# 1 Application of cascading thermoelectric generator and cooler for waste heat 2 recovery from solid oxide fuel cells

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9 Abstract: Besides electricity generation, solid oxide fuel cells (SOFCs) produce a significant amount of waste heat, which needs to be immediately removed to ensure durable operation of SOFCs. 10 However, the removal of waste heat greatly decreases the efficiency of SOFCs. In this study, a new 11 hybrid system mainly consisting of a thermoelectric generator, a thermoelectric cooler and an SOFC 12 is proposed to recover the waste heat from SOFC for performance enhancement. The thermodynamic 13 14 and electrochemical irreversible losses in each component are fully considered. An analytical relationship between the SOFC operating current density and the thermoelectric devices 15 dimensionless electric current is derived, from which the range of SOFC operating current density 16 that permits the thermoelectric devices to effectively work is determined. The equivalent power 17 output and efficiency for the hybrid system are specified under different operating current density 18 regions. The feasibility and effectiveness are illustrated by comparing the proposed hybrid system 19 with the stand-alone SOFC. It is found that the power density and efficiency of the proposed system 20 allow 2.3% and 4.6% larger than that of the stand-alone SOFC, respectively. Finally, various 21 parametric analyses are performed to discuss the effects of some design and operation parameters on 22 the hybrid system performance. 23

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25 Key Words: Solid oxide fuel cell; thermoelectric generator; thermoelectric cooler; waste heat

- 26 recovery; parametric study
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## 29 1. Introduction

The worldwide energy and environment crisis raise a strong demand for development of 30 31 efficient and clean energy technologies [1]. Fuel cells are promising power sources as they can efficiently and environmental-friendly convert the fuel chemical energy into electricity without 32 33 intermediary complicated energy conversion processes [2]. Among various fuel cells, SOFCs have attracted considerable interests due to their low emissions, fuel flexibility, inexpensive metal catalyst 34 and high electrochemical reaction rate [3-5]. In literatures, a great number of studies have focused 35 attention on aspects such as new electrode material fabrication [6, 7], lowering operating temperature 36 37 [8, 9], durability improvement [10, 11], new cell prototype development [12, 13], and single cell theoretical modeling [14-16]. 38

The high operating temperature of SOFCs also produces substantial amounts of high-grade heat 39 40 that are capable of powering a wide range of bottoming thermodynamic devices [17-21]. By developing cogeneration or trigeneration systems, the energy and exergy efficiencies of SOFC-based 41 hybrid systems could reach 80% and 60%, respectively [22-24]. Extensive studies have been 42 43 conducted on SOFC-based hybrid systems fueled with various kinds of fuels [25-27] and integrated with different bottom cycles [28-32] by means of various analysis approaches [33-35]. Liao et al. 44 45 proposed thermophotovoltaic cells to efficiently exploit the waste heat from SOFCs and compared the proposed hybrid system with some other SOFC based hybrid systems [28]. Mehrpooya et al. [29] 46 47 introduced a combined system containing SOFC-GT (SOFC-gas turbine) system, steam Rankine cycle and absorption refrigeration system. They used energy and exergy as well as economic factors 48 to discriminate optimum operation points of the combined system. Ma et al. [30] carried out 49 thermodynamic analyses of a trigeneration system by employing an ammonia-water mixture 50

thermodynamic cycle to harvest the waste heat from a natural gas fueled SOFC-GT. They examined 51 the dependence of system performance on several important thermodynamic parameters. Ebrahimi et 52 53 al. [31] proposed a novel cycle combining SOFC, micro gas turbine (MGT), and organic Rankine cycle (ORC) for power production. They evaluated the cycle behavior and investigated the effects of 54 55 ten design parameters on the overall cycle electrical efficiency. Eveloy et al. [32] integrated a hybrid SOFC-GT system and a reverse osmosis plant to enhance power generation and desalinate seawater. 56 Compared with existing standard gas turbine cycle, the proposed system could improve the exergy 57 efficiency by approximately 29% and simultaneously produce additional 494 m<sup>3</sup>/h fresh water. 58 59 Rokni et al. [33] performed thermodynamic and thermoeconomic analyses of a biomass gasified SOFC/Stirling heat engine hybrid system. It was found that a thermal efficiency of 0.424 LHV and a 60 net electric capacity of 120 kWe were obtained when the feedstock was 89.4 kg/h. Lee et al. [34] 61 62 evaluated the environmental impacts associated with a SOFC-based combined heat and power (CHP) generation system. It was showed that in the total environmental impact of manufacturing, the SOFC 63 stack accounted for 72% and the remaining balance-of-plant were responsible for the rest 28%. 64 65 Aminyavari et al. [35] implemented exergetic, economic and environmental analyses on an internal-reforming SOFC-GT hybrid system integrated with a steam Rankine cycle. After 66 multi-objective optimization procedures, the final optimum results demonstrated that the exergy 67 efficiency and total cost rate were 65.11% and 0.1374 €/s, respectively. 68

Thermoelectric devices include three semiconductor thermoelectric systems that convert waste heat into electric power (i.e., thermoelectric generator, TEG) or convert electricity into thermal energy for heating (i.e., thermoelectric heat pump, THP) or cooling (i.e., thermoelectric cooler, TEC) [36, 37]. As thermoelectric devices are compact, quiet, environmental-friendly and highly reliable, they are widely used in solar energy conversion [38], electronic cooling [39], residential air conditioning [40], and waste heat recovery [41, 42]. As all-solid-state energy converters, thermoelectric devices are natural good choices to recover the waste heat from SOFCs. To date, some scholars have employed TEGs to harvest waste heat from high-temperature fuel cells such as molten carbonate fuel cell [43], phosphoric acid fuel cell [44] and SOFC [45] for additional power generation. However, no one has yet used thermoelectric devices to recover the waste heat from SOFCs for cooling production, which is usually needed in buildings.

80 In this work, we present a new hybrid system that uses cascading thermoelectric devices to 81 recover the waste heat from hydrogen-fueled SOFCs for cooling applications. Based on electrochemistry and non-equilibrium thermodynamics, the primary irreversible losses of each 82 component with the hybrid system are described. The integration characteristics between the SOFC 83 84 and thermoelectric devices will be investigated. Analytical expressions for evaluating the hybrid system performance will be given, through which the generic performance characteristics are 85 discussed in detail. The feasibility and effectiveness for the proposed system will be demonstrated by 86 87 comparing with the stand-alone SOFCs. Furthermore, extensive parametric studies will be employed to reveal the sensitivity of the hybrid system performance to some design parameters and operating 88 conditions. 89

## 90 2. System description

The proposed hybrid system consists of an SOFC, two thermoelectric devices and a regenerator, as shown in Fig. 1. The thermoelectric devices consist of a TEG and a TEC, and the regenerator absorbs the heat in the outlet exhaust products to preheats the inlet reactants from ambient temperature  $T_0$  to the SOFC operating temperature T. The SOFC electrochemically converts the

95	fuel chemical energy into electrical power and high-grade waste heat. One part of the waste heat,	
96	$Q_{H}$ (J s <sup>-1</sup> ), is transferred from the SOFC at temperature T to the TEG for additional electrical	
97	power generation via the Seebeck effect, and the generated electricity is subsequently delivered to	
98	power the TEC, which extract heat, $Q_c$ (J s <sup>-1</sup> ), from the cooled space at temperature $T_c$ based on	
99	the Peltier effect. Another part of the waste heat, $Q_R$ (J s <sup>-1</sup> ), is consumed to compensate the	
100	regenerative losses in the regenerator. The rest part of the waste heat, $Q_L$ (J s <sup>-1</sup> ), is directly rejected	
101	to the environment. $Q_1$ and $Q_2$ are heat-transfer rates between the environment and the TEG and	
102	TEC, respectively.	
103	For simplification, following assumptions are adopted [46-50]:	
104	• SOFC and thermoelectric devices are in steady states;	
105	• Operating temperature and operating pressure of the SOFC are constants and uniform ;	
106	• Reactants are completely consumed in the SOFC;	
107	• Newton's law is used to describe the heat transfers within the system;	
108	• Thermoelectric elements in TEG and TEC are identical;	
109	• Geometric configurations of the thermoelectric devices are in the optimum form;	
110	• Thermoelectric elements are insulated both electrically and thermally from their	
111	surroundings, except at reservoir-junction contacts;	
112	• Electric current flows along the arm of a thermoelectric element;	
113	• External heat-transfer irreversibilities between the thermoelectric devices and the heat	
114	reservoirs are neglected;	
115	• Seebeck coefficient, thermal conductance, electrical resistance, and figure of merit of the	
116	thermoelectric devices are independent of temperature;	

• Thompson effects in thermoelectric devices are neglected.

## 118 **2.1. SOFC**

119 The typical SOFC shown in Fig. 1 is made of Ni | YSZ | LSM with hydrogen as fuel and air as 120 oxidant. The SOFC electrochemical performance is deteriorated by activation, concentration and 121 ohmic overpotentials, which can be characterized by the Bulter-Volmer equation, dusty gas model 122 and Ohm's law, respectively. Adopting the electrochemical model in previous papers [51, 52], the 123 power output  $P_{SOFC}$  and efficiency  $\eta_{SOFC}$  for a SOFC are given by

124 
$$P_{SOFC} = VI = jA \Big( E - V_{act,a} - V_{act,c} - V_{con,a} - V_{con,c} - V_{ohm} \Big),$$
(1)

125 and

126 
$$\eta_{SOFC} = \frac{P_{SOFC}}{-\Delta H}$$
, (2)

127 where

128 
$$V_{act,l} = \frac{RT}{F} \sinh^{-1} \left( \frac{j}{2j_{0,l}} \right) = \frac{RT}{F} \ln \left[ \frac{j}{2j_{0,l}} + \sqrt{\left( \frac{j}{2j_{0,l}} \right)^2 + 1} \right] \qquad (l = a, c),$$
(3)

129 
$$V_{con,a} = \frac{RT}{2F} \ln\left(\frac{1+j/j_{lH_2O}}{1-j/j_{lH_2}}\right),$$
 (4)

130 
$$V_{con,c} = \frac{RT}{4F} \ln \left[ \frac{C_{O_2}^0}{C_{T,c} / \delta_{O_2} + (C_{O_2}^0 - C_{T,c} / \delta_{O_2}) \exp(L_c jA\delta_{O_2} / (4FC_{T,c}D_{O_2}^{eff}))} \right],$$
(5)

131 
$$V_{ohm} = j \left( \frac{L_a}{\sigma_a} + \frac{L_c}{\sigma_c} + \frac{L_e}{\sigma_e} \right), \tag{6}$$

132 
$$j_{0,a} = \gamma_a \frac{72X[D_p - (D_p + D_s)\mathcal{E}]\mathcal{E}}{D_s^2 D_p^2 (1 - \sqrt{1 - X^2})} \left(\frac{P_{H_2}}{P_{ref}}\right) \left(\frac{P_{H_2O}}{P_{ref}}\right) \exp\left(-\frac{E_{act,a}}{RT}\right),$$
 (7)

133 
$$j_{0,c} = \gamma_c \frac{72X[D_p - (D_p + D_s)\varepsilon]\varepsilon}{D_s^2 D_p^2 (1 - \sqrt{1 - X^2})} \left(\frac{P_{O_2}}{P_{ref}}\right)^{0.25} \exp\left(\frac{-E_{act,c}}{RT}\right),$$
 (8)

134 and

135 
$$-\Delta \dot{H} = -I\Delta h/(2F)$$

## 137 **2.2. Thermoelectric devices**

As shown in Fig. 1, the TEG and TEC are operated between the heat sink (i.e., the ambience) 138 and the SOFC and the cooled space, respectively. The number of thermoelectric elements in TEG 139 and TEC are m and n, respectively, and the thermoelectric elements are electrically connected in 140 serials. Each element consists of a P-type semiconductor leg and an N-type semiconductor leg which 141 142 are connected by a thin copper. Neglecting the Thomson effect, the internal irreversible losses inside 143 a thermoelectric element are mainly from the Joule heat and the heat-conduction losses between the hot junction and cold junction. The Joule heat generates an amount of heat  $I_g^2 R_{te}$ , where  $I_g$  is the 144 electrical current flowing through a thermoelectric element, and  $R_{te}$  is the internal electrical 145 146 resistance of a thermoelectric element. The heat-conduction losses in TEG and TEC are, respectively,  $mK(T-T_0)$  and  $nK(T_0-T_c)$ , where K is the thermal conductance of a thermoelectric element. 147 Based on the non-equilibrium thermodynamics, the heat balance equations can be expressed as [47] 148

149 
$$Q_{H} = \alpha m I_{g} T - 0.5 m I_{g}^{2} R_{te} + m K (T - T_{0}), \qquad (10)$$

150 
$$Q_{1} = \alpha m I_{g} T_{0} + 0.5 m I_{g}^{2} R_{te} + m K (T - T_{0}), \qquad (11)$$

151 
$$Q_2 = \alpha n I_g T_0 + 0.5 n I_g^2 R_{te} - n K (T_0 - T_C), \qquad (12)$$

152 and

153 
$$Q_{c} = \alpha n I_{g} T_{c} - 0.5 n I_{g}^{2} R_{te} - n K (T_{0} - T_{c}), \qquad (13)$$

where  $\alpha_P$ ,  $\alpha_N$  and  $\alpha = (\alpha_P - \alpha_N)$  are the Seebeck coefficients of a P-type semiconductor leg, an N-type semiconductor leg and a thermoelectric element, respectively.

156 Based on Eqs. (10) - (13), one may define an internal structure parameter x to describe the

157 ratio of thermoelectric element numbers between the TEG and the TEC, i.e.,

158 
$$x = m/n = \frac{1 - \tau_2 + i/(ZT_0)}{1/\tau_1 - 1 - i/(ZT_0)},$$
(14)

159 where  $\tau_1 = T_0/T$ ,  $\tau_2 = T_C/T_0$ ,  $\tau = \tau_1 \tau_2 = T_C/T$ ,  $i = \alpha I_g/K$  and  $Z = \alpha^2/(KR_{te})$  are dimensionless

160 electric current and figure of merit of a thermoelectric element, respectively.

161 From Eqs. (10) – (14), the coefficient of performance (COP)  $\psi$  and the cooling rate (CR)  $\Phi$ 

162 of the cascading thermoelectric devices can be, respectively, expressed as

163 
$$\psi = \frac{Q_C}{Q_H} = \frac{\left[i\tau_2 - i^2/(2ZT_0) - 1 + \tau_2\right] \left[1 - \tau_1 - i\tau_1/(ZT_0)\right]}{\left[i - i^2/(2ZT_0) + 1 - \tau_1\right] \left[1 - \tau_2 + i/(ZT_0)\right]},$$
(15)

164 and

171

Eq.

(14),

the

165 
$$\Phi = Q_{c} = Km(1+1/x)T_{0}\frac{\left[i\tau_{2}-i^{2}/(2ZT_{0})-1+\tau_{2}\right]\left[1-\tau_{1}-i\tau_{1}/(ZT_{0})\right]}{1-\tau}.$$
(16)

166 When the thermoelectric devices begin to work, both the COP and the CR are larger than zero, 167 i.e.,  $\psi > 0$  and  $\Phi > 0$ . Solving the inequalities, the effective dimensionless electric current range is 168 given by

169 
$$i_1 < i < i_2,$$
 (17)

170 where 
$$i_1 = ZT_0\tau_2 \left[ 1 - \sqrt{1 - 2(1 - \tau_2)/(ZT_0\tau_2^2)} \right]$$
 and  $i_2 = ZT_0(1/\tau_1 - 1)$ . Substituting  $i_1$  and  $i_2$  into

internal

structure

parameters

are

172 
$$x_1 = \left(\tau_1 - \tau_1 \sqrt{1 - 2(1 - \tau_2)/(ZT_0\tau_2^2)}\right) / \left[1 - \tau_1 - \left(1 - \sqrt{1 - 2(1 - \tau_2)/(ZT_0\tau_2^2)}\right)\tau\right]$$
 and  $x_2 \to \infty$ ,

corresponding

173 respectively. To make the thermoelectric devices effective, the internal structure parameter of the174 thermoelectric devices should be designed as

175 
$$x > x_1$$
. (18)

176 Considering the exergy content difference between the cooling load and the electric power [53], 177 the equivalent power output  $P_{te}$  and efficiency  $\eta_{te}$  for the cascading thermoelectric devices can be 178 expressed as

179 
$$P_{td} = Q_C \left| 1 - T_0 / T_C \right| = K T_0 m \left( 1 + 1 / x \right) \left| 1 - T_0 / T_C \right| \frac{\left[ i \tau_2 - i^2 / (2ZT_0) - 1 + \tau_2 \right] \left[ 1 - \tau_1 - i \tau_1 / (ZT_0) \right]}{(1 - \tau)}, \quad (19)$$

180 and

181 
$$\eta_{td} = \frac{P_{td}}{Q_H} = KT_0 m (1 + 1/x) |1 - T_0/T_C| \frac{\left[i\tau_2 - i^2/(2ZT_0) - 1 + \tau_2\right] \left[1 - \tau_1 - i\tau_1/(ZT_0)\right]}{(1 - \tau)Q_H}.$$
 (20)

182

## 183 **2.3. Regenerator**

184 The thermodynamic losses in the regenerator are often expressed as [54]:

185 
$$Q_R = K_{re} A_{re} (1 - \beta) (T - T_0),$$
 (21)

186 where  $K_{re}$ ,  $A_{re}$  and  $\beta$  are the heat-transfer coefficient, heat-transfer area and the effectiveness of 187 the regenerator, respectively.

## 188 **2.4. Performance of the hybrid system**

189 The heat leakage rate  $Q_L$  between the SOFC and the environment can be described by [54]

190 
$$Q_L = K_L A_L (T - T_0),$$
 (22)

- 191 where  $K_L$  and  $A_L$  are the heat leakage coefficient and area, respectively.
- 192 According to the energy conservation law, one has

193 
$$Q_{H} = -\Delta \dot{H} - P_{SOFC} - Q_{R} - Q_{L} = -\frac{A\Delta h}{2F} \left[ \left( 1 - \eta_{SOFC} \right) j - \frac{2Fc_{1} \left( T - T_{0} \right)}{-\Delta h} - \frac{2Fc_{2} \left( T - T_{0} \right)}{-\Delta h} \right],$$
(23)

where  $c_1 = K_{re}A_{re}(1-\xi)/A$  and  $c_2 = K_LA_L/A$  are temperature-independent composite constants which are associated with the regenerative losses and the heat leakage, respectively.

Based on Eqs. (10) and (23), the numerical relationship between the dimensionless electric current of the thermoelectric devices, i, and the operating current density of SOFC, j, is determined by Eq. (24)

199 
$$i = ZT - \sqrt{Z^2 T^2 + 2Z (T - T_0) - \frac{ZA}{mK} \left[ \frac{-\Delta h}{F} (1 - \eta_{SOFC}) j - 2(c_1 + c_2) (T - T_0) \right]}.$$
 (24)

200 Using Eqs. (14) and (24) and the parameters given in Table 1 [43, 49, 51, 52, 55], one can generate the curves of  $x \sim j$  for different  $T_c$  and  $T_0$ , as shown in Fig. 2 (a). It is seen that x first 201 smoothly and then sharply increases with increasing j, and x increases as  $T_c$  decreases or  $T_0$ 202 increases. Compared with the variation of  $T_c$ , x is more sensitive to the variation of  $T_0$ . Fig. 2 (b) 203 shows the equivalent power density varying with the equivalent efficiency of the thermoelectric 204 devices at different  $T_0$  or  $T_c$ .  $P_{td,max}^*$ ,  $\eta_{td,max}$ ,  $P_{td,\eta}^*$  and  $\eta_{td,P}$  move towards larger ones as  $T_c$ 205 decreases or  $T_0$  increases. In a word, the thermoelectric devices display better performance under 206 the larger temperature gap  $(T_0 - T_C)$  condition. 207

Replacing the symbol *i* in Eq. (24) by the  $i_1$  and  $i_2$  in Eq. (17) respectively, one may numerically determine the lower bound  $j_1$  and upper bound  $j_2$  between which the thermoelectric devices enable to work. Thus, the effective operating current density interval is given by

211 
$$\Delta j = j_2 - j_1.$$
 (25)

Thus, the overall equivalent power output *P* and efficiency  $\eta$  for the proposed hybrid system can be, respectively, given by

214 
$$P = \begin{cases} = P_{SOFC} + P_{td} & (j_1 < j < j_2) \\ = P_{SOFC} & (j \le j_1 \text{ or } j \ge j_2) \end{cases}$$
(26)

215 and

216 
$$\eta = \begin{cases} = \frac{P_{SOFC} + P_{td}}{\bullet} & (j_1 < j < j_2) \\ -\Delta H & \\ = \eta_{SOFC} & (j \le j_1 \text{ or } j \ge j_2) \end{cases}$$
(27)

217

## 218 **3. Generic performance characteristics**

Figure 3 shows the generic performance characteristics and comparisons between the SOFC and 219 the thermoelectric devices and the proposed hybrid system. It is seen that  $P_{SOFC}^*$ ,  $P_{td}^*$  and  $P^*$  first 220 increase and then decrease as j increases. Different from the trends of power densities,  $\eta_{SOFC}$ 221 222 continuously decreases as j increases in the entire range, while  $\eta_{td}$  first increases and then decreases in the region of  $j_1 < j < j_2$ , and  $\eta$  first quickly decreases then somewhat increases and 223 finally drops as j increases. Outside the region of  $j_1 < j < j_2$ , the curves of  $P^* \sim j$  and  $\eta \sim j$ 224 are respectively overlapped with that of  $P_{SOFC}^* \sim j$  and  $\eta_{SOFC} \sim j$ , and the values of  $P_{td}^*$  and  $\eta_{td}$ 225 are equal to 0. It is also observed that  $P_{\max}^*$  is larger than both  $P_{SOFC,\max}^*$  and  $P_{td,\max}^*$ , and  $\eta_P$  is 226 larger than  $\eta_{SOFC, P}$ . For the parameters in Table 1,  $P_{max}^*$  is about 2.3% larger than  $P_{SOFC, max}^*$ , and 227  $\eta_P$  is about 4.6% larger than  $\eta_{SOFC, P}$ . Compared with the stand-alone SOFC, the performance 228 improvement of the proposed hybrid system is not adequately obvious. This is because the 229 230 heat-electricity efficiency of TEGs is relatively low and a large exergy destruction occurs in the cooling processes. Moreover,  $j_P$  is always different from  $j_{fc,P}$  because  $P_{SOFC}^*$  and  $P_{td}^*$  achieve 231 their peak values at different operating current densities. Combining the power output and efficiency 232 233 criteria, the optimum operating ranges for current density, power density and efficiency are suggested to be located in  $j \leq j_P$ ,  $P^* \leq P^*_{\max}$  and  $\eta \geq \eta_P$ , respectively. 234

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## 236 **4. Parametric studies**

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237 4.1. Effect of m
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A larger *m* indicates more thermoelectric elements are employed in TEG and TEC, which facilitates the performance improvement of the thermoelectric devices. As shown in Fig. 4 (a),  $P_{td,max}^*$ ,  $j_{td,P}$ ,  $j_{td,\eta}$ ,  $j_1$ ,  $j_2$  and  $\Delta j$  increase while  $\eta_{td,max}$  almost keeps invariant as *m*  increases, and curves of  $P_{td}^* \sim j$  and  $\eta_{td} \sim j$  move rightward with increasing m. For the hybrid system, the effects of m are only in the region of  $j_1 < j < j_2$ , as shown in Fig. 4 (b). It is interesting to note that  $P_{max}^*$  first increases and then decrease with the increasing m, and consequently, there exists an optimum value for m at which  $P_{max}^*$  attains its maximum. This is because the increase in  $P_{td}^*$  is less significantly than the decrease in  $P_{SOFC}^*$  for a larger m at which  $j_{td,P}$  exceeds  $j_{SOFC,P}$ . For parameters in Table 1, an optimum value for m is located between 8 and 12.

#### 248 **4.2. Effect of** *T*

249 A higher operating temperature T not only improves the performances of the SOFC and the thermoelectric devices but also leads to larger thermodynamic losses within the system. Because the 250 performance deterioration caused by the thermodynamic losses is less significant than the 251 252 performance improvements in the SOFC and thermoelectric devices, a higher operating temperature is desired. As shown in Fig. 5,  $P^*$  and  $\eta$  increase with increasing T, and the values of  $j_P$ ,  $j_S$ , 253  $j_1$ ,  $j_2$  and  $\Delta j$  increase with increasing T. The effect of T occurs in the whole range of j 254 255 and becomes more significantly at elevated T. However, a larger T would cause some problems such as performance degradation, slow start-up and shutdown cycles and higher costs for balance of 256 plant (BOP). Lowing the operating temperature of SOFCs to the intermediate temperature range 257 (500–700°C) has become an important topic in SOFC community [56]. 258

#### 259 **4.3. Effects of** *p*

Operating pressure not only affects the SOFC performance (via open circuit potential and overpotentials) but also influences the waste heat quantity transferred to the thermoelectric devices. Similar to T, the effects of operating pressure p on the system performance is in the whole region of *j*. Figure 6 shows that both  $P^*$  and  $\eta$  increase with increasing *p*, and the values of  $P^*_{\text{max}}$ ,  $P^*_{SOFC,\text{max}}$ ,  $j_p$ ,  $j_s$ ,  $j_1$ ,  $j_2$  and  $\Delta j$  are also increased with increasing *p*. The effect of *p* on the system performance becomes more significantly at larger operating current densities. For performance improvement, a larger *p* is always more preferable, but it also consumes some additional electricity in the inlet reactants compression processes. The black solid lines in Fig. 6 represents the operating pressure is chosen as 1.0 atm, which is the usual choice in practice.

#### 269 **4.4. Effects of** *K*

Thermal conductance K significantly affects the thermoelectric devices performance, as 270 shown in Fig. 7 (a). Similar to the effects of m,  $P_{td,max}^*$ ,  $j_{td,P}$ ,  $j_{td,\eta}$ ,  $j_1$ ,  $j_2$  and  $\Delta j$  increase 271 while  $\eta_{td,max}$  almost keeps invariant as K increases, and the curves of  $P_{td}^* \sim j$  and  $\eta_{td} \sim j$  move 272 rightward with increasing m. Different from T and p, Figure 7 (b) shows that the effects of K 273 on the whole system performance are only in the region of  $j_1 < j < j_2$ . Outside this region, the 274 curves of  $P^* \sim j$  and  $\eta \sim j$  are overlapped with that of the  $P^*_{SOFC} \sim j$  and  $\eta_{SOFC} \sim j$ , 275 respectively. The value of  $P_{\max}^*$  first increases and then decreases with increasing K, while the 276 value of  $j_P$  continuously increases as K increases. At a small K,  $P_{td}^*$  is much smaller than 277  $P_{SOFC}^*$  such that the whole system performance improvement is not obvious. As K increases, the 278 increase in  $P_{td}^*$  is less significantly than the decrease in  $P_{SOFC}^*$ , especially for the cases of 279  $j_{td,P} > j_{SOFC,P}$ . For the parameters in Table 1, an optimum value for K is found to be between 0.04 280 and 0.08. 281

#### 282 **4.5. Effects of** $c_1/c_2$

The integrated parameters  $c_1$  and  $c_2$  are closely related with the thermodynamic losses within the hybrid system. As shown in Fig. 8, the value of  $P_{\text{max}}^*$  almost keeps invariant for small  $c_1$  and  $c_2$ , and the effects of  $c_1$  and  $c_2$  only occur in the region of  $j_1 < j < j_2$ . As  $c_1$  and/or  $c_2$  increase, the value of  $P_{\text{max}}^*$  drops evidently, especially for the cases of  $j_{td,P} > j_{SOFC,P}$ . It is also seen that the values of  $j_P$ ,  $j_1$  and  $j_2$  are increased as  $c_1$  and/or  $c_2$  are increased. Numerical calculations further show that the value of  $\Delta j$  slightly decreases as  $c_1$  and/or  $c_2$  increase. The black solid lines in Fig. 8 represent a special case that both regenerative losses  $Q_R$  and heat leakage  $Q_L$  are negligible. In such a situation, Eqs. (23) and (24) can be, respectively, simplified into

$$Q_{H} = -\frac{jA\Delta h}{2F} \left(1 - \eta_{SOFC}\right), \qquad (28)$$

292 and

293 
$$i = ZT - \sqrt{Z^2 T^2 + 2Z (T - T_0) - \frac{ZA}{mK} \left[ \frac{-\Delta h}{F} (1 - \eta_{SOFC}) j \right]}.$$
 (29)

294

#### 295 **4. Conclusions**

A novel hybrid system consisting of SOFCs and cascading thermoelectric devices is proposed to 296 recover waste heat from SOFCs for simultaneous power generation and cooling applications. A 297 theoretical model is derived to evaluate the hybrid system performance, considering various 298 irreversible losses in the system. A numerical relationship for the output electric currents of the 299 SOFC and the cascading thermoelectric devices is derived, and the current density interval of SOFC 300 that allows the thermoelectric devices to work is determined. The internal structure parameter x301 and equivalent power density and efficiency of the thermoelectric devices varying with the heat 302 reservoir temperatures are revealed. The performance parameters for the hybrid system are specified 303 under different operating conditions, and the generic performance characteristics are demonstrated. 304 305 Numerical calculations show that the power density and efficiency of the proposed system allow 2.3% and 4.6% larger than that of the stand-alone SOFC, respectively. Comprehensive parametric 306

307	studies are conducted to discuss the effects of some design and operation parameters on the hybrid
308	system performance. It is found that there exist optimum values for the number of thermoelectric
309	elements in TEG and the thermal conductance of a thermoelectric element for maximizing the hybrid
310	system equivalent power density.

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## 315 **References**

- 316 [1] Panwar NL, Kaushik SC, Kothari S. Role of renewable energy sources in environmental
- 317 protection: a review. Renew Sust Energ Rev 2011; 15: 1513-24.
- 318 [2] Lucia U. Overview of fuel cells. Renew Sust Energ Rev 2014; 30: 164-9.
- 319 [3] Mekhilef S, Saidur R, Safari A. Comparative study of different fuel cell technologies. Renew
- 320 Sust Energ Rev 2012; 16: 981-9.
- 321 [4] Choudhury A, Chandra H, Arora A. Application of solid oxide fuel cell technology for power
- 322 generation—A review. Renew Sust Energ Rev 2013; 20: 430-42.
- 323 [5] Dong F, Ni M, He W, Chen Y, Yang G, Chen D, Shao Z. An efficient electrocatalyst as cathode
- material for solid oxide fuel cells:  $BaFe_{0.95}Sn_{0.05}O_{3-\delta}$ . J Power Sources 2016; 326: 459-65.
- [6] Sengodan S, Choi S, Jun A, Shin TH, Ju YW, Jeong HY, et al. Layered oxygen-deficient double
- perovskite as an efficient and stable anode for direct hydrocarbon solid oxide fuel cells. Nat Mat
  2015; 14: 205-9.
- 328 [7] Mahato N, Banerjee A, Gupta A, Omar S, Balani K. Progress in material selection for solid oxide
- fuel cell technology: A review. Prog Mat Sci 2015; 72: 141-337.
- [8] Huang J, Xie F, Wang C, Mao Z. Development of solid oxide fuel cell materials for
  intermediate-to-low temperature operation. Int J Hydrogen Energy 2012; 37: 877-83.
- [9] Recent progress on solid oxide fuel cell: Lowing temperature and utilizing non-hydrogen fuels.
- 333 Int J Hydrogen Energy 2013; 38: 16498-517.
- 334 [10] Lanzini A, Leone P, Guerra C, Smeacetto F, Brandon NP, Santarelli M. Durability of anode
- supported Solid Oxide Fuel Cells (SOFC) under direct dry-reforming of methane. Chem Eng J 2013;
- 336 220: 254-63.

- [11] Sumi H, Yamaguchi T, Suzuki T, Shimada H, Hamamoto K, Fujishiro Y. Effects of anode
  microstructures on durability of microtubular solid oxide fuel cells during internal steam reforming
  of methane. Electrochem Commun 2014; 49: 34-7.
- [12] Fan L, Su PC. Layer-structured LiNi<sub>0.8</sub>Co<sub>0.2</sub>O<sub>2</sub>: A new triple ( $H^+/O^{2-}/e^{-}$ ) conducting cathode for
- low temperature proton conducting solid oxide fuel cells. J Power Sources 2016; 306: 369-77.
- 342 [13] Huang K, Singhal SC. Cathode-supported tubular solid oxide fuel cell technology: A critical
- 343 review. J Power Sources 2013; 237: 84-97.
- [14] He W, Zou J, Wang B, Vilayurganapathy S, Zhou M, Lin X, et al. Gas transport in porous
- electrodes of solid oxide fuel cells: A review on diffusion and diffusivity measurement. J Power
  Sources 2013; 237: 64-73.
- [15] Bertei A, Nicolella C. Common inconsistencies in modeling gas transport in porous electrode:
  The dusty-gas model and the Fick's law. J Power Sources 2015; 279: 133-7.
- [16] Abdeljawad F, Volker B, Davis R, McMeeking RM, Haataja M. Connecting microstructural
  coarsening processes to electrochemical performance in solid oxide fuel cells: An integrated
  modeling approach. J Power Sources 2014; 250: 319-31.
- - [17] McLarty D, Brouwer J, Samuelsen S. Fuel cell–gas turbine hybrid system design part I: Steady
    state performance. J Power Sources 2014; 257: 412-20.
  - [18] Rokni M. Thermodynamic analysis of SOFC (solid oxide fuel cell)–Stirling hybrid plants using
    alternative fuels. Energy 2013; 61: 87-97.
  - [19] Rokni M. Biomass gasification integrated with a solid oxide fuel cell and Stirling engine.
    Energy 2014; 77: 6-18.
  - 358 [20] Buonomano A, Calise F, d'Accadia MD, Palombo A, Vicidomini M. Hybrid solid oxide fuel

- cells–gas turbine systems for combined heat and power: a review. Appl Energy 2015; 156: 32-85.
- 360 [21] Zhang X, Chan SH, Li G, Ho HK, Li J, Feng Z. A review of integration strategies for solid oxide
- 361 fuel cells. J Power Sources 2010; 195: 685-702.
- 362 [22] Khani L, Mahmoudi SMS, Chitsaz A, Rosen MA. Energy and exergoeconomic evaluation of a
- new power/cooling cogeneration system based on a solid oxide fuel cell. Energy 2016; 94: 64-77.
- [23] Tippawan P, Arpornwichanop A, Dincer I. Energy and exergy analyses of an ethanol-fueled
  solid oxide fuel cell for a trigeneration system. Energy 2015; 87: 228-39.
- [24] Ranjbar F, Chitsaz A, Mahmoudi SMS, Khalilarya S, Rosen MA. Energy and exergy
  assessments of a novel trigeneration system based on a solid oxide fuel cell. Energy Convers
  Managem 2014; 87: 318-27.
- 369 [25] Gholamian E, Zare V, Mousavi SM. Integration of biomass gasification with a solid oxide fuel
- 370 cell in a combined cooling, heating and power system: A thermodynamic and environmental analysis.
- 371 Int J Hydrogen Energy 2016; 41: 20396-406.
- [26] Lv X, Gu C, Liu X, Weng Y. Effect of gasified biomass fuel on load characteristics of an
  intermediate-temperature solid oxide fuel cell and gas turbine hybrid system. Int J Hydrogen Energy
  2016; 41: 9563-76.
- 375 [27] Borji M, Atashkari K, Ghorbani S, Nariman-Zadeh N. Parametric analysis and Pareto
  376 optimization of an integrated autothermal biomass gasification, solid oxide fuel cell and micro gas
  377 turbine CHP system. Int J Hydrogen Energy 2015; 40: 14202-23.
- [28] Liao T, Cai L, Zhao Y, Chen J. Efficiently exploiting the waste heat in solid oxide fuel cell by
  means of thermophotovoltaic cell. J Power Sources 2016; 306: 666-73.
- 380 [29] Mehrpooya M, Dehghani H, Moosavian SMA. Optimal design of solid oxide fuel cell,

- ammonia-water single effect absorption cycle and Rankine steam cycle hybrid system. J Power
  Sources 2016; 306: 107-23.
- [30] Ma S, Wang J, Yan Z, Dai Y, Lu B. Thermodynamic analysis of a new combined cooling, heat
  and power system driven by solid oxide fuel cell based on ammonia–water mixture. J Power Sources
  2011; 196: 8463-71.
- [31] Ebrahimi M, Moradpoor I. Combined solid oxide fuel cell, micro-gas turbine and organic
  Rankine cycle for power generation (SOFC–MGT–ORC). Energy Convers Managem 2016; 116:
  120-33.
- [32] Eveloy V, Rodgers P, Qiu L. Integration of an atmospheric solid oxide fuel cell-gas turbine
  system with reverse osmosis for distributed seawater desalination in a process facility. Energy
  Convers Managem 2016; 126: 944-59.
- [33] Rokni M. Thermodynamic and thermoeconomic analysis of a system with biomass gasification,
  solid oxide fuel cell (SOFC) and Stirling engine. Energy 2014; 76: 19-31.
- 394 [34] Lee YD, Ahn KY, Morosuk T, Tsatsaronis G. Environmental impact assessment of a solid-oxide
- fuel-cell-based combined-heat-and-power-generation system. Energy 2015; 79: 455-466.
- 396 [35] Aminyavari M, Mamaghani A H, Shirazi A, Najafi B, Rinaldi F. Exergetic, economic, and
- 397 environmental evaluations and multi-objective optimization of an internal-reforming SOFC-gas
- turbine cycle coupled with a Rankine cycle. Appl Therm Eng 2016; 108: 833-46.
- [36] Bell LE. Cooling, heating, generating power, and recovering waste heat with thermoelectric
  systems. Science 2008; 321: 1457-61.
- 401 [37] Elsheikh MH, Shnawah DA, Sabri MFM, Said SBM, Hassan MH, Bashir MB, et al. A review
- 402 on thermoelectric renewable energy: Principle parameters that affect their performance. Renew Sust

- 403 Energ Rev 2014; 30: 337-55.
- [38] Moraes FS, Santos LC, Alencar RN, Alencar RN, Sempels EV, Sandoval V SC, et al. Solar
  thermoelectric generator performance relative to air speed. Energy Convers Managem 2015; 99:
  326-33.
- 407 [39] Ma M, Yu J. An analysis on a two-stage cascade thermoelectric cooler for electronics cooling
  408 applications. Int J Refrig 2014; 38: 352-57.
- 409 [40] Kim YW, Ramousse J, Fraisse G, Dalicieux P, Baranek P. Optimal sizing of a thermoelectric
- 410 heat pump (THP) for heating energy-efficient buildings. Energy Build 2014; 70: 106-16.
- 411 [41] Sun X, Liang X, Shu G, Tian H, Wei H, Wang X. Comparison of the two-stage and traditional
- 412 single-stage thermoelectric generator in recovering the waste heat of the high temperature exhaust
- 413 gas of internal combustion engine. Energy 2014; 77: 489-98.
- [42] Zhang H, Wang H, Zhu X, Qiu YJ, Li K, Chen R, et al. A review of waste heat recovery
  technologies towards molten slag in steel industry. Appl energy 2013; 112: 956-66.
- 416 [43] Wu S, Zhang H, Ni M. Performance assessment of a hybrid system integrating a molten
- 417 carbonate fuel cell and a thermoelectric generator. Energy 2016; 112: 520-7.
- 418 [44] Chen X, Wang Y, Cai L, Zhou Y. Maximum power output and load matching of a phosphoric
- acid fuel cell-thermoelectric generator hybrid system. J Power Sources 2015; 294: 430-6.
- 420 [45] Chen X, Pan Y, Chen J. Performance and evaluation of a fuel cell-thermoelectric generator
- 421 hybrid system. Fuel Cells 2010; 10: 1164-70.
- 422 [46] Chan SH, Khor KA, Xia ZT. A complete polarization model of a solid oxide fuel cell and its
- sensitivity to the change of cell component thickness. J Power Sources 2001; 93: 130-40.
- 424 [47] Chen L, Li J, Sun F, Wu C. Performance optimization of a two-stage semiconductor

- 425 thermoelectric-generator. Appl Energy 2005; 82: 300-12.
- [48] Khattab NM, Shenawy ETE. Optimal operation of thermoelectric cooler driven by solar
  thermoelectric generator. Energy Convers Manag 2006; 47: 407-26.
- [49] Chen X, Lin B, Chen J. The parametric optimum design of a new combined system of
  semiconductor thermoelectric devices. Appl Energy 2006; 83: 681-6.
- 430 [50] Chen WH, Wang CC, Hung CI. Geometric effect on cooling power and performance of an
- 431 integrated thermoelectric generation-cooling system. Energy Convers Manag 2014; 87: 566-75.
- 432 [51] Ni M, Leung MKH, Leung DYC. Parametric study of solid oxide fuel cell performance. Energy
- 433 Convers Manag 2007; 48: 1525-35.
- 434 [52] Zhang H, Chen J, Zhang J. Performance analysis and parametric study of a solid oxide fuel cell
- 435 fueled by carbon monoxide. Int J Hydrogen Energy 2013; 38: 16354-64.
- 436 [53] Chen X, Wang Y, Zhou Y. Equivalent power output and parametric optimum design of a PEM
- 437 fuel cell-based hybrid system. Int J Electr Power Energy Sys 2014; 63: 429-33.
- 438 [54] Zhao M, Zhang H, Hu Z, Zhang Z, Zhang J. Performance characteristics of a direct carbon fuel
- 439 cell/thermoelectric generator hybrid system. Energy Convers Manag 2015; 89: 683-9.
- 440 [55] Liang X, Sun X, Tian H, Shu G, Wang Y, Wang X. Comparison and parameter optimization of a
- 441 two-stage thermoelectric generator using high temperature exhaust of internal combustion engine.
- 442 Appl Energy 2014; 130: 190-9.
- [56] Wachsman ED, Lee KT. Lowering the temperature of solid oxide fuel cells. Science 2011; 334:
  935-9.
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- 446

#### 447 **Table captions:**

448 Table 1. Parameters used in the modeling [43, 49, 51, 52, 55].

### 449 **Figure captions:**

450 Fig. 1. A conceptual diagram of an SOFC/ thermoelectric devices hybrid system.

451 Fig. 2. Curves of (a)  $x \sim j$ , and (b)  $P_{td}^* \sim \eta_{td}$  at different  $T_0$  or  $T_C$ , where  $P_{td}^* = P_{td} / A$  is the 452 equivalent power density of the thermoelectric devices,  $P_{td,max}^*$  and  $\eta_{td,max}$  are respectively 453 the maximum power density and maximum efficiency of the thermoelectric devices,  $P_{td,\eta}^*$ 454 and  $\eta_{td,P}$  are the power density at  $\eta_{td,max}$  and the efficiency at  $P_{td,max}^*$ , respectively.

Fig. 3. Comparisons of (a) power densities and (b) efficiencies between the SOFC, thermoelectric 455 devices and hybrid system, where  $P_{SOFC}^* = P_{SOFC} / A$  and  $P^* = P / A$  are, power densities for 456 SOFC and hybrid system, respectively;  $P_{SOFC,max}^*$ ,  $P_{td,max}^*$  and  $P_{max}^*$  are maximum power 457 densities of the SOFC, thermoelectric devices and hybrid system, respectively;  $\eta_{td,max}$  is the 458 maximum efficiency of the thermoelectric devices;  $j_P$  and  $\eta_P$  are operating current 459 density and efficiency at  $P_{\max}^*$ , respectively;  $j_{fc,P}$  is the operating current density at 460  $P_{SOFC,\max}^*$ ;  $j_{td,P}$  and  $j_{td,\eta}$  are operating current densities at  $P_{td,\max}^*$  and  $\eta_{td,\max}$ , respectively; 461  $j_s$  is the stagnation current density from which the SOFC does not output electricity any 462 463 more.

- 464 Fig. 4. Effects of the number of thermoelectric elements in TEG on the hybrid system performance.
- 465 Fig. 5. Effects of the operating temperature on the hybrid system performance.
- 466 Fig. 6. Effects of the operating pressure on the hybrid system performance.
- 467 Fig. 7. Effects of the thermal conductance of a thermoelectric element on the hybrid system468 performance.

469 Fig. 8. Effects of the thermodynamic losses related parameters on the hybrid system performance.

## 471 Table 1

Parameter	Value	
Operating pressure, $P$ (atm)	1.0	
Operating temperature, $T(K)$	1073	
Anode interface gas compositions	95 % H <sub>2</sub> +5 % H <sub>2</sub> O	
Cathode interface gas compositions	79 % N <sub>2</sub> +21% O <sub>2</sub>	
Activation energy for anode, $E_{acta}$ (J mol <sup>-1</sup> )	1.0×10 <sup>5</sup> [51]	
Activation energy for cathode, $E_{actc}$ (J mol <sup>-1</sup> )	1.2×10 <sup>5</sup> [51]	
Electrode porosity, $\varepsilon$	0.48 [51]	
Electrode tortuosity, $\xi$	5.4 [51]	
Average pore diameter, $D_p$ (m)	3.0×10 <sup>-6</sup> [51]	
Average grain size, $D_s$ (m)	1.5×10 <sup>-6</sup> [51]	
Average length of grain contact, <i>X</i>	0.7 [51]	
Anode thickness, $L_a$ (m)	5.0×10 <sup>-4</sup>	
Anode electric conductivity, $\sigma_a (\Omega^{-1} \text{ m}^{-1})$	8.0×10 <sup>4</sup> [52]	
Cathode thickness, $L_c$ (m)	5.0×10 <sup>-5</sup>	
Cathode electric conductivity, $\sigma_c (\Omega^{-1} \text{ m}^{-1})$	8.4×10 <sup>3</sup> [52]	
Electrolyte thickness, $L_e$ (m)	5.0×10 <sup>-5</sup>	
Electrolyte ionic conductivity, $\sigma_e (\Omega^{-1} \text{ m}^{-1})$	3.34×10 <sup>4</sup> exp(-1.03×10 <sup>4</sup> /T) [52]	
Effective surface area of the SOFC, $A(m^2)$	4.0×10 <sup>-2</sup>	
Sectional area of a thermoelectric element, (m <sup>2</sup> )	0.005 [55]	
Heat conductivity of a thermoelectric element, $K(W)$	0.04	
$K^{-1} m^{-1}$ )	0.04	
Figure of merit of the thermoelectric materials, $ZT_0$	1.0 [49]	
Number of TEGs, <i>m</i>	8	
Constants in Eq. (23), $c_1$ ; $c_2$ (W m <sup>-2</sup> K <sup>-1</sup> )	0.1; 0.1 [43]	
Temperature of the ambience, $T_0$ (K)	305	
Temperature of cooled space , $T_C$ (K)	290	

473 Fig. 1.







480 Fig. 3.



485 Fig. 4.





489 Fig. 5.



493 Fig. 6.







501 Fig. 8.

