

# EXPERIMENTAL INVESTIGATION OF THE INTERACTION OF FLUID TRANSIENTS WITH AN IN-LINE AIR POCKET

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## ABSTRACT

Entrapped air blocking the flow in pipeline systems is a common cause of increased pumping costs. At present, air is generally removed via valves or pipeline excavation and drilling. This becomes inefficient in large networks where the precise location of the air is unknown. Fluid

transients are a potential tool for detecting and locating air in pipelines. The effect of a stationary air pocket part of the way along the pipe which occupies the main flow path and acts as a blockage without causing a hydraulic jump or column separation has not previously been studied experimentally. This paper presents experimental results for a transient pulse interacting with an in-line air pocket for a range of pocket sizes and system pressures. In accordance with impedance theory, the reflective power of the air increases with pocket size. Other notable characteristics of the interaction include frequency dependent transmissivity, an out-of-phase reflection, and a substantial reflection under zero base flow. These effects set air pockets apart from solid blockages, allowing a transient detection methodology to differentiate between the two cases although they have similar effects at steady state.

## INTRODUCTION

A safe and reliable water supply is essential to supporting the health and sanitation of communities all over the world, as well as generating significant economic benefits. Functional water supply has become an expected service in developed nations, with significant investments required to install and maintain the associated infrastructure. During the period 2009 to 2019, New Zealand's operational expenditure for supplying public drinking water was estimated at NZ\$65 million per year, with a capital expenditure of NZ\$390 million per year (Auditor-General 2010). An integral part of modern water supply systems is pipelines. To most efficiently manage networks, regular condition assessment is required to diagnose anomalies. The ideal method will provide information about the type and the location of the anomaly, enabling a targeted repair or removal plan. Non-invasive testing methods are preferred as this will minimise cost and disruption to the system.

Entrapped air in a pipeline is a common issue and can pose a range of problems for network operators. Dissolved air exists naturally in water, with the amount of dissolution dependent on temperature and pressure. Water used in civil engineering applications contains approximately 2% air (Lauchlan et al. 2005), which may leave solution due to low pressure regions created by pump action or local turbulence, creating tiny bubbles which coalesce to form accumulated pockets (Young 1999). Other mechanisms by which air can enter pipelines include through pipe filling

51 (Lee 1991), as a byproduct of biological activity (National Research Council 1982), through joints,  
52 fittings, and leaks (Spellman 2013), or via transfer from surge control devices (Lauchlan et al. 2005).  
53 Under steady state conditions, accumulated in-line air reduces the pipe cross-section, causing a flow  
54 restriction and resulting in increased head loss, energy consumption, and ultimately pumping cost,  
55 similar to a solid blockage. Pozos et al. (2010) found that pumping accounts for approximately 75%  
56 of the operating costs of a distribution network, and entrapped air can reduce the overall efficiency  
57 by 30%. If left unchecked, the gradual growth of the pocket could cripple the operation of the  
58 system, particularly for undulating networks. Air pockets can also compromise system resilience,  
59 as their presence may exacerbate the transient pressures experienced during water hammer effects  
60 (Lauchlan et al. 2005). When the air cannot be easily swept downstream or bled through a valve,  
61 expensive and intrusive methods such as pipeline excavation or drilling vents at pipe high points  
62 may be required.

63 Fluid transients are a potential non-invasive tool for the detection and characterisation of pipeline  
64 faults, including trapped air pockets. When a transient wave encounters a flow anomaly, such as an  
65 air pocket, it is divided into reflected and transmitted components. If the impact of that particular  
66 anomaly on the reflection and transmission of the pulse is understood, measuring the evolution of  
67 pressure in the pipe after the controlled generation of a transient wave could allow the anomaly to  
68 be located and characterised. It is particularly useful to be able to differentiate between different  
69 flow-blocking elements, as in many cases air can be cheaply flushed out by changing the flow  
70 regime, whereas the removal of solid blockages or faulty valves invariably requires excavation.

71 The majority of the existing experimental investigations into the air-transient interaction focus  
72 on air pockets trapped at the end of a dead-end pipe, acted upon by a compression wave. Ocasio  
73 (1976) found that entrapped dead-end air could lead to extreme surges following an instantaneous  
74 valve opening. In the field, Jönsson (1985) observed that, for an air pocket trapped next to a valve,  
75 smaller equilibrium air volumes led to faster oscillations and larger transient peaks. Experiments  
76 by Lee and Martin (1999) and Lee (2005) for dead-end pockets ranging between 3% and 44.8%  
77 of the total pipe volume agreed with this observation. However, for the largest pocket volumes

78 tested, the peak pressures were smaller than those obtained for the no air case, though a physical  
79 reasoning is not provided for this observation. Vasconcelos and Leite (2012) reached a similar  
80 conclusion for the case of a dead-end air pocket with base flow, while Lai et al. (2000) found  
81 that the peak pressures experienced are also influenced by the percentage of air in the void. Zhou  
82 (2000) presented experimental and observational studies into the case of an air pocket at the end  
83 of a pipe, adjacent to an orifice which allows limited air release. Large pockets were displaced  
84 and compressed by the transient wave, while smaller pockets were forced out the adjacent orifice.  
85 For smaller air volumes, the peak pressures increased as the cushioning effect of the air decreased.  
86 Zhou et al. (2011) found that for dead-end air volumes below approximately 0.05% of the total pipe  
87 volume peak pressures begin to decrease again, as below this threshold there is limited space for  
88 water column movement and hence a decrease in the water impact force.

89 The case of a stationary air pocket in the middle of the pipe has not been investigated to the  
90 same extent. Cabrera et al. (1992), Izquierdo et al. (1999), and Fuertes et al. (1999) carried out  
91 numerical investigations, using the rigid column model, into the case of system start-up when  
92 long columns of air are trapped in an undulating pipeline, entirely blocking the pipe cross-section.  
93 Pozos (2007) successfully utilised a linear equation to identify locations where air would gather in  
94 experimental systems, confirming the theory that air gravitates to and becomes fixed at high points.  
95 Pozos-Estrada (2017) carried out laboratory experiments to verify the open channel flow model for  
96 large in-line pockets followed by a hydraulic jump, finding that the presence of the pocket reduces  
97 the amplitude of transmitted pressure oscillations. To investigate the scenario of smaller pocket  
98 volumes which do not create a hydraulic jump, Kim (2008) carried out a set of experiments and  
99 numerical investigations for a range of air pocket volumes located at the pipe mid-point for a range  
100 of initial hydrostatic pressures and base flow velocities. The air pocket was isolated inside a brass  
101 block adjacent to the flow, meaning that the air was outside the main flow path (off-line) rather than  
102 in-line with flow. The air pocket was found to result in major changes to the shape and magnitude  
103 of the incident compression wave compared to the no-air case, with the air pocket creating high  
104 frequency pressure drops due to the sudden drop in fluid density. These changes were strongly

105 dependent on the pocket volume and pressure condition. The advantage of the brass block approach  
106 is that the air is isolated outside the main flow path, so the effects of base flow can be investigated  
107 without risk of the air being swept elsewhere by the flow.

108 The purpose of this study is to carry out experimental investigations into the reflection and  
109 transmission of a rapid transient through an in-line air pocket for a range of air volumes and initial  
110 hydrostatic pressures. This complements other studies by Kim (2008) and Pozos-Estrada (2017)  
111 for discrete air pockets located part of the way along the pipe for the cases where the air pocket  
112 was off-line, or large enough to cause a hydraulic jump. A greater knowledge of the observable  
113 effects of this form of air on an incident transient wave would assist in the development of a fault  
114 detection framework, as this is a common scenario compromising the efficiency of supply networks  
115 (Lauchlan et al. 2005). The experimental results will be used to identify the effects of the in-line  
116 air pocket on a transient pulse. Some of the effects of air pockets at steady state, such as a reduced  
117 flow rate or increased pumping cost, are shared with other flow-constricting faults such as solid  
118 blockages and partially closed valves, but air pockets may be significantly cheaper to remove once  
119 identified. This means it is particularly useful to identify effects on the transient which are unique  
120 to air pockets.

## 121 **EXPERIMENTAL PROCEDURE**

122 The experiments were conducted at the University of Canterbury Fluids Laboratory using the  
123 experimental apparatus shown in Fig. 1. The system consisted of a downstream reservoir capable  
124 of being pressurised up to 3.0 bar, a 41.6 m steel pipeline with a 22.25 mm internal diameter,  
125 and a closed solenoid valve located at the upstream end of the pipe, 14.50 m from the air pocket  
126 location. The solenoid valve was adjacent to the upstream reservoir which is not pressurised. The  
127 pipe was set at a constant angle of 3.5°, resulting in a height difference of 2.51 m between the  
128 two ends of the pipe. A steel test section containing a crest was inserted into the pipeline at the  
129 location shown in Fig. 1. Air was inserted into the test section via a bleed valve using a plastic  
130 measuring syringe which allowed the volume of air,  $V$ , at atmospheric pressure to be measured  
131 before insertion. The air was also extracted and measured using the syringe at the end of each test to

132 ensure no air had moved elsewhere in the pipe. To measure the transient pressure disturbances, PCB  
133 Piezotronics Model 102A07 dynamic pressure transducers with a sampling frequency of 10,000 Hz  
134 were installed along the pipe at four locations. The transducers have a 345 kPa measuring range, a  
135 natural frequency of over 250 kHz, and an uncertainty of 3.45 kPa. PT1 was located at the transient  
136 generation point at the end of the pipe, 14.50 m upstream of the air pocket. PT2 was located 8.29 m  
137 downstream of the transient generation point, 6.21 m upstream of the air pocket. PT3 was located  
138 6.30 m downstream of the air pocket, while PT4 was located at the air pocket.

139 Previous work into transient interactions with in-line air (Kim 2008) (Pozos-Estrada 2017)  
140 has generally focused on transients generated by flow stoppage, and has therefore used a sudden  
141 valve closure to interrupt base flow and generate a compression wave. However, as the air in this  
142 investigation is located in the main flow path, tests were carried out with no base flow to prevent air  
143 being pushed from the system, moved to another location, or sheared by the flow. Therefore, the  
144 transient was generated via a rapid opening and closure of the electronically controlled solenoid  
145 valve, with the sudden start and stop of flow causing an expansion pulse which propagates back  
146 and forth along the pipeline. The pressure response was recorded at the four transducers for five  
147 seconds from the opening of the valve, enough time for the transient to dissipate entirely. Based  
148 on the wave speed measured for the system (1348.5 m/s),  $a$ , and the length of the pipe,  $L$ , this  
149 corresponds to approximately 167 cycles, where the pipeline period  $T = \frac{4L}{a}$ .

150 As well as the no-air pipe case, fourteen air pocket volumes were tested, ranging from 2.9 ml  
151 to 40 ml at atmospheric pressure ( $V = \{2.9; 3.5; 7.1; 7.8; 9.9; 11.3; 15.5; 16.0; 16.5; 21.6; 26.5;$   
152  $33.9; 34.6; 40.0\}$  ml). These volumes are below 2% of the total pipe volume, so could realistically  
153 occur as a result of air vaporisation. Tests were run for each air pocket volume at initial hydrostatic  
154 pressures ranging between 0.5 bar and 3.0 bar in 0.5 bar increments. The pocket volumes used range  
155 from a very small collection of air which barely obstructs the flow, to pockets which almost entirely  
156 block the crest at low initial hydrostatic pressures. This range of scenarios could realistically occur  
157 in a pipeline and provides a comprehensive study of the effect of an air pocket in a pipe system. To  
158 assess experimental error, testing was repeated ten times for each set of experimental conditions.

159 The standard error between the ten tests was observed to be less than 0.05% of the absolute pressure  
160 readings on average. To ensure no air became trapped elsewhere in the system, the pipe was bled at  
161 several side discharge valves along its length after each pressure increase and a period of sustained  
162 base flow with the upstream valve open was applied between each air pocket test.

163 The Baccara solenoid valve was programmed to open and close over a period of 6 ms. The  
164 control system for the valve was designed and made at the University of Canterbury. Based on  
165 the experimental wave speed determined for the system, the closure time of 6 ms corresponds to a  
166 pulse length of approximately 8.1 metres, or 20% of the total pipe length ( $0.2L$ ). The pulse length  
167 provides an indication of the level of interference that may be expected in the pressure trace. As  
168 the pulse is shorter than the pipe itself, the reflections from the air pocket and system boundaries  
169 will not immediately blend together, allowing the extraction and analysis of individual pulses.

## 170 NUMERICAL MODELLING

### 171 Governing Equations

172 The results of a simple numerical model for the air-water interaction will be used to carry out  
173 an energy balance for the system. A 1D model is required to complete the energy balance. The  
174 air pocket volumes to be tested are small enough that the elastic water model is applicable, and  
175 the movement of the air-water interface does not need to be considered (Chaiko and Brinckman  
176 2002). The Method of Characteristics (MOC) scheme is used to solve the mass and momentum  
177 conservation equations which govern 1D unsteady pipe flow (Wylie et al. 1993)

$$178 \frac{\partial V}{\partial t} + g \frac{\partial H}{\partial x} + gh_f = 0, \quad (1)$$

$$179 \frac{\partial H}{\partial t} + \frac{a^2}{g} \frac{\partial V}{\partial x} = 0, \quad (2)$$

180 where  $H$  is the piezometric head,  $V$  the fluid mean velocity,  $x$  the distance along the pipe,  $t$  the  
181 time,  $g$  acceleration due to gravity, and  $h_f$  the friction loss per unit length including both steady  
182 and unsteady components. The value of  $a$  was assumed to be constant along the whole pipe. Eqs. 1

183 and 2 are reduced to a set of characteristic equations by the MOC scheme, which can be solved  
 184 simultaneously for the head  $H_{i,j}$  and flow velocity  $U_{i,j}$  at the end of time step  $j$  at a given node  $i$  in  
 185 the MOC grid. The MOC grid was split into 180 spatial nodes distributed evenly along the pipe,  
 186 with the time step selected to ensure the Courant number ( $\frac{a\Delta t}{\Delta x}$ ) is fixed at unity. Sensitivity testing  
 187 with a range of discretizations showed that the size of the spatial grid had only a minor impact on  
 188 the solution compared to the additional computational time required. For example, increasing the  
 189 discretization to 1000 nodes results in an average difference of less than 1% in the pressure pulse  
 190 amplitudes predicted.

191 For high-speed transients, inaccuracies can arise in model predictions of energy loss and phase  
 192 shift as a result of the changing velocity profile, turbulence, and laminar-turbulent transitions. The  
 193 inclusion of unsteady friction in the model accounts for this effect. The methodology developed by  
 194 Zielke (1968) was used for calculating friction terms

$$195 \quad h_{f,(i,j)} = \frac{32\nu}{gD^2} V_{i,j} + \frac{16\nu}{gD^2} \sum_{k=1,3,\dots}^{j-1} (V_{i,j-k+1} - V_{i,j-k-1}) W(j\Delta t), \quad (3)$$

196 where  $h_f$  is the total friction loss including both unsteady and steady friction,  $D$  the pipe diam-  
 197 eter,  $\nu$  the kinematic viscosity of the fluid, and  $W$  a weighting function based on the dimensionless  
 198 time which can be found in Zielke (1968). The method accounts for the velocity history of the  
 199 given node as well as the current flow velocity. The method and Zielke's weighting function are  
 200 suited to laminar flow regimes. The lack of base flow in the experimental system means that the  
 201 flow velocities generated are small, and will satisfy this requirement.

## 202 **Accumulator Model**

203 The accumulator model incorporates an air pocket of a selected volume at a given nodal point.  
 204 It is assumed that there is no column separation, i.e., the air does not occupy the full cross section of  
 205 the pipe. This assumption was used by Burrows and Qiu (1995) in a previous numerical study, and  
 206 the air volumes tested satisfy such an assumption. In addition, the initial hydrostatic pressure is high  
 207 and the generated pressure disturbance is small relative to this, and therefore column separation



208 is unlikely to occur. The pressure within the air pocket at any instant is assumed to be the same  
 209 throughout the air pocket volume, and the compressibility of the liquid in the computational reach  
 210 containing the air pocket is considered to be negligible compared to the compressibility of the air  
 211 (Wylie et al. 1993). The polytropic relationship can be written at the end of the time interval  $\Delta t$  as

$$212 \quad (H_A - z)(V + \Delta V)^n = C_A , \quad (4)$$

213 where  $H_A$  is the absolute head at the pocket,  $z$  the elevation of the pipe above the datum,  $V$   
 214 the pocket volume at the beginning of the time interval  $\Delta t$ ,  $\Delta V$  the volume change across the time  
 215 interval,  $n$  the polytropic exponent, and  $C_A$  the polytropic constant. Applying continuity principles,  
 216 the volume change can be expressed as

$$217 \quad \Delta V = \frac{2\Delta t}{\pi D^2} [(V_{i+1,j-1} - V_{i-1,j-1}) + (V_{i+1,j} - V_{i-1,j})] , \quad (5)$$

218 Combining the characteristic equations, the polytropic relationship, and Eqs. 4 and 5 yields  
 219 a non-linear equation with  $H_P$  as the only unknown which can be solved using a root-finding  
 220 algorithm.

## 221 **Energy Equation**

222 The energy equation (Karney 1990) (Karney et al. 2015) (Duan et al. 2017) will be used to  
 223 assess the energy balance in the system. The energy equation is

$$224 \quad \frac{dU}{dt} + \frac{dU_a}{dt} + \frac{dT_e}{dt} + D' + W' = 0 , \quad (6)$$

225 where  $U$  is the internal energy,  $U_a$  the elastic energy stored by the air pocket,  $T_e$  the kinetic  
 226 energy,  $D'$  the rate of viscous energy dissipation, and  $W'$  the rate at which work is done on the fluid  
 227 at each boundary. The extended versions of these terms can be found in Karney (1990) and Karney  
 228 et al. (2015). The fluid pressure and velocity, evaluated numerically for each spatial node at each  
 229 time step, are used to evaluate the energy balance for each time step. The equation may also be  
 230 used to calculate the total energy in each form at each time step.

## RESULTS

### Experimental Results

#### *Time Domain Observations*

The experimental investigation involved the collection of pressure measurements at the transient generation point, upstream of the air pocket, and downstream of the air pocket. Thus it is possible to assess the properties of both the reflected and transmitted waves. Figs. 2 and 3 show traces measured at PT1, (the transient generation point), PT2 (6.21 m upstream of the pocket), PT4 (at the air pocket section), and PT3 (6.30 m downstream of the pocket) for a set of representative air volumes. The approximate obstruction created by each air volume for the 3.0 bar scenario is shown in Fig. 4. The pressure traces presented have been normalised by the initial hydrostatic pressure such that  $H^* = \frac{H}{H_0}$ , where  $H$  is the measured gauge pressure at any time and  $H_0$  is the steady state initial hydrostatic pressure. The elapsed time since the start of the transient event  $t$  is normalised by the pipeline period  $T$ , such that  $t^* = \frac{t}{T}$ .

In the experiments, the air pocket volumes were measured outside the pipe at atmospheric pressure before and after each test using a measuring syringe. This volume is converted to a pressurised volume inside the pipe using the reversible polytropic relation,  $H_A V^n = C_A$ . The polytropic exponent may range between 1.0 and 1.4, but an average value of 1.2 has been commonly used in previous research on air-water interactions (Martin 1976) (Wylie et al. 1993) (Izquierdo et al. 1999) (Carlos et al. 2011), and is used here. Using this equation, the volumes measured at atmospheric pressure can be converted into steady state volumes within the pipe once pressurised. The steady state in-pipe volumes are then converted to a length scale, as this can be used to understand the compression behaviour of the pocket. In Figs. 2 and 3, the pocket length scale,  $L_P$ , is approximated as  $L_P \sim V^{\frac{1}{3}}$ .  $L_P$  is normalised by the length of the pipe such that  $L_P^* = \frac{L_P}{L}$ . The work done on the pocket by the transient wave scales as  $P A_P V_P T_P$ , where  $P$  is the pressure on the pocket,  $A_P$  the pocket surface area,  $V_P$  the radial velocity of the air-water interface, and  $T_P$  the duration of the compression phase. When the compression length scale ( $V_P T_P$ ) is less than the pocket length scale ( $L_P$ ), the pocket is compressed but does not collapse. When the compression

258 length scale is longer than the pocket length, the pocket collapses, resulting in large pressure spikes.  
259 Examples of this scenario include the experiments by Jönsson (1985) and Lee and Martin (1999)  
260 which observed peak pressure enhancements of four or five times the initial hydrostatic pressure.

261 Figs. 2 and 3 show that the partial reflections occurring at the pocket result in significantly more  
262 pressure peaks in the transient trace than observed in the no-air case. For instance, by  $t^* \approx 0.5$ ,  
263 the arrival time of the first reflected pulse at the upstream sensor (PT2) for the no-air case, four  
264 pulses have arrived at PT2 for the air pocket scenarios. While the first reflected and transmitted  
265 pulses are fairly clear, as boxed in Figs. 2 and 3, interference patterns develop beyond  $t^* \approx 0.3$   
266 as reflections from the air pocket and the ends of the system begin to interfere with each other.  
267 As boxed in Figs. 2 and 3, the reflected pulse is followed by a low pressure peak and extended  
268 tail which gradually levels off towards zero. From a diagnostic standpoint, Meniconi et al. (2016)  
269 has shown that this effect is not unique to the in-line air pocket, and a pressure drop following the  
270 reflected pulse may also be observed for solid blockage situations where the path of the pressure  
271 wave around the blockage is almost straight.

272 It is also worth noting that the pressure trace for the smallest pocket length varies significantly  
273 from the other three traces, which follow each other reasonably closely. This suggests that below a  
274 certain pocket volume threshold small changes in pocket volume begin to have a more significant  
275 effect on the transient behaviour, or the dominant physical processes of the transient-air interaction  
276 begin to change. This may be explained by the underlying physical theory of the interaction.  
277 Continuity and momentum theory state that

$$278 \quad \frac{dV}{dt} = Q_a \quad (7)$$

$$279 \quad \frac{dH_a}{dx} = 0 \quad (8)$$

280 where  $Q_a$  is the flow rate at the air-fluid interface due to the volume change of the air pocket  
281 under the transient pressure condition. Eqs. 7 and 8 state that any change in the air pocket volume

282 results in a corresponding change to the system flow rate, and that the pressure of the air pocket is  
283 homogeneous. Differentiating the polytropic equation and applying Eq. 7 gives

$$284 \quad \frac{dH_a}{dt} = -\frac{nH_a}{V} Q_a \quad (9)$$

285 Consequently, the transient variation of the hydraulic properties, pressure and flow rate, depend  
286 on the volume of the pocket as well as the instantaneous pressure state. If the above equation is  
287 considered in terms of the transient fluctuations in pressure and volume, it becomes

$$288 \quad \frac{dh_a}{dt} = -\frac{n}{V_0 + V_t} Q_a \quad (10)$$

289 where  $h_a$  is the transient fluctuation in pressure,  $V_0$  is the steady state pocket volume, and  $V_t$   
290 is the transient fluctuation in pocket volume. Therefore it can be concluded that for large pockets,  
291 where transient volume changes are small relative to the steady state air volume, the transient  
292 behaviour is largely dependent on the initial state of the air pocket ( $V_0$ ). Meanwhile, for relatively  
293 small pockets, where volume fluctuations are significant compared to the steady state volume, the  
294 transient behaviour is instead dependent on the instantaneous change in air pocket volume ( $V_t$ ).  
295 The results of the accumulator model were used to check the expected volume fluctuations for  
296 each experimental case. The smallest pocket sizes tested, which display a very different transient  
297 response, experience considerably greater relative volume changes than the mid- to upper- range  
298 of volumes. For instance, for the 3.0 bar case the two smallest volumes experience relative volume  
299 changes of approximately 10% of the starting volume, compared to other pocket volumes where  
300 the relative volume change is less than 5%. This observation may therefore be attributable to the  
301 changing air-transient dynamics as pocket volume is reduced.

302 The pressure traces indicate that increasing the air pocket size increases the amplitude of the  
303 reflected pressure pulses and decreases the amplitude of the transmitted pulses. This can be  
304 explained by impedance theory. The impedance,  $Z$ , of a pipe is given by  $Z = \frac{\rho a}{A}$  where  $\rho$  is the fluid  
305 density and  $A$  is the cross-sectional area of the pipe (Gong et al. 2013). It can be used to determine

306 the reflection coefficient,  $RC$ , which is the amplitude of the reflected pulse relative to the amplitude  
 307 of the incident pulse. It is defined as  $RC = \frac{Z_A - Z_0}{Z_A + Z_0}$  where  $Z_A$  is the impedance of the pipe section  
 308 containing the air pocket and  $Z_0$  is the impedance of the pipe without the air pocket.  $Z_A$  is smaller  
 309 than  $Z_0$ , due to the low density of the air and the local reduction in wave speed caused by the  
 310 air's compressibility. As the size of the air pocket increases,  $Z_A$  decreases, therefore increasing the  
 311 absolute value of  $RC$  in agreement with experimental observations. In addition, the theoretical  $RC$   
 312 is negative, accounting for the out of phase reflection observed. This phase change is the opposite  
 313 of what would be observed for a solid flow constriction, which has a greater impedance than the  
 314 clear pipe. This is a useful point of difference which may be utilised in diagnostic testing when a  
 315 loss of flow or increase in pumping costs is observed in the system.

### 316 *Reflection and Transmission Coefficients*

317 Reflection and transmission coefficients provide a quantitative measure of the air pocket's effect  
 318 on the incident transient pulse. These coefficients are calculated as

$$319 \quad RC = \frac{H_R}{H_I} - \frac{H_{R,0}}{H_{I,0}}, \quad (11)$$

$$320 \quad TC = \frac{H_T}{H_I}, \quad (12)$$

321 where  $RC$  is the reflection coefficient,  $TC$  the transmission coefficient,  $H_I$  the peak amplitude  
 322 of the incident pulse measured upstream of the pocket at PT2,  $H_R$  the peak amplitude of the first  
 323 reflected pulse measured upstream of the pocket at PT2, and  $H_T$  the peak amplitude of the first  
 324 transmitted pulse measured downstream of the pocket at PT3. Small reflections were observed from  
 325 the crest section for the no-air case. To clearly identify the effect of the injected air on the response,  
 326 a reflection coefficient was calculated for the no-air case at each initial hydrostatic pressure ( $\frac{H_{R,0}}{H_{I,0}}$ )  
 327 and subtracted from the reflection coefficients calculated for the air pocket cases ( $\frac{H_R}{H_I}$ ) at that initial  
 328 hydrostatic pressure. The values used in the calculation are marked on example pressure traces in  
 329 Fig. 5.

330 The reflection and transmission coefficients for each steady state pressurised pocket length are  
331 shown in Figs. 6 and 7. Sensitivity testing showed that the general trends observed are independent  
332 of the polytropic constant used to obtain the steady state air length within the pipe, and the standard  
333 error in  $RC$  and  $TC$  due to experimental variation is approximately 2%. For the no-air case  $TC$   
334 is slightly less than 1, indicating that there is a small quantity of energy loss across the 12.85 m  
335 pipe section between PT2 and PT3 when air is not present. In accordance with impedance theory  
336 introduced previously, the absolute value of  $RC$  increases with pocket length. The experimental  $RC$   
337 values are in agreement with those estimated using the theoretical equations introduced previously,  
338 particularly for the upper range of pocket sizes. The average error is less than 4%, as shown in Fig.  
339 8. The theoretical values for  $RC$  were calculated using a weighted average density for the crest  
340 section, and a wave speed at the crest section estimated using the void ratio of the crest section and  
341 the wave speed equation presented by Lee (1991).

342 The range of  $RC$  and  $TC$  observed can be compared to the values expected for solid blockages  
343 under similar conditions. Solid flow blockages generate reflections with an amplitude dependent  
344 on the base flow of the system, with severe flow constrictions required to generate significant  
345 reflections under zero base flow. The smallest air pocket volumes block only approximately 6%  
346 of the total pipe cross-section, but generate reflections under zero base flow comparable to solid  
347 blockages which almost entirely block the pipe cross-section (Meniconi et al. 2011). This is a  
348 useful diagnostic property of the air pocket. If flow loss is observed in an operational pipeline, it  
349 can be tested under zero base flow conditions and the amplitude of the transient reflection compared  
350 to the degree of flow loss observed when operational to differentiate between air pockets and solid  
351 blockages.

352 As discussed previously, past studies have observed reflected peak amplitudes which signifi-  
353 cantly exceed the initial hydrostatic pressure due to pocket collapse. For this set of experiments,  
354 the sum of  $RC$  and  $TC$  reached a maximum of approximately 1.2. The duration of the original  
355 transient pulse used in this work (6 ms) is approximately two orders of magnitude less than the  
356 compression duration used in Jönsson (1985) and Lee and Martin (1999) ( $T_P \sim 0.5 - 3$  s). The base

357 flows of approximately 1 m/s applied in Jönsson (1985) and higher driving pressures of up to 8 bar  
358 in Lee and Martin (1999) also result in higher radial velocities. The maximum velocities predicted  
359 by the numerical model for this experimental case are in the order of 0.1 m/s. Meanwhile, the  
360 pocket length scales used by Jönsson (1985) and Lee and Martin (1999) ( $L_P \sim 0.4 - 0.8$  m) are only  
361 approximately one order of magnitude greater than those used here ( $L_P \sim 0.02$  m). Therefore the  
362 size of the compression length scale relative to the initial pocket length is much smaller than was  
363 used for the above studies. The lack of base flow and the short duration of the original transient  
364 pulse mean the compression scale is too small to result in pocket collapse and, unlike previous  
365 studies, large pressure spikes are not observed.

### 366 *Spectral Analysis*

367 The shapes of the incident, reflected, and transmitted pulses are quantified using their frequency  
368 content, calculated using a direct Fourier transform (DFT). This method enables both the main peaks  
369 and the extended tails of the reflected and transmitted pulses to be included in the analysis. However,  
370 the experimental trace is subject to interference from ongoing reflections and in the majority of  
371 cases the low pressure tail is interrupted by the arrival of further reflections, as shown in Figs. 2 and  
372 3. It was necessary to artificially generate data points to complete the pulses, with the placement  
373 of these additional points based on the shape of the preceding data and modelled pulses generated  
374 using non-reflecting boundary conditions. Sensitivity testing indicated that while artificial points  
375 completing the tail were required to achieve a reasonable result, small variations in their placement  
376 did not have a significant effect on the shape of the DFT obtained.

377 Fig. 9 shows the DFT amplitude for the frequencies contained in the incident and resultant  
378 pulses for a set of representative air lengths. The DFT amplitude is normalised by the initial  
379 hydrostatic pressure ( $h^* = \frac{h}{H_0}$ ), while the frequency is normalised by the inverse of the pipeline  
380 period ( $\omega^* = T\omega$ ). Several key trends are visible in the DFTs for the particular pocket length,  
381 configuration, and pressure disturbance used. The upper range of frequencies ( $\omega^* \approx 20 - 70$ )  
382 contained in the incident pulse are present in the reflected pulse at approximately the same amplitude  
383 (within 4%). In the transmitted pulse the amplitude of this frequency range is approximately 3%

384 of the incident amplitude, meaning the upper range of frequencies contained in the incident pulse  
385 is primarily reflected back by the air pocket. This frequency dependent transmissivity is due to the  
386 compressibility of the air, and has previously been observed in the field of acoustics (Domenico  
387 1982) (Leighton et al. 1998). Significant reductions in transmissivity are observed for signal  
388 frequencies above the air pocket's resonant frequency, and this frequency content is reflected back  
389 by the air. Calculating the resonant frequency for an in-line air pocket is difficult due to the unknown  
390 geometry of the pocket (Jang et al. 2009). However, for the off-line pocket case, where the geometry  
391 is known, the DFT agrees with theoretical predictions of the resonant frequency, as ascertained  
392 by the authors in yet to be published research. The frequency dependent behaviour has therefore  
393 been quantified using a cut-off frequency for transmission by the air pocket, defined here as the  
394 frequency where the amplitude of the transmitted pulse DFT is first less than 5% of the amplitude  
395 of the incident pulse DFT. The cut-off frequencies are marked with vertical lines on Fig. 9. The  
396 cut-off frequency decreases with increasing air volume, consistent with theoretical expectations for  
397 the resonant frequency (Jang et al. 2009). This effect is not observed for other pipeline anomalies  
398 such as solid blockages and leaks, which do not impose a significant change in shape on the incident  
399 pulse during reflection and transmission (Brunone 1999) (Meniconi et al. 2011).

400 It was expected that the DFTs of the reflected and transmitted pulses would form smooth curves  
401 with reduced amplitude relative to the incident pulse for the entire frequency range. However, at  
402 larger pocket lengths there is some irregularity in the DFT of the reflected pulse for  $\omega^* \lesssim 10$ . There  
403 is also an increase in the amplitude of the reflected and transmitted frequencies above that of the  
404 incident pulse for  $\omega^* \lesssim 5$ . In the time domain, the low pressure tails of the reflected and transmitted  
405 pulses for a large pocket display many small fluctuations and are of long duration. This is the likely  
406 source of the irregularities observed in the low frequency response, though the physical reasoning  
407 for this is unclear, with further numerical and experimental analysis needed.

408 Transmission and reflection coefficients can be calculated in the frequency domain by comparing  
409 the DFT amplitudes for the transmitted and reflected pulses to the DFT amplitude of the incident  
410 pulse at each frequency:



$$RC_{\omega} = \frac{h_{R,\omega}}{h_{I,\omega}} \quad (13)$$

$$TC_{\omega} = \frac{h_{T,\omega}}{h_{I,\omega}} \quad (14)$$

where  $RC_{\omega}$  and  $TC_{\omega}$  are the reflection and transmission coefficients for a given frequency,  $\omega$ , and  $h_{I,\omega}$ ,  $h_{R,\omega}$ , and  $h_{T,\omega}$  are DFT amplitudes of the incident, reflected and transmitted pulses at that frequency. Summing the squares of  $RC_{\omega}$  and  $TC_{\omega}$  at each frequency gives a measure of the energy contained in the reflected and transmitted pulses relative to the incident pulse, and therefore of the energy amplification or dissipation which occurs during the reflection and transmission process. Fig. 10 shows the total energy contained in the reflected and transmitted pulses at each frequency relative to the incident pulse for four representative air lengths. The relative energy ranges between 0.85 and 1 for  $\omega^* \gtrsim 5$ . The average relative energy across the range of frequencies in the reflected and transmitted pulses is also less than 1 for the cases tested, despite the amplification observed at low frequencies. This indicates that energy losses occur between the incident pulse and the reflected and transmitted pulses generated by the pocket. This may be explained by the energy balance theory introduced previously. The results of the numerical model provide a fair match to the experimental data, with example predictions for the pressure traces measured upstream and downstream of the pocket shown in Fig. 11. There are noticeable discrepancies in the wave amplitudes and arrival times, but the results of the model can be used to obtain a general representation of the distribution of system energy between kinetic, internal, air storage, and viscous dissipation forms. Fig. 12 shows the variation in the kinetic, internal, and air storage energy of the system for  $t^* = 0 - 1.5$ . The energies are scaled by the initial energy stored by the air pocket ( $E^* = \frac{E}{U_{a,0}}$ ). Viscous dissipation accounts for less than 2% of the system's kinetic energy, and is therefore too small to be shown. The compressibility of the air and the lack of base flow in the system mean that the majority of the system energy is stored in the air pocket. Given that viscous dissipation is negligible within the time-frame of the first air-transient interaction, it is likely that the energy loss observed in the frequency domain

435 is therefore attributable to conversion to air pocket storage during the compression and expansion  
436 phases.

### 437 **Effects of Initial Hydrostatic Pressure**

438 Initial hydrostatic pressure has been shown to have an effect on the transient trace for the  
439 dead-end pocket scenario (Zhou et al. 2002) and the brass block case (Kim 2008). The *RCs* and  
440 *TCs* calculated previously provide a quantitative assessment of the effects of initial hydrostatic  
441 pressure on the in-line pocket interaction with the transient. Fig. 7 shows that for the no-air case  
442 *TC* increases as the initial hydrostatic pressure is increased, however the total range of *TC* for  
443 the no-air case is less than 0.02. For larger air lengths ( $L^* \gtrsim 0.06$ ), Figs. 6 and 7 show that the  
444 variation in *RC* and *TC* with initial hydrostatic pressure is comparable to the no air case. However,  
445 the effect of initial hydrostatic pressure on the reflected and transmitted pulse amplitude becomes  
446 increasingly significant as the air length is reduced below this threshold. This suggests that when  
447 assessing the size of entrapped air pocket from transient reflections and transmissions the initial  
448 hydrostatic pressure should be taken into account.

449 Inspection of the DFTs for air pockets which occupy a similar length when compressed to  
450 different initial hydrostatic pressures suggests there is no relationship between initial hydrostatic  
451 pressure and DFT amplitude. This also applies to the cut-off frequency observed for the transmitted  
452 pulse, suggesting it is only influenced by the size of the pocket but not the initial hydrostatic pressure  
453 for the given experimental conditions. These findings are useful in a diagnostic scenario under  
454 similar conditions as the air pocket size may be estimated from the cut-off frequency alone.

### 455 **CONCLUSIONS AND RECOMMENDATIONS**

456 Controlled experimental investigations are needed to distinguish the effects of entrapped in-line  
457 air pockets on fluid transients. The purpose of this study was to present experimental data for the  
458 in-line air pocket case under realistic system conditions and to characterise the effects of air on the  
459 transient in terms of reflection and transmission. To assist in developing a diagnostic framework,  
460 it is useful to note how the effects of air compare to other faults which cause a flow constriction

461 at steady state. Air pockets can often be cheaper to remove than solid blockages, meaning it is  
462 advantageous to be able to differentiate between the two cases when flow loss is observed.

463 The experimental results show that the reflective power of the air pocket increases with its length,  
464 in agreement with impedance theory. Though the low pressure tail following the transient reflection  
465 may also be observed for a solid blockage, the out-of-phase reflection from the flow constriction  
466 is unique to the air pocket. Unlike a solid blockage, air pockets also result in a sizeable reflection  
467 under zero base flow conditions regardless of the degree of cross-section blockage. Linking the  
468 amplitude of the transient reflection under zero base flow to the observed flow loss during operation  
469 can therefore be used to differentiate between air and solid blockages.

470 Analysis in the frequency domain shows that the air pocket transmits only the lower range of  
471 frequencies contained in the incident pulse, with the upper range of frequencies being primarily  
472 reflected. This frequency dependent transmissivity is also unique to air among flow-blocking  
473 elements. The transmission cut-off frequency decreases as pocket length increases, similar to the  
474 theoretical resonant frequency of trapped air. The reflection and transmission coefficients calculated  
475 in the frequency domain also indicate that, on average, the incident pulse loses energy over the  
476 range of frequencies contained within it during reflection and transmission. An investigation of  
477 energy distribution within the system indicated that this energy loss is likely to be due to conversion  
478 to air pocket storage.

479 Six different initial hydrostatic pressures were used in the experimental tests to assess the effects  
480 of steady state pressure on the transient behaviour. As the air length is reduced, the effect of initial  
481 hydrostatic pressure on the amplitude of the transmitted and reflected pulses becomes increasingly  
482 significant.

#### 483 **DATA AVAILABILITY STATEMENT**

484 Some or all data, models, or code generated or used during the study are available from the  
485 corresponding author by request.

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489 **NOTATION**

490 *The following symbols are used in this paper:*

- $a$  = wave speed
- $A$  = pipe cross-sectional area
- $A_P$  = air pocket surface area
- $C_A$  = polytropic constant
- $D$  = pipe diameter
- $D'$  = viscous energy dissipation rate
- $E$  = energy
- $g$  = gravitational acceleration
- $h$  = DFT amplitude
- $h_f$  = total friction loss
- $H$  = piezometric head
- $i$  = spatial index
- $j$  = temporal index
- $L_p$  = pocket length scale
- $L$  = pipe length
- $n$  = polytropic exponent
- $P$  = air pocket pressure
- $Q$  = flow rate
- $RC$  = reflection coefficient
- $t$  = time
- $\Delta t$  = computational time step
- $TC$  = transmission coefficient
- $T$  = pipeline period
- $T_e$  = kinetic energy

$T_P$  = duration of pocket compression  
 $V$  = air pocket volume  
 $V$  = fluid velocity  
 $V_P$  = radial velocity of the air-water interface  
 $U$  = internal energy  
 $U_a$  = energy stored by air pocket  
 $W$  = unsteady friction weighting function  
 $W'$  = boundary work rate  
 $x$  = longitudinal distance  
 $z$  = elevation  
 $Z$  = impedance  
 $\nu$  = kinematic viscosity  
 $\rho$  = density and  
 $\omega$  = frequency.

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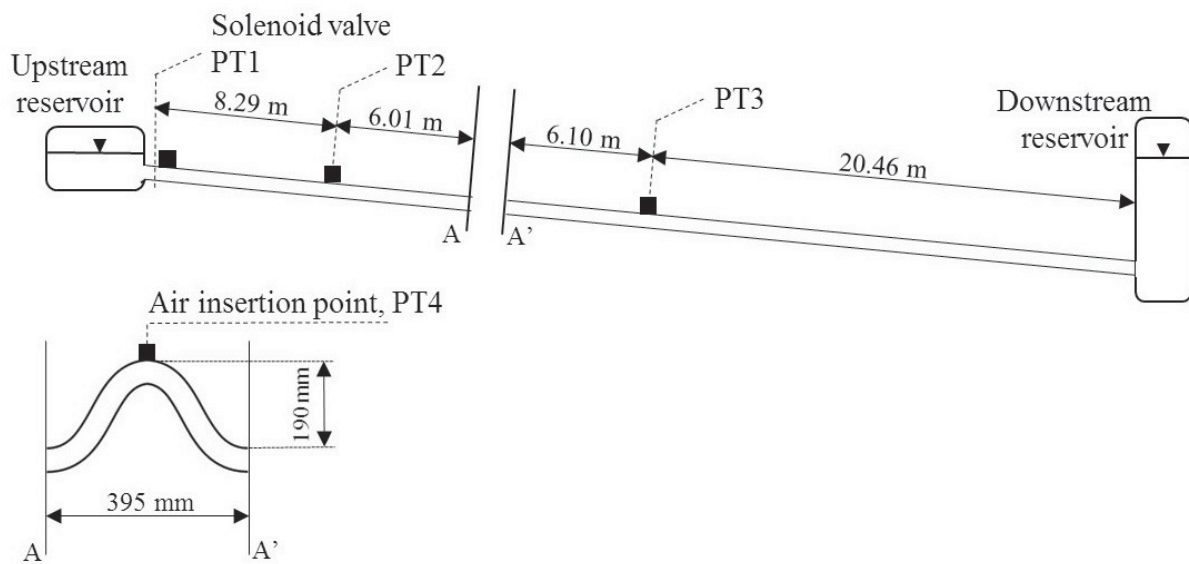
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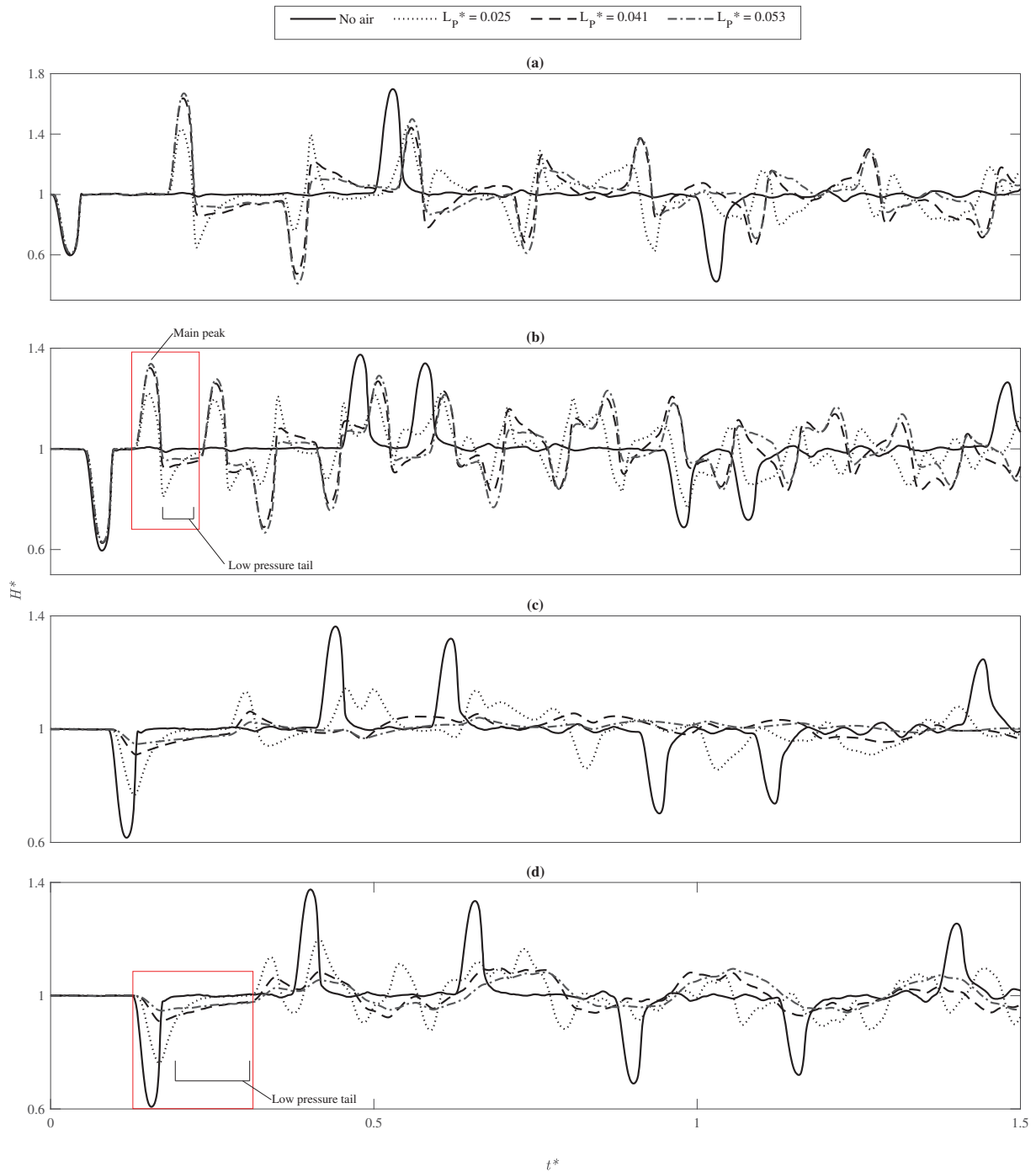
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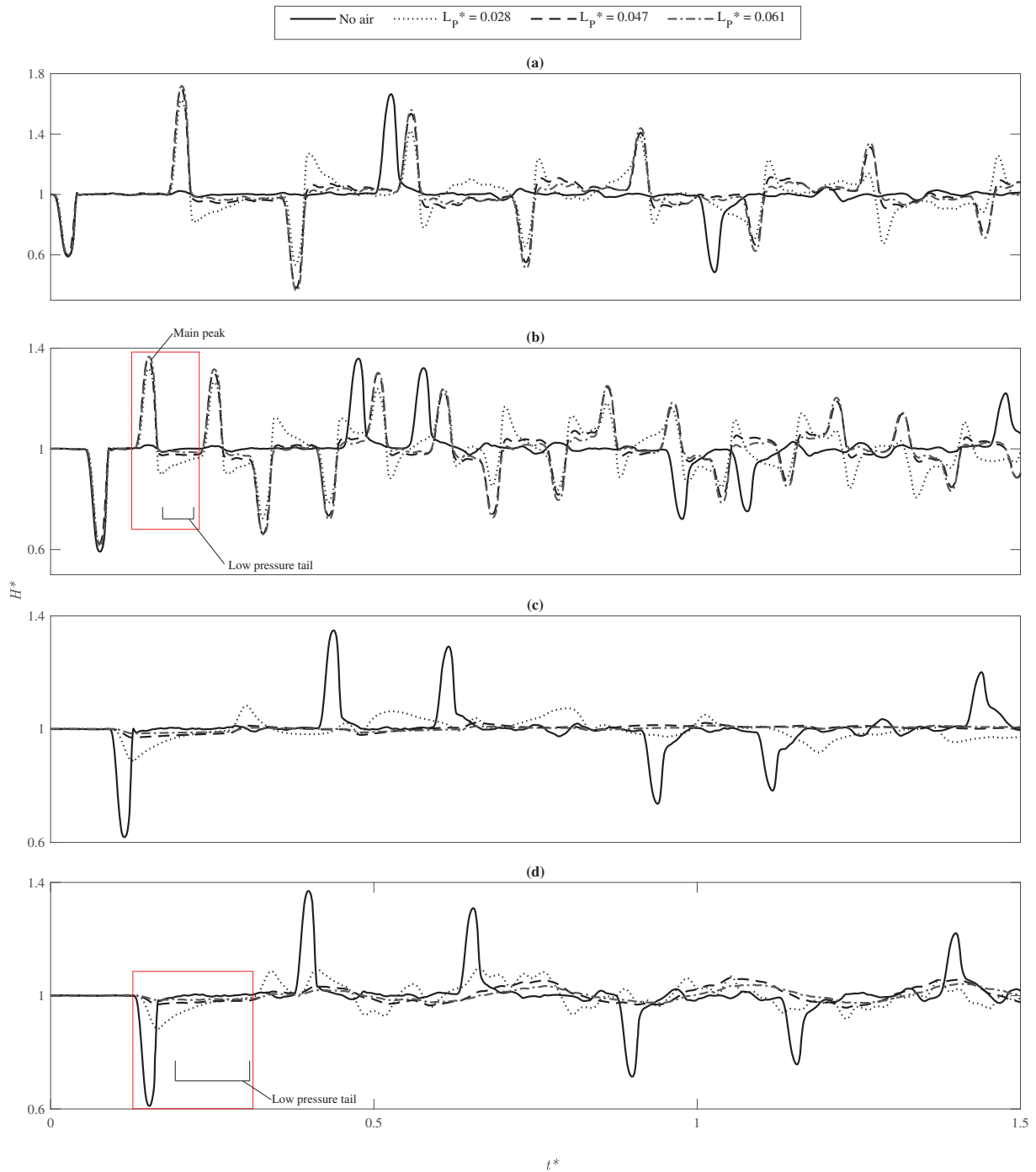
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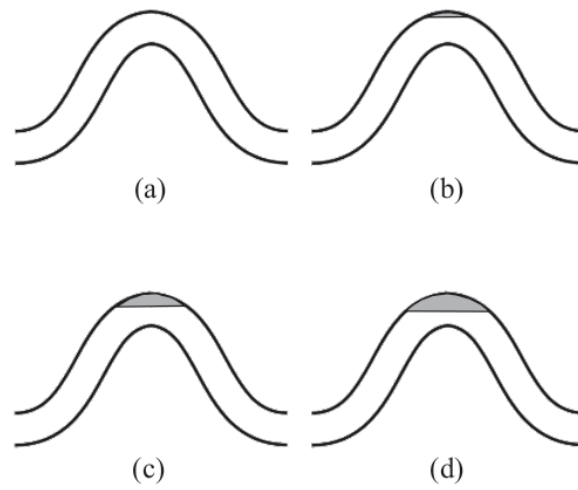
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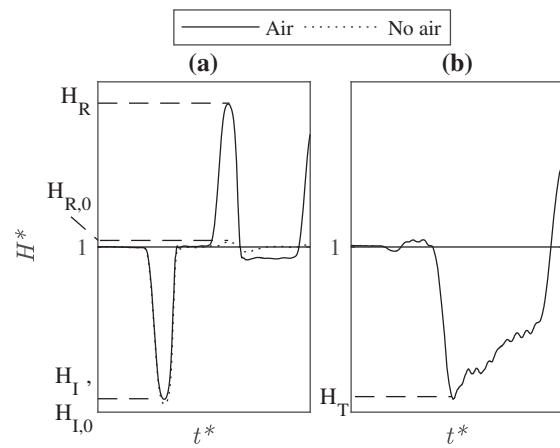
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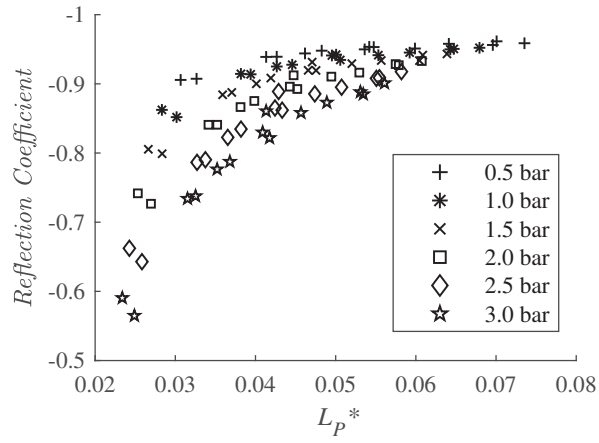
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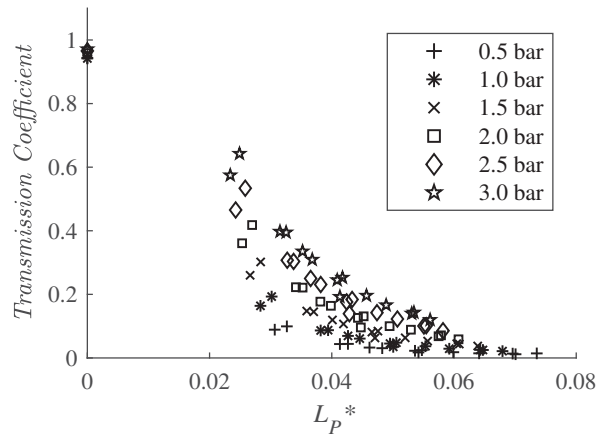


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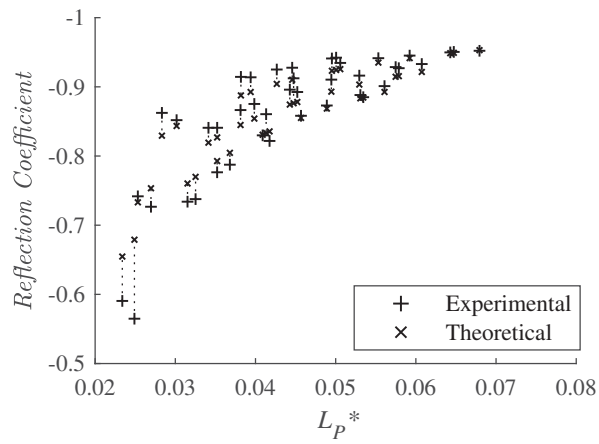


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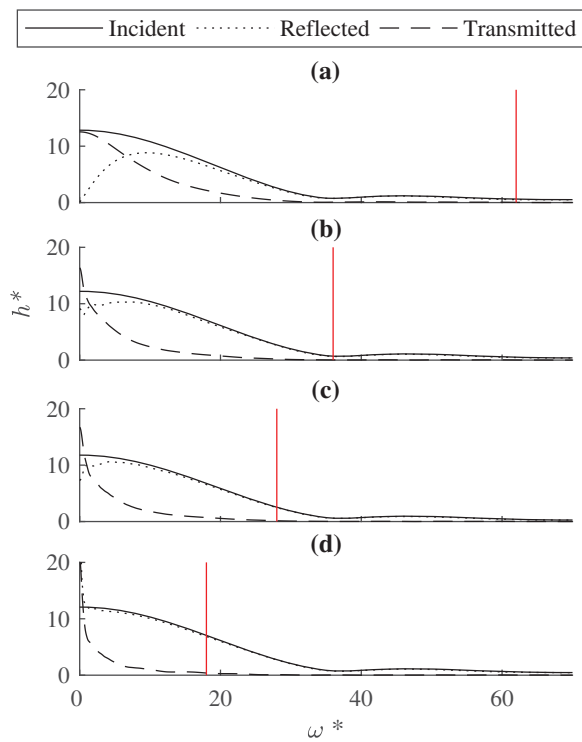




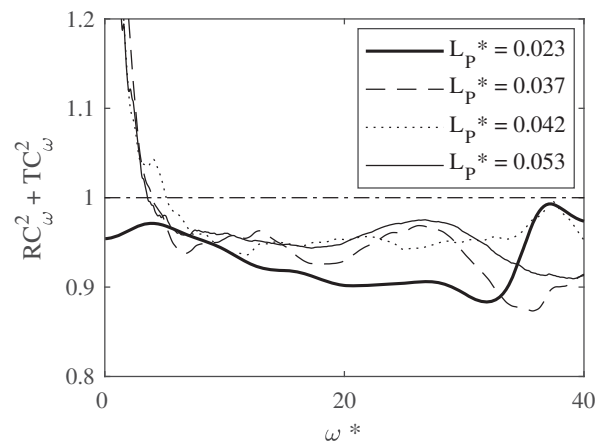
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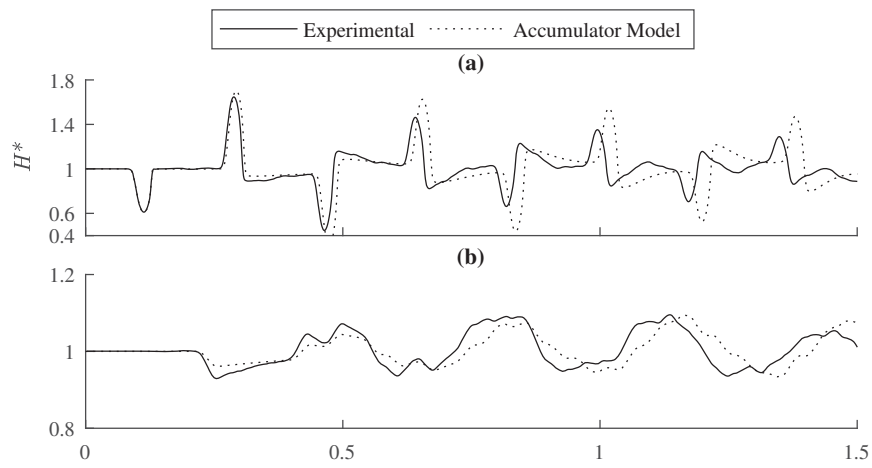
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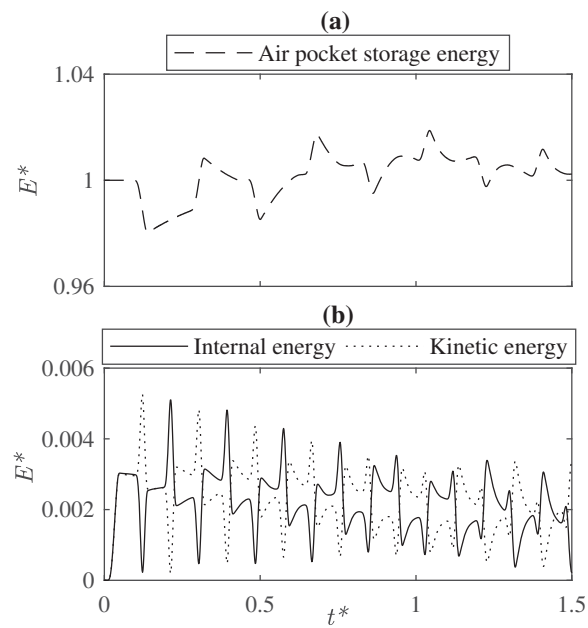
**Fig. 9.** DFT amplitude of incident, reflected, and transmitted pulses at an initial hydrostatic pressure of 3.0 bar for air pocket length (a)  $L_p^* = 0.023$ , (b)  $L_p^* = 0.037$ , (c)  $L_p^* = 0.042$  (d)  $L_p^* = 0.053$ . Cut-off frequencies for the transmitted pulse DFT are marked by a vertical line.



**Fig. 10.** Summed squares of reflection and transmission coefficients for frequencies contained within the incident pulse for air pockets at a initial hydrostatic pressure of 3.0 bar. A reference line is included at  $RC_{\omega}^2 + TC_{\omega}^2 = 1$ .



**Fig. 11.** Modelled and experimental pressure traces for  $L_p^* = 0.042$  at 3.0 bar initial hydrostatic pressure (a) upstream of the pocket at PT2 and (b) downstream of the pocket at PT3



**Fig. 12.** Air storage, internal, and kinetic energy for  $L_p^* = 0.042$  at 3.0 bar initial hydrostatic pressure