to unveil the atomic mechanisms of of
12 multifold twinning and detwinning.



13
14 Fig. 8 MD simulated twinning process of 5-F NT. (a) The initial NG G1 without NTs inside. (b-f) Dynamic
15 twinning process showing that TB1, TB2, TB3, TB4, and TBs are all formed by partials nucleation from
16 GBs.

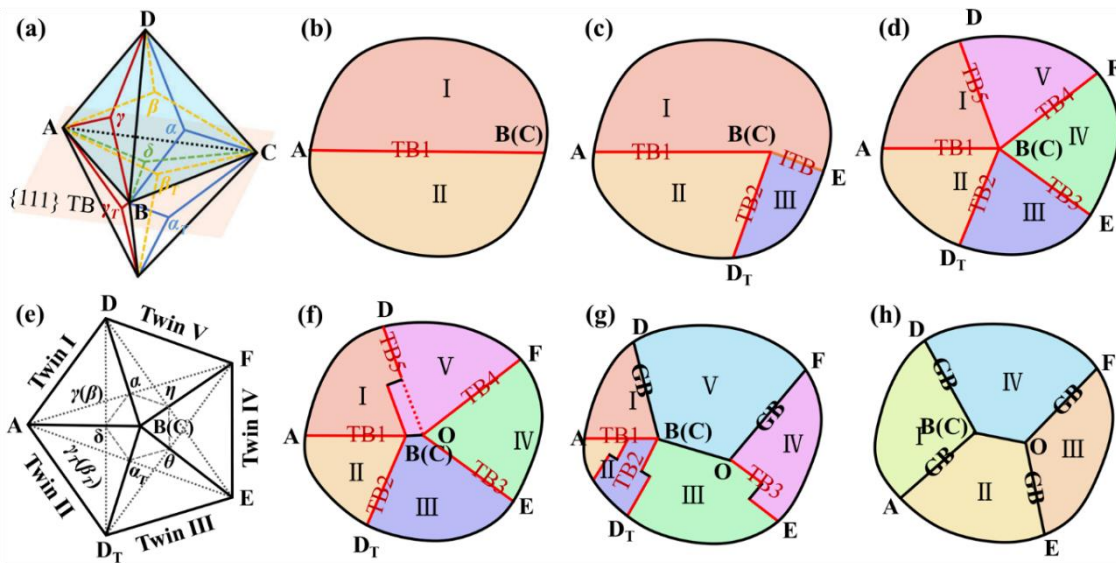
17 Fig. 8 shows a series of atomic-scale images to present the microstructure evolution of a
18 5-F NT formation during the simulated SPDT process. At first, several partials are found in Fig.
19 8(a) to nucleate and emit from GB of one NG, which is labeled as G1 under projection zone

1 [110]. Three Shockley partials with Burgers vectors of $\mathbf{b}_{p1} = \frac{1}{6}[\bar{1}2\bar{1}]$, $\mathbf{b}_{p2} = \frac{1}{6}[2\bar{1}1]$, and $\mathbf{b}_{p3} =$
2 $\frac{1}{6}[\bar{1}\bar{1}2]$ can be indexed to slip on three consecutive (111) planes, which apparently generate a
3 total \mathbf{b} of zero. This is a typical zero-macrostrain RAP twinning mechanism, as no deformation
4 affecting the neighboring lattice structures, which is consistent with the experiment results. The
5 zero-macrostrain RAP twinning grows laterally along with the three layers of the $\{111\}$ planes
6 in grain G1, resulting in the formation of short TB1, as shown in Fig. 8(b). In addition, some
7 partials are also emitted from GBs for forming TB2 and TB3, which are verified in the
8 subsequent Fig. 8(c). A typical 2-F twin is formed with intersectant TB2 and TB3. Then TB1
9 extends with steps to become 3-F twins as shown in Fig. 8(c). The TB2 and TB3 are both
10 extended, and the pole of 3-F twin is migrated from the periphery of the grain to the center. In
11 addition, some partials are ready for TB4 and TB5 in the GBs as shown in Fig. 8(d). TB4 is
12 formed and jointed to 3-F twin to become the 4-F twin. The pole of 4-F twin further migrates
13 to the center of the grain as shown in Fig. 8(e). Finally, TB5 is formed and jointed to 4-F twin
14 to become the 5-F twin. The pole of the 5-F twin is near the center of the grain. As a result, our
15 simulated results successfully verify the zero-macrostrain multifold twinning mechanism.



16
17 Fig. 9 MD simulated detwinning process of 5-F NT. (a) The pole splitting of NG G1 including the 5-F twin.
18 (b) The grain G1 includes the fourfold twin. (c) The grain G1 includes the threefold twin. (d) The grain G1
19 includes the twofold twin. (e) The grain G1 includes the single twin. (f) The grain G1 without twins inside.

1 Besides, Fig. 9 presents successive images to show the detwinning process of a 5-F NT
 2 inside a NG labeled as G1. Firstly, the symmetry of 5-F NT is initially broken by the pole
 3 splitting as shown in Fig. 9(a). The 5-F NT is consequently divided into two regions, i.e., a 2-
 4 F NT (TB1 and TB2) and a 3-F (TB3, TB4 and TB5) NT regions, respectively. Then, TB4 is
 5 transformed by TB migration and partial dislocation slipping is detected accordingly, as shown
 6 in Fig. 9(b), forming two 2-F NTs. It implies that the 2-F NTs are more stable in relatively
 7 smaller NGs, in comparison with higher multifold NTs in relatively larger NGs, which is
 8 consistent with the experiment results. Subsequently, the detwinning process of two 2-F NTs
 9 is continued (Fig. 9(c-d)). To be specific, TB5 and TB3 are both shrunk significantly and
 10 gradually transformed to one conventional GBs by partial dislocation slipping to form a new
 11 grain G2. Finally, TB1 and TB2 are further migrated and integrated to a GB by partial
 12 dislocation slipping, eliminating the TB inside of G1. As a result, the multifold detwinning
 13 process can further refine the original G1 into two NGs (i.e., G1 and G2) with smaller gain
 14 sizes, which is consistent with our experiment results.



15
 16 Fig. 10 (a) Illustration of the double FCC Thompson tetrahedron. (b)-(d) Schematic illustration of formation
 17 process of multifold NT. (e) Thompson tetrahedron Relationship in 5-F twins. (f)-(h) Schematic illustration
 18 of detwinning process of multifold NT.

19 A double FCC Thompson tetrahedron is used to uncover the twinning and detwinning
 20 mechanisms of multifold NTs as shown in Fig. 10(a). Vertex-to-vertex, vertex-to-orthocenter
 21 and orthocenter to-orthocenter represent perfect dislocation, partial dislocation and stair-rod
 22 dislocation, respectively [63]. Based on experiment and MD results, the 5-F twin units are

1 corresponding to five adjoining Thompson tetrahedrons as shown in Fig. 10(a) and (e). On one
2 hand, the formation mechanism of multifold NTs is attributed to the partial dislocation
3 nucleating and slipping from GBs. The first step is the formation of a simple twin (ABC) with
4 domains I and II via partial dislocation emissions from GBs under applied external stress action
5 as shown in Fig. 10(b). The variation in stress orientation can also activate another partial
6 emitted from the GB to nucleate a new twin (BCD_T), forming a twin domain III and an ITB,
7 which effectively converts the regular twin in Fig. 10(b) into a 2-F twin as shown in Fig. 10(c).
8 Note that ITBs also can provide the twinning dislocations for the nucleation of the multifold
9 NTs. Under varying stress orientations, several partials with various glide directions to be
10 activated sequentially to finally form the 3-F, 4-F and 5-F, respectively.

11 On the other hand, the symmetry-breaking mechanism dominates the detwinning process
12 of the multifold NT for the further grain refinement in our work. It includes symmetry-breaking
13 twin morphology (TBs migration, twin pole splitting and migration). Fig. 10(f) schematically
14 illustrates that the detwinning process is related with the TB5 migration. The partial dislocation
15 is nucleated near the TB1 and then glides along TB1 away from the twin pole. The continuous
16 TBs migration induces the twin pole migration along TB1. As a result, symmetric twin pole
17 B(C) migration is completed by partial dislocations slipping. Moreover, the partial dislocation
18 slipping or step on TB2 leads to a several-layer migration of TB2 as shown in Fig. 10(c). Then
19 the partial dislocations and the stair-rod dislocations dissociated from the random partial
20 dislocations on the curved TB2 induce to further symmetry-breaking of twin pole. Moreover,
21 with further TBs migration and twin pole splitting, new conventional GBs can be formed from
22 TBs though partials activities-mediated grain rotation, leading to the grain refinement.

4.3 Strengthening-softening transition mechanism in NNT region

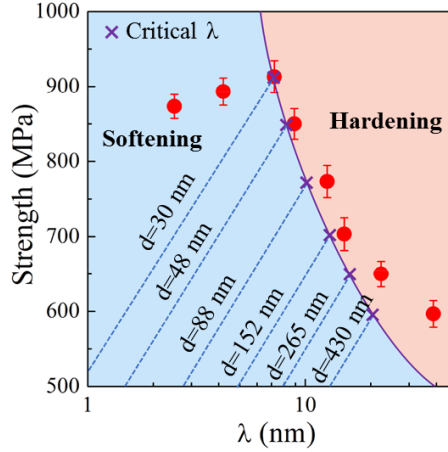


Fig. 11 Yield stress of NNT region as a function of twin thickness for different grain sizes.

Combined with the statistical TEM data and nanoindentation tests, deformation NTs present a clear size effect on the strengthening-softening transition in the NNT region. On one hand, the detwinning occurs when the grain size is down to ~ 48 nm. The detwinning process exhibits the strain relaxation of TBs. Several types of theoretical models have been developed to predict the critical thickness for the strengthening-softening transition in NT metals. For example, a dislocation-based theoretical model was developed by incorporating the functions of densities of dislocations pile-up zones of TBs (including primary and secondary twin lamellae) and GBs to describe the twin thickness and grain size-dependent flow stress of hierarchical NT metals [20, 64], thus yielding the critical values for the strengthening-softening transition. It should be noted that the intersection effect of multifold TBs and partial dislocations is hardly to quantitatively evaluate. On the other hand, a dislocation nucleation-based model has been proposed to describe the dependence of material strength (σ) on twin thickness and grain size in the following equation [19]:

$$\sigma = \frac{\Delta U}{SV^*} - \frac{k_B T}{SV^*} \ln\left(\frac{d V_D}{\lambda \dot{\epsilon}}\right) \quad (6)$$

The first component in the right side of Eq. (6) can be regarded as the athermal shear resistance and the second component is due to thermal softening. Accordingly, the critical λ for the strengthening-softening transition in the present work can be directly derived from the intersection points of the yield stress versus λ curve and the measured Hall-Petch curve at different grain sizes. More specifically, ΔU , S , V^* , k_B , T , V_D and $\dot{\epsilon}$ are the activation energy, factor related to local stress concentration and geometry, activation volume, Boltzmann

1 constant, temperature, Debye frequency ($1.3 \times 10^{13} \text{s}^{-1}$), and macroscopic strain rate, respectively.
2 According to previous experimental studies, $k_B T / SV^*$ is about 200 MPa, The corresponding
3 athermal shear resistance is near the ideal shear strength as $\sim G/10$ ($G = 54.6 \text{ GPa}$ for Cu [19]).
4 In our experiment, $\dot{\epsilon}$ is $\sim 4.6 \times 10^5 \text{ s}^{-1}$. As a result, Fig. 11 presents the compared yield stress
5 (Tabor relation, $\sigma_y \approx H/3$ [49]) of NNT Cu from experimental data and the model predictions
6 based on Eq. (6). According to Eq. (6), for example, the critical calculated λ is $\sim 7.25 \text{ nm}$ when
7 the NG $d \approx 30 \text{ nm}$, while it is $\sim 16.8 \text{ nm}$ for the NG with $d \approx 260 \text{ nm}$. In our study, deformation
8 NTs play a strengthening role when d is larger than 30 nm because the corresponding twin
9 thickness is thicker than the critical λ . This result is consistent with previous reports that the
10 NTs show an excellent mechanical stability in pure Cu when d is larger than $\sim 30 \text{ nm}$ [6].
11 However, NTs transform to a softening role when d is below 30 nm because the corresponding
12 twin thickness is below the critical λ . It is indicated that the grain size and twin thickness effects
13 on the strengthening mechanism reported in our study and previous prediction are universal in
14 FCC twin-structured materials. For these small-size twin-free NGs, the softening behavior is
15 dominated by pure GB-mediated plasticity.

16 **5 Concluding remarks**

17 In this work, GNS Cu layer containing both gradient NNT sub-layer region and extremely
18 refined twin-free NG surface layer with grain size of $\sim 10 \text{ nm}$ has been achieved by the high-
19 speed SPDT technique. Microstructure evolution and plastic deformation mechanisms of the
20 NNT layer are atomically explored via HRTEM characterizations and MD simulations. First,
21 the overall grain refinement process for GNS layer is gradually transited from dislocation
22 activities-mediated mechanism in CGs and sub-grains to twinning-mediated mechanisms in
23 UFGs with decreasing grain size in the deformed sub-surface region. Second, the deformation
24 multifold twinning with zero-macrostrain is found to refine the microstructure for the formation
25 of gradient NNT regions. Specifically, zero-macrostrain deformation multifold NTs can be
26 formed by either immigration of 9R structural ITBs by cooperative activation of partials or
27 RAP from GBs. However, the propensity of deformation NTs firstly increases and then
28 decreases in small-size NGs once the grain size below $\sim 48 \text{ nm}$ and finally form extremely fine
29 twin-free NGs at the topmost surface layer. The detwinning process of multifold NTs play a

1 key role in the continual refinement of NGs as well. The detwinning process of multifold NTs
2 is associated with the symmetry-breaking of the twin morphology (TBs migration, twin pole
3 splitting and migration). Third, a GBs and TBs strengthening mechanism is found with the
4 grain refinement from UFGs to NGs. However, a strengthening-softening transition is occurred
5 when the grain size reduces to ~30 nm. The softening mechanism is attributed to the coupled
6 effects of grain size and twin thickness on deformation method in NNT structures and the pure
7 GB-mediated plasticity in extremely fine twin-free NGs. A series of critical twin thicknesses
8 for softening in nanograins with different grain sizes are discussed to be consistent with our
9 experimental statistics.

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18 **Competing interests**

19 The authors declare no competing interests.

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