

## Tunable compensation temperature through ferromagnetic coupling in perpendicular Tb<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>/Eu<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub> bilayer heterostructure

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### Abstract

Rare-earth ion garnets (ReIG) with magnetization compensation are being extensively studied, such as in the ferrimagnetic insulator (FMI)/heavy metal (HM) heterostructures, with primary focus on the interface effect between single-layer garnets and HM. Here, we study the anomalous Hall behavior of bilayer garnet in Tb<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub> (TbIG)/Eu<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub> (EuIG)/Pt system. TbIG (30 nm)/EuIG (*t* nm) films with strong perpendicular magnetic anisotropy (PMA) were deposited on single-crystal Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub> (GGG) (111) substrates using pulsed laser deposition. Subsequently, a 5 nm layer of Pt was sputtered and patterned into Hall bars. Tunable compensation temperature ( $T_{comp}$ ) was achieved in the system by changing the thickness of EuIG, which is ascribed to the ferromagnetic coupling of Fe sublattices in the two different garnets. This study provides guidance for designing garnet spintronic devices with controllable compensation behavior.

**Keywords:** iron garnet, magnetization compensation, perpendicular magnetic anisotropy, spin Hall effect

## 1. Introduction

Rare-earth (Re) ion garnets (ReIG) films are heavily studied in the ferromagnetic insulator (FMI)/heavy metal (HM) systems, of which the most well-known is  $\text{Y}_3\text{Fe}_5\text{O}_{12}$  (YIG)/Pt [1-5]. Much effort was made into exploring phenomena such as the spin pumping effect [6, 7] spin-Hall effect [8-10], inverse spin-Hall effect [1, 11], and spin Seebeck effect [12, 13] in these systems. Meanwhile, due to the strong temperature dependence of magnetization in Re ions (like Tb, Gd, Dy, etc.) and antiparallel alignment of  $\text{Fe}^{3+}$  moments in ReIG, some ReIGs show magnetization compensation at certain temperatures ( $T_{comp}$ ) where the saturation magnetization temporarily vanishes [14-19].

For ReIG with perpendicular magnetic anisotropy (PMA), hysteretic behaviour can be observed through the anomalous Hall effect resistance ( $R_{AHE}$ ) of the corresponding FMI/HM system, and recent studies attempted to explain the phenomena [16, 20-22]. Advanced technologies like polarized neutron reflectivity and X-ray circular dichroism are used to study the magnetic proximity behavior of the FMI/HM interface and the coupling between sublattices [20], revealing the competitive relationships of sublattices magnetism around  $T_{comp}$ .

Previous studies on ReIG/HM have identified various phenomena associated with the magnetization compensation behaviors in ReIG, including temperature dependence of  $R_{AHE}$  ReIG/HM across  $T_{comp}$ , interfacial modification in ReIG/HM system to regulate the spin-Hall magnetotransport [20], or the relation between  $T_{comp}$  with the thickness of single-layer ReIG film [23]. Particularly, two sign reversals in hysteretic  $R_{AHE}$  with changing temperatures can be observed in ReIG/Pt with ReIG possessing compensation points. In TbIG/Pt for example, the sign reversal around 220 K coincides with the  $T_{comp}$  of TbIG [14, 24, 25]. Similar  $T_{comp}$  phenomenon is also observed in DyIG/Pt and GdIG/Pt [18, 26]. The second  $R_{AHE}$  sign reversal occurs typically at temperatures below  $T_{comp}$ , and is suggested to arise from the competition between the magnetic proximity effect (MPE) induced in the Pt layer and the spin Hall (SH) magnetotransport at the interface [20, 27, 28].

Relatively little attention is paid to multilayers composed of different ReIG materials. Some studies were made on exploring the spin-Hall transport behavior by constructing trilayer structures with an antiferromagnetic spacer (e.g. NiO) sandwiched between two ReIG layers,

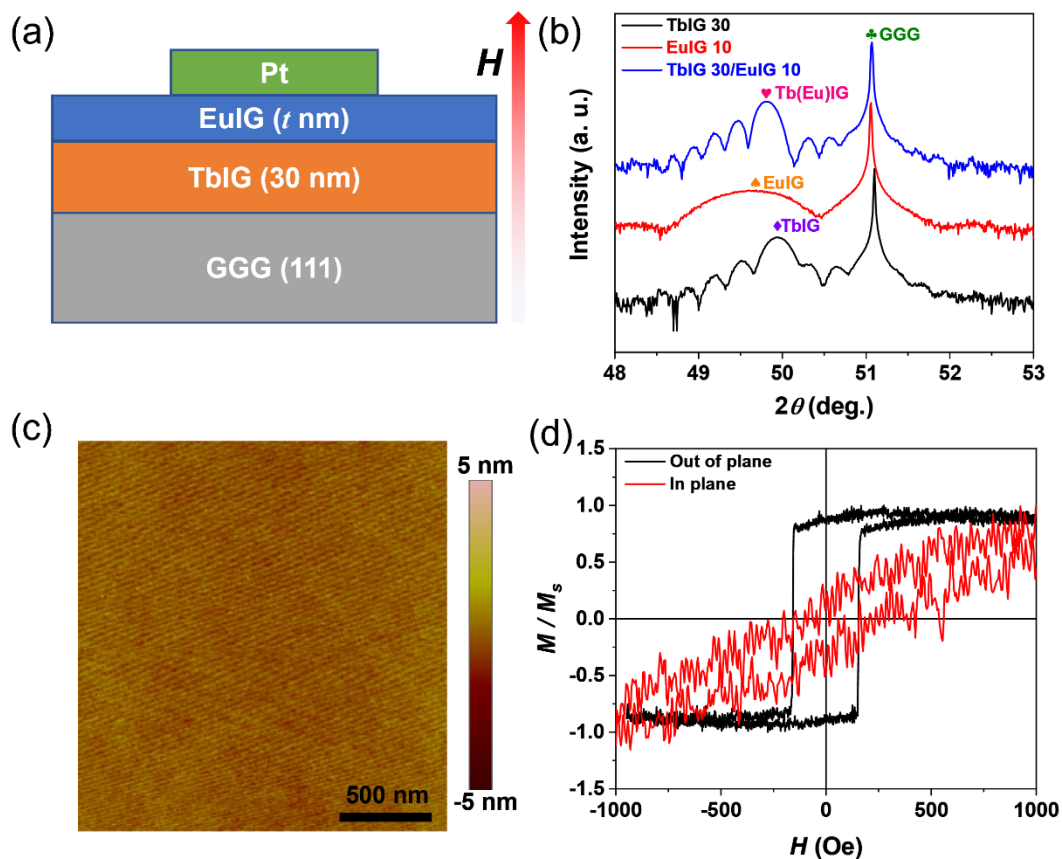
forming the so-called magnon valves [29, 30]. The large lattice mismatch between NiO and ReIG systems leads to differences in the crystallinity of top and bottom garnet layers, and all-ReIG systems with similar crystal structures can avoid these issues. The impact of the ReIG materials in close proximity on the magnetic and spin magnetotransport behaviour is worth exploring.

In this work, we demonstrate the adjustable extrinsic magnetic compensation point by constructing bilayer garnet films (TbIG and EuIG). While the compensation point is an intrinsic property of some garnets like TbIG, independent of additional magnetic moments, the modulation of extrinsic magnetization compensation in iron garnet films can be achieved by constructing ReIG bilayers composed of two different garnets. This extrinsic compensation behavior originates from the combined magnetic contributions of different layers. Here, the bottom TbIG has fixed thickness, the top EuIG layer thickness is varied to study the impact on the spin-Hall transport behaviour in the topmost Pt layer. Particular attention is paid to the effect of lattice-matching EuIG insertion on the  $R_{AHE}$  behavior in the Pt layer as compared to the control TbIG/Pt sample. EuIG has a garnet structure with lattice constant ( $a_{EuIG} = 12.500$  Å) [31] similar to that of TbIG ( $a_{TbIG} = 12.436$  Å) [32] and  $Gd_3Ga_5O_{12}$  (GGG) ( $a_{GGG} = 12.376$  Å) [31], the latter of which is commonly used for epitaxial growth of ReIG thin films. Specially, GGG(111)/TbIG and GGG(111)/EuIG can maintain the PMA because of the in-plane compressive strain and positive magnetostrictive constants in [111] direction [33]. Besides, EuIG alone does not exhibit magnetization compensation [34], making it a suitable candidate to explore the impact on TbIG/Pt through observing magnetization compensation regulation in the heterostructures. The temperature dependence of anomalous Hall resistance ( $R_{AHE}$ ) was measured on the samples to probe the  $T_{comp}$ . The experimental results indicate that extrinsic  $T_{comp}$  can be tuned in the TbIG/EuIG system through varying the EuIG thickness, and the interface coupling situation at TbIG/EuIG was discussed.

## 2. Experimental Details

For film and device fabrication, TbIG (30 nm)/EuIG ( $t$  nm) (with  $t$  ranging between 0 to 20 nm) were deposited on GGG (111) substrates by pulsed laser deposition (PLD). The films were grown at 710 °C in an oxygen ambient of 100 mTorr, using a KrF excimer laser with a

wavelength of  $\lambda=248$  nm, pulses energy of 340 J, and a repetition rate of 2 Hz. The deposition sequence is shown in Fig. 1(a). Before deposition, substrates were annealed in air at 1000 °C for 6 hours to produce a reconstructed GGG surface, promoting the smooth growth of the films [14]. After deposition, 5 nm of Pt was deposited *ex-situ* by d.c. magnetron sputtering and subsequently patterned into Hall bars using photolithography and broad-beam ion milling. The specific thickness was measured through the high-resolution transmission electron microscope (HRTEM) image and found to be approximately 30 nm (see Figs. S1), which matches the value we calibrated using calibration sample.



**Fig. 1.** (a) Schematic illustration of TbIG/EuIG/Pt device. (b) XRD diffraction profile of single-layer TbIG (30 nm) and EuIG (10 nm), and the TbIG (30 nm)/EuIG (10 nm) bilayer. (c) AFM image of GGG/TbIG (30 nm)/EuIG (10 nm) film. (d) In-plane (red) and out-of-plane (black) normalized  $M$ - $H$  hysteresis loops of TbIG (30 nm)/EuIG (10 nm) at room temperature as measured by VSM.

High-resolution X-ray diffractometry (XRD, Rigaku SmartLab) was used to characterize

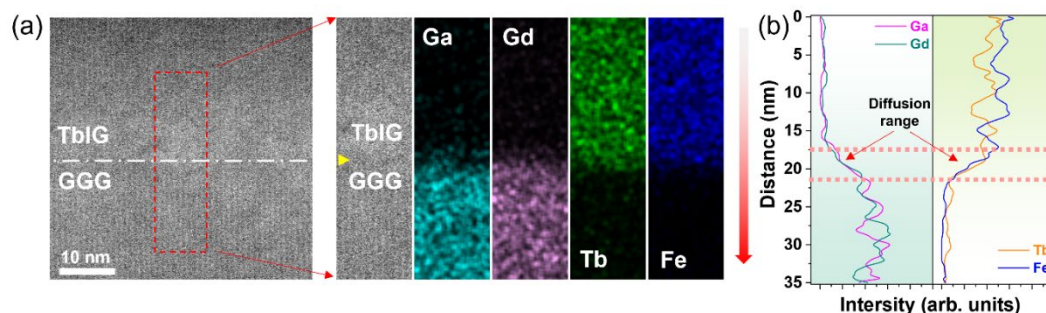
the microstructure of TbIG/EuIG bilayers. The surface morphology was probed using atomic force microscopy (AFM, Asylum 3D infinity). Transmission electron microscopy (TEM, JEM-F200) equipped with high-angle annular dark field (HAADF) and EDX mappings were used for inspecting the crystallinity and elemental distribution, with the specimen prepared by focused ion beam microscopy (FIB, Helios 5 UX). Magnetic hysteresis loops were measured by a vibrating sample magnetometer (VSM, Lakeshore). Magnetotransport properties were measured by a physical property measurement system (PPMS, Quantum Design).  $R_{AHE}$  were detected from the samples with external magnetic field applied perpendicular to the substrates.

### 3. Results and Discussion

Fig. 1(b) shows the X-ray  $2\theta$  scan of single layer TbIG(30 nm) and EuIG(10 nm) films, as well as TbIG (30 nm)/EuIG (10 nm) bilayers. In addition to the sharp GGG (444) substrate peak, the EuIG peak is observed at  $2\theta = 49.61^\circ$  and is lower than the TbIG peak ( $2\theta = 49.93^\circ$ ). As both the lattice parameters of EuIG and TbIG are larger than that of GGG, all films show in-plane compressive strain, and EuIG peak is shifted towards lower  $2\theta$  value due to the larger lattice size. For the bilayer sample, the combined peak position at  $2\theta = 49.81^\circ$  is between that of single-layered EuIG and TbIG. The actual thickness of TbIG (30 nm)/EuIG (10 nm) bilayer sample can be confirmed by the TEM image (Fig. S1 in Supporting Information), which is consistent with our expected thickness. Epitaxial relationship between the films and the substrate can be evidenced from the phi scan (see Figs. S1 and S2). The surface morphology was probed using AFM. Fig. 1(c) presents the surface morphology of GGG/TbIG (30 nm)/EuIG (10 nm) sample. The root-mean-square roughness of 0.34 nm indicates an atomically smooth sample surface.

PMA in ReIG facilitates the observation of hysteretic AHE signals and spin-orbit torque-based magnetization reversal in ReIG/Pt systems [24, 35]. Previous studies showed that single-layer EuIG and TbIG thin films on GGG (111) substrates exhibit out-of-plane easy axis [14, 36, 37]. To verify that PMA is retained in the ReIG bilayers, in-plane and out-of-plane magnetic hysteresis loops of TbIG (30 nm)/EuIG (10 nm) film were measured by VSM at room temperature. As shown in Fig. 1(d), the out-of-plane  $M-H$  shows a squared loop, indicating the

easy axis of the bilayer is along the sample normal direction.

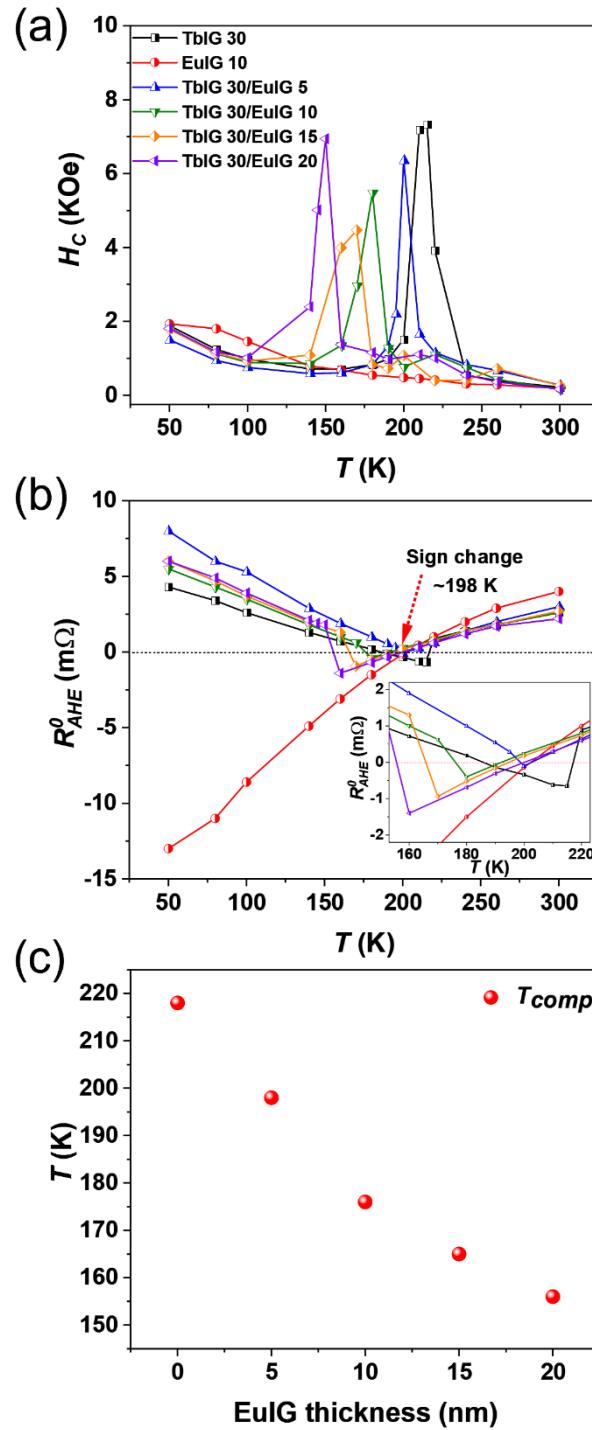


**Fig. 2.** (a) STEM image of the GGG/TbIG interface. The red dashed rectangle range was extracted for EDX mapping analysis. (b) The average signal intensity of different elements (Ga, Gd, Tb, and Fe) was obtained from the line scan.

Fig. 2 displays STEM and the energy-dispersive x-ray spectroscopy (EDX) images across the GGG/TbIG interface. The STEM image in Fig. 2(a) shows a highly crystallized and flat GGG/TbIG interface, consistent with the XRD and AFM results in Figs. 1(b) and 1(c). EDX element distribution analysis was conducted in selected region of Fig. 2(a). The distribution of various elements (Ga, Gd, Tb, and Fe) in Fig. 2(a) indicates diffusion across the interface. Line scan analysis results [Fig. 2(b)] suggest an interdiffusion range of around 4 nm across the substrate/film interface. Such transient layer is commonly observed in ReIG films [38-40]. The interdiffusion processes at substrate/garnet interface can generate a continuous composition profile without abrupt changes in the lattice parameters. Cross-sectional TEM (Fig. S1) indicates a change of garnet lattice without detectable dislocations throughout the thickness of the bilayer film. The average lattice plane spacing  $d_{111}$  and  $d_{110}$  were measured (Fig. S3). Due to the small lattice mismatch (0.48%) between GGG and TbIG,  $d_{111}$  and  $d_{110}$  show no obvious change and are close to that of GGG substrate. While the thickness of the transient layer at GGG/TbIG interface depends on the deposition parameters, it is justified to assume that being constant in our bilayer samples, and the impact on the magnetization and  $T_{comp}$  on all TbIG/EuIG samples should be identical.

While the majority of previous studies focused on MPE or spin-Hall transport at the interface of ReIG/Pt [14, 37], little attention was paid on the influence of an adjacent iron garnet layer with different Re composition (ReIG') on an existing ReIG/Pt system. In this study, we

placed EuIG of different thicknesses in proximity with Pt, while a TbIG (30 nm) layer serves as the adjacent ReIG', forming a multilayer stack of TbIG(30 nm)/EuIG ( $t$  nm)/Pt.



**Fig. 3.** Temperature dependence of (a)  $H_c$  and (b)  $R_{AHE}^0$ . All  $H_c$  and  $R_{AHE}^0$  were obtained from the  $R_{AHE}$ - $H$  loops at corresponding temperatures. The inset in (b) shows the amplified part of the  $R_{AHE}^0$ - $T$  around  $R_{AHE}^0$  cross-over. (c) EuIG thickness dependent  $T_{comp}$ .

$R_{AHE}$ - $H$  loops of the samples at various temperatures are plotted in Figs. S4-S9 of Supporting Information, and the corresponding  $H_c$  (as extracted at  $R_{AHE} = 0$ ) and  $R_{AHE}$  at zero fields ( $R_{AHE}^0$ ) are shown in Figs. 3(a) and 3(b). Divergence of  $H_c$  can be observed from Fig. 3(a). Both  $Tb^{3+}$  and  $Fe^{3+}$  in ReIG show temperature dependencies, but  $Tb^{3+}$  decays more rapidly and cancel out with  $Fe^{3+}$  at around 222 K [23, 41]. As temperature approaches  $T_{comp}$ , the magnetization of  $Tb^{3+}$  and  $Fe^{3+}$  sublattices cancel out, forming a saturation magnetization close to zero and a corresponding  $H_c$  divergence due to the decreased Zeeman energy for magnetization reversal [42].

Meanwhile, the  $T_{comp}$  greatly affects the spin-Hall transport of ReIG/Pt. As the temperature decreases and passes through  $T_{comp}$ ,  $Tb^{3+}$  replaces  $Fe^{3+}$  and dominates the overall magnetization, while the two types of ions remain antiparallel. Meanwhile, it is known that Fe-Pt coupling determines the spin-Hall magnetotransport behavior [20]. A cross-over at  $T_{comp}$  therefore leads to an abrupt  $R_{AHE}^0$  sign reversal as  $Fe^{3+}$  reorient itself, as evidenced by the rapid  $R_{AHE}^0$  sign change around  $T_{comp}$  [inset, Fig. 3(b)]; detailed measurements show that such  $R_{AHE}^0$  sign change can occur within a 5-K temperature interval.

From the above, it can be summarized that both divergent  $H_c$  and  $R_{AHE}^0$  sign reversal coincides with  $T_{comp}$ . The divergent  $H_c$  provides direct evidence for the existence of  $T_{comp}$ , the precise identification of which may be difficult due to the exceedingly large fields involved. Meanwhile,  $R_{AHE}^0$  reflects the ReIG/Pt interfacial spin-Hall transport, and its good temperature sensitivity provides a convenient probe for  $T_{comp}$  for the ReIG system.

It should be noted that EuIG does not possess  $T_{comp}$  in bulk, as supported by the absence of  $H_c$  divergence in EuIG (10 nm)/Pt [Fig. 3(a)]. Because the ground state of dodecahedral site  $Eu^{3+}$  has total angular momentum  $J = 0$  according to Hund's rule, the magnetic contribution of  $Eu^{3+}$  to EuIG magnetization can be ignored [34, 43]. In turn, the magnetization of EuIG is solely decided by  $Fe^{3+}$  ions, thus ruling out the occurrence of  $T_{comp}$  in EuIG. However,  $H_c$  divergence is clearly observed among all TbIG/EuIG/Pt samples in Fig. 3(a), and is accompanied by abrupt  $R_{AHE}^0$  sign change at similar temperatures in Fig. 3(b). This suggests a magnetization compensation behavior in the TbIG/EuIG bilayer, similar compensation behavior can be observed in the in-plane YIG/GdIG bilayer system [44].

More importantly, a dependence of such magnetization compensation in TbIG/EuIG with

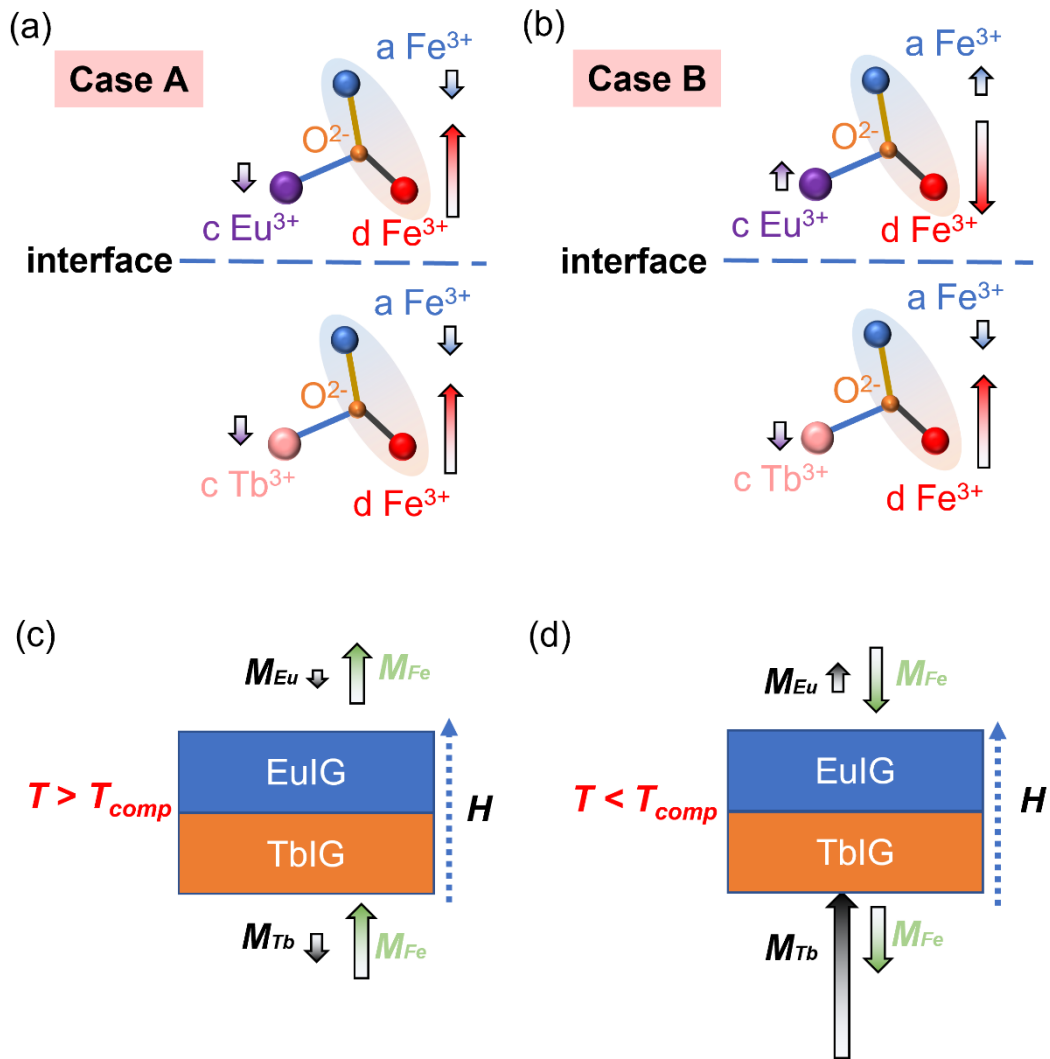
EuIG thickness can be seen in Figs. 3(a) and 3(b). To this end,  $T_{comp}$  was extracted from the  $R_{AHE}^0$  sign cross-over points for various TbIG/EuIG ( $t$ ) samples and is plotted in Fig. 3(c). As the thickness of EuIG increases,  $T_{comp}$  gradually decreases from 218 K ( $t = 0$  nm) to 156 K ( $t = 20$  nm).

In addition to the cross-over of  $R_{AHE}^0$  at  $T_{comp}$  (which coincides with  $H_c$  divergence), another cross-over can be observed at around 198 K [Fig. 3(b)] and is invariant for all samples (including single-layer EuIG). This cross-over is typically attributed to the competition between MPE-induced AHE in the Pt layer and the SH-induced AHE at the ReIG/Pt interface [20]. The magnetic proximity effect is a common phenomenon that induces a magnetic moment in the heavy metal interface when in contact with a magnetic insulator, resulting in limited ferromagnetic ordering in Pt and the production of an AHE signal. Additionally, the spin Hall effect can convert electron current into spin current, and the corresponding inverse spin Hall effect also exists at the FMI/HM interface. The AHE signal, which differs from MPE-induced part, can be activated through the spin current in the heavy metal and shows opposite direction. Because of the different temperature dependence of SH and MPE, at high temperatures, thermal disturbance weakens MPE-induced AHE at EuIG/Pt interface, and the spin current-induced AHE is prevalent. The proximity effect gradually dominates as the temperature decrease, leading to a gradual variation of  $R_{AHE}^0$  around this cross-over point.

While the competition between MPE-induced AHE and SH-induced AHE has been studied in previous works [20, 28], Fig. 3(b) suggested that the  $R_{AHE}^0$  sign of single-layer TbIG and EuIG are opposite at the lowest temperatures. As mentioned previously, the magnetization of EuIG is dominated by  $d$ -site  $Fe^{3+}$ , and  $T_{comp}$  is not observed in this system; this is reflected in the EuIG/Pt spin-Hall transport measurement, at which  $R_{AHE}^0$  sign reversal occurs only when MPE-induced AHE and SH-induced AHE cancel out.

However, the  $R_{AHE}^0$  in TbIG/Pt and TbIG/EuIG/Pt systems show two cross-over of signs with the EuIG thickness studied. As mentioned before, these two reversals follow different mechanisms. As shown in Fig. 3(b), the abrupt  $R_{AHE}^0$  sign change is accompanied by a divergent  $H_c$  and is related to  $T_{comp}$ , which shows a strong EuIG thickness dependence [Fig. 3(c)]. This  $R_{AHE}^0$  sign change originates from the reorientation of  $Fe^{3+}$  in ReIG films at  $T_{comp}$ . It is known that the antiferromagnetic coupling exists in  $a$ -site  $Fe^{3+}$ / $d$ -site  $Fe^{3+}$  and  $d$ -site  $Fe^{3+}$ / $c$ -

site  $\text{Tb}^{3+}$  ions in TbIG, the combined action of different site ions contributes to its intrinsic compensation behavior. The a-site  $\text{Fe}^{3+}$ /d-site  $\text{Fe}^{3+}$  sublattices (with d-site being dominant among the two) have much stronger exchange coupling (exchange constant  $J_{ad} \cong 2.62 \text{ meV}$ ) compared to the  $\text{Fe}^{3+}/\text{Tb}^{3+}$  coupling ( $J_{ac} \cong 0.045 \text{ meV}$  and  $J_{dc} \cong 0.21 \text{ meV}$ ) [45]. Therefore, the net magnetization of TbIG is determined by the  $\text{Fe}^{3+}$  at above  $T_{comp}$ . While the magnetization of  $\text{Tb}^{3+}$  ions have stronger temperature dependence than  $\text{Fe}^{3+}$ , the strongly enhanced  $\text{Fe}^{3+}/\text{Tb}^{3+}$  coupling eventually overcomes the magnetic coupling among  $\text{Fe}^{3+}$ , causing the net magnetization to be dominated by  $\text{Tb}^{3+}$  at below  $T_{comp}$ .



**Fig. 4.** Possible coupling situations across TbIG/EuIG. (a) Case A model assumes ferromagnetic coupling between  $\text{Fe}_{EuIG}$  and  $\text{Fe}_{TbIG}$ , as in contrast with the antiferromagnetic coupling of  $\text{Fe}^{3+}$  sublattices across the interface in (b) Case B. Schematic illustration of net magnetic moment directions of different elements (c) below and (d) above  $T_{comp}$  in the

TbIG/EuIG system.

While the change in  $T_{comp}$  could be related to the thickness of the transient layer at the TbIG/EuIG interface. Considering a fixed transient layer because of the same deposition parameters, the value (TbIG/EuIG interface)/(total EuIG thickness) decreases with the increase of the EuIG thickness. The reduced relative thickness leads to a continuous decrease in  $T_{comp}$ . The other cross-over point is manifested through a continuous and gentle  $R_{AHE}^0$  variation with no divergent  $H_c$ , and is related to the competition between MPE-induced AHE and SH-induced AHE. As mentioned, this  $R_{AHE}^0$  sign change occurs at  $\sim 198$  K in all samples.

Interestingly, all the bilayer films still maintain two cross-over points despite the absence of  $T_{comp}$  in EuIG. The  $T_{comp}$  extracted from the TbIG/EuIG/Pt samples decreases with rising EuIG thickness, indicating that TbIG plays a role in modulating the  $R_{AHE}^0$  signals as detected from the EuIG/Pt interface, which we argue to arise from the coupling between the EuIG and TbIG layers.

Although the existence of the transient layer at TbIG/EuIG interface may affect the overall magnetic properties, identical conditions are again expected in the bilayers, and the magnetic contribution of  $\text{Eu}^{3+}$  can be ignored. Based on this, we propose a reasonable theoretical model to explain the trend of  $T_{comp}$  change. For the convenience of understanding, we consider the interfacial coupling of the  $\text{Fe}^{3+}$  sublattices in the EuIG and TbIG layers ( $\text{Fe}_{EuIG}$  and  $\text{Fe}_{TbIG}$ ) across the TbIG/EuIG interface. Noting that the  $\text{Fe}^{3+}$  sublattices are formed as a consequence of the antiferromagnetic alignment of  $a$ -site and  $d$ -site  $\text{Fe}^{3+}$  ions. There could be two possible coupling scenarios. Case A (Fig. 4a) shows that the  $\text{Fe}_{TbIG}$ - $\text{Fe}_{EuIG}$  across the TbIG/EuIG interface are ferromagnetically coupled. In Case B [Fig. 4(b)], the interfacial  $\text{Fe}_{TbIG}$ - $\text{Fe}_{EuIG}$  are antiferromagnetically coupled.

To analyse the possibility of the coupling cases, we first discuss the overall magnetization changes at above and below  $T_{comp}$ . It is noticed that all the samples show positive  $R_{AHE}^0$  signs at above  $T_{comp}$ , [Fig. 3(b)]. Since at high temperatures both the magnetizations of TbIG and EuIG are dominated by  $\text{Fe}^{3+}$  sublattices. this results in the overall magnetizations of both EuIG and TbIG pointing toward to the same direction [Fig. 4(c)]. The same  $R_{AHE}^0$  signs are therefore observed in both TbIG/Pt and TbIG/EuIG/Pt samples. When the temperature drops below  $T_{comp}$ , although  $R_{AHE}^0$  signs reversal occurs in both TbIG/Pt and TbIG/EuIG/Pt samples, the total

magnetization directions of the EuIG and TbIG layer are entirely different. As shown in Fig. 4(d), at temperatures below  $T_{comp}$ , the magnetization of EuIG is still dominated by  $d$ -site  $Fe^{3+}$ , while in the TbIG layer the  $Tb^{3+}$  sublattice overcome the  $Fe^{3+}$  sublattices and dominate the overall magnetization. Because the magnetic moments direction of different sublattices have been reversed, the overall magnetization of the EuIG and TbIG layers display an antiparallel alignment.

Based on the above discussion, we can start to analyse the two cases in Fig. 4. When Case A ( $Fe_{TbIG}$ - $Fe_{EuIG}$  is ferromagnetically coupled) occurs, the parallel alignment of  $Fe^{3+}$  sublattices in both EuIG and TbIG implies that a larger  $Tb^{3+}$  moment  $M_{Tb}$  is required to balance with the overall  $Fe^{3+}$  moments in both TbIG and EuIG layers. Therefore, complete cancellation of  $M_{Fe}$  by the (highly temperature dependent)  $M_{Tb}$  can only be achieved at lower temperatures, implying a lower  $T_{comp}$  with increasing EuIG thickness. The trend of  $T_{comp}$  variation with EuIG thickness in Fig. 3(c) supports such an interpretation. Besides, Fig. 4(a) shows the magnetic moment directions of the Re and Fe sublattices in each iron garnet layer. The parallel alignment of  $Fe^{3+}$  sublattices in EuIG and TbIG is also consistent with the descriptions in Figs. 4(c) and 4(d). If the  $Fe^{3+}$  sublattices were antiferromagnetically coupled across the interface [Case B, Fig. 4(b)], the total magnetization  $M_{EuIG}$  would be in antiparallel alignment with  $M_{TbIG}$  above  $T_{comp}$ , which contradicts the description in Fig. 4(c) and inconsistent with the  $T_{comp}$  change shown in Fig. 3(c).

So, the  $Fe_{TbIG}$ - $Fe_{EuIG}$  at the interface is ferromagnetically coupled under TbIG/EuIG system with perpendicular magnetic anisotropy structures. Jakob *et al.* also noted on magnetic coupling in YIG/GdIG with in-plane anisotropy [44], suggesting the rationality of the Case A model [Fig. 4(a)]. Besides, it should be noticed that in our device structure, EuIG (which has not  $T_{comp}$  in bulk) is in direct contact with Pt during  $R_{AHE}$  measurements, thus providing a more direct proof of coupling in TbIG/EuIG system. The results presented here provide insights on better understanding the influence of adjacent iron garnet layers on the magnetization compensation and spin-Hall transport in garnet films with PMA structures, and would be useful for designing garnet heterostructures for spintronic devices such as magnon valves [29, 46].

#### 4. Conclusions

In summary, different thickness TbIG/EuIG system with tunable compensation temperature was studied. The  $T_{comp}$  can be tuned from 218 K (EuIG = 0 nm) to 156 K (EuIG = 20 nm) by changing the thickness of EuIG because of the ferromagnetic coupling of  $Fe^{3+}$  sublattices in the two different layers. This study provides an idea for controlling the compensation behavior in spintronic devices, and it would be helpful for designing the magnon valve with multilayer ferromagnetic devices.

### Data Availability

The data will be made available on request.

### Acknowledgements

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### Appendix A. Supplementary data

Supplementary data to this article can be found online.

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