

1 **Multiple-risk assessment of water supply, hydropower and**
2 **environment nexus in the water resources system**

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8 **Abstract:** Hydropower has been one of the effective and reliable renewable sources
9 utilized for electricity generation globally, which forms over 70 % of all the renewable
10 energy measures since 2016. However, this effective energy source can be greatly
11 affected by the uneven spatiotemporal distributions of water resources in the catchment,
12 leading to the potential risks of insufficient water supply, hydropower and ecological
13 water uses. In this study, the multi-dimensional models by coupling water supply,
14 hydropower generation and environment effects were developed to improve the
15 efficiency and sustainability of water resources utilization. To this end, the joint
16 distributions and conditional expectation models were established to analyze the nexus
17 of water supply, hydropower and environment variables, thereby to evaluate multiple
18 risks in the water resources system. For the validation and demonstration of the
19 proposed method, the upper Yangtze River Basin was selected for a case study through
20 multivariate analysis under different conditions. The application results of bivariate
21 analysis indicated that the probability of water supply exceeding a threshold value
22 decreases gradually with the increase of hydropower generation, which means that the
23 risk of insufficient water supply increases with the increasing of the hydropower
24 generation. Specifically, when the frequency of hydropower generation exceeds 90 %,

25 both the expected values of water supply sufficiency and water use sustainability will
26 decrease sharply, causing potential risks of water supply insufficiency and environment
27 damage at upstream of the dam. Furthermore, the application results of trivariate
28 analysis evidenced that different combinations of hydropower generation and
29 ecological water use may be achievable for optimally compromising the water
30 resources supply and utilization. The results and findings of this study may provide
31 useful implications for effective multiple function-based development of water
32 resources, with aims to reduce the water supply risks as well as to improve the water
33 utilization efficiency and environmental sustainability.

34 **Keywords:** water resources system, water supply, hydropower, water-energy-
35 environment nexus, multiple-risk assessment

36 **1. Introduction**

37 Freshwater is one of most valuable and crucial natural resources for agricultural,
38 industrial, municipal, and environmental uses. In the early times of human history, the
39 global freshwater is more than enough to fulfill the demands and requirements of
40 different water use purposes , so that the ecosystems and environment conditions on
41 the Earth can be well maintained during that period. However, in the recent and modern
42 times, the rapid progress and development of the human society, including economic
43 and population increases as well as agricultural and industrial activities, have resulted
44 in and subsequently accelerated the water withdrawals over the world. Moreover, it is
45 indicated that by 2050, the world population is projected to reach 9.8 billion, which

46 may result in 55 % more water required to meet the basic demands worldwide (Kaneda
47 et al., 2015). Thus, the competition among various purposes of water use will become
48 more and more intense and critical worldwide in the future. From this perspective,
49 water scarcity has been a crucial problem globally, which may affect every continent
50 and around 2.8 billion people on the Earth with at least one month out of every year.
51 More precisely, water scarcity is the shortage of water resources available to meet the
52 demands of water usage within a region. Currently, more than 1.2 billion people are
53 lacking access to potable water (Onda et al., 2012). As a result, the shortage situation
54 of water will sacrifice partially or fully the household, industrial, agricultural, and
55 environment demands.

56 On the other hand, with the increasing population and GDP, the global electricity
57 demand will reach around 38,700 terawatt-hours by 2050 from 25,000 terawatt-hours
58 in 2017 (i.e., with about 55 % increase), driving new investment in power generation
59 capacity. Hydropower is one of the promising renewable sources for electrical power
60 generation, accounting for over 70 % of total renewable electricity globally in recently
61 years (Pazheri et al., 2014). With total amount of 1,064 GW installed capacity in 2016,
62 hydropower has contributed to more than 16 % of the global electricity among all
63 energy sources (Ciriminna et al., 2018). Moreover, hydropower has also been found to
64 be a renewable and reliable energy resource with high flexibility and consistency,
65 which can meet both requirements of base-load electricity and unexpected demands
66 (e.g. with pumped storage technology) (Dell et al., 2001; Duan and Gao, 2019).
67 Estimates from the World Energy Council have indicated that the availability of the

68 untapped hydropower potential worldwide attains to approximately 10,000 TW·h/year
69 since 2015, of which the main hydropower generation potential countries include
70 China, USA, Brazil, Canada, India, and Russia (Ahamd, 2019). In this regard, the
71 variabilities in water supply and policies governing water use are important factors for
72 defining the efficiency and capacity of hydropower generation (Macknick et al., 2012).
73 At the same time, these variations in hydropower generation may affect the quantity
74 and quality of basin water supply.

75 Environment is another key issue in water resources management (Williams,
76 2011). The Water Security Series has set out key concepts in water management in the
77 context of the global need for environmental sustainability. Rational water resources
78 management could be an improvement of the environment. With the increasing
79 demand of essential resources (food, water and energy) due to the rapid growth of
80 global population, the water resources systems and ecosystems have suffered from
81 severe pressures for maintaining their sustainability. As a result, it has been gradually
82 emphasized in the relevant policy and management worldwide for the importance of
83 the environmental water needs and allocations (e.g. Postel and Richter, 2003). The
84 report from the World's Local Bank has also confirmed that the priority of water
85 allocations for social and environmental purposes has been and will be increasingly
86 recognized in water laws around the world (Dinar et al., 1997).

87 Consequently, how the allocation, use, and management of water resources are
88 addressed will have dramatic impacts on the environment, economy, and quality of
89 human life. Water, energy and environment can interdependently support and influence

90 the overall economic development and societal progress. In addition, the
91 environmental need for water must be balanced against human water use. On this point,
92 it is important to analyze the water supply, hydropower generation and environment
93 impact in the water resources system together, so as to understand and emphasize the
94 dependences and interactions of all these aspects (Wu and Chen, 2013; Stenberg,
95 2010).

96 Recently, many researches have been carried out concerning the water-energy
97 nexus, water-food nexus, and energy-food nexus (Siddiqi and Anadon, 2011;
98 McCornick et al., 2008; Biggs et al., 2015; Zhang et al., 2019). To respond the influence
99 of the global climate change and societal development (e.g., population and economic
100 growth, globalization and urbanization), the water-food-energy (WFE) nexus has been
101 conceptualized and used recently by different researchers in the community (Endo et
102 al., 2015; Leck et al., 2015). In fact, the WPE systems are essentially interconnected
103 within a practical water cycle that is interfered largely by different human activities
104 (Sivapalan et al., 2012, 2014; Feng et al., 2016). In this regard, the WPE systems should
105 be described and investigated as a comprehensive nexus (which is defined as WPE
106 nexus in this study), because of its complex interconnections and interdependences
107 (Feng et al., 2016). Due to the uneven spatiotemporal distributions of water resources,
108 the WPE nexus may be encountered with multiple risks of insufficient water supply,
109 inadequate hydropower generation, deteriorative environmental condition and others.
110 In recent years, few researches have focused on risk analysis associated with water-
111 energy nexus (Gallagher et al., 2016; Cai et al., 2019). Specifically, the water, food and

112 energy policy and management has been prescribed as a crucial risk role for their
113 research directions (Gallagher et al., 2016). Hussien et al. (2018) assessed the risk of
114 water-energy-food nexus by exceeding a threshold. Cai et al. (2019) analyzed
115 integrated risk of water-energy nexus through a comprehensive method of system
116 dynamics, orthogonal design and copula analysis. Zhang et al. (2019) assessed the risk
117 and structure of the dynamics of water-food-energy nexus based on a water footprint
118 method. However, so far there are very few studies on the risk assessment of the WPE
119 nexus.

120 For river basins, the water supply, hydropower generation and environmental
121 water use are related and linked by water flows in the basin. Usually, the water
122 resources used for water supply in the basin at the upstream of the dam cannot be used
123 for hydropower generation at downstream (Whittington et al., 2005). As a result, there
124 is great of conflicts among these different water uses, which forms a typical benefit-
125 risk problem in water resources system. To this end, a Bayesian approach could be a
126 useful tool to analyze the conflict problem of water resources (Varouchakis et al., 2016,
127 2019). For example, Varouchakis et al. (2016) used the Bayesian approach to analyze
128 the cost-benefit-risk for water resources management. However, so far in the
129 hydrological community, there is no study focusing on the comprehensive risk
130 assessment for the WPE system under different influential conditions.

131 Since the water supply, hydropower generation and environment are dependent in
132 a water resources system (Stickler et al., 2013), a joint analysis method, namely copula
133 method, can be a useful method to involve these kinds of dependences, which will also

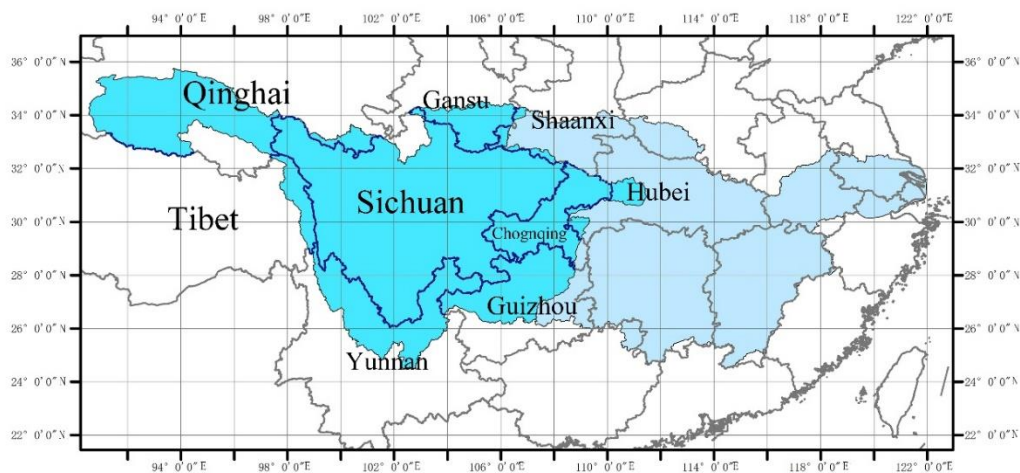
134 be introduced in this study for the WPE nexus investigation. Meanwhile, multivariate
135 distribution functions are useful tools and have been commonly applied in the
136 hydrological research community for analyzing multiple dependent variables and
137 corresponding dependence structures (Chebana and Ouarda, 2011). Specifically, the
138 multivariate distribution function has been widely used for rainfall frequency analysis,
139 flood frequency analysis, and stochastic simulation (Yin et al., 2018; Tu et al., 2016,
140 2018).

141 In this study, three variables were defined for representing the water supply,
142 hydropower and environmental water use, respectively. The WPE nexus was analyzed
143 based on the multivariate distribution functions as follows. First, a joint distribution
144 was established to simulate the dependences among different variables. Second, the
145 conditional distribution was derived for each representative variable. Third, the
146 conditional expectation composition (CEC) method was proposed for the risk analysis.
147 Based on the proposed model. The multiple risks of the WPE nexus were
148 systematically evaluated and discussed through the case study of the upper Yangtze
149 River basin.

150 **2. Study area and data material**

151 The Yangtze River, the longest river in the Asia region and the third longest river
152 in the world, has a length of 3,915 miles (6,300 kilometers). From its origin to the
153 Yichang city is usually defined as the upper reach of the Yangtze River. This upper
154 reach of the Yangtze River flows across the Plateau of Tibet and receives confluence

155 discharges from many different tributaries (large and small). The mainstream elevation
156 descends under through deep valleys in the east Plateau mountains and then appears
157 onto the Yunnan-Guizhou Plateau, where summer season is warm and winter season is
158 cold. The area of the upper Yangtze River covers about 0.85 million km². In the upper
159 Yangtze River, the water resources can reach 585.33 billion m³. The average water
160 resources per capita attains to 32,000 m³. In this study, the upper Yangtze section was
161 selected for the case study, of which the basin mainly involves the Chongqing city,
162 Tibet, Qinghai, Yunnan, Guizhou and Sichuan provinces. The water use data of these
163 provinces were collected for the analysis. For clarity, the skeleton of the research area
164 is given in Figure 1, in which the deep blue area is the upper Yangtze River Basin.



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Figure 1 Skeleton of the Yangtze River Basin.

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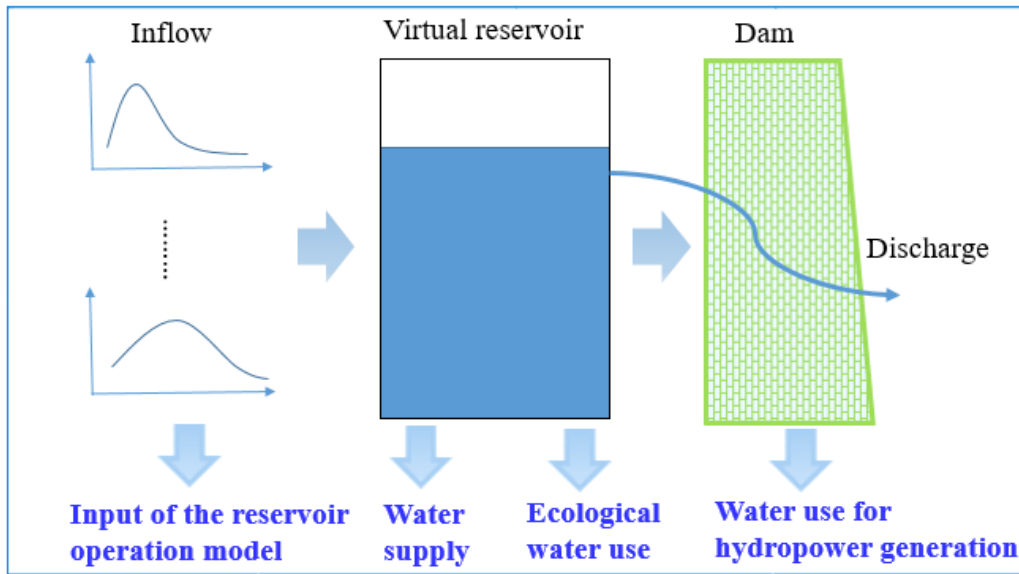
In a water resources system, water use is mainly composed of domestic water use, ecological water use, agricultural water use, and industrial water use. Since the environment and ecology has been emphasized more and more for their importance to daily practice, the ecological water use was taken in this study as a variable for

171 representing the environmental situation in the water resources system. Thus, the water
172 use is divided into two kinds. One kind is named as water supply defined as W in this
173 study, including all the water use for human beings, such as domestic, agricultural and
174 industrial water uses. The other kind is called environmental water use, including the
175 ecological water use in the basin, which was defined as E in this study. In addition to
176 these two variables, the water use for hydropower generation was also considered in
177 this study, defined as P herein, which is quantified by the hydropower generation
178 capacity in this study.

179 Taking the upper Yangtze River Basin as a virtual reservoir, the relation among
180 water supply, hydropower generation and environmental water use in the basin can be
181 described in Figure 2. The natural flow is the input of the reservoir system. The flow
182 stored in the virtual reservoir can be used for water supply, hydropower generation and
183 preserving the ecosystem. As for the water allocation strategy, the water withdrawn in
184 the upstream of the dam for water supply and/or ecological use will not flow through
185 the dam for electricity generation.

186 In this study, the water consumption data of the provinces involved in this research
187 area (Figure 1) were collected for the model development and analysis. Specifically,
188 the data of water supply and ecological water use were obtained from the China Water
189 Resources Bulletin, China Hydrological Yearbook and Yangtze & Southwest Rivers
190 Water Resources Bulletin. The duration of the data set covers from 1998 to 2015. In
191 terms of the hydropower generation, with the construction of the reservoirs and the
192 increase of hydropower generation every year, the number of the reservoirs will be

193 fixed at the same level in order to rationally analyze the nexus of the water supply,
 194 hydropower generation and environment. For the analysis, the number of the reservoirs
 195 was set to 60 at the current level. The hydropower generation data was derived based
 196 on the reservoir operation.



197

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Figure 2 The virtual reservoir of the upper Yangtze River Basin.

199 **3. Establishment of the joint distributions**

200 In order to investigate the water supply, hydropower generation and environment
 201 nexus in a water resources system, a joint distribution was established in this section.

202 Three variables were defined as follows. The first variable W represents the water use
 203 for human needs, including the domestic water demand, industrial and agricultural
 204 water demand. The second variable is related to the water used for hydropower
 205 generation. Since the amount of water used for hydropower is not easily quantified, the
 206 hydropower generation capacity is taken into account in this study, defined as variable
 207 P . In order to analyze the impact of water allocation on environment, the third variable
 208 E represents the water use for the basin environment.

209 3.1 Establishment of the marginal distributions

210 First the samples of the three variables (W, P, E) are assumed to be independent
211 and identically distributed (IID). The marginal distribution was established based on
212 the univariate hydrological frequency method. Many probability distribution models
213 were developed and applied for hydrological studies, which mainly include the
214 following two types: (a) two-parameter distributions such as Gumbel, Weibull, Gamma
215 and Lognormal distributions (Leigh and Du, 2015; Jiang et al., 2015; Villarini et al.,
216 2009); and (b) three-parameter distributions such as general extreme value (GEV)
217 distribution (Cannon, 2011; El Adlouni et al., 2007) and Pearson type III distribution
218 (Chen et al., 2011, 2015). The commonly used distributions in hydrology are selected
219 to fit variables. In this study, the L-moment analysis method was used to evaluate the
220 coefficients of these marginal distributions. The established marginal distribution is
221 given by

$$222 \quad u_W = F(W) = \int_0^w f_1(w)dw \quad (1a)$$

$$223 \quad u_P = F(P) = \int_0^p f_2(p)dp \quad (1b)$$

$$224 \quad u_E = F(E) = \int_0^e f_3(e)de \quad (1c)$$

225 where $f_1(w)$, $f_2(p)$ and $f_3(e)$ are probability density functions of water supply,
226 hydropower and environment, respectively; u_W, u_P , and u_E or $F(W), F(P)$, and
227 $F(E)$ are their corresponding cumulative distribution functions, respectively.

228 In order to evaluate the performance of the marginal distributions, the empirical
229 probability was needed. For the univariate case, the empirical probabilities were

230 estimated by the Weibull plotting position formula (Makkonen, 2008),

$$231 \quad F_{emp}(X_i) = \frac{i}{n+1}; i = 1, 2, \dots, n \quad (2)$$

232 where X_i is observed data; n is the sample size; and $F_{emp}(X_i)$ is the empirical
233 exceedance probability of the i^{th} observed data X_i .

234 **3.2 Establishment of joint distributions**

235 Bivariate and trivariate joint distributions were established to analyze the WPE
236 nexus. For this purpose, the copula functions were used to establish such joint
237 distributions (Sklar, 1959). The main advantage of copulas is attributed to its flexibility
238 in the arbitrary selection of marginal dependence structures (Nelsen, 2006). The
239 procedures for establishing the joint distribution were detailed as follows.

240 **3.2.1 Establishment of bivariate joint distributions**

241 As mentioned above, the variables W , P and E follow the selected marginal
242 distribution functions $F(W)$, $F(P)$, and $F(E)$ respectively, so that there exist bivariate
243 copulas that combine these marginal distribution functions to joint distributions.
244 Accordingly, the three bivariate joint distributions are obtained for this study as follows.

$$245 \quad F(W, P) = C(F(W), F(P)) = C(u_W, u_P) \quad (3a)$$

$$246 \quad F(W, E) = C(F(W), F(E)) = C(u_W, u_E) \quad (3b)$$

$$247 \quad F(P, E) = C(F(P), F(E)) = C(u_P, u_E) \quad (3c)$$

248 For bivariate case, Archimedes copulas have been widely used in the hydrology
249 field (Nelson, 2006). Therefore, the Gumbel, Frank, and Clayton copulas of the

250 Archimedes copulas family were considered in this study.

251 **3.2.2 Establishment of trivariate joint distribution**

252 The trivariate joint distribution $F(W, P, E)$, was established in this section. Since
253 this is for high dimensional joint distributions, the Archimedes copulas can only
254 simulate the $n-1$ dependence structure. For this purpose, the metaelliptical copula was
255 used hereafter to build the trivariate joint distribution. The metaelliptical copula can
256 model arbitrary pairwise dependencies between variables through a correlation matrix
257 (Chen et al., 2013). The expression for trivariate distribution is given by

$$258 \quad C(W, P, E) = \Phi_3(\Phi_1^{-1}(u_W), \Phi_2^{-1}(u_P), \Phi_3^{-1}(u_E); \boldsymbol{\rho}) \quad (4)$$

259 where $\Phi_3(\cdot)$ is the three-dimensional standard normal distribution; Φ_i^{-1} is the
260 inverse function of standard normal distribution; and $\boldsymbol{\rho}$ is the correlation matrix.

261 For a multivariate case, the empirical probability can be expressed by (Zhang and
262 Singh 2007a, b)

$$263 \quad C'(u_1(i), u_2(i), \dots, u_d(i)) = \frac{\sum_{j=1}^n \mathbf{1}(U_1(j) \leq u_1(i), U_2(j) \leq u_2(i), \dots, U_d(j) \leq u_d(i))}{n} \quad (5)$$

264 **3.3 Model performance evaluation**

265 In order to evaluate the performance of the developed marginal and joint
266 distributions, the Root Mean Square Error (RMSE), Akaike Information Criterion
267 (AIC) and K-S test were used together in this study for a comprehensive evaluation.

268 The RMSE can be expressed by

$$269 \quad RMSE_1 = \sqrt{\frac{\sum_{i=1}^n (F(x_i) - F_{emp}(x_i))^2}{n}} \quad (6a)$$

$$270 \quad RMSE_2 = \sqrt{\frac{\sum_{i=1}^n (C(u_{1i}, u_{2i}) - C'(u_1(i), u_2(i)))^2}{n}} \quad (6b)$$

$$271 \quad RMSE_3 = \sqrt{\frac{\sum_{i=1}^n (C(u_{1i}, u_{2i}, u_{3i}) - C'(u_1(i), u_2(i), u_3(i)))^2}{n}} \quad (6c)$$

272 where n is the sample size; $RMSE_1$, $RMSE_2$ and $RMSE_3$ are the RMSE values
 273 for marginal distributions, two-dimensional and three-dimensional joint distributions,
 274 respectively; $F(x_i)$ and $C(\cdot)$ are the theoretical probabilities of the marginal and
 275 joint distributions respectively; and $F_{emp}(x_i)$ and $C'(\cdot)$ are the empirical probabilities
 276 of the marginal and joint distributions respectively.

277 **4. WPE nexus analysis**

278 The conditional distribution and conditional expectation model were proposed to
 279 analyze the nexus of water supply, hydropower and environment variables.

280 **4.1 Bivariate analysis of WPE nexus**

281 The bivariate analysis model was built for investigating the bivariate nexus of
 282 water supply, hydropower, and environment. Accordingly, the nexus of water supply-
 283 hydropower, hydropower-environment, and water supply-environment were analyzed
 284 respectively based on the model established below.

285 Based on the bivariate joint distributions in Equation (3a-c), the pairwise
 286 conditional distribution function was constructed to analyze the risk or probability of

287 variable $X_1 > x_1$ given $X_2 = x_2$. The variables X_1 and X_2 can be any two of water supply,
 288 hydropower, and environment. Two-dimensional conditional probability model can be
 289 expressed by

$$\begin{aligned}
 C(X_1 | X_2) &= P(X_1 \geq x_1 | X_2 = x_2) \\
 &= \int_{x_1}^{+\infty} \frac{f(x_1, x_2)}{f(x_2)} dx_1 \\
 &= \int_{x_1}^{+\infty} \frac{c(u_1, u_2) f(x_1) f(x_2)}{f(x_2)} dx_1 \\
 &= \int_{u_1}^1 c(u_1, u_2) du_1
 \end{aligned} \tag{7}$$

291 where $f(x_1, x_2)$ is the joint probability density function (PDF) of variables x_1 and x_2 ;
 292 $f(x_1)$ and $f(x_2)$ are the PDFs of variables x_1 and x_2 respectively; u_1 and u_2 are the
 293 cumulative distribution functions (CDFs) of variables x_1 and x_2 respectively; and
 294 $c(u_1, u_2)$ is the density function of copula function.

295 The conditional distribution model can be used to evaluate the risk or probability
 296 of WPE nexus in the water resources system. However, in order to assess the
 297 expectation values of variable x_1 under the conditional of $X_2 = x_2$, the two-dimensional
 298 conditional expectation model was established as follows:

$$\begin{aligned}
 \bar{E}(x_1 | x_2) &= \int_0^{+\infty} x_1 \cdot f(x_1 | x_2) dx_1 \\
 &= \int_0^{+\infty} x_1 \cdot f(x_1) \cdot c(u_1, u_2) dx_1
 \end{aligned} \tag{8}$$

300 This model can be used to evaluate the average value of variable X_1 under the
 301 condition of $X_2 = x_2$. Taking the water supply W and hydropower generation P for an

302 example, the expected value of water supply W given $P_2 = p_2$ can be calculated by the
 303 established two-dimensional conditional distribution. This value indicates the average
 304 water supply value given $P_2 = p_2$.

305 **4.2 Trivariate analysis of WPE nexus**

306 In this section, the trivariate model was established to analyze the nexus of water
 307 supply, hydropower, and environment in the water resources system. The three-
 308 dimensional conditional probability model and conditional expectation model were
 309 proposed here to evaluate the probability and expected value of variable X_1 given
 310 variables $X_2 = x_2$ and $X_3 = x_3$. The three-dimensional conditional probability model and
 311 conditional expectation model are expressed in Equations (9) and (10) respectively as
 312 below.

$$C(X_1 | X_2, X_3) = P(X_1 \geq x_1 | X_2 = x_2, X_3 = x_3)$$

$$= \int_{x_1}^{+\infty} \frac{c(u_1, u_2, u_3) f(x_1) f(x_2) f(x_3)}{c(u_2, u_3) f(x_2) f(x_3)} dx_1 \quad (9)$$

$$= \int_{u_1}^1 \frac{c(u_1, u_2, u_3)}{c(u_1, u_2)} du_1$$

$$\bar{E}(x_1 | x_2, x_3) = \int_0^{+\infty} x_1 \cdot f(x_1 | x_2, x_3) dx_1$$

$$= \int_0^{+\infty} x_1 \cdot f(x_1) \cdot \frac{c(u_1, u_2, u_3)}{c(u_2, u_3)} dx_1 \quad (10)$$

315 where u_1, u_2 and u_3 are the cumulative distribution functions of variables x_1, x_2 and x_3
 316 respectively; and $c(u_1, u_2, u_3)$ is the density function of three-dimensional copula.

317 The variables X_1, X_2 and X_3 represent water supply, hydropower generation and

318 environment in the water resources system. This trivariate model can be used to
319 evaluate the average value of variable X_1 under the condition of $X_2 = x_2$ and $X_3 = x_3$.
320 For example, considering the correlations among water supply W , hydropower
321 generation P and environment E , the expected value of water supply W under the
322 condition of hydropower generation $P = p$ and the environment $E = e$, can be calculated
323 by the established three-dimensional conditional distribution. This value indicates the
324 average water supply value given $P = p$ and $E = e$.

325 These expected values from the trivariate model analysis can provide a reference
326 for rational and efficient water resources allocation, so as to improve the water
327 resources utilization and reduce the potential risks of the water resources system
328 development.

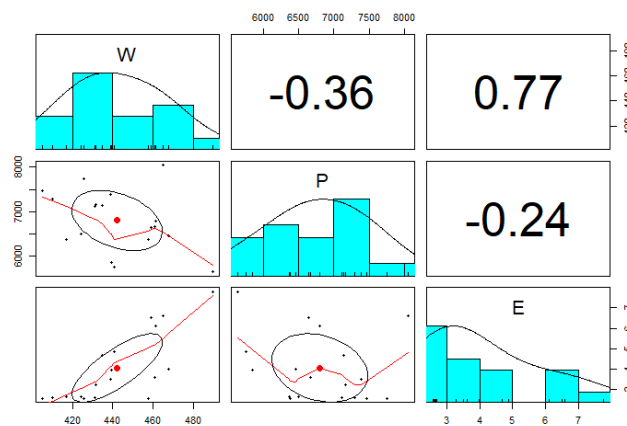
329 **5. Results analysis**

330 The proposed model was applied to the case study. First, the correlations among
331 water supply, power generation and environment were analyzed. Then, the marginal
332 distribution and joint distribution were established. Third, the conditional probability
333 and expectation models were built to analyze the multiple risks in WPE nexus.

334 **5.1 Correlation analysis of WPE nexus**

335 The correlations between water supply and hydropower, water supply and
336 environment, and hydropower generation and environment were calculated based on
337 the Pearson linear correlation coefficient, as shown in Figure 3. On one hand, the
338 results reveal that negative correlations exist between water supply and hydropower

339 generation and between hydropower generation and environment. That is, when the
 340 hydropower generation capacity increases, the water uses for human beings (water
 341 supply) and environment in the basin with decrease accordingly. On the other hand,
 342 there exists a positive correlation between water supply and environment. This is
 343 reasonable, since for dry years more water would be withdrawn for human beings and
 344 environment in the basin, and vice versa. Thus, the water supply and environment
 345 present positive correlation to each other.



346

347 **Figure 3** Correlation analysis of WPE nexus in the water resources system.

348 **5.2 Results of joint distributions**

349 For the case study, the marginal distributions of water supply, hydropower
 350 generation and environment were first obtained, followed by their joint distributions
 351 by different copula functions.

352 **5.2.1 Marginal distributions**

353 The commonly used marginal distributions were employed to fit the water supply,
 354 hydropower generation and environment series, respectively. The RMSE and K-S test
 355 indicators were used to evaluate the performance of the marginal distributions, and the

356 goodness-of-fit results are given in Table 1. Based on these results, the GPA, GEV and
357 GPA distributions are selected as the marginal distributions of water supply,
358 hydropower generation and environment variables respectively, and the parameters of
359 these distributions are listed in Table 2. The empirical probabilities of the marginal
360 distributions were calculated by Equation (2). In order to better compare the fitting, the
361 Q-Q plot (Quantile-Quantile plot) and P-P plot (Probability-Probability plot) were used
362 for the observed and calculated data. The fitting curves of the marginal distributions
363 are plotted in Figure 4. The comparison of results from these figures confirms that the
364 marginal distributions can fit well with the empirical distributions.

365

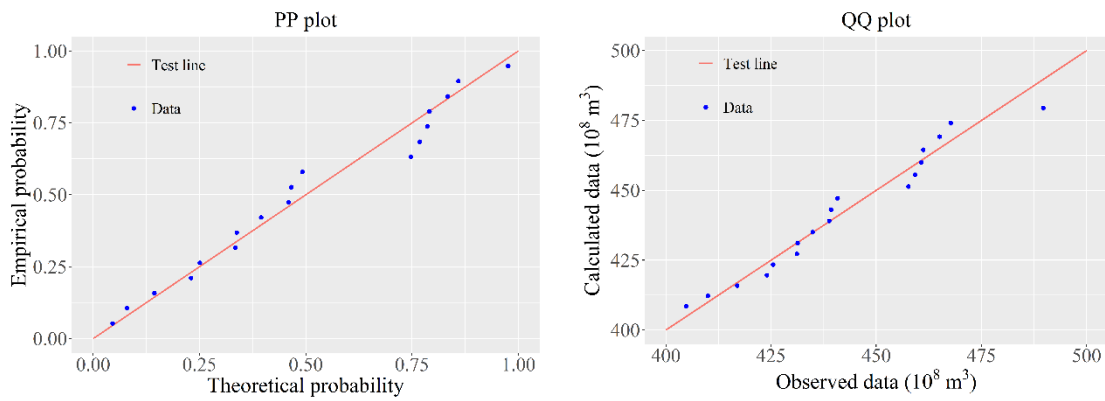
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Table 1 Goodness-of-fit results of marginal distributions.

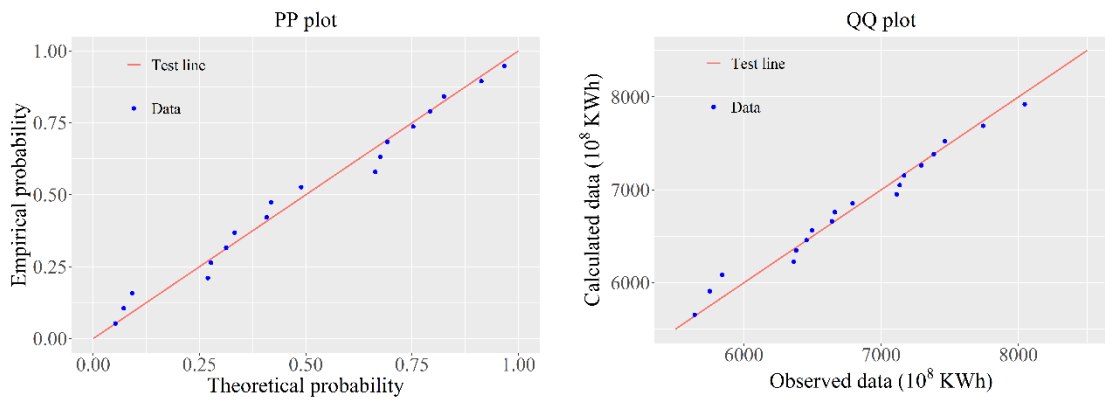
Distributions	Water supply			Hydropower			Environment		
	RMSE	AIC	K-S (P-value)	RMSE	AIC	K-S (P-value)	RMSE	AIC	K-S (P-value)
Exponential	0.0855	-33.73	0.7658	0.1033	-27.31	0.7658	0.0633	-40.25	0.9639
Gamma	0.0505	-48.80	0.9715	0.0415	-56.77	0.9999	0.0765	-33.72	0.7658
Normal	0.0518	-47.96	0.9715	0.0393	-58.51	0.9999	0.0971	-26.67	0.7658
Gumbel	0.0548	-48.60	0.9715	0.0645	-43.50	0.9715	0.0744	-34.89	0.7658
Weibull	0.0471	-50.73	0.9715	0.0375	-59.40	0.9999	0.0629	-40.31	0.9639
GEV	0.0476	-50.66	0.9715	0.0374	-59.48	0.9999	0.0746	-36.34	0.7658
GLO	0.0572	-45.71	0.9715	0.0453	-55.40	0.9715	0.0784	-35.16	0.7658
GPA	0.0468	-50.31	0.9999	0.0454	-51.42	0.9999	0.0625	-40.47	0.9639
GNO	0.0493	-49.67	0.9715	0.0388	-58.90	0.9999	0.0705	-37.61	0.7658
P-III	0.0492	-49.72	0.9715	0.0388	-58.90	0.9999	0.0631	-40.31	0.9639

Table 2 Estimated parameters for the marginal distributions.

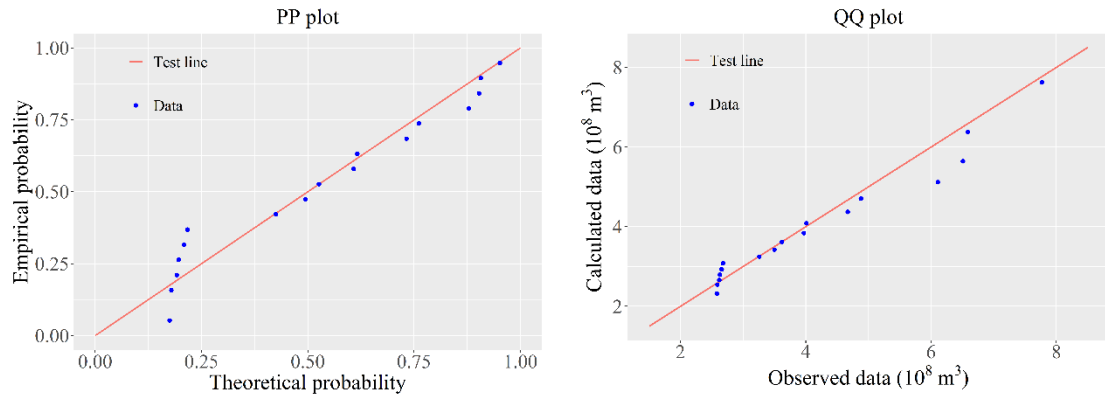
Indicators	Distributions	Estimated parameters		
		k	σ	μ
Water supply	GPA	-0.85015	69.051	404.84
Hydropower	GEV	-0.30922	707.21	6,561.2
Environment	GPA	-0.01966	1.8897	2.2157



(a) Water supply



(b) Hydropower



(c) Environment

372 **Figure 4** P-P and Q-Q plots for the variables of water supply, hydropower and environment.

373 **5.2.2 Multivariate Joint distributions**

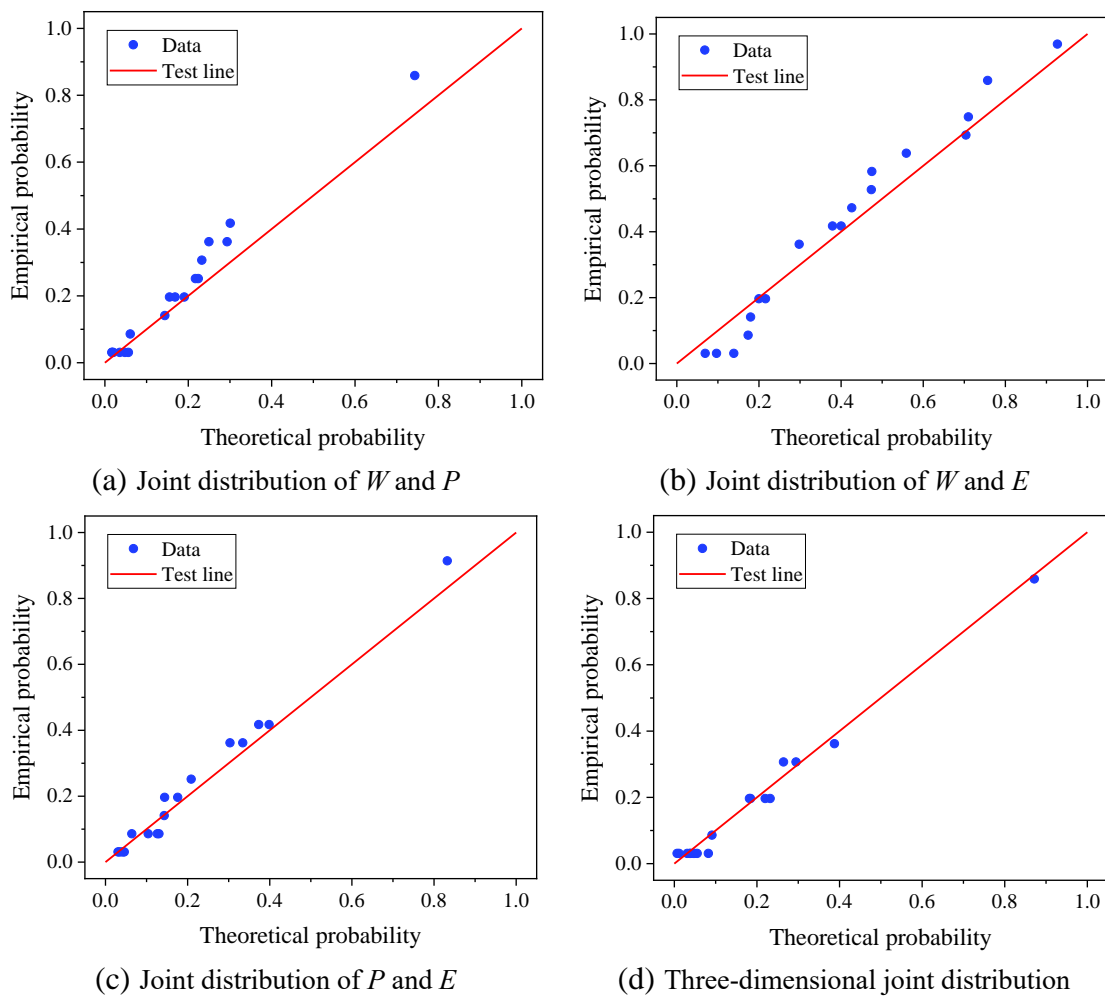
374 In this study, the Gumbel, Frank, and Clayton copulas were used to construct the
 375 two-dimensional joint distributions in the water resources system. Similarly, the
 376 performance and capability of the two-dimensional joint distributions were assessed
 377 through the analysis results of RMSE index and K-S test. The results are obtained and
 378 shown in Table 3, indicating that it is preferable to select the Frank copula to build the
 379 two-dimensional joint distributions in the water resources system. While for three-
 380 dimensional case, Gaussian copula was more suitable to construct the three-
 381 dimensional joint distribution. The parameters and fitting curves of these joint
 382 distributions are shown in Table 3 and Figure 5, respectively. It can be found from
 383 Figure 5 that the selected copula function fits very well with the empirical frequencies.
 384 The RMSE values and K-S test results in in Table 3 can testify again the suitability and
 385 validity of the used copula functions for this case study. Specifically, the RMSE values
 386 are relatively small for all the four joint distribution and the results of the K-S test (P-
 387 value) also demonstrate that the selection of the copula functions is acceptable to

388 construct the joint distributions.

389 **Table 3** Estimated parameters, RMSE and P-value of the K-S test for the joint distributions.

Indicators	(W, P)	(W, E)	(P, E)	(W, P, E)
Selected	Frank	Frank	Frank	Gaussian
Parameters	-3.1491	8.3879	-2.2240	Figure 3
RMSE	0.056	0.062	0.0357	0.0234
K-S (P-value)	0.7088	0.9448	0.7088	0.982

390



391

Figure 5 Fitting curves of joint distributions.

392 **5.3 Multiple-risk analysis of WPE nexus**

393 Based on the established conditional probability and expectation models, the

394 potential risks in the water resources system under different threshold conditions were

395 evaluated in this section.

396 **5.3.1 Results of bivariate risk analysis**

397 The conditional distributions and conditional expectation models were used to
 398 assess the potential risks related to the water supply, hydropower and environment in
 399 the water resources system.

400 First, according to Equation (7), the two-dimensional conditional distribution
 401 model was established to calculate the probabilities of $X_1 > x_1$ given $X_2 = x_2$, and the
 402 results of water supply and hydropower, water supply and environment, and
 403 hydropower and environment are given in Tables 4, 5 and 6, respectively.

404 **Table 4** Results of conditional probability analysis for water supply and hydropower nexus

$C(W P)$			$C(P W)$		
$P (10^8 \text{ kW}\cdot\text{h})$ $F(P)$	$W (10^8 \text{ m}^3)$ $F(W)$	$C (W \geq w$ $ P=p)$	$W (10^8 \text{ m}^3)$ $F(W)$	$P (10^8 \text{ kW}\cdot\text{h})$ $F(P)$	$C (P \geq p$ $ W=w)$
7,185 (70 %)	456.88 (70 %)	0.1631	456.88 (70 %)	7,185 (70 %)	0.1631
	465.39 (80 %)	0.0952		7,410 (80 %)	0.0952
	474.59 (90 %)	0.0416		7,708 (90 %)	0.0416
7,410 (80 %)	456.88 (70 %)	0.1246	465.39 (80 %)	7,185 (70 %)	0.1246
	465.39 (80 %)	0.0713		7,410 (80 %)	0.0713
	474.59 (90 %)	0.0307		7,708 (90 %)	0.0307
7,708 (90 %)	456.88 (70 %)	0.0941	474.59 (90 %)	7,185 (70 %)	0.0941
	465.39 (80 %)	0.0531		7,410 (80 %)	0.0531
	474.59 (90 %)	0.0226		7,708 (90 %)	0.0226

405 The two-dimensional conditional distribution was used to calculate the probability
 406 of water supply exceeding a threshold value ($W > w$) given hydropower generation $P=p$,

407 or the probability of hydropower generation exceeding a threshold value ($P > p$) given
408 water supply $W=w$. The results in Table 4 show that, under the condition of hydropower
409 generation being $7,185 \times 10^8$ kW·h with an occurrence frequency of 70 %, the
410 probability of water supply exceeding 456.88×10^8 m³ (with frequency of 70 %) is
411 16.31 %, and that of water supply exceeding 465.39×10^8 m³ (with frequency of 80 %) or
412 474.59×10^8 m³ (with frequency of 90 %) reduces to only 9.52 % or 4.48 %, respectively.
413 Moreover, the results also indicate that the probability of water supply
414 exceeding a threshold value, for example 456.88×10^8 m³, decreases gradually with an
415 increase of hydropower generation capacity. Therefore, in order to improve the water
416 use efficiency, it is expected to achieve a balance of the water resources allocation
417 between water supply and hydropower generation.

418 **Table 5** Results of conditional probability analysis for water supply and environment nexus.

$C(W E)$			$C(E W)$		
E (10^8 m ³) $F(E)$	W (10^8 m ³) $F(W)$	$F(W \geq w$ $ E=e)$	W (10^8 m ³) $F(W)$	E (10^8 m ³) $F(E)$	$F(E \geq e$ $ W=w)$
4.4641 (70 %)	456.88 (70 %)	0.4797	456.88 (70 %)	4.4641 (70 %)	0.4797
	465.39 (80 %)	0.2603		5.2094 (80 %)	0.2603
	474.59 (90 %)	0.0959		6.4699 (90 %)	0.0959
5.2094 (80 %)	456.88 (70 %)	0.6808	465.39 (80 %)	4.4641 (70 %)	0.6808
	465.39 (80 %)	0.4488		5.2094 (80 %)	0.4488
	474.59 (90 %)	0.1971		6.4699 (90 %)	0.1971
6.4699 (90 %)	456.88 (70 %)	0.8315	474.59 (90 %)	4.4641 (70 %)	0.8315
	465.39 (80 %)	0.6532		5.2094 (80 %)	0.6532
	474.59 (90 %)	0.3623		6.4699 (90 %)	0.3623

419 According to the former correlation analysis, there is a positive correlation

420 between water supply and environmental water use. When the water supply increases,
 421 the ecological water use will inevitably increase, as shown in Table 5. It is also found
 422 from Table 5 that under the condition of ecological water use being $5.0294 \times 10^8 \text{ m}^3$
 423 (with frequency of 80 %), the probability of water supply exceeding $465.39 \times 10^8 \text{ m}^3$
 424 (with frequency of 80 %) is 44.88 %. With the increase of ecological water use to
 425 $6.4699 \times 10^8 \text{ m}^3$ (with frequency of 90 %), the probability of water supply exceeding
 426 $465.39 \times 10^8 \text{ m}^3$ increases to 65.32 %.

427 **Table 6** Results of conditional probability analysis for hydropower and environment nexus.

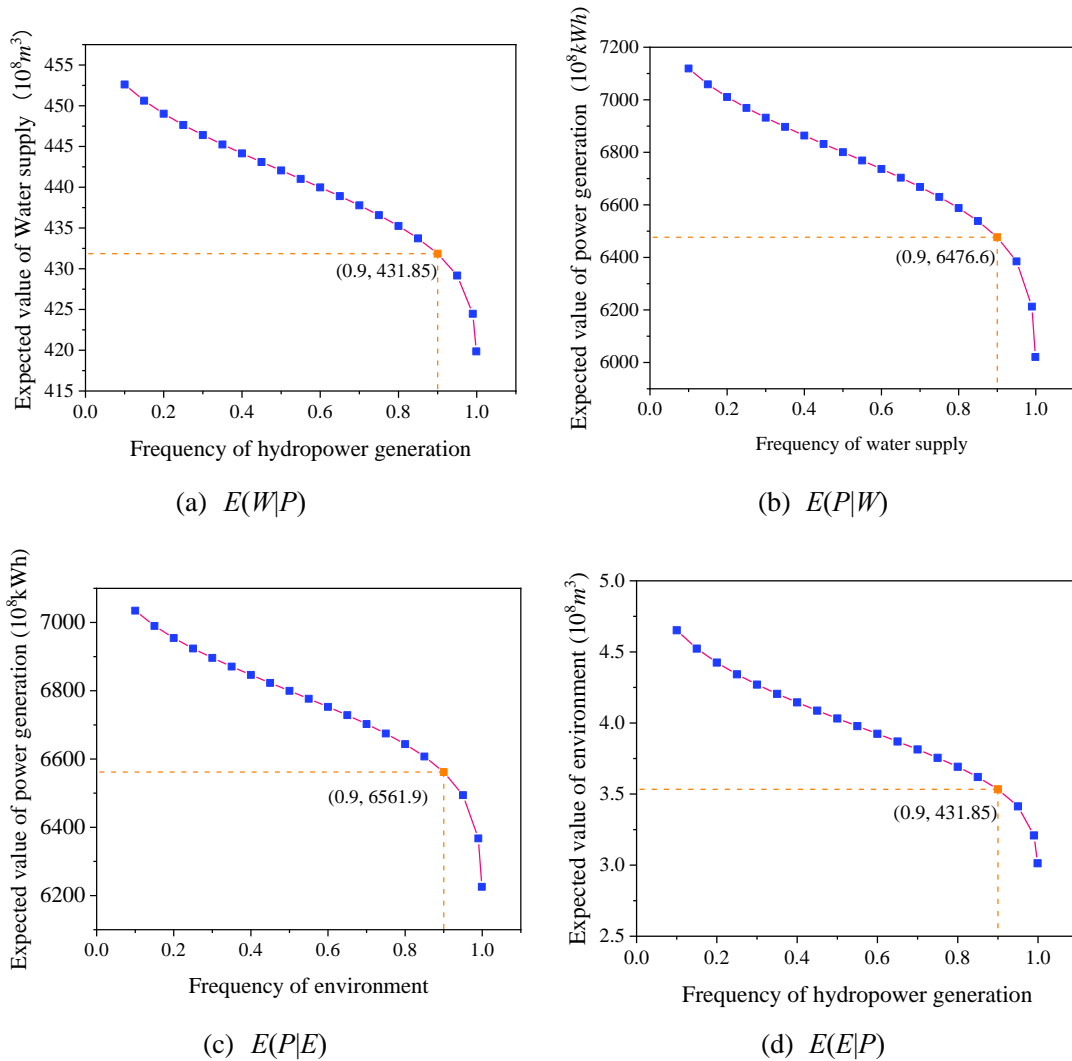
$C(P E)$			$C(E P)$		
$E (10^8 \text{ m}^3)$ $F(E)$	$P(10^8 \text{ kW}\cdot\text{h})$ $F(P)$	$F(P \geq p$ $ E=e)$	$P (10^8 \text{ kW}\cdot\text{h})$ $F(P)$	$E (10^8 \text{ m}^3)$ $F(E)$	$F(E \geq e$ $ P=p)$
4.4641 (70 %)	7,185 (70 %)	0.2022	7,185 (70 %)	4.4641 (70 %)	0.2022
	7,410 (80 %)	0.1244		5.2094 (80 %)	0.1244
	7,708 (90 %)	0.0572		6.4699 (90 %)	0.0572
5.2094 (80 %)	7,185 (70 %)	0.1687	7,410 (80 %)	4.4641 (70 %)	0.1687
	7,410 (80 %)	0.1021		5.2094 (80 %)	0.1021
	7,708 (90 %)	0.0464		6.4699 (90 %)	0.0464
6.4699 (90 %)	7,185 (70 %)	0.1397	7,708 (90 %)	4.4641 (70 %)	0.1397
	7,410 (80 %)	0.0835		5.2094 (80 %)	0.0835
	7,708 (90 %)	0.0375		6.4699 (90 %)	0.0375

428 For the hydropower and environmental water consumption subsystem, since there
 429 is a competition relationship between them (i.e., negative correlation in Figure 3), the
 430 ecological water consumption decreases with the increase of hydropower generation
 431 capacity in the basin, with results shown in Table 6. The probability of ecological water
 432 consumption exceeding $4.4641 \times 10^8 \text{ m}^3$ (corresponding to a frequency of 70 %) is 20.22 %

433 under the condition of hydropower generation being $7,185 \times 10^8$ kW·h (corresponding
434 to a frequency of 70 %). However, under the condition of hydropower generation being
435 $7,708 \times 10^8$ kW·h (with corresponding frequency of 90 %), the probability of ecological
436 water consumption exceeding 6.4699×10^8 m³ (with same frequency of 90 %) reduces
437 to 3.75 % only. Therefore, in order to reduce the risks of water supply insufficiency, the
438 allocation of water resources for hydropower and ecological water consumption in the
439 basin should not be too high.

440 In order to further analyze the expected level of each variable under different
441 conditions, the two-dimensional conditional expectation model was used to calculate
442 these expected levels. The results are obtained and plotted in Figure 6. It is indicated
443 from Figure 6(a) that the expected value of water supply decreases with the increase of
444 hydropower generation. Particularly, when the frequency of hydropower generation
445 exceeds 90 %, the expected value of water supply decreases sharply. Thus, the
446 frequency of hydropower generation exceeding this point may lead to an obvious
447 reduction of water resources utilization efficiency in the water resources system, which
448 means that the water supply in the basin will be seriously insufficient. Furthermore,
449 Figure 6(b) shows that the expected value of hydropower generation will decrease
450 sharply when the frequency of water supply exceeds 90 %, indicating the water supply
451 in the basin should not exceed this threshold value so as to maintain the overall
452 sustainability and efficiency of the water resources system. Similarly, results in Figures
453 6(c) and (d) demonstrate that a threshold value is also existent between the
454 environmental water consumption and hydropower generation. When the

455 environmental water consumption and hydropower generation exceeds this threshold
 456 value, the utilization efficiency of water resources in the subsystems will decrease, and
 457 thereby the hydropower generation or ecological water consumption in the basin will
 458 be seriously insufficient.



459 **Figure 6** Expected level for two-dimensional water resources system.

460 A synergistic relationship is expected for the water supply and environmental
 461 water consumption subsystems. However, when the water supply and environmental
 462 consumption increase, the expected value of hydropower generation will decrease
 463 accordingly. Therefore, it is necessary to perform a more comprehensive analysis the

464 water resources system by simultaneously considering the water supply, hydropower
 465 generation and environmental water variables, which is elaborated in the following
 466 study.

467 **5.3.2 Results of trivariate risk analysis**

468 For the studied case in Figure 1, concerning the multiple uses of water supply,
 469 hydropower generation and environmental water, the results of three-dimensional
 470 conditional probability model are obtained and shown in Table 7.

471 Table 7 Results of the three-dimensional conditional probabilities

H	$F(H)$	E	$F(E)$	W	$F(W)$	$C(W P, E)$
7,410	80 %	5.2094	80 %	465.39	80 %	27.61 %
7,410	80 %	5.2094	80 %	474.59	90 %	9.31 %
W	$F(W)$	E	$F(E)$	H	$F(H)$	$C(H W, E)$
465.39	80 %	5.2094	80 %	7,410	80 %	11.15 %
465.39	80 %	5.2094	80 %	7,708	90 %	4.55 %
W	$F(W)$	H	$F(H)$	E	$F(E)$	$C(E W, H)$
465.39	80 %	7,410	80 %	5.2094	80 %	39.64 %
465.39	80 %	7,410	80 %	6.4699	90 %	16.69 %

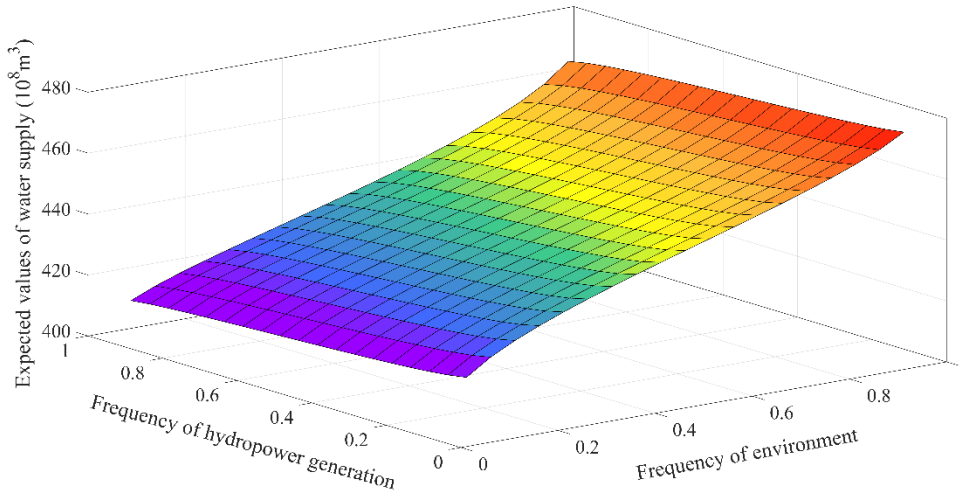
472 Given the hydropower generation of $7,410 \times 10^8 \text{ kW} \cdot \text{h}$ and the ecological water use
 473 of $5.2094 \times 10^8 \text{ m}^3$, the probabilities of the water supply exceeding $465.39 \times 10^8 \text{ m}^3$ and
 474 $474.59 \times 10^8 \text{ m}^3$ are 27.61 % and 9.31 % respectively. Clearly, the probability of water
 475 supply exceeding $465.39 \times 10^8 \text{ m}^3$ calculated by the three-dimensional model is greater
 476 than that calculated by the two-dimensional model, namely

477
$$C(W \geq 465.39 | H = 7,410, E = 5.2094) = 27.61 \%$$

$$> C(W \geq 465.39 | H = 7,410) = 11.01 \% \tag{10}$$

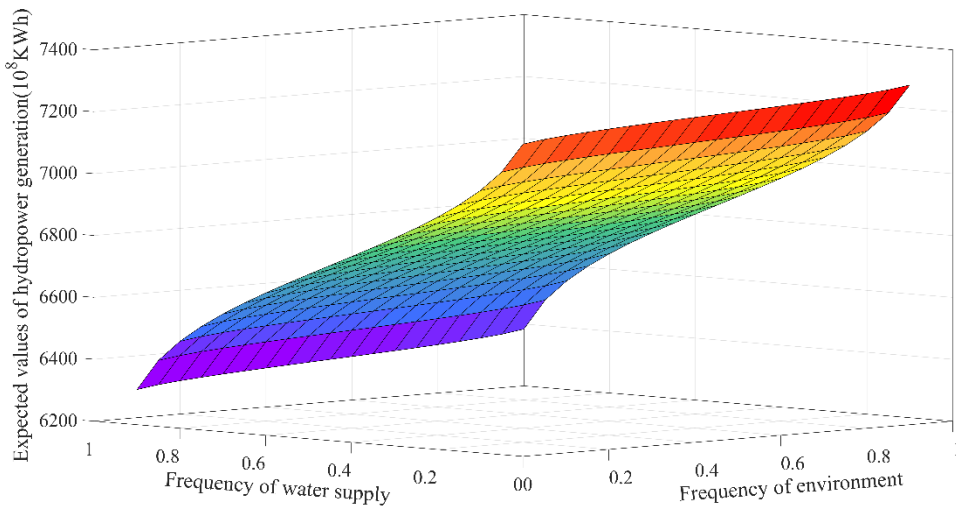
478 This difference may be explained as follows. For two-dimensional model, the
479 competitive relation exists in the water supply and hydropower generation sub-systems.
480 While for the three-dimensional model, in addition to the competitive relation between
481 the water supply and hydropower generation, the positive relationship between
482 upstream ecological water consumption and water supply is also considered in the
483 analysis. In other words, the increase of ecological water consumption indicates
484 abundant precipitation and water resources in that year, and therefore the probability of
485 water supply exceeding a certain threshold also becomes relatively high in the water
486 resources system.

487 For clarity, the variation of the expected level of a specific variable with the
488 frequencies of the other two variables is calculated by the three-dimensional conditional
489 expectation model, and the results are plotted in Figure 7. It is shown from Figure 7(a)
490 that the expected values of water supply decreases with the increase of both the
491 hydropower generation capacity and the ecological water consumption. For the
492 expected value of water supply being $465.39 \times 10^8 \text{ m}^3$ (with corresponding frequency of
493 80 %), many different combinations of hydropower generation and ecological water
494 consumption could be retrieved, with some of which shown in Table 8. For example,
495 when the ecological water consumption is $5.64 \times 10^8 \text{ m}^3$ (i.e., $F(E)=84.2 \%$) and the
496 hydropower generation is $5,892 \times 10^8 \text{ kW}\cdot\text{h}$ (i.e., $F(P)=10.1 \%$), the expected level of
497 water supply may attain to $465.39 \times 10^8 \text{ m}^3$. However, under this situation, the potential
498 risk of low hydropower generation capacity appears in the water resource system.



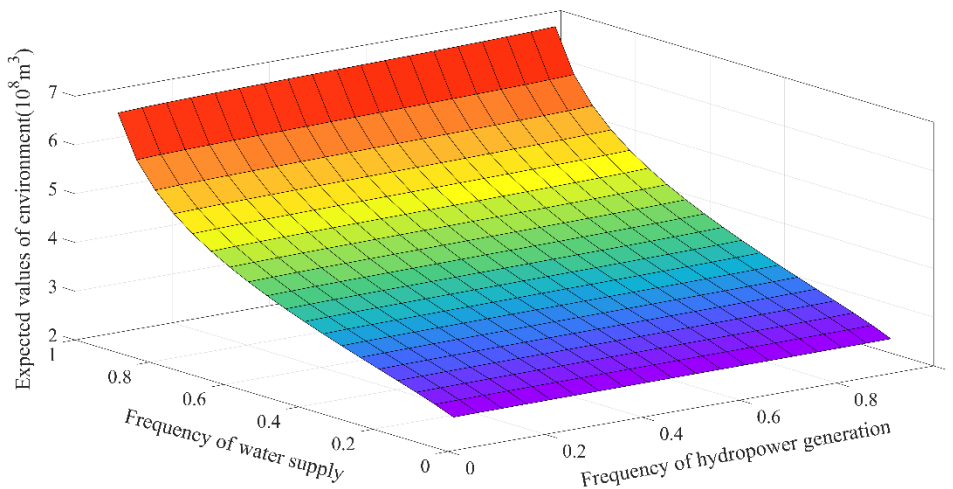
499
500

(a) Expected values of water supply



501
502

(b) Expected values of hydropower generation



503
504

(c) Expected values of environment

505

Figure 7 Expected levels for three-dimensional water resources system.

506 **Table 8** Expected water supply value for specific hydropower generation ($P=p$) and environmental
 507 water consumption ($E=e$)

Expected water supply value ($F(W)$)	$F(P)$	Hydropower generation ($\times 10^8$ kW·h)	$F(E)$	Ecological water consumption ($\times 10^8$ m ³)
	10.1 %	5,892	84.2 %	5.64
465.39 $\times 10^8$ m ³ (80 %)	20.4 %	6,209	86.5 %	5.93
	50 %	6,806	90.1 %	6.49
	70.1 %	7,188	92 %	6.87
	95 %	7,935	95.1 %	7.75

508

509 **Table 9** Expected hydropower generation for specific water supply $W=w$ and environmental water
 510 consumption $E = e$.

Expected hydropower generation value ($F(P)$)	$F(W)$	Water supply ($\times 10^8$ m ³)	$F(E)$	Ecological water consumption ($\times 10^8$ m ³)
	6 %	409	11.1 %	2.44
7,186 $\times 10^8$ kW·h (70 %)	7.4 %	409.98	43.3 %	3.28
	8 %	410.40	59.3 %	3.90
	8.3 %	410.61	66.6 %	4.27
	9.5 %	411.45	87.6 %	6.08

511 In Figure 7(b), the expected hydropower generation value decreases with the
 512 increase of water supply, while slowly increases with the ecological water consumption.

513 Similarly, the expected hydropower generation values were calculated by the proposed
 514 model, and the results are listed in Table 9. For the expected value of hydropower
 515 generation being 7,186 $\times 10^8$ kW·h, different combinations of water supply and
 516 ecological water consumption can also be retrieved, as shown in Table 9. For instance,
 517 if the ecological water consumption is 6.08 $\times 10^8$ m³ (i.e., $F(E)=87.6$ %), the water

518 supply becomes only $411.45 \times 10^8 \text{ m}^3$ and its corresponding frequency is less than 10 %,
 519 indicating the potential risk of water supply insufficiency in the water resources system.
 520 Therefore, under this condition, it is difficult to maximize the overall efficiency of water
 521 resources utilization in this system.

522 **Table 10** Expected environmental water use for specific water supply ($W=w$) and hydropower
 523 generation ($P=p$)

Expected environmental water use ($F(E)$)	$F(W)$	Water supply ($\times 10^8 \text{ m}^3$)	$F(P)$	Hydropower generation ($\times 10^8 \text{ kW}\cdot\text{h}$)
	81.5 %	466.71	97.9 %	8,153
$5.2094 \times 10^8 \text{ m}^3$	82.5 %	467.61	64.4 %	7,074
(80 %)	83.5 %	468.51	8.7 %	5,834
	84 %	468.96	1.2 %	5,226

524
 525 Figure 7(c) shows the expected environmental water use increases with the water
 526 supply, and the results are listed in Table 10. Meanwhile, the expected environmental
 527 water use slowly increases with the increase of hydropower generation capacity. In
 528 order to achieve the expected ecological water consumption of $5.2094 \times 10^8 \text{ m}^3$, with the
 529 water supply of $466.71 \times 10^8 \text{ m}^3$ (i.e., $F(w)=81.5 \%$), the frequency of hydropower
 530 generation can reach relatively high level at 97.9 %. However, the frequency of
 531 hydropower generation declines sharply with the increase of the water supply. For
 532 instance, when the frequency of water supply increases from 81.5 % to 84.0 %, the
 533 frequency of hydropower generation decreases from 97.9 % to 1.2 % only. In order
 534 words, when the frequencies of water supply and hydropower generation are 81.5 %
 535 and 97.9 % respectively, the expected ecological water consumption can attain to

536 $5.2094 \times 10^8 \text{ m}^3$. From this perspective, it is feasible to maximize the overall efficiency
 537 of water resources utilization and at the same time, to minimize the potential multiple
 538 risks in the water resources system.

539 **Table 11** Comparisons of expected values calculated by the bivariate and trivariate models (10^8 m^3)

$F(E)$	$\bar{E}(W E)$	$\bar{E}(W H, E); F(H) = 0.8$	$\bar{E}(W H, E); F(H) = 0.9$
0.1	418.93	417.39	416.27
0.2	425.57	423.30	421.86
0.3	431.20	428.37	426.74
0.4	436.45	433.16	431.39
0.5	441.59	437.92	436.05
0.6	446.81	442.84	440.92
0.7	452.36	448.17	446.25
0.8	458.58	454.30	452.43
0.9	466.32	462.22	460.54

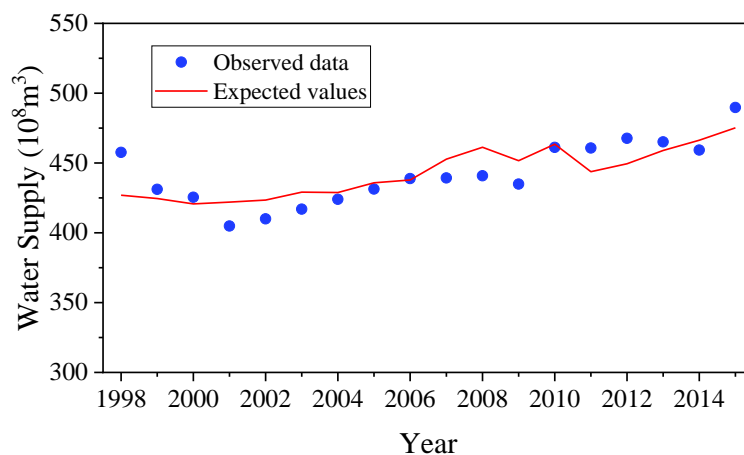
540

541 For further inspection, the results of the two-dimensional and three-dimensional
 542 conditional expectation models are compared and shown in Table 11. In the
 543 table, $\bar{E}(W|E)$ represents the expected value of water supply when the upstream
 544 ecological water use is given; and $\bar{E}(W|H, E)$ represents the expected value of water
 545 supply, when the hydropower generation and the upstream ecological water use are
 546 given. It can be seen from Table 11 that when considering the impact of hydropower
 547 generation, the expected value of water supply will decrease due to the competitive
 548 relationship between the hydropower generation and water supply, namely $\bar{E}(W|E) > \bar{E}$
 549 $(W|H, E) |_{F(H)=0.8} > \bar{E}(W|H, E) |_{F(H)=0.9}$.

550

551 **5.3.3 Comparative analysis with the observed data**

552 In order to testify the rationality of the proposed model, the observed hydropower
553 and ecological water consumption data were substituted into the model to calculate the
554 expected value of water supply with fixing hydropower generation and environmental
555 water use. First, the probabilities $F(W)$, $F(P)$ and $F(E)$ were calculated by the marginal
556 distribution based on the observed data. Then, two variables, namely the hydropower
557 generation and environmental water use were set as conditional constraints, and the
558 expected water supply values were calculated by the proposed model. Finally, the
559 calculated expected values were compared with the observed data, as shown in Figure
560 8. The overall results of Figure 8 imply that the expected water supply values from the
561 proposed model may represent the average level of the data. Specifically, the calculated
562 expected values are not far from the observed data, in which 9 years' data exceeding
563 the expected values and other 9 years' data below the expected values. Consequently,
564 the comparison of Figure 8 demonstrates the rationality and accuracy of the proposed
565 method in this study.



566

567 **Figure 8** Comparison between the observed data and expected values by the proposed model.

568 **6. Discussions**

569 Global climate change brings great challenge in hydrological predictions and
570 increases the uncertainties in water resources system management. Thus, the impacts
571 caused by climate change on the water resources system should be further studied and
572 analyzed.

573 Climate change affects the intensity and distribution of the rainfall in the basin.
574 which also influences the soil erosion. The sediment deposition from the upstream
575 catchment may lead to the gradual decrease of the effective reservoir volume, so as to
576 affect the operations and functions of the reservoir system (Chaudhry et al., 2014; Chen,
577 2018). The hydropower generation of the reservoir also reduces with the decrease of
578 the reservoir storage volume (Chen, 2018). Therefore, the change in sediment yield can
579 affect the reservoir storage volume and hydropower production.

580 In addition, the uncertainties in the runoff prediction also impose an influence on
581 the hydropower generation. Because of the uncertainties in hydrological model, there
582 are errors in runoff predictions. The predicted runoff is usually used as the inputs of the
583 reservoir operation model. When the predicted runoff in the flood season is larger, the
584 reservoir will increase the discharge for flood control. However, increasing the
585 discharge of the reservoir can affect the efficiency of hydropower generation. Therefore,
586 the uncertainty of runoff forecast leads to the uncertainty of reservoir operation process.
587 To summarize, identifying the major sources of uncertainties of the water resources
588 system and reducing it can improve the accuracy of quantitative evaluation of the water
589 resources system.

590 Finally, it is worthy of noting that there are also some limitations for using the
591 proposed models in this study for multiple-risk analysis in the water resources system.
592 First, variables in the proposed models must be relevant. Second, the proposed model
593 is not applicable when the correlation between variables is too small.

594 **7. Conclusions**

595 This paper investigated the multiple-risk assessment for the water resources
596 system under a comprehensive nexus of water supply, hydropower, and environment
597 (termed as WPE nexus in this study). A joint analysis method, namely copula method,
598 was introduced to address the dependences of the three variables (water supply,
599 hydropower and environment) in the WPE nexus. The marginal distributions of these
600 three variables were first built based on the hydrological distributions, followed by the
601 bivariate and trivariate joint distributions established using the copulas. The nexus
602 analysis of the three variables of water supply, hydropower generation and environment
603 was performed for their influences and contributions to the risk of the water resources
604 system. To this end, the conditional probabilities and the expected values were
605 calculated for the multiple-risk evaluation. For demonstration of the developed method
606 framework, the upper Yangtze River Basin was selected for the case study. Based on
607 the application results and analysis, the main findings and conclusions are summarized
608 as follows.

609 (1) Based on the correlation analysis, the results revealed the negative correlations
610 between water supply and hydropower generation as well as between the

611 hydropower generation and environmental water consumption, indicating the
612 competitive relations within these variables. Meanwhile, a positive correlation
613 was found between water supply and environment, which implies the
614 synergistic relationship between these two variables;

615 (2) Relatively small RMSE values were observed between the empirical and
616 theoretical probabilities. The results of both RMSE and P-values (for K-S test)
617 confirmed the suitability of the selection of copula functions to construct the
618 joint distributions for the studied case in this study;

619 (3) Bivariate nexus analysis demonstrated that the probability of water supply
620 exceeding a threshold value decreases gradually with the increase of
621 hydropower generation, while increases with the growing of the ecological
622 water consumption; and that of the ecological water consumption decreases
623 with the increase of hydropower generation. In particular, when the frequency
624 of hydropower generation exceeds 90 %, the expected values of both water
625 supply and environment will present sharply decreasing trends.

626 (4) Through the trivariate nexus analysis, many different combinations of
627 hydropower generation and ecological water consumption could be retrieved
628 to achieve the expected water supply values in the water resources system.
629 However, potential risks were also observed for some specific combinations
630 for practical use. Based on the trivariate nexus analysis method, an overall
631 balanced situation is expected to be achieved for the WPE nexus of the water

632 resources system.

633 The contributions and novelty of this study may include following aspects: (i) the
634 WPE nexus in the water resources system was first investigated using the bivariate and
635 trivariate distribution methods; (ii) the expectation model was proposed to analyze the
636 complex dependence relationships of WPE nexus in the water resources system; (iii)
637 the proposed models and methods were testified through the observation data from the
638 Water Resources Bulletin of China. The results and findings of this study may provide
639 useful framework and basis for the water resources system management, in the context
640 of multi-function system development for water supply and demand, hydropower and
641 environment.

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