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1	Quantification of bituminous mortar ageing and its application in ravelling evaluation of
2	porous asphalt wearing courses
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10	Abstract: Bituminous mortar, consisting of bitumen, filler and fine aggregates (<0.5 mm),
11	plays a dominating role on the viscoelastic properties of Porous Asphalt (PA), and its ageing
12	is one of the key factors causing the ravelling of PA wearing courses. This research is to
13	quantify the ageing effect on the rheological characteristics of bituminous mortars and apply
14	it in evaluation of the ravelling resistance of PA wearing courses. Bituminous mortars for two
15	types of PA (one with base bitumen and the other with Styrene-Butadiene-Styrene (SBS)
16	modified bitumen) were artificially aged in the laboratory. Cylindrical specimens were then
17	prepared with the aged mortars and their complex shear modulus and shear fatigue life were
18	characterized through the Dynamic Shear Rheometer (DSR) tests. Finite element models
19	containing the structural geometries and material responses of the two PA wearing courses
20	were created. Their stresses and strains under traffic loads were simulated and analysed. The
21	experimental results showed that ageing had more influence on the complex shear modulus of
22	the base mortar compared to the SBS mortar. However, its effects on fatigue resistance are
23	opposite. The numerical modelling results indicated that after ageing, the ravelling resistance
24	of the PA wearing course with base mortar decreased more.
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26	Keywords: Porous asphalt; Bituminous mortar; Ageing; Dynamic shear rheometer; Finite
27	element modelling
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29	1. Introduction
30	Due to its extremely high population density, Hong Kong has shown increasing interests in
31	low-noise road surfacing (LNRS) materials, such as Porous Asphalt (PA). PA is an open-
32	graded asphalt mixture composed of aggregate skeleton, bituminous mortar and high

percentage of air voids. Because of the high air void content (>20%), PA wearing courses have excellent performance in rolling noise reduction. Both base bitumen without polymer 34

modification and polymer modified bitumen have been used to build PA wearing courses in
Hong Kong. But the PA with polymer modified bitumen was found more cost-effective
because of its higher durability, and has been used as the standard surfacing material in
highways in force since 2007 [1].

Japan, which decided to use PA for all highways as a standard surface material, has long-term 39 experience with PA wearing courses. The Japan experience has shown that PA with 40 41 conventional polymer modified bitumen containing 5% Styrene-Butadiene-Styrene (SBS) has 42 poor durability. It was found that a special polymer modified bitumen containing 9% SBS extended the service life of the PA wearing courses, and has been used in force since 1998 [2, 43 3]. Within the United States, Georgia Department of Transportation (DOT) developed the 44 specification for the first generation of PA in the 1990s. After that a number of states in the 45 southern part of the Unities State specified PA and utilized it as the wearing course on all 46 47 interstates. Most agencies specified polymer modified bitumen. Researches and field applications indicate that polymer modified bitumen, together with stabilizing fibre, can 48 49 extend the service life and eliminate the ravelling problems [4-7]. The Netherlands, which has PA wearing courses on more than 90% of its main highway network, also has long-term 50 experience with PA wearing courses. But contradictory to the experience in Hong Kong and 51 many other regions, the Dutch experience has shown that polymer modified bitumen has no 52 effect on the service life extension of PA wearing courses. It was reported that polymer 53 modified bitumen was only useful to obtain a higher binder content in PA which led to a 54 better behaviour in the field, but the same improvement could be obtained with base bitumen 55 and drainage inhibitor [8-13]. These oversea experiences can lead to different polices for the 56 design of PA wearing courses at large scaled application. Thus, it is worth to study and 57 understand the benefits of using base and polymer modified bitumen in PA to improve the 58 design of PA wearing courses in Hong Kong. 59

Bituminous mortar, also commonly known as fine aggregate matrix in North America, 60 61 consists of bitumen, filler and fine aggregates smaller than the minimum aggregate size in the 62 aggregate skeleton. It plays a dominating role on the viscoelastic properties of PA. Various studies have shown the potential of testing bituminous mortar as an efficient and repeatable 63 approach to predict the performance of asphalt mixture. For instance, Mohammad et al. [12, 64 13] investigated the viscoelastic behaviour of the bituminous mortar and hot mix asphalt. 65 Certain linkages between them were found and used to explain the effect of hydrated lime 66 67 under moisture damage conditions. Huurman et al. [14-17] designed a mechanistic lifetime 68 optimization tool for PA, based on the experimental tests of the behaviour of bituminous

mortar and the adhesive bond between stone and bituminous mortar. It was found that the 69 lifetime optimization tool calculations had a strong correlation with the full-scale PA 70 performance. Underwood and Kim [18] found that bituminous mortar can be useful for both 71 practical and model tasks with proper material design and testing. Sousa et al. [19] developed 72 a new procedure for preparing bituminous mortar specimens and conducted fracture 73 mechanics-based analysis of damage in bituminous mortar. He et al. [20] reported that the 74 75 bituminous mortar testing can be considered as an effective alternative approach to chemical 76 binder extraction for characterizing the properties of blended binders in asphalt mixtures containing high quantities of reclaimed asphalt pavement. 77

The high air void content makes PA more sensitive to damage due to traffic and 78 79 environmental effects than dense-graded mixtures. Ravelling, defined as the loss of stone particles from the pavement surface, is the most common type of damage of PA. Due to 80 ravelling, the average service life of PA wearing courses is usually shorter than that of dense-81 graded wearing courses [8-10]. Ageing of bituminous binder is believed to be one of the main 82 83 reasons for ravelling damage of PA wearing courses [21, 22]. Therefore, the benefits of using base and polymer modified bitumen in PA can be investigated through quantification of 84 bituminous mortar ageing and evaluation of ravelling resistance of PA wearing courses with 85 86 aged mortars.

The main objectives of this study are to quantify the ageing effect on the rheological 87 characteristics of bituminous mortars and apply it in evaluation of the ravelling resistance of 88 PA wearing courses. To achieve these objectives, bituminous mortars for two typical types of 89 PA wearing courses, one with base bitumen and the other with SBS modified bitumen, were 90 91 artificially aged in the laboratory. Cylindrical specimens were then prepared with these aged 92 mortars and tested using the Dynamic Shear Rheometer (DSR). Their rheological properties 93 were characterized by constructing the master curves of complex shear modulus and phase angle, and determining the shear fatigue lives at various shear strain levels, respectively. 94 95 Finite element models containing the structural geometries and material responses of the two 96 PA wearing courses were created in the program ABAQUS. The stresses and strains in these two PA wearing courses under traffic loads were simulated and analysed. 97

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### 99 2. Experimental Programs and Numerical Models

#### 100 2.1 Materials

Bituminous mortars for two types of PA were studied in this research. One is the PA 0/16,
which has been widely used as highway surfacing material in the Netherlands. It consists of

crushed stones with a nominal maximum aggregate size of 16 mm, crushed sand, mineral 103 104 filler and base bitumen with a penetration grade of 70/100. Its bitumen content is 5.5% by mass of total mineral aggregates [9]. The other is the PA 0/10, which is the typical type of PA 105 used in Hong Kong. This mixture consists of crushed stones with a nominal maximum 106 aggregate size of 10 mm, crushed sand, mineral filler and SBS modified bitumen with a 107 Superpave performance grade of PG76. It has a bitumen content of 5.8% by mass of total 108 mineral aggregates [1]. The gradations of these two asphalt mixtures are presented in Table 1. 109 The gradations of PA 0/16 and PA 0/10 were used to calculate the material compositions of 110 their bituminous mortars. 111

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Table 1: Gradations of the asphalt mixtures PA 0/16 and PA 0/10.

Mixture	Sieve size (mm)	22.4	16.0	11.2	8.0	5.6	2.0	0.5	0.18	0.063
PA 0/16	PA 0/16 Passing percentage		97.0	73.0	47.0	22.0	15.0	9.3	6.0	4.5
PA 0/10	Passing percentage	100	100	97.0	65.0	21.0	14.0	8.0	5.8	4.2

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According to Muraya's research on aggregate skeletons of asphalt mixtures [23], the 115 aggregate skeleton in PA is composed of aggregates with sizes larger than 0.5 mm. Therefore, 116 117 the bituminous mortar used in this research contained fine aggregates with sizes smaller than 0.5 mm. In order to determine binder content of the bituminous mortar, it was assumed that 118 all mineral aggregates in PA mixture are coated with a thin bitumen film of 10 µm [14, 15]. 119 The binder content of bituminous mortars was calculated by deducting the amount of bitumen 120 that coats the aggregates with sizes larger than 0.5 mm from the total amount of bitumen used 121 in the asphalt mixture. The surfaces of aggregates were estimated by simplifying the 122 aggregates as spheres with representative sizes. Table 2 presents the material compositions of 123 the two bituminous mortars used in this research. 124

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Table 2: Material compositions of the bituminous mortars.

Mortar type	Mixture	Fine aggregates (0.5-0.063 mm)	Mineral filler (<0.063 mm)	Binder
Mortar with base bitumen	PA 0/16	33%	31%	36%
Mortar with SBS modified bitumen	PA 0/10	27%	33%	40%

To prepare bituminous mortar, fine aggregates, mineral filler and bitumen were completely mixed at a temperature of 165 °C. Afterwards, the bituminous mortar was aged in an oven at 165 °C for 2 hours and then in a Pressure Ageing Vessel (PAV) at 100 °C for 80 hours under an air pressure of 2.1 MPa. During the ageing process, 50 gram of bituminous mortar was placed on a steel plate with a diameter of 140 mm.

Cylindrical mortar specimens for testing were prepared with both the fresh and aged bituminous mortars. A picture of the cylindrical mortar specimens and the schematic diagram of its geometry are given in Figure 1 (a) and (b), respectively. The total height of the cylindrical mortar specimen is 20 mm. At both ends, the cylindrical mortar specimen is enclosed by a steel block to allow clamping it into the measuring system of DSR. Over the central 10 mm length, the cylindrical mortar specimen has a constant diameter of 6 mm.

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Figure 1: Bituminous mortar specimens and the mould for preparation: (a) cylindrical mortar
specimens; (b) schematic diagram of specimen geometry; (c) Teflon mould; (d) filling mortar
into the mould.

A specially designed Teflon mould as shown in Figure 1 (c) was used to prepare the 146 cylindrical mortar specimens. The bituminous mortar was first cooled down on silicon paper 147 at room temperature. During the cooling process, the bituminous mortar was shaped into 148 cylinders with a diameter of around 6 mm (see Figure 1 (d)). After heating the Teflon mould 149 up to a temperature of 165 °C in an oven, these cylinders were inserted into the pre-heated 150 Teflon mould and kept in the oven for 10 minutes. Then they were taken out from the oven 151 and cooled down at room temperature. In order to remove the cylinder mortar specimens from 152 the Teflon mould, they were stored in a fridge at a temperature of -10 °C for 2 hours. Then the 153 Teflon mould was split by releasing the screws, after which the specimens could be removed 154 without any damage. Before testing, all the cylindrical mortar specimens were stored in a 155 156 fridge at a temperature of 5 °C to avoid development of any deformation.

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## 158 2.2 Test methods

The dynamic shear tests for measuring the rheological properties of the cylindrical mortar specimens were performed with the DSR MCR702. A special feature of this DSR equipment is that it can perform rheological tests with one drive unit for applying loading at bottom and another drive unit for recoding response at top simultaneously, which delivers more precise results. A special measuring system designed for solid specimen was used to mount the cylindrical mortar specimens in the DSR (see Figure 2 (b)).

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Figure 2: Dynamic shear test devices: (a) front view of DSR MCR702; (b) measuring system
 for solid specimens.

The dynamic shear tests were conducted in the strain-controlled mode. In the tests, a 170 sinusoidal deformation at a certain shear strain level was applied to the testing specimen. The 171 applied deformation and the corresponding torque were measured and the phase lag between 172 these two signals was determined. For the measurement of complex shear modulus, frequency 173 sweep tests from 100 to 0.01 Hz were performed on five mortar specimens at the test 174 temperatures of -10, 0, 10, 20 and 30 °C, respectively. In order to determine the strain level at 175 176 which the mortar behaves linearly, a strain amplitude sweep test at each test temperature was 177 carried out in advance. For the measurement of shear fatigue life, a continuous oscillating deformation was applied to each test specimen until it was broken. Various strain levels, 178 which were high enough to develop fatigue damage, were chosen for different types of 179 180 bituminous mortar in shear fatigue tests. For each type of bituminous mortar, shear fatigue tests were performed on nine specimens at 10 °C and 10 Hz. 181

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### 183 **2.3 Finite element models**

184 From the high-resolution Computed Tomography (CT) scanning image of PA, its three components (i.e. aggregate skeleton, bituminous mortar and air voids) can be discriminated 185 clearly (see Figure 3 (b) and (d)). Two-dimensional finite element models allowing the real 186 structure of the PA to be simulated, were created in the program ABAQUS, based on the 187 high-resolution CT scanning images of PA 0/16 and PA 0/10. The method of creating the 188 finite element models has been reported in previous studies [24, 25]. The PA 0/16 and PA 189 190 0/10 models used in this research (see Figure 3 (a) and (c)), have dimensions of 150 mm in length and 25 mm in height. 191

192 In the finite element models, the stone particles which have much higher stiffness than bituminous mortars, were simulated as rigid bodies in order to limit the mathematical size of 193 194 the models. The material response of bituminous mortars was a time domain viscoelastic material mode that is built in ABAQUS by means of Prony series. The terms in Prony series 195 196 were calibrated using the frequency-dependent master curve data from DSR tests [25, 26]. In 197 Hagos's research on the effect of ageing on binder properties on PA [21], it was concluded that ageing is the main reason for ravelling failure in PA wearing course because of its effects 198 199 on the cohesive characteristic of the binding material. So in the finite element modelling of 200 this research the stone particles were tied together with the bituminous mortars. The adhesive 201 behaviour between mortar and stone was not investigated.

The load signals applied in models were derived from actually occurring contact stresses between tire and pavement surface. The program TyreStress [27] was used to simulate the tire contact stresses. A 425/65 R22.5 tire with a load of 50 kN and a tire inflation pressure of 0.8 MPa was used to generate the tire contact stress distributions. Then the vertical and longitudinal stress signals as a function of time were obtained for the wheel load travelling at a speed of 80 km/h. Afterwards, the stress signals were transformed into force signals that can be applied on the stone particles at the surface of the models. The method of acquiring the load signals and the load signals themselves can be found in a former research [25].

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PA 0/16; (c) and (d) for PA 0/10.

- 214
- 215 3. Results and Discussion

# 216 **3.1 Chemical properties of reclaimed bituminous binders**

- 217 In order to determine laboratory ageing level, the chemical properties of reclaimed bituminous
- 218 binders from the laboratory-aged mortars were compared with those of reclaimed bituminous
- 219 binders from field-aged asphalt mixtures. The field-aged asphalt mixtures were obtained from

Figure 3: Structural models and CT scanning images for PA wearing courses: (a) and (b) for

two PA wearing courses which were both approximately 5 years old [9, 28]. The bituminous 220 221 binders used in those two PA wearing courses were base bitumen and SBS modified bitumen, respectively. They had similar engineering properties as the bituminous binders used for 222 preparing the mortars in this research, although they were from different sources. In this paper, 223 the reclaimed bituminous binders from the laboratory-aged mortars with base bitumen and 224 SBS modified bitumen are referred to as aged base bitumen @ lab and aged modified bitumen 225 @ lab, respectively. The reclaimed bituminous binders from the field-aged asphalt mixtures 226 with base bitumen and SBS modified bitumen are referred to as aged base bitumen @ field 227 and aged modified bitumen @ field, respectively. 228

Ageing of bituminous binders is mainly caused by oxidation. The presence of oxidation 229 230 groups are therefore important factors for detecting ageing in infrared spectra. The oxidation groups for bituminous binders, namely ketones (C=O) at the wavenumber of 1700 cm<sup>-1</sup> and 231 sulfoxides (S=O) at the wavenumber of 1030 cm<sup>-1</sup>, are two important ageing indicators. 232 Figure 4 illustrates the representative infrared spectra of the reclaimed bituminous binders at a 233 wavenumber region of 1800-600 cm<sup>-1</sup>. The specific absorption peaks at the wavenumber of 234 around 1700 cm<sup>-1</sup> are observed in the infrared spectra of all aged bituminous binders, but not 235 in those of the fresh bituminous binders. The specific absorption peaks at the wavenumber of 236 around 1030 cm<sup>-1</sup> in the infrared spectra of all aged bituminous binders are larger than those 237 of the fresh bituminous binders. 238





Figure 4: Representative infrared spectra of the reclaimed bituminous binders.

From the infrared spectra, the semi-quantitative method proposed by Lamontagne et al. [29] was used to determine the ageing levels of the reclaimed bituminous binders. In this semiquantitative method, the sum of the areas at some specific bands is believed not to be influenced by ageing and therefore can be used as a reference. Areas of the specific bands are compared with this reference. Several structural and functional indices can be calculated from the band areas using Equations 1 to 6:

Aromaticity index=
$$\frac{A_{1600}}{\Sigma A}$$
 (1)

$$Aliphatic index = \frac{A_{1460} + A_{1376}}{\sum A}$$
(2)

Branched aliphatic=
$$\frac{A_{1376}}{A_{1460} + A_{1376}}$$
 (3)

$$Long \ chains = \frac{A_{724}}{A_{1460} + A_{1376}} \tag{4}$$

$$Carbonyl index = \frac{A_{1700}}{\sum A}$$
(5)

$$Sulfoxide index = \frac{A_{1030}}{\sum A}$$
(6)

248 Where  $A_{xxx}$  represents the area at a specific band of spectrum;  $\Sigma A$  is the summation of areas 249 from  $A_{(2953, 2923, 2862)}$ ;  $A_{1700}$ ,  $A_{1600}$ ,  $A_{1460}$ ,  $A_{1376}$ ,  $A_{1030}$ ,  $A_{864}$ ,  $A_{814}$ ,  $A_{743}$  and  $A_{724}$ .

The carbonyl index and sulfoxide index are functional indices representing the rate of oxidation groups in the bituminous binders, while others are structural indices. Table 3 presents the structural and functional indices of the reclaimed bituminous binders.

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Table 3: Structural and functional indices of the reclaimed bituminous binders.

Material	Aromatici -ty index	Aliphatic index	Branched aliphatic	Long chains	Carbonyl index	Sulfoxide index
Fresh base bitumen	0.052	0.275	0.174	0.037	0.000	0.021
Aged base bitumen @ lab	0.058	0.264	0.179	0.039	0.018	0.032
Aged base bitumen @ field	0.048	0.250	0.152	0.059	0.017	0.031
Fresh modified bitumen	0.069	0.261	0.142	0.072	0.000	0.021
Aged modified bitumen @ lab	0.063	0.248	0.149	0.074	0.017	0.038
Aged modified bitumen @ field	0.045	0.255	0.158	0.035	0.020	0.031

Compared with the fresh base bitumen, the aged base bitumen @ lab showed significant 256 higher carbonyl and sulfoxide indices, while the structural indices did not change obviously. 257 Similar findings were obtained between the aged modified bitumen @ lab and fresh modified 258 bitumen as well. The carbonyl and sulfoxide indices of the aged base bitumen @ lab were 259 close to those of the aged base bitumen @ field. The differences in their structural indices 260 may be due to the difference in binder sources. The aged modified bitumen @ lab also 261 showed similar carbonyl and sulfoxide indices compared with the aged modified bitumen @ 262 field. In other words, the ageing performed on the bituminous mortars in this research 263 simulated approximately 5-year field ageing of PA wearing courses, in terms of the carbonyl 264 and sulfoxide indices of the reclaimed bituminous binders. 265

In addition, it can be found that the aged base bitumen and aged modified bitumen exhibited very similar carbonyl and sulfoxide indices. This means that after the long-term ageing, the base bitumen and modified bitumen tend to have a similar ageing level.

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### 270 **3.2** Complex shear modulus of bituminous mortars

Master curves of the complex shear modulus and phase angle as a function of the reduced frequency were constructed at a reference temperature of 10 °C by using the time-temperature superposition principle. The shift factors used to obtain the master curves were determined by means of the Williams-Landel-Ferry (WLF) formula given in Equation 7:

$$\log a_T = \frac{-C_1(T - T_0)}{C_2 + (T - T_0)} \tag{7}$$

275 Where  $a_T$  is shift factor; *T* is test temperature;  $T_0$  is reference temperature;  $C_1$  and  $C_2$  are 276 constants.

To fit the frequency-dependent master curves, the Modified Huet-Sayegh (MHS) model developed by Woldekidan et al. [16] was chosen in this research. The MHS model is capable of describing the response of bituminous binders as well as mixtures over a wide frequency window. In the MHS model, a linear dashpot is placed in series with the original Huet-Sayegh (HS) model [30]. This improves the low frequency region fitting of the model to the master curve data and also allows the model to simulate viscous deformations. Equation 8 provides the mathematical expression of the MHS model:

$$J^{*}(\omega) = \frac{G'}{|G^{*}(\omega)|^{2}} - i\left[\frac{G''}{|G^{*}(\omega)|^{2}} + \frac{1}{\eta_{3}\omega}\right] = J'(\omega) - iJ''(\omega)$$
(8)

284 Where  $J^*(\omega)$  represents the complex creep compliance of the MHS model;  $G^*$  is the complex 285 shear modulus of original HS model; G' is the storage shear modulus of original HS model; 286 *G*" is the loss shear modulus of original HS model;  $\eta_3$  is linear dashpot parameter;  $J'(\omega)$ 287 represents the storage creep compliance of the MHS model; and  $J''(\omega)$  represents the loss 288 creep compliance of the MHS model.

The expressions for the complex, storage and loss shear modulus of original HS model can be obtained using the following equations [30]:

$$G^{*}(\omega) = G_{0} + \frac{G_{\infty} - G_{0}}{1 + \delta_{1}(i\omega\tau_{1})^{-m_{1}} + \delta_{2}(i\omega\tau_{2})^{-m_{2}}}$$
(9)

$$\delta_i = \frac{\tau_{i(G_{\infty} - G_0)}}{\eta_i} \tag{10}$$

$$G' = G_0 + A \frac{G_\infty - G_0}{A^2 + B^2}$$
(11)

$$G'' = B \frac{G_{\infty} - G_0}{A^2 + B^2}$$
(12)

$$A = 1 + \delta_1 \frac{\cos\left(m_1 \frac{\pi}{2}\right)}{(\omega\tau)^{m_1}} + \delta_2 \frac{\cos\left(m_2 \frac{\pi}{2}\right)}{(\omega\tau)^{m_2}}$$
(13)

$$B = \delta_1 \frac{\sin\left(m_1 \frac{\pi}{2}\right)}{(\omega\tau)^{m_1}} + \delta_2 \frac{\sin\left(m_2 \frac{\pi}{2}\right)}{(\omega\tau)^{m_2}}$$
(14)

Where  $G_{\infty}$  is the instantaneous shear modulus;  $G_0$  is the rubbery shear modulus;  $\delta_1$  and  $\delta_2$  are model parameters;  $m_1$  and  $m_2$  are the parabolic dashpot coefficients;  $\eta_1$  and  $\eta_2$  are parabolic dashpots' parameters;  $\tau_1$  and  $\tau_2$  are time constants; and *A* and *B* are the variables.

The MHS model has a total of nine independent parameters. For response modelling of bituminous materials, only one time constant ( $\tau = \tau_1 = \tau_2$ ) is usually used and the model parameter  $\delta_2$  is considered as unity [31]. Consequently, only seven parameters are required to describe the complete response of bituminous materials covering various temperature and frequency regions.

299 For each type of bituminous mortar, the measured complex shear moduli and phase angles of 300 five cylindrical mortar specimens at five test temperatures were shifted to the reference temperature of 10 °C in order to create master curves. Then the master curve data were fitted 301 302 by means of the MHS model. The master curves of the complex shear moduli and phase angles of the fresh and aged bituminous mortars are shown in Figure 5. The high anastomosis 303 304 within test results from five specimens in the master curves implies that the rheological tests of the cylindrical mortar specimens provided very good testing repeatability. As expected, 305 306 ageing increased the complex shear modulus and decreased the phase angle significantly over a wide frequency range (1.0E-04 to 1.0E+04 Hz), indicating that the aged bituminous mortars 307 became stiffer. 308



Figure 5: Master curves of the complex shear modulus and phase angle of bituminous mortars at a reference temperature of 10 °C: (a) mortars with base bitumen; (b) mortars with SBS modified bitumen. 

The fresh mortar with base bitumen showed lower complex shear moduli and higher phase angles than the fresh mortar with SBS modified bitumen, especially at frequencies lower than 

1 Hz. However, after ageing, their complex shear moduli and phase angles were similar at all
frequencies. Hence, it can be concluded that ageing had more influence on the complex shear
modulus and phase angle of the mortar with base bitumen compared with the mortar with
SBS modified bitumen.

For the fresh mortar with SBS modified bitumen, reduction in phase angles at a low frequency range from 1.0E-05 to 1.0E-03 Hz (corresponding to high temperature range) was observed. This phenomenon also occurs in the master curve of phase angle of SBS modified bitumen, which is attributed to the SBS polymers network in binder. However, for the aged mortar with SBS modified bitumen, no such reduction in phase angles was found. The possible reason is that the SBS polymers had degraded after ageing.

Besides, Figure 5 shows that the master curves of complex shear modulus and phase angle for all bituminous mortars are well described by the MHS model. Table 4 presents the model parameters of these master curves. The values of the coefficient of determination ( $\mathbb{R}^2$ ) are all higher than 0.99. This proves the good agreement between the MHS model prediction and the measured data. The model fitted data were used to calibrate the Prony series terms of the bituminous mortars for finite element modelling.

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Table 4: Model parameters of the master curves of complex shear modulus and phase anglesof the bituminous mortars.

Parameters			Mortar with	base bitumen	Mortar with SBS modified bitumen		
			fresh aged		fresh	aged	
WLF	<b>C</b> <sub>1</sub>	[-]	17.5	29.6	29.7	62.2	
formula	$C_2$	[-]	130.4	195.2	204.3	403.5	
	$m_1$	[-]	0.743	0.529	0.687	0.525	
	m <sub>2</sub>	[-]	0.311	0.230	0.270	0.205	
MIIC	$\delta_1$	[-]	3.35E-02	1.97E-02	1.59E-02	1.33E-02	
MH5 model	τ	[s]	1.80E-06	1.34E-05	9.81E-06	1.02E-05	
model	G∞	[MPa]	2815	4004	2576	3094	
	$G_0$	[MPa]	3.36E-04	2.39E-02	4.74E-02	4.60E-02	
	η3	[MPa·s]	136	148200	19397	169374	
<b>D</b> <sup>2</sup>	@ G*	[-]	0.999	0.999	0.999	0.999	
K-	$(a)\theta$	[-]	0.999	0.999	0.997	0.998	

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### 337 **3.3 Shear fatigue life of bituminous mortars**

Reduction of the complex shear modulus in shear fatigue test was considered by plotting the complex shear modulus versus the number of loading cycles. Figure 6 shows an example of the shear fatigue test result of a bituminous mortar in the strain-controlled mode. The complex 341 shear modulus drops sharply at the initial stage of the test followed by a relatively linear low-342 rate decrease during the middle portion of the test. Afterwards, a sharp decrease of the 343 complex shear modulus to a very low value occurs during the back portion of the test. Finally, 344 the curve flattens towards the end of the test.

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Figure 6: Example of the shear fatigue test result and the illustration of determining the shear
fatigue life of a bituminous mortar specimen.

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The failure criterion based on the 50% of initial stiffness (or modulus) method is commonly 350 used in the fatigue tests of asphalt mixture under the strain-controlled mode. However, this 351 352 criterion seems not able to capture the true fatigue failure of bituminous mortars, since 50% complex shear modulus reduction was often reached before the crack initiation in the 353 bituminous mortars. The fatigue resistance evaluation method for asphaltic mixtures proposed 354 by Rowe and Bouldin [32], which is based on energy ratio, was adopted to define the fatigue 355 356 life of bituminous mortars in this research. In that method, the fatigue curves in the straincontrolled mode are subdivided into four regions: the initial specimen heating region, the 357 micro-crack formation region, the crack formation and propagation region, and finally the 358 specimen breakdown region (see Figure 6). The fatigue failure is defined as the point when 359 the curve transitions from the micro-crack formation region to the crack formation and 360 361 propagation region.

The transition point (Nt) is determined based upon evaluation of the product of stiffness and number of loading cycles. The meaning of the transition point can be explained mathematically using the Taylor's series expansion given in Equation 15 and 16. In the micro-crack formation region, the first differential  $(dE^*/dn)$  is a negative constant. The second differential  $(d^2E^*/dn^2)$  equals to zero. As cracks form and begin to propagate, the first differential  $(dE^*/dn)$  is still negative but increasing in magnitude. The second differential  $(d^2E^*/dn^2)$  becomes negative. So the product of stiffness and number of loading cycles reduces in the crack formation and propagation region. The resulting maximum indicates the transition point between micro-crack formation and crack formation. The transition point is a reasonably acceptable failure point, as reported by Kim et al. [33, 34].

$$E^* = E_0^* + n\frac{dE^*}{dn} + \frac{n^2}{2!}\frac{d^2E^*}{dn^2} + \frac{n^3}{3!}\frac{d^3E^*}{dn^3} + \cdots$$
(15)

$$E^*n = E_0^*n + n^2 \frac{dE^*}{dn} + \frac{n^3}{2!} \frac{d^2 E^*}{dn^2} + \frac{n^4}{3!} \frac{d^3 E^*}{dn^3} + \dots$$
(16)

Where  $E^*$  is stiffness or modulus;  $E_0^*$  is the initial stiffness or modulus; and *n* is number of loading cycles.

For each type of bituminous mortar, fatigue lives at nine strain levels were successfully acquired by means of analysing the transition points of cylindrical mortar specimens from the shear fatigue tests. The number of loading cycles to failure at applied strain levels was plotted on a log-log scale, as shown in Figure 7.

378



379

Figure 7: Fatigue relations between the number of loading cycles to failure and shear strain
for fresh and aged bituminous mortars under the strain-controlled mode.

382

In Figure 7, the fresh mortar with base bitumen showed a longer fatigue life than its aged mortar at shear strain of higher than 8.6E-03. When shear strain is lower than 8.6E-03, its

aged mortar had a longer fatigue life. The fresh mortar with SBS modified bitumen showed a 385 longer fatigue life than its aged mortar at shear strain of higher than 3.7E-03. When shear 386 strain is lower than 3.7E-03, its aged mortar had a longer fatigue life. This means ageing 387 decreased the fatigue life of bituminous mortar at high strain levels, but increased its fatigue 388 life at low strain levels. The fresh mortar with SBS modified bitumen showed higher fatigue 389 life than fresh mortar with base bitumen. After ageing, the aged mortar with SBS modified 390 391 bitumen still behaved better in fatigue resistance than the aged mortar with base bitumen. But 392 the difference in fatigue lives between aged bituminous mortars is smaller than that between fresh bituminous mortars. Thus, it can be concluded that ageing resulted in more changes in 393 the fatigue life of mortar with SBS modified bitumen than that of mortar with base bitumen. 394

395 Bituminous mortars exhibit viscoelastic behaviour, which leads to energy dissipation during cyclic loading. Dissipated energy is often used by researchers to explain fatigue damage 396 397 development. Huurman et al. [14-15] proposed a mortar fatigue model based on the dissipated energy concept to explain the mortar fatigue behaviour. In their mortar fatigue model, the 398 399 dissipated energy per cycle in the initial phase is considered to be indicative for the fatigue life. The dissipated energy per cycle in the initial phase can be determined by the total area of 400 various stress-strain hysteresis loops. Equations 17 and 18 provides the mathematical 401 expression of that mortar fatigue model. 402

$$N_f = (W_0/W_{initial})^n \tag{17}$$

$$W_{initial} = \int \sigma_{ij} d\varepsilon_{ij} \tag{18}$$

403 Where  $N_f$  is the number of loading cycles to failure;  $W_0$  is the reference energy;  $W_{initial}$  is the 404 dissipated energy per cycle in initial phase; *n* is material constant;  $\tau_{ij}$  is stress components; and 405  $\varepsilon_{ij}$  is strain components.

406 This mortar fatigue model will be used to interpret the stress and strain signals obtained from 407 finite element modelling of PA wearing courses such that the mortar fatigue life can be predicted. For the shear fatigue test, the initial dissipated energy per cycle is equal to the area 408 of the hysteresis loop obtained by plotting the shear stress against the shear strain. The initial 409 dissipated energy per cycle for each mortar specimen measured in the shear fatigue test was 410 calculated. In this research nine shear fatigue tests at different shear levels were performed for 411 each type of bituminous mortar. The number of loading cycles to failure mentioned above 412 was then plotted against the initial dissipated energy per cycle on a log-log scale. As indicated 413 in Figure 8, the number of loading cycles to failure follows a linear relation with the initial 414

dissipated energy per cycle on a log-log scale. Based on these data, the mortar parameters (reference energy  $W_0$  and material constant *n*) were determined by the method of least square fitting. The obtained model parameters are given in Table 5. The values of coefficient of determination ( $\mathbb{R}^2$ ) indicate that the mortar fatigue model shows a good fit with the test results.



420

Figure 8: Relations between the number of loading cycles to failure and initial dissipated
energy per cycle for fresh and aged bituminous mortars at 10 °C.

423

Table 5: Parameters of the mortar fatigue model based on the initial dissipated energy per

425

Mortar type		W <sub>0</sub> [MPa]	n [-]	$\mathbb{R}^2$
Mortar with base	Aortar with base fresh		1.468	0.993
bitumen aged		1.059	2.825	0.992
Mortar with SBS	fresh	7.322	2.293	0.975
modified bitumen aged		1.771	2.709	0.954

cycle.

426

## 427 **3.4 Stress and strain simulation in PA models**

The material responses of fresh and aged mortars with base bitumen were input into the PA
0/16 model for simulation. While the material responses of fresh and aged mortars with SBS

430 modified bitumen were implemented in the simulation of PA 0/10 model. The shear stresses

and strains that develops within the bituminous mortar in the model were output for analysis,

as well as the shear stresses and strains. Figure 9 shows impressions of the distribution of
maximum principal stress in the PA 0/16 and PA 0/10 models. Because ravelling of PA
wearing course normally starts at the first stones on the surface, several critical locations
within the bituminous mortar between the first stones on surface of the model were selected
for analysis (see Figure 10). At all the selected locations, the bituminous mortar shows
relatively higher levels of maximum principal stress or shear stress.



440 Figure 9: Impressions of the maximum principal stress distribution in the PA 0/16 model (a)
441 and PA 0/10 model (b).



444 Figure 10: Selected locations for analysis from the PA 0/16 model (a) and PA 0/10 model (b).

446 Figure 11 presents an example of the hysteresis loops from shear stress and strain signals at location 1 in the PA 0/16 model. At this location, the shear stress changed slightly after 447 ageing. While the shear strain had a large decrease after ageing. The initial dissipated energy 448 per cycle at this location can be calculated from these hysteresis loops. For the fresh mortar 449 with base bitumen it is 4.8E-04 MPa. For the aged mortar with base bitumen the value is 450 9.4E-05 MPa. Based to Equation 17 and Table 5, the fatigue lives of these mortars at location 451 452 1 can be calculated. The predicted fatigue lives of fresh and aged mortars at location 1 in PA 0/16 model are 3.3E+06 and 2.8E+11, respectively. The results of peak values of shear stress 453 and strain from other locations in the PA 0/16 and 0/10 models are given in Table 6. The 454 results of initial dissipated energy per cycle and predicted fatigue life that were calculated 455 456 from the obtained shear stress and strain signals are presented as well.

As indicated in Table 6, aged mortars always showed higher values of predicted fatigue life 457 than fresh mortars at the same location. This is consistent with the findings from shear fatigue 458 tests that aged mortars had a longer fatigue life than fresh mortars at low levels of shear 459 460 strains. Comparing the predicted fatigue lives between the PA 0/16 and 0/10 models, it can be found that bituminous mortar with SBS modified bitumen (in PA 0/16 model) had higher 461 values of predicted fatigue life than bituminous mortar with base bitumen (in PA 0/10 model) 462 before and after ageing. It indicates that the PA 0/10 wearing course with SBS modified 463 bitumen had a better ravelling resistance than the PA 0/16 wearing course with base bitumen. 464 But it should be noted that this advantage had weakened as the ageing of bituminous mortars. 465 466



468 Figure 11: Example of the hysteresis loops from shear stress and strain signals at location 1 in
469 the PA 0/16 model.

4	7	1

Table 6: Results from the stress and strain simulation in the PA models.

Model	Loca -tion	Mor- tar	Max. principal stress [MPa]	Max. principal strain [-]	Shear stress [MPa]	Shear strain [-]	Initial dissipated energy [MPa]	Predicted fatigue life [-]
		fresh	0.831	1.11E-03	0.441	1.80E-03	4.8E-04	3.3E+06
	1	aged	0.739	3.65E-04	0.404	6.27E-04	9.4E-05	2.8E+11
		Δ	-11%	-67.0%	-8.3%	-65.1%		
DA		fresh	-2.191	1.37E-03	-0.777	-2.87E-03	1.5E-03	6.2E+05
PA 0/16	2	aged	-2.259	5.35E-04	-0.799	-1.12E-03	4.1E-04	4.4E+09
0/10		Δ	3%	-60.9%	2.7%	-61.1%		
	3	fresh	-1.594	2.12E-03	-1.473	-5.22E-03	4.9E-03	1.1E+05
		aged	-1.595	8.62E-04	-1.519	-2.10E-03	1.4E-03	1.4E+08
		Δ	0%	-59.4%	3.1%	-59.7%		
	1	fresh	-1.405	1.77E-04	-0.255	-6.78E-04	1.1E-04	1.2E+11
		aged	-1.425	9.84E-05	-0.273	-3.94E-04	5.0E-05	2.1E+12
		Δ	1.4%	-44.5%	7.1%	-42.0%		
DA		fresh	0.766	8.83E-04	-0.439	-1.48E-03	3.4E-04	8.6E+09
PA 0/10	2	aged	0.770	4.47E-04	-0.442	-7.56E-04	1.2E-04	2.0E+11
0/10		Δ	0.5%	-49.3%	0.7%	-49.0%		
		fresh	1.650	1.59E-03	-0.701	-2.42E-03	8.9E-04	9.5E+08
	3	aged	1.635	8.09E-04	-0.710	-1.24E-03	3.3E-04	1.3E+10
		Δ	-0.9%	-49.2%	1.3%	-48.5%		

472

473 The shear stresses within bituminous mortars in the PA models changed slightly or nothing 474 after ageing. However, the shear strains decreased significantly. For the PA 0/16 model, an average decrement of 62.0% was found in the shear strains after ageing. For the PA 0/10 475 model, an average decrement of 46.5% was found in the shear strains after ageing. Ageing 476 477 resulted in stiffer bituminous mortars allowing less development of strain in the PA models. Table 6 also gives the results of peak values of maximum principal stress and strain from 478 479 different locations of the PA models for comparison. The tendency of maximum principal stress is similar as that of shear stress. For the PA 0/16 model, an average decrement of 62.4% 480 was found in the maximum principal strains after ageing. For the PA 0/10 model, an average 481 decrement of 47.7% was found in the maximum principal strains after ageing. An interesting 482 483 finding is that the decrements of the maximum principal strain and shear strain in the PA 0/16 484 model are approximately 15% higher than those in the PA 0/10 model. It indicates that ageing caused less change on the flexibility of bituminous mortar with SBS modified bitumen than 485 that of bituminous mortar with base bitumen. 486

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- 488

#### 489 **4.** Conclusions

Based on the findings and analysis presented in this paper, the following conclusions can be 490 drawn: (1) The rheological tests on the cylindrical mortar specimens provided very good 491 result repeatability, as evidenced by the high anastomosis within the test results from different 492 mortar specimens; (2) The master curves of complex shear modulus and phase angle of 493 bituminous mortars were well described by the MHS model. Ageing had more influence on 494 495 the complex shear modulus and phase angle of bituminous mortar with base bitumen compared with the bituminous mortar with SBS modified bitumen; (3) The fatigue failure of 496 497 bituminous mortars in the strain-controlled shear fatigue test should be defined as the point when the fatigue curve transitions from the micro-crack formation region to the crack 498 499 formation and propagation region, based upon evaluation of the product of stiffness and 500 number of loading cycles. Ageing caused more changes on the fatigue resistance of the mortar with SBS modified bitumen than that of the mortar with base bitumen; (4) The bituminous 501 mortars with similar complex shear modulus can have different performances of fatigue 502 503 resistance; (5) The PA 0/10 wearing course with SBS mortar had a better ravelling resistance 504 than the PA 0/16 wearing course with base mortar; (6) Ageing had more significant effect on 505 the ravelling resistance of the PA 0/16 wearing course with base mortar than the PA 0/10 wearing course with SBS mortar. 506

507 This study has developed an efficient and reliable test protocol to quantify the ageing effects 508 on the rheological characteristics of bituminous mortar. By following this protocol, future 509 research can be conducted on measuring the properties of bituminous mortar under different 510 ageing and rejuvenating conditions, based on which effective numerical models can be built 511 to predict the performance of PA and evaluate the effectiveness of various preservative 512 maintenance techniques for PA wearing courses.

513

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