

# 1     **Temperature analysis of a long-span suspension bridge based on field** 2                                   **monitoring and numerical simulation**

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5

## 6     **Abstract**

7     Structural temperature is an important form of loading for bridges, particularly for long-span steel  
8     structures. In this study, the temperature distribution of the Humber Bridge in United Kingdom is  
9     investigated based on numerical simulation and field measurements. A 2D fine finite element (FE)  
10    model of a typical section of the box girder of this long-span suspension bridge is constructed. The  
11    time-dependent thermal boundary conditions are determined based on the field meteorological  
12    measurements with external surface heat convection coefficients varying according to differing local  
13    wind speeds they experience. Pre-analysis is adopted to determine the initial thermal condition of the  
14    model, then transient heat-transfer analysis is performed and the time-dependent temperature  
15    distribution of the bridge is obtained leading to numerical temperature data at different locations in  
16    different time that are in good agreement with the measured counterparts. The vertical and  
17    transversal temperature differences of the box girder are also investigated. Both measured and  
18    numerical results show that the transversal temperature variation across the streamlined girder is  
19    significant. The effects of the box girder shape, pavement of the upper webs, and bridge orientation  
20    on the transversal temperature difference are finally investigated.  
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22    **Keywords:** long-span suspension bridge, temperature behavior, field monitoring, heat-transfer  
23    analysis, transversal temperature difference  
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## 25 **1. Introduction**

26

27 Bridges are subject to daily, seasonally, and annually varying environmental thermal effects caused  
28 by solar radiation and surrounding air temperature. The changes in structural temperature and  
29 temperature distribution of a bridge result in movements and deformations, heavy demands on  
30 connections and supports and potentially excessive stresses and cracks. For example, repeated cycles  
31 of heating and cooling induced by thermal actions may result in large amplitude stress cycles and  
32 fatigue damages. In fact structural behavior of bridges is more significantly affected by  
33 environmental thermal effects than by external operational loads (Priestley, 1976, 1978; Kennedy and  
34 Soliman, 1987; Salawu, 1997; Xia et al., 2011; Bojovic and Velovic, 2014).

35

36 Analyzing the thermal effects on bridges mainly consists of two studies: structural temperature and  
37 induced structural responses. To calculate temperature-induced responses and evaluate the thermal  
38 effects on bridge behavior, the entire structural temperature distribution must be accurately known.  
39 Since the 1960s, considerable efforts have been devoted to investigating temperature distribution and  
40 thermal effects on bridges based on laboratory experiments and field investigations and Zuk (1965)  
41 was considered the first to study the thermal behavior of bridges. He identified the effects of solar  
42 radiation, air temperature, wind, humidity, and material types on temperature distribution by  
43 investigating several highway bridges. Emanuel and Reynolds (1978) investigated the temperature  
44 variations of a composite-girder highway bridge and calculated the bridge temperatures as a function  
45 of time by using finite element (FE) analysis. Since the negative effects of temperature are mainly  
46 induced by uneven temperature distribution, the temperature gradient (difference) of various types of  
47 bridges became the research focus then. Priestley (1976, 1978) analyzed the vertical temperature  
48 gradients of pre-stressed and reinforced concrete bridges and compared the analytical results with  
49 those from laboratory and field experiments. Kennedy (1987) studied the temperature distribution of  
50 composite bridges and proposed the linear temperature distribution through the depth of the slab and  
51 uniform distribution through the depth of the steel beam by synthesizing several theoretical and  
52 experimental studies on prototype bridges. Churchward and Yehuda (1981) continuously recorded  
53 the temperature of a post-stressed twin box concrete bridge and presented an analytical expression of

54 the vertical temperature profile as a function of the maximum differential temperature and  
55 environmental parameter insolation. A long-term field measurement was conducted by Dilger et al.  
56 (1981) to investigate the thermal effects on a continuous, steel-concrete composite box girder bridge  
57 during its construction and its first three years of operation.

58

59 Analytical equations and numerical methods have also been proposed to calculate the temperature  
60 distribution of simple structures, including girder bridges, since the 1970s (Emerson, 1973; Hunt and  
61 Nigel, 1975; Priestley, 1976; Kehlbeck, 1981; Elbadry and Ghali, 1983). These methods are basically  
62 one-dimensional (1D) approaches that assume temperature only varies along the depth of the  
63 cross-section and that variations along other directions are insignificant. As structural configuration  
64 becomes increasingly complicated, the 1D models can hardly capture the temperature variation and  
65 distribution of relatively complicated structures, including box girder bridges. Elbadry and Ghali  
66 (1983) proposed a two-dimensional (2D) FE method to determine the time-dependent temperature  
67 variation of a concrete box girder bridge by considering geometry, location, orientation, material, and  
68 meteorological conditions. Tong et al. (2001, 2002) conducted such a study on a steel bridge in Hong  
69 Kong while Lucas et al. (2003) statistically analyzed the average temperature and thermal gradient of  
70 a steel box girder bridge. These studies show that steel bridges have a large temperature gradient  
71 along the cross-section and significant variation over time because of the high conductivity of steel.

72

73 Naturally the top surface of a box-girder bridge receives more solar radiation than the web and soffit  
74 in general, resulting in considerable vertical temperature difference, an effect that has been widely  
75 investigated, with detailed specifications provided in bridge design codes, for example Eurocode 1  
76 (European Committee for Standardization, 2003). The transversal temperature difference (TTD) is  
77 usually smaller than the vertical difference for most types of bridge, especially for concrete bridges  
78 (Mondal and DeWolf, 2007), hence present codes do not provide much information on this. However,  
79 particular types of bridge may also experience significant TTD and the induced structural responses,  
80 such as transverse movements, can pose a significant threat to structural performance (Moorthy and  
81 Roeder, 1992). For example, Kromanis et al. (2014) investigated the quasi-static temperature effects  
82 on the Cleddau Bridge based on continuous monitoring measurements, showing the TTD up to 15  
83 degrees. It resulted in plan bending of the main box girder, generating plan rotations at the roller

84 bearings. These movements, which were not considered at the design stage, imposed large forces on  
85 the bearings and led to their degradation.

86

87 The number of constructed long-span bridges has dramatically increased over the past decades.  
88 These bridges have a complicated temperature distribution because their main structural elements,  
89 including decks, towers, and main cables, have different thermal characteristics. The temperature  
90 action of these bridges is a major concern, and long-term monitoring has become a standard  
91 procedure through rapid development of structural health monitoring (SHM). While the prime focus  
92 of these systems is deformations and their temporal and spatial derivatives, a number of exercises  
93 have used temperature data to study thermal effects. For example Xu et al. (2010) analyzed the  
94 temperature characteristics of Tsing Ma Bridge using several years of monitoring data, while Xia et  
95 al. (2013) performed extensive thermal and structural analyses of the temperature effects on the  
96 bridge. Ding et al. (2012, 2013) used long-term monitoring data to estimate the extreme temperature  
97 differences of a steel box girder suspension bridge, while Westgate (2012) and de Battista et al. (2014)  
98 investigated the effects of traffic and thermal actions on the static and dynamic responses of Tamar  
99 Suspension Bridge.

100

101 To resist wind loading these long-span bridges normally have a wide cross-section, resulting in  
102 relatively large transversal temperature differences, an effect which has not been sufficiently  
103 investigated in previous studies. The Humber Bridge, on which a long-term SHM system has been  
104 installed, provides an opportunity for an in-depth study of this issue. This paper is organized as  
105 follows:

- 106 1. The Humber Bridge and the installed SHM system are briefly introduced.
- 107 2. The thermal boundary conditions of the bridge are discussed.
- 108 3. The FE model of the box girder is developed, and thermal analyses are performed for each  
109 model.
- 110 4. The analytical results are compared with the measurements to validate the method.
- 111 5. Time-dependent structural temperature and distribution are obtained.
- 112 6. The temperature differences, particularly TTD, of the box girder are investigated.
- 113 7. Conclusions and suggestions are drawn for analyzing temperature actions of long-span

114 suspension bridges.

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116

## 117 **2. Humber Bridge and the monitoring system**

### 118 **2.1 Humber Bridge**

119

120 The Humber Bridge, completed in June 1981 has a total length of 2220 m with an asymmetric layout  
121 comprising the 280 m Hessle side span, 1410 m main span, and 530 m Barton (south) side span, as  
122 shown in Fig. 1. The main span was the longest in the world for 17 years from its inauguration and is  
123 at the time of writing the seventh longest of its type in the world.

124

125 The bridge girder is not continuous through the towers, having a complex arrangement of bearings  
126 and expansion joints to accommodate movement due to wind, traffic and thermal loading. It was  
127 assembled from 124 box segments, each typically 18.1 m long, 22 m wide, and 4.5 m high, with four  
128 stiffened bulkheads and has cantilevered footpaths and cycle tracks bringing the total width to 28 m.  
129 The upper roadway surface of the box is an 18.2 m wide orthotropic steel deck that was originally  
130 covered with 41 mm thick rubberized bitumen asphalt, but which has been replaced at least once  
131 while cantilevers retain a thin asphalt surfacing (Brownjohn et al., 1987).

132

### 133 **2.2 SHM system of the Humber Bridge**

134

135 The bridge has several systems for monitoring traffic, weather and main cable condition (Lynch,  
136 2012). However, the most relevant monitoring system for this study was installed on the bridge in  
137 2011. The SHM system consists of three modules: the sensors, the transmission network, and the  
138 data management system (Koo et al., 2011, Brownjohn et al., 2014). The sensors are divided into  
139 four types according to the sensing parameter.

140 1) Sensors for meteorological parameters. A new weather station was installed at the mid-span of  
141 the bridge which supplements data from anemometers and air temperature sensors previously

142 by the operator. Meteorological data from nearby Humberside Airport are also available and  
143 are integrated into the database of the SHM system.

144 2) Sensors for dynamics responses. Three servo-accelerometers feed acceleration signals into an  
145 automated process for real-time estimation of modal frequencies and damping ratios.

146 3) Sensors for static responses. Real-time kinematic position data are available for GPS antennae  
147 fixed to each main cable at mid-span, with correction data are provided by a reference station  
148 at the Hessle anchorage. This system provides the primary position data for the bridge. Four  
149 laser extensometers, one on each columns of the Hessle and Barton towers provide bearing  
150 movement data.

151 4) Sensors for structural temperature. Four thermocouples were installed to record the  
152 temperature of the box girder at the mid-span located on the top ( $T_t$ ), bottom ( $T_b$ ), east ( $T_e$ ),  
153 and west ( $T_w$ ) surfaces of the box girder. Fig. 2 depicts the two temperature sensors installed  
154 during construction at the middle of the left lanes of the northbound carriageway to collect  
155 the surface temperature of the asphalt ( $T_s$ ) and the ground temperature ( $T_g$ ) in the interface  
156 between the steel surface and paved asphalt.

157

158

### 159 **3. Thermal analysis of bridge structures**

#### 160 **3.1 Thermal environment of a box girder bridge**

161

162 The temperature differences along the longitudinal direction of a bridge are generally neglected.  
163 Therefore, a single box girder section can be used to analyze the temperature distribution of the  
164 bridge, the thermal environment of which is shown in Fig. 3. The heat transfer process of a box  
165 girder bridge exposed to the open environment consists of heat conduction, heat convection, and  
166 thermal radiation (Kehlbeck, 1981). Heat conduction exists in the interior of the box girder and is  
167 governed by the Fourier heat-transfer equation. Heat convection is a kind of energy exchange  
168 between the solid surface and the surrounding fluid that results from the diffusion and bulk motion of  
169 the fluid. Thermal radiation is a kind of energy transfer caused by the structural surface emitting and

170 absorbing radiation.

171

172 Several forms of radiation, including solar, atmospheric, diffuse, reflected, environmental, and  
173 structural irradiation, are emitted or absorbed by a bridge surface. The direct solar radiation from the  
174 sun striking is the main radiation factor affecting bridges. Atmospheric radiation is the gas in the  
175 atmosphere emitting radiation, and governed by the Stefan–Boltzmann law. Diffuse radiation is the  
176 solar radiation scattered by molecules and particles in the atmosphere. The environmental radiation is  
177 the sum of the radiation emitted by surrounding matter of the ground surface, including structures,  
178 trees, rocks, and roads. This radiation also follows the Stefan–Boltzmann law. Reflected radiation  
179 describes the non-atmospheric effects such as the ground reflecting the direct solar and diffuse  
180 radiations. The structural irradiation is the radiation emitted from the bridge surface, also governed  
181 by the Stefan–Boltzmann law.

182

### 183 **3.2 Heat transfer analysis**

184

#### 185 **(1) Heat transfer theory**

186 The temperature of a point in a structure can be expressed as  $T = T(x, y, z, t)$ , where  $x$ ,  $y$ , and  $z$  are the  
187 Cartesian coordinates of the point and  $t$  is the time. Heat transfer theory is governed by the typical  
188 Fourier heat-transfer equation:

$$189 \quad \rho c \frac{\partial T}{\partial t} = k \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) \quad (1)$$

190 where  $k$  is the isotropic thermal conductivity coefficient,  $\rho$  is the density, and  $c$  is the specific heat of  
191 the material. The temperature field of a structure at a specific time can be obtained by solving the  
192 above Fourier partial differential equation under initial and boundary conditions, which will be  
193 briefed in following sections.

194

#### 195 **(2) Thermal boundary conditions**

196 The boundary conditions for structural thermal analysis can be generally classified into three types  
197 (Lienhard and Lienhard, 2003). Type 1 denotes that the temperature of the structural boundary is

198 exactly known, Type 2 the heat flux on the structural boundary is determinate, and Type 3 the heat  
199 flux on the boundary is proportional to the difference between the air temperature and the bridge  
200 surface temperature.

201

202 The boundary conditions associated with Eq. 1 for the thermal analysis of a bridge can be written as  
203 a combination of Types 2 and 3 (Elbadry and Ghali, 1983).

$$204 \quad k \frac{\partial T}{\partial n} = h(T_a - T_v) + q \quad (2)$$

205 where  $n$  is normal to the surface,  $h = h_c + h_r$  ( $\text{W}/\text{m}^2\text{K}$ ) is the heat transfer coefficient combining the  
206 heat transfer coefficients of convection ( $h_c$ ) and thermal irradiation ( $h_r$ ),  $T_a$  is the air temperature,  $T_v$   
207 is the structural surface temperature, and  $q$  is the boundary heat exchange per unit area (heat fluxes,  
208 positive for inflow).

209

210 The heat transfer coefficient of convection ( $h_c$ ) is related to wind speed. Kehlbeck (1981) proposed  
211 an empirical equation to calculate the convection coefficient when wind speed  $w \leq 5$  m/s:

$$212 \quad h_c = 2.6 \times (\sqrt[4]{|T_a - T_v|} + 1.54 \times w) \quad (3a)$$

213 The following empirical equation is used for wind speed  $w > 5$  m/s (Elbadry and Ghali, 1983; Dilger  
214 et al., 1983).

$$215 \quad h_c = 6.31 \times w^{0.656} + 3.25 \times \exp(-1.91 \times w) \quad (3b)$$

216 The heat transfer coefficient of thermal radiation ( $h_r$ ) depends on the structural material, surface  
217 temperature, and air temperature (Kreith, 1973; Elbadry and Ghali, 1983).

218

219 The heat fluxes  $q$  absorbed by structural surface that are caused by all external radiation  
220 contributions can be expressed as follows:

$$221 \quad q = \alpha I \quad (4)$$

222 where  $\alpha$  ( $0 < \alpha < 1$ ) is the absorptivity coefficient of the surface material, and  $I$  is the sum of the  
223 external radiation received by a surface. For the case of a structure exposed to an open environment,  
224 the emitting radiation (structural irradiation  $G_v$ ) is considered as the thermal irradiation by using the  
225 heat transfer coefficients ( $h_r$ ) in Eq. 3. The absorbed radiation is calculated as heat fluxes  $q$  in Eq. 4,



226 which consists of the direct solar radiation ( $I_s$ ), diffuse radiation (H), atmospheric radiation ( $G_a$ ) from  
227 the sky, ground surface radiation ( $G_g$ ), and the reflected radiation ( $I_r$ ) from the ground surface. The  
228 absorbed radiation is depicted as follows:

$$229 \quad I = I_s + H + G_a + G_g + I_r \quad (5)$$

230

### 231 **(3) Initial temperature condition for thermal analysis**

232 On-site temperature sensors are not sufficient to provide the complete initial temperature of the  
233 bridge. Hence a pre-analysis for one or several consecutive days is performed. The initial  
234 temperatures of the bridge in the pre-analysis are assumed uniform and the thermal boundary  
235 conditions are applied. After the pre-analysis, the temperature distribution of the bridge is  
236 non-uniform, thus providing the initial condition of the subsequent thermal analysis.

237

238

## 239 **4. Temperature distribution simulation of Humber Bridge**

### 240 **4.1 Thermal analysis of the box girder section**

241

#### 242 **(1) FE model of box girder**

243 The temperature along the longitudinal direction of the bridge is assumed to be constant. Therefore,  
244 the FE model of a typical box girder section is constructed using ANSYS (2005) to investigate the  
245 temperature distribution of the box girder. Fig. 4 shows the details of the box girder section and the  
246 FE model which consists of 38,620 elements. The model uses PLANE55 elements for several  
247 materials: steel for the stiffened plate, asphalt for roadway, and air filling the inside hollow of the box  
248 section. PLANE55 is a type of 2D element with four nodes, each having a single degree of freedom  
249 of temperature and is endowed with thermal conduction capability making it suitable for the 2D,  
250 steady-state or transient thermal analysis.

251

252 The thermal boundary conditions of the exterior and interior structural surfaces are separately applied  
253 in the conventional thermal analysis of box girders. Also the surrounding air of both the exterior and

254 the interior of the box girder are considered totally independent. Consequently, the thermal  
255 equilibrium of the entire system can hardly be maintained. In the present thermal analysis, the air  
256 filling inside the box is modeled by using the elements of PLANE55, thus, the thermal boundary  
257 conditions of convection on the interior surfaces of the box are not necessary. The interaction of the  
258 thermal radiation of the interior surfaces is calculated by using the AUX12 radiation matrix and the  
259 results applied to the inside surface by using the super-element MATRIX50 in ANSYS (2005).

260

## 261 (2) Thermal boundary condition

262 The thermal analysis in ANSYS cannot deal with the two thermal boundary conditions (Types 2 and  
263 3) simultaneously on the same surface. Eq. (2) can be converted as follows:

$$264 \quad k \frac{\partial T}{\partial n} = h \left( T_a + \frac{q}{h} - T_v \right) = h (T_{eq} - T_v) \quad (6)$$

265 where  $T_{eq}$  includes both the air temperature and radiation and is referred to as “equivalent air  
266 temperature.”

267

268 The wind blowing across the bridge surface significantly affects the heat transfer convection  
269 coefficient (see Eq. 3) and consequently influences the accuracy of the thermal analysis results.  
270 Previous studies on bridge thermal analysis used a constant value of wind speed for all structural  
271 surfaces. However, the box girder consists of several surfaces with different azimuth angles so the  
272 variation of local wind speeds on different bridge surfaces must be considered.

273

274 As shown in Fig. 5, the cross-section of the box girder is divided into three zones according to the  
275 wind incidence angle  $\theta_w$ : windward side ( $\theta_w \leq 45^\circ$ ), crosswind side ( $45^\circ < \theta_w \leq 90^\circ$ ), and leeward side.  
276 The wind speeds on these zones take 80%, 70%, and 60% of the incident wind speed  $w$ , respectively.

277

## 278 (3) Temperature variation of the box girder section

279 The extreme environmental conditions, including strong solar radiation, high air temperature, and  
280 low wind speed, normally generate high temperature differences throughout the box girder. Thus, a  
281 typical sunny day on 24 July 2012 with relatively high solar radiation and air temperature was  
282 selected. Fig. 6 shows the measured wind speed and wind direction and Fig. 7 shows the air

283 temperature and cloud cover. The wind speed, wind direction, and air temperature were recorded by  
284 the weather station at the mid-span of Humber Bridge. The cloud cover condition was obtained from  
285 the meteorological measurements at the Humberside Airport from the National Oceanic and  
286 Atmospheric Administration website (NOAA). The maximum cloud cover in daytime is only 25%,  
287 which can be considered a clear day.

288

289 Based on the measured meteorological data, the thermal boundary conditions are calculated and  
290 applied to the FE model for transient heat transfer analysis. The initial temperature of the box girder  
291 is obtained from the final results of a pre-analysis of the previous day. The main material parameters  
292 are summarized in Table 1 (Kehlbeck, 1981; Tong, et al., 2001; Xia et al., 2013).

293

294 The temperature variation of the box girder on 24 July 2012 is calculated and compared with the  
295 corresponding measurements in Fig. 8. The structural temperature slightly decreased and reached the  
296 minimum in the early morning. The temperature then increased to the maximum in the early  
297 afternoon and decreased in the evening and midnight.

298

299 The temperature of the entire bridge reached a minimum of approximately 10 °C at around 05:00.  
300 This finding indicates that the entire bridge had an approximately uniform temperature distribution at  
301 this moment. However, different components reached their maximum temperature at different time  
302 instants. The asphalt cover had a maximum temperature at approximately 15:00, the top of inside  
303 surface of box girder reached the maximum temperature at around 16:00, the bottom surface a little  
304 later. The structural temperature of the east side reached the maximum at around 11:00, five hours  
305 earlier than the west side, at approximately 16:00. For this type of box-girder bridge, the exterior  
306 reaches the maximum temperature earlier than the interior, the top earlier than the bottom, and the  
307 east earlier than the west. The maximum temperature values were approximately 35, 34.5, 34, and  
308 26 °C for the asphalt, interface, girder top, and girder bottom, respectively.

309

310 The simulated temperatures at the observed points correlate well with the field measurements.  
311 Therefore, the effectiveness of the heat transfer analysis is verified. Some measured temperatures  
312 exhibit abrupt changes, which have not been well predicted in the numerical simulation. This

313 condition is most likely attributed to the transient local cloud cover affecting solar radiation.

314

315

## 316 **5. Temperature gradient of the box girder**

317

318 The temperature gradients of the box girder of the Humber Bridge in both vertical and transversal  
319 direction are investigated in this section.

320

### 321 **5.1 Vertical temperature gradient of the box girder**

322

323 To study the typical seasonal temperature behavior of the bridge, four sunny days in different seasons  
324 are selected for thermal analysis. The selected days are 11 February, 16 May, 24 July, and 6 October  
325 2012. According to the measured air temperature, 11 February was the coldest in winter, whereas 24  
326 July was the hottest in summer. The days of 16 May and 6 October can represent the weather  
327 conditions of spring and autumn, respectively.

328

329 The vertical temperature differences of the box girder in different seasons are obtained from the  
330 numerical analysis and plotted in Fig. 9. Fig. 9(a) depicts the variation of the temperature difference  
331 of the cross-section over time. The temperature difference in this simulation refers to the difference  
332 between the maximum and minimum temperatures of the section along the web on one side, which  
333 may occur at different points at different time instances. The temperature difference of the section  
334 was considerable, and the difference in daytime was significantly larger than the difference at night.  
335 The vertical temperature difference was small before sunrise, increasing to a maximum at noon, then  
336 decreasing until after sunset. The east side had the largest temperature difference at about 9:00 and  
337 the west side had the maximum at approximately 15:00. Moreover, the maximum vertical  
338 temperature difference of the west side was larger than the east side. The vertical temperature  
339 difference was largest in summer and smallest in winter

340

341 The vertical temperature gradient profile is shown in Fig. 9(b). The upper web had higher  
342 temperature than other components because it received more direct solar radiation. The lower web  
343 and bottom deck had the lowest temperature because they were blocked from direct solar radiation.  
344 The east and west sides of the box girder reached peak temperatures different times, as shown in Fig.  
345 9(a). This finding indicates that TTD existed in the east and west upper webs.

346

## 347 **5.2 TTD of box girder**

348

349 Eurocode 1 for thermal actions (European Committee for Standardization, 2003) states that in usual  
350 cases only the vertical temperature difference must be considered. However, the TTD must also be  
351 considered in particular cases such as that in which one side is more exposed to sunlight than the  
352 other. The box girder of the Humber Bridge is streamlined with inclined webs on the east and west  
353 sides that may cause significant TTD due to receiving different solar radiation.

354

355 Here the measured TTD between the sensors installed on the east and west deck of the bridge ( $T_e$  and  
356  $T_w$ , see Fig. 2) is investigated first. Fig. 10(a) shows the absolute value of TTD in two clear days,  
357 representing the summer and spring, respectively. In the morning the east side received much more  
358 solar radiation than the west and the temperature difference reached the maximum of 12 °C at 8:00 in  
359 summer and 5°C at 11:00 in winter. On the contrary, in the afternoon the west side received much  
360 more solar radiation than the east and the TTD reached the maximum of 13°C at 17:00 in summer  
361 and 5°C at 15:00 in winter. Therefore, summer has more significant TTD. Fig. 10(b) shows the daily  
362 maximum TTD in 2012, and the maximal TTD could be as high as 18°C. In general, significant TTD  
363 occurred from March to September.

364

365 Eurocode 1 (European Committee for Standardization, 2003) recommends 5°C as the linear TTD  
366 between outer edges of a bridge if no other information is available and no indications of higher  
367 values exist. However, the present results show that the TTD of the Humber Bridge reaches as high  
368 as 18 °C and that value over a longer period of monitoring is likely higher. As described previously,  
369 the maximal TTD observed at the Cleddau Bridge was as 15°C. Cleddau is also a steel box girder

370 bridge, albeit one with a very different section to Humber, but the need to consider TTD for such  
371 bridges seems to be clear.

372

373 To investigate the TTD of the entire box girder, the numerical results are then examined. Fig. 11(a)  
374 shows the maximal TTD during four chosen days. The peaks occurred around 9:00 and 15:00.  
375 Similar to the measurement data, summer and spring have larger TTD than winter and autumn.

376

377 The distribution of the TTD along the deck on 24 July 2012 is illustrated in Fig. 11(b). Again the east  
378 upper web had much higher temperature in the morning, the top deck had slightly higher temperature  
379 than both upper webs at noon, and the west web took the maximum temperature in the afternoon. An  
380 abrupt change in temperature occurred at the connection between the deck and webs. Therefore, the  
381 inclined upper webs play the critical role in the TTD.

382

### 383 **5.3 Effect of box girder profile on TTD**

384

385 To study the effect of inclined upper webs on TTD, three different box girder shapes are investigated.  
386 Case 1 is the current section of the Humber Bridge; in Case 2 the footpath is at the mid-height of the  
387 section; and Case 3 the upper webs are flush with the top deck. The TTD variation on 24 July 2012  
388 for three cases is shown in Fig. 12. The three cases have similar distribution of TTD. However, Case  
389 2 with deepest upper webs shows the largest TTD. In Case 3, the upper webs are located at almost  
390 the same level as the upper deck but have higher temperature than the latter. This is because the  
391 former are made of steel and are directly exposed to open environment whereas the latter is covered  
392 by a 40 mm thick asphalt pavement, which has a low thermal conductivity. Next the effect of asphalt  
393 cover on TTD will be investigated.

394

395 The upper webs are assumed to be covered with 40 mm of asphalt, same as the upper deck. The  
396 corresponding TTDs for the above three shapes are illustrated in Fig. 13. The TTDs decrease  
397 significantly as compared with those without asphalt cover. In particular, the maximum TTD  
398 decreases from 17°C to 11°C in Case 2 and from 10°C to 3°C in Case 3.

399

400 The effects of bridge orientation with respect to the sun (the bridge azimuth) on TTD are also  
401 investigated based on the current box girder section of the Humber Bridge. Four typical orientations,  
402  $0^\circ$ ,  $45^\circ$ ,  $90^\circ$  and  $-45^\circ$  as defined in Fig. 14 are considered. It is noted the actual Humber Bridge is  
403 almost in the south-north direction, corresponding to  $0^\circ$ . Here the variation of wind speed on  
404 different surfaces is not considered for simplicity and thus the convection coefficient is uniform for  
405 all surfaces. The TTD on the day is illustrated in Fig. 14. Although the time variation of TTD is  
406 different for different orientations, the maximal TTD is almost similar. Detailed investigations show  
407 that regardless the bridge orientation, when one upper web receives direct solar radiation in the  
408 morning, the opposite upper web is blocked from solar radiation by the upper deck. Therefore, the  
409 bridge orientation has a slight effect on the maximum value of TTD in one day.

410  
411

## 412 **6. Conclusions and Discussions**

413

414 Accurately analyzing the temperature behavior of long-span bridges is a challenge because of  
415 complex configuration and high uncertain and varying meteorological environment. This study  
416 investigates the temperature behavior of the Humber Bridge, a long-span steel suspension bridge for  
417 which a high resolution FE model is constructed. Thermal boundary conditions are calculated  
418 accounting for various environmental conditions on different surfaces and transient heat transfer  
419 analyses in different seasons performed by using the ANSYS FE software package. The numerical  
420 results are verified through a comparison with the measurements.

421

422 The boundary and initial conditions and the thermal coefficients significantly affect the results of the  
423 thermal analysis. The new approaches employed in the present numerical analysis are as follows:

- 424 (1) The air inside the box girder is modeled by using air elements and the thermal radiation of  
425 the interior surface is analyzed by using the AUX12 Radiation Matrix. This method provides  
426 a more reasonable way to ensure the thermal equilibrium condition in thermal analysis of box  
427 girder bridges. The method also improves the computational efficiency by eliminating the  
428 thermal boundary conditions of the interior surfaces.

429 (2) Different wind speeds on different exterior surfaces are adopted in calculating the heat  
430 convection coefficients of the surface.

431 (3) A pre-analysis approach is adopted to obtain the initial thermal condition of the bridge. After  
432 the 24 hours pre-analysis, the thermal distribution of the entire bridge can be used as the  
433 initial thermal condition.

434 Employing the above approaches, the numerical results in different seasons concur with the field  
435 measurements.

436

437 The streamlined steel box girder (with inclined upper webs) is designed to perform well for wind  
438 loading. However, this study has shown that this type of girder may exhibit significant vertical and  
439 transversal temperature difference because the upper webs on each side receive very different solar  
440 radiation in daytime. In particular, the TTD has not been considered sufficiently in previous studies  
441 and current standards. Such a large TTD may cause in-plane bending of the box girder (or deck) and  
442 thus generate rotations at the bearings. To avoid resulting excessive movement or forces of bearings  
443 special attention must be given during design and analysis. Parametric studies with the established  
444 numerical model show that deep upper webs play a critical role in TTD and asphalt cover can reduce  
445 TTD considerably. The bridge orientation has limited effect on the maximum TTD.

446

447

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449

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Table 1. Material parameters for thermal analysis

Parameters	Notation	Steel	Asphalt	Air	Concrete
Density	$\rho$ (kg/m <sup>3</sup> )	7850	1530	$1.2 \times 10^{-3}$	2400
Heat capacity	$c$ (J/kg/°C)	460	1075	1.007	925
Thermal conductivity	$k$ (W/m/°C)	60	1.80	0.026	2.71
Emissivity coefficient	$\varepsilon_v$	0.80	0.92	0	0.88
Absorptivity coefficient	$\alpha$	0.75	0.90	0	0.65

535