

# Chord plastification in high strength steel circular hollow section X-joints: testing, modelling and strength predictions

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## Abstract

This paper presents experimental and numerical investigations on cold-formed high strength steel (CFHSS) circular hollow section (CHS) X-joints. The CFHSS CHS members had nominal 0.2% proof stress up to 1100 MPa. The geometric parameters of the X-joints were designed by varying the ratios of  $\beta$ ,  $2\gamma$  and  $\tau$ . Seventeen X-joint tests were conducted by applying axial compressive load through the braces without preloading in chords. Non-linear finite element model (FEM) was then developed for the CFHSS CHS X-joints. After successful validation of ultimate strengths, failure modes and load-deformation curves, parametric studies were performed by using the verified FEM. The chord plastification failure of the X-joints was mainly found in both test and numerical studies. The relationship between the joint strengths and the variation of geometric ratios were investigated. The strengths of the X-joints obtained in this study together with the test strengths collected from the literature were used to assess the strength predictions by CIDECT and EN-1993-1-8, as well as those from the literature. It was found that the current predictions generally provided unconservative predictions. A new equation that considers the effects of geometric ratios on the strengths was proposed based on both the test and numerical results. By adopting the newly proposed equation, the predictions are improved and provide the least scattered results when compared with the other predictions.

**Key words:** Cold-formed high strength steel; chord plastification; circular hollow section; experimental investigation; numerical investigation; tubular X-joints.

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## 26    **1. Introduction**

27        With the advancements in material and fabrication techniques, steel tubular members with higher  
28 strength have been produced in different section profiles. Nowadays, steel tubular members with yield  
29 strength (0.2% proof stress) over 1000 MPa are available in the market. The application of higher  
30 strength steel tubular members can reduce dimensions and numbers of members in steel structures,  
31 reducing the overall weight of the structure with the associated reductions in transportation, handling,  
32 erection time and costs of foundation [1]. These advantages are favoured by architects, engineers and  
33 developers. However, the current international steel design specifications [2-4] are applicable for  
34 structural steel with yield strength (0.2% proof stress) up to 700 MPa, for example, the European Code  
35 EN 1993-1-12 [2]. This gap in terms of steel grades between the market and design specifications has  
36 driven the investigations on high strength steel (nominal yield strength not less than 690 MPa) in material  
37 properties [5-11], beams subjected to three-point bending and/or four-point bending [12-15], columns  
38 subjected to axial compression and/or combined axial compression and bending [16-25] as well as bolted  
39 connections [26-33] and welded joints [34-42] in the last decade. Furthermore, the high strength steel  
40 tubular members were also investigated in composite structures, such as concrete-filled steel tubular  
41 columns [43-44]. Appropriate design rules have been proposed to overcome the shortage of the current  
42 steel design specifications, such as design of beams subjected to bending [13,15], columns under axial  
43 compression [18-20] as well as combined compression and bending [22], and tubular T-joints [41]. The  
44 fatigue of high strength steel is also an important issue due to the increased strength and reduced material  
45 ductility when compared with conventional strength steel.

46        Welded steel tubular joints are widely used in onshore and offshore structures. Design guides for  
47 tubular joints under different loading conditions have been developed based on extensive research  
48 projects on steel tubular structures. These research projects were mainly conducted under the direction

49 of Comité International pour le Développement et l'Etude de la Construction Tubulaire (CIDECT) and  
50 International Institute of Welding (IIW) Sub-commission XV-E [45-46]. The IIW published its first  
51 edition of design recommendations on static strength of steel tubular joints [47] in 1981, the second  
52 edition [48] in 1989 and then the third edition [49] in 2009. At the same period, the CIDECT provided  
53 its first edition of the design guides for circular hollow section (CHS) joints [50] in 1991 and rectangular  
54 hollow section (RHS) joints [51] in 1992; and the second edition for CHS joints [52] in 2008 and RHS  
55 joints [53] in 2009. These design guidelines [47-53] are applicable for steel tubular joints under  
56 predominantly static loading. The design recommendations proposed by IIW and CIDECT have been  
57 adopted by many international standards [3,4, 54-56] around the world. These designs are generally valid  
58 for both cold-formed and hot-finished steel members with nominal 0.2% proof stress (yield strength) not  
59 exceeding 460 MPa and nominal wall thickness in the range from 2.5 mm to 25.0 mm, as discussed by  
60 Tong and Zhao [46]. The emerged higher strength steel tubular members are not covered by these design  
61 guidelines. Hence, these design guidelines may not cater for the needs in the safe and reliable design of  
62 tubular joints in steel structures.

63 In terms of the effects on strength of welded steel tubular joints due to the higher steel grades utilised,  
64 the current version (2<sup>nd</sup> Version) of CIDECT [52,53], as compared to its first edition [50,51] for steel  
65 grade up to S355 (having nominal yield strength of 355 MPa), extended the steel grade up to S460  
66 (having nominal yield strength of 460 MPa) by limiting the design yield strength (0.2% proof stress,  $f_{0.2}$ )  
67 not higher than 0.8 times the ultimate strength ( $0.8f_u$ ), and imposing a further reduction factor of 0.9 in  
68 the design. Likewise, a reduction factor of 0.9 is specified in EN 1993-1-8 [55] to enable the design  
69 equation applicable to steel grades exceeding S355 but limited to S460. The EN 1993-1-12 [2] further  
70 extended the design to steel grade up to S700 by multiplying another reduction of 0.8. These reduction  
71 factors are imposed mainly for the consideration of possibly lower rotation and deformation capacity as

well as for the required sufficient ductility [52,53]. The suitability of these design rules with reduction factors for high strength steel tubular joints are controversial [41], for example, the recent numerical investigations on high strength steel (nominal yield strength up to 1100 MPa) CHS X-joints by Lan *et al.* [38] showed that the strength predictions by CIDECT [52] and EN-1993-1-8 [55] became increasingly unconservative as steel yield strength increased.

Design rules for welded CHS X-joints (both brace and chord members) were developed mainly based on the analytical model firstly proposed by Togo [57]. The proposed model indicates that the chord plastification strength of the joints subjected to axial loading in braces is the function of the yield strength together with the square of chord wall thickness ( $t_0$ ). Based on this principle, design equations for CHS X-joints were developed by carrying out extensive experimental and numerical investigations, where the key geometric parameters were considered in the equations including the ratios of brace outer diameter ( $d_1$ ) to chord outer diameter ( $d_0$ ) in  $\beta = d_1/d_0$ , the  $d_0$  to chord wall thickness ( $t_0$ ) ratio in  $2\gamma = d_0/t_0$  as well as brace wall thickness ( $t_1$ ) to the  $t_0$  in  $\tau = t_1/t_0$ . With the shortcomings of the current design guidelines along with the rapid development in high strength steel tubular members as discussed earlier, the purposes of this study are to investigate the effects of the key geometric parameters on the chord plastification strengths of cold-formed high strength steel (CFHSS) CHS X-joints by experimental testing and numerical modelling; and to assess the applicability of the existing design guidelines for the CFHSS CHS X-joints with nominal 0.2% proof stress up to 1100 MPa. The CFHSS X-joints were loaded by axial compressive force in braces without chord preloading. Finally, a new design equation is derived for the strength prediction of CFHSS CHS X-joints failed by chord plastification (chord face failure), based on the test and numerical results obtained in this study and the test results in literature.

## 2. Experimental investigation

### 2.1 Design of test specimens

A series of CFHSS CHS X-joint (see Figure 1) tests was conducted in this study. The CFHSS members had the nominal 0.2% proof stress ( $f_{0.2,n}$ ) up to 1100 MPa, and five different sections ( $D \times t$  in millimetre) with the nominal outer diameter ( $D$ ) and thickness ( $t$ ) of 22×4, 55×11, 89×4, 108×4 and 133×4. The sections of 89×4, 108×4 and 133×4 were used as the chord members of the X-joints. The nominal section size that had outer diameter smaller than or equal to that of the chord member was paired as the brace member. In the design of test specimens, the geometric parameters that are related to the resistance of CHS X-joints were considered, namely, the ratios of  $\beta$  ( $\beta = d_1/d_0$ ),  $2\gamma$  ( $2\gamma = d_0/t_0$ ) and  $\tau$  ( $\tau = t_1/t_0$ ). The  $t_1$  is the brace wall thickness. It should be noted that the section of 89×4 had the  $f_{0.2,n}$  of 900 MPa and 1100 MPa, as distinguished by 89×4<sup>^</sup> and 89×4<sup>\*</sup>, respectively, in the content of this paper. Hence, four series of X-joints were designed based on the selection of chord members (i.e., the 89×4<sup>^</sup>, 89×4<sup>\*</sup>, 108×4 and 133×4), as shown in Table 1. The specimens were generally identified by two segments, namely, segment of the brace section followed by that of the chord section (brace - chord). If it was a repeated test specimen, it was indicated by -r in the labelling.

The nominal chord length ( $l_0$ ) was taken as the sum of the brace outer diameter ( $d_1$ ) and 4.0~5.0 times chord outer diameter ( $d_0$ ). The value of  $l_0 = 6d_0$  was adopted by Lan *et al.* [58] for high strength steel CHS X-joints, while  $l_0 = d_1 + 4d_0$  was adopted by Pandey and Young [42] for high strength steel tubular X-joints. In this investigation, the design principle of  $l_0$  was considered that the adequate load distribution in the chord member was achieved and the stresses at the brace and chord intersection were not affected by the chord ends, as illustrated in the numerical analysis in this study. The chord length of the X-joint specimens in this study satisfied the minimum member length ( $d_1 + 3d_0$ ) for the Interior-One-Flange (IOF) loading case of web crippling tests specified in NAS [59]. The nominal brace length ( $l_1$ )

118 was designed as  $2d_l$  that measured from the crown of the chord to the brace end [42,58]. It should be  
119 noted that the chord and brace tubes were fabricated by press-braked and cold-rolled, respectively, for  
120 the high strength steel CHS X-joints tested by Lan *et al.* [58]. The tubes were fabricated from one  
121 Chinese Q960 steel plate with a nominal yield stress of 960 MPa [58]. In the present study, the tubes of  
122 22×4 and 55×11 were hot-rolled seamless sections, while the tubes of 89×4, 108×4 and 133×4 were  
123 cold-formed circular hollow sections.

124 In all the CFHSS CHS X-joint specimens, the chord member was oriented such the weld seam of the  
125 section was at 90 degree away from the top of the chord (see Figure 1). The weld seam of the brace  
126 member was oriented at 90 degree from the longitudinal direction of the chord member. The brace  
127 member was wire-cut at both ends with one end flat and another end fitting the profile of the paired  
128 chord [60]. The dimensions of each CFHSS CHS X-joint specimen were measured and the average  
129 values for each dimension are tabulated in Table 1. The geometric ratios of  $\beta$ ,  $\tau$  and  $2\gamma$  were calculated  
130 from the measurements. The smaller measured values of the upper and lower braces were used in the  
131 determination of  $\beta$  and  $\tau$  ratios. In summary, the  $\beta$ ,  $\tau$  and  $2\gamma$  of the test specimens varied from 0.17 to  
132 1.00, from 0.96 to 2.77 and from 22.50 to 34.22, respectively.

## 133 2.2 Welding and material properties

134 A robotic gas metal arc welding (GMAW) was employed in the welding between brace and chord of  
135 the CFHSS CHS X-joints, which is the same as those used for CFHSS tubular joins in [40,42]. The AWS  
136 D1.1M Specification [61] was followed in the fabrication of the X-joints. A low alloy carbon steel wire  
137 with a diameter of 1.2 mm was used as a filler material. It conformed to Class ER120S-G of the AWS  
138 A5.28M Specification [62]. The  $f_{0.2,n}$ , nominal tensile strength ( $f_{u,n}$ ) and elongation of the steel wire were  
139 930 MPa, 980 MPa and 19%, respectively [40,42]. The sizes of weld legs (see  $\Delta_1$  and  $\Delta_2$  in Figure 2(a))  
140 in the X-joint specimens were greater than the minimum value specified in the AWS D1.1M

141 Specification [61]. This minimum value is set as the maximum of  $1.5t_{min}$  or 3 mm, where  $t_{min}$  is the  
142 thickness of the thinner tube. The welding throat thickness ( $\Delta_3$ ) of the specimens was also measured, as  
143 illustrated in Figure 3. The welding details at the joint saddle for those specimens with  $\beta = 1.0$  were  
144 illustrated in Figure 2(b). The average measured values of the CHS X-joint specimens are also tabulated  
145 in Table 2.

146 Tensile coupon tests were conducted to obtain the material properties of the CHS. The coupons were  
147 machined from the centre of the face at  $90^\circ$  from the seam weld in the CFHSS tubes, which represented  
148 the crown location at the chord of the X-joints (see Figure 1). The dimension of the coupon specimens  
149 had 4 mm width and 25 mm gauge length. The specimens were tested between two pins through specially  
150 designed grips such that tension load was applied through the centroid of the coupon [8]. Two strain  
151 gauges were used to measure the initial Young's modulus of the material, while an extensometer was  
152 used to obtain the rest of the stress-strain curve until fracture. The material properties that based on the  
153 25 mm gauge length of the coupon specimen were obtained, including the modulus of elasticity ( $E$ ), the  
154 measured static 0.01% proof stress ( $f_{0.01}$ ),  $f_{0.2}$  and tensile strength ( $f_u$ ), strain at tensile strength ( $\epsilon_u$ ) and  
155 fracture failure ( $\epsilon_f$ ), as shown in Table 3. The Ramberg-Osgood parameter ( $n$ ) was calculated according  
156 to  $n = \ln(0.2/0.01)/\ln(f_{0.2}/f_{0.01})$ .

### 157 2.3 Test rig and procedure

158 The CFHSS CHS X-joints were tested in a servo-controlled hydraulic testing machine. The photo of  
159 test setup for specimen 89×4\* - 108×4 is shown in Figure 4. The bottom end of the lower brace was  
160 placed on a hardened high strength steel bearing plate with flat surface. A special ball bearing head was  
161 used at the top of the testing machine. The ball bearing can be self-adjusted to fully contact the top end  
162 of the upper brace by applying a small loading. After concentrically positioning the X-joint with  
163 alignments checking, the actuator ram of the testing machine was slowly moved up until an axial load

164 of around 4.0 kN was applied on the specimen. The X-joint specimen was preloaded. This process  
165 enabled the free-rotated ball bearing to fully contact the upper brace end. Any gaps in the specimen and  
166 steel bearing plates were eliminated. After the preloading process, the position of the ball bearing was  
167 locked from any rotations in the rest of the test.

168 The local deformations of the CFHSS X-joint specimens were carefully measured by the calibrated  
169 linear variable displacement transducers (LVDTs), as illustrated in Figure 5. The chord face indentations  
170 of the specimen were measured at the chord crown on each side of the brace by the 4 LVDTs, namely  
171 the No.1~4 shown in Figure 5(a). The extension arms were attached to the tips of the respective LVDTs  
172 such that the position next to the welding closest to the adjacent brace face was measured, i.e., around  
173 6.0 mm from the adjacent brace face. (Note that the welding length of  $\Delta_1$  is around 6.0 mm as shown in  
174 Table 2). Two horizontal LVDTs (No.5 and No.6 shown in Figure 5(b)) were used to measure chord  
175 horizontal deflections at the middle of the chord. Their tips were assembled with Poly Methyl  
176 Methacrylate (PMMA) plates (see Figure 4) to ensure the chord horizontal deformations were captured  
177 during testing. Hence, the maximum chord horizontal deformations could be fully captured. In addition,  
178 two vertical LVDTs (No.7 and No.8 shown in Figure 5(a)) were used to record the overall axial  
179 displacement of the actuator ram throughout the test.

180 Displacement control mode was adopted in the tests of CFHSS CHS X-joints. A constant loading  
181 rate of 0.3 mm/min was adopted throughout the tests. The tests were generally paused for 90 s at two  
182 moments, namely near the ultimate loads and at post ultimate loads. The static drops were obtained from  
183 the pauses; hence the effects of loading rates could be isolated from the test strengths. The tests did not  
184 stop until a clear drop of loading was observed. A data acquisition system was used to record the applied  
185 load and the LVDTs readings during the tests.

## 186 2.4 Test results



187 The test results of the CFHSS CHS X-joints are summarized in Table 4. The test strengths were  
188 determined from the static load-deformation curves. The static load-deformation curves were obtained  
189 from the static drops as mentioned earlier. All the specimens experienced a clear ultimate load (peak  
190 load) in the load-deformation curves and failed by chord plastification (chord face failure). The ultimate  
191 load ( $P_u$ ) and the corresponding axial shortening ( $\mu_u$ ) at one side (half of the average readings from  
192 LVDTs Nos.7&8) were tabulated in Table 4. In addition, the load ( $P_{3\%}$ ) corresponding to the axial  
193 shortening of  $\mu_{0.03}$  ( $\mu_{0.03}=0.03d_o$ ) at one side was also obtained from the test curve and shown in Table  
194 4. However, the values of  $\mu_u$  and  $\mu_{0.03}$  were obtained based on half of the average readings of the two  
195 LVDTs (i.e., Nos.7&8). The measurements obtained from the 4 LVDTs (i.e., Nos.1~4) were not used.  
196 This is because that slight tilting of the chords (from the crown of the joint to the chord end) was observed  
197 due to the relatively large chord indentation in the tests. This affected the accurate measurements of the  
198 4 LVDTs that were positioned at the chord ends. The major axial deformation of the X-joints was due  
199 to the indentation of the chords. Figures 6(a) and 7(a) illustrate the applied load versus the chord side  
200 wall deformation curves, for specimens with chords of 133×4 and 108×4, respectively. The chord side  
201 wall deformations were obtained by the average values from LVDTs of Nos.5&6. The corresponding  
202 loads versus the measured axial shortenings (half of the average values from LVDTs of Nos.7&8) were  
203 shown in Figures 6(b) and 7(b). The chord deformation of specimen 89×4<sup>^</sup> - 108×4 during test is  
204 illustrated in Figure 8(a).

### 205 **3. Numerical investigation**

#### 206 *3.1 General*

207 The finite element model (FEM) using the ABAQUS program of version 6.20 [63] was developed  
208 to simulate the tests of axial loaded CFHSS CHS X-joint specimens. The FEM was validated by the  
209 comparisons of strengths, failure modes and load-deformation curves between the numerical results and

210 test results. After successful validation, extensive parametric studies by using the FEM were performed.

### 211 3.2 Development of FEM and validation

212 The measured specimen dimensions (see Table 1) were used in the development of X-joints in FEM.  
213 The shell element type S4R was selected to simulate the brace member and chord member of the CHS  
214 X-joints. The previous study by Lan *et al.* [37] showed that the differences of the finite element analysis  
215 (FEA) results were comparable with a maximum deviation of 5%, when comparing the results from  
216 FEM using S4R element without considering weld detail and those using solid element type C3D8R  
217 with considering weld detail in CHS X-joints. In their analysis, the specimens with the maximum chord  
218 diameter of 244.7 mm and thickness of 22.0 mm tested by Puthli *et al.* [35] were used. Hence, in this  
219 study, the weld detail of the X-joint specimens was not considered. A more recent study by Lan *et al.*  
220 [38] found that the effects of reduced material properties in heat affected zones (HAZ) on the strengths  
221 of CFHSS CHS X-joints was relatively insignificant, as the stress in the HAZ could be effectively  
222 redistributed to the adjacent areas of base metals. In addition, it was explained that the improved yield  
223 strength of steel in CHS X-joints was generally under-utilised due to the adopted indentation limit [38],  
224 which will also be illustrated in the curves of the parametric studies in this paper. The effect of steel  
225 material properties due to HAZ in the weld region was thus not modelled in the FEM. The finer mesh  
226 sizes were adopted in the weld region with a length of  $d_0$  from the centre line of the joint to the chord  
227 end or brace end (see Figure 8(b)); however, coarse elements were used for the rest parts of the X-joints  
228 [37-38].

229 The engineering stress-strain ( $\sigma$ - $\varepsilon$ ) curves obtained from the coupon tests were converted to true  
230 stress ( $\sigma_{true}$ ) and logarithmic plastic strain ( $\varepsilon_{true}^{pl}$ ) curves by following Equations (1)-(2):

$$231 \quad \sigma_{true} = \sigma (1 + \varepsilon) \quad (1)$$

$$232 \quad \varepsilon_{true}^{pl} = \ln(1 + \varepsilon) - \frac{\sigma_{true}}{E_s} \quad (2)$$

233 The converted true stress-true plastic strain curves were assigned to the corresponding braces and  
 234 chords in the FEM. The boundary conditions of the X-joints were simulated according to the conditions  
 235 in the tests. Two reference points (RP1 at the end of upper brace and RP2 at the end of lower brace) were  
 236 defined at the brace ends (see Figure 9). They were fully coupled with the respective brace end surfaces.  
 237 Hence, the RP1 and RP2 were restricted in all degrees of freedom, except for the axial displacement of  
 238 the RP1. The geometrical nonlinearity (\*NLGEOM) was activated in the FEM to consider the large  
 239 deformation of the X-joint. The reference points of RP3 and RP4 (see Figure 9) were defined in the  
 240 crowns of the chord, with 6 mm away from the outer surfaces of the upper brace and lower brace to  
 241 monitor the chord face indentation. The reference point of RP5 was defined at middle of the chord  
 242 surface to monitor the horizontal deformation of the X-joint, as shown in Figure 9. The loads were  
 243 applied by specifying axial displacements to the RP1 of the FEM, which was identical to the test  
 244 programme by displacement control test method. Static analysis method was used in performing the  
 245 FEA.

246 All the specimens from the FEA failed by chord plastification, the same failure mode as those of the  
 247 test specimens. The strengths obtained from the FEA, namely the strength ( $P_{FE-I}$ ) corresponding to the  
 248  $\mu_{0.03}$  which was based on half value of the axial shortening as those defined from the tests. and the  
 249 ultimate strength ( $P_{FE-u}$ ) were shown in Table 4. The test strengths were compared with the FEA  
 250 strengths by  $P_{3\%}/P_{FE-I}$  and  $P_u/P_{FE-u}$ . The mean values of  $P_{3\%}/P_{FE-I}$  and  $P_u/P_{FE-u}$  were 0.98 and 0.95 with  
 251 the corresponding coefficient of variation (COV) of 0.062 and 0.070. Figure 8(a) illustrates the  
 252 comparison of failure mode between test and FEA for specimen 89×4<sup>^</sup>-108×4. The elevation view of  
 253 the specimen failure and the stress contour are shown in Figure 8(b). Generally, the higher stresses  
 254 (reaching yield stress) were found within the length of  $1.0d_o$  from the centreline of the joint. Similar  
 255 findings were illustrated in Lan *et al.* [37,38]. Figures 10(a)-(b) further illustrate the comparison of load

256 versus the deformation curves of the CFHSS CHS X-joints between the test and FEA results. Half  
257 displacement of RF1 and the total deformation of RF5 were used in plotting the axial shortening and  
258 chord horizontal deformation curves, respectively. Overall, it is shown that the developed FEM could  
259 replicate the tests of CFHSS CHS X-joints in terms of joint strengths, failure mode and histories of  
260 applied load versus deformations. The results obtained from RP3 and RP4 will be used to determine the  
261 chord indentation and the corresponding joint strength of test specimens in the later analysis of this study.

### 262 3.3 Parametric studies

263 After successful validation of the FEM, the FEM was used to perform the parametric studies for the  
264 structural performance of CFHSS CHS X-joints subject to axial compression in braces. The geometric  
265 parameters of the CHS X-joint design equations [52,55] were considered, and their interactions were  
266 reflected in the parameters of the  $\beta$ ,  $\tau$  and  $2\gamma$ . The length of the braces was taken as  $2d_l$  and that of the  
267 chords was taken as  $(d_l + 5d_o)$ . Same as those test specimens, the chord members of the CFHSS CHS  
268 X-joints in the parametric studies were not preloaded.

269 The designed X-joints for the parametric studies are summarized in Table 5. In the joint designs,  
270 three different chord members based on the commonly used steel product catalogue were selected to  
271 represent the relatively small, medium and large sizes of CHS members, with the dimensions ( $D \times t$  in  
272 millimetre) of  $88.9 \times 6.3$ ,  $273 \times 12.5$  and  $508 \times 12.5$ , respectively. Hence, there are three series of X-joints  
273 in terms of chord outer diameter variations ( $d_o$ ) as represented by Series A, B and C in the content of this  
274 paper. In each series, the geometric parameters of the joints were determined based on the predetermined  
275 values of  $\beta$ ,  $\tau$  and  $2\gamma$ . The values of  $\beta$ ,  $\tau$  and  $2\gamma$  were mainly set as 0.40, 1.00 and 14.11 in Series A. In  
276 Series A, the effects of  $\beta$ ,  $\tau$  and  $2\gamma$  on the joint behaviour were studied by verifying one factor while  
277 maintaining the other two factors the same (see Table 5). Hence, the cross-sectional dimensions of the  
278 brace and chord members were then determined. By using the same principle, the values of  $\beta$ ,  $\tau$  and  $2\gamma$

279 were mainly set as 0.60, 0.60 and 21.84 & 0.80, 0.40 and 40.64 for Series B and C, respectively. Same  
280 labelling system was adopted as that for the test specimens. Details of the specimens with the geometric  
281 ratios are shown in Tables 6-8, for Series A, B and C, respectively.

282 The material properties of section 108×4 (see Table 1) obtained from the coupon tests were used in  
283 the parametric studies. In total, 75 parametric results were generated for the CFHSS CHS X-joints  
284 subjected to axial loading in braces. All these 75 X-joints mainly failed by chord plastification. In each  
285 series, the curves of load versus the chord side wall deformation and those of load versus the chord  
286 indentation are plotted, as shown in Figures 11-13 for specimens Series A, and in Figures 14-16 for  
287 Series B and Figures 17-19 for Series C. The chord face indentation ( $\mu$ ) was obtained by half of the  
288 difference in axial displacements of RP3 and RP4, i.e.,  $(|\Delta_{RP3}| - |\Delta_{RP4}|)/2$ . In the figure of each series,  
289 the value of chord face indentation equal to  $3\%d_0$  was identified. The strengths ( $P_{FE-0.03}$ ) of the X-joints  
290 corresponding to chord face indentation of  $3\%d_0$  were obtained. It should be noted that six specimens  
291 did not reach the chord face indentation value of  $3\%d_0$  due to the premature of brace local buckling.  
292 These specimens were marked by #, as shown in Tables 6-8, and they were not used in the further  
293 analysis. Some specimens experienced chord face indentation of  $3\%d_0$  but still not reached the peak  
294 strength although they were axially loaded with total end shortening of over 50 mm, particularly for  
295 those of Series C (see Figures 17-19). Hence, the strengths ( $P_{FE}$ ) of the X-joints in parametric studies  
296 were determined by  $P_{FE} = P_{FE-u}$  if  $\mu_p \leq 3\%d_0$ ; otherwise,  $P_{FE} = P_{FE-0.03}$  if  $\mu_p > 3\%d_0$ .  $P_{FE-u}$  and  $\mu_p$  are the  
297 ultimate (peak) strengths and the corresponding chord face indentation of an X-joint. Same strength  
298 definitions with respect to  $3\%d_0$  have been widely adopted for CHS X-joints in the literature [36-38].  
299 The strengths ( $P_{FE}$ ) of the X-joints in parametric studies are tabulated in Tables 6-8.

## 300 4. Structural performance

### 301 4.1 Deformation capacity and ductility

302 The current design guidelines are generally strength-based, but without specifying any requirements  
303 for the deformation capacity and ductility of steel tubular joints [58], including those in this study. The  
304 chord face indentation limit of  $3\%d_o$  for steel CHS X-joints was firstly suggested by Lu *et al.* [64], as  
305 they found that for the steel tubular joints exhibiting peak loads generally had the chord face indentations  
306 within  $2.5\%d_o \sim 4\%d_o$  in the load-deformation curves. Hence, the chord face indentation limit of  $3\%d_o$   
307 was proposed for the steel tubular X-joints without exhibiting peak loads because of material strain  
308 hardening and membrane action. It should be noted that such limit was based on steel tubular joints made  
309 up of normal strength steel, but not high strength steel. However, the recent experimental investigation  
310 on six CFHSS CHS X-joints with  $f_{0.2}/f_u$  ranging from 0.87 to 0.91 and  $\epsilon_f$  ranging from 13.5% to 17.8%  
311 in chord members, as well as values of the  $\beta$  ranging from 0.60 to 0.93, showed that the deformation  
312 capacity of the joints could be considered as reasonably sufficient, as evidenced by the indentations at  
313 peak loads that were generally at least twice of the respective values of  $3\%d_o$  [58].

314 The ductility of CFHSS members in the X-joint specimens is also relatively low with the yield ratio  
315 ( $f_{0.2}/f_u$ ) of around 0.90 and the fracture strain ( $\epsilon_f$ ) around 11.0% (see Table 3). However, as also found by  
316 Lan *et al.* [58], it is shown that all testing curves exhibited similar slow-descending without sudden drop  
317 of loads after reaching the peak loads (see the test curves of the present study in Figures 6-7). Similar  
318 findings were shown in the curves (see Figures 11-19) that were obtained from the parametric studies of  
319 this paper, except for those failed by brace local buckling. For the X-joints with chords members of  
320 medium and large sizes ( $d_o=273$  and  $508$  mm), almost all the curves had not reached the peak loads after  
321 experiencing the chord face indentation of  $0.03d_o$ . Larger deformation capacity of these specimens could  
322 be anticipated from the figures. Hence, this is favourable for the application of the CFHSS CHS X-joints  
323 when the issue of joint deformation and ductility was a concern. Note that this study mainly focusses on  
324 the X-joint specimens that failed by chord plastification without preloading in the chords.

## 4.2 The effects of geometric parameters

The effects of geometric parameters on the strengths of CFHSS CHS X-joints failed by chord plastification were analysed. In the investigation of the effects due to the variations of  $\beta$  in each sub-series, the strengths ( $P_{FE}$ ) were normalized by the strength corresponding to  $\beta = 0.9$ . By following this, the strengths ( $P_{FE}$ ) in the sub-series were normalized by 817.2 kN in Table 6 for  $\tau = 1.00$  and  $2\gamma = 21.84$ , and by 3201.3 kN in Table 7 for  $\tau = 0.60$  and  $2\gamma = 21.84$  and by 2978.2 kN in Table 8 for  $\tau = 0.40$  and  $2\gamma = 40.64$ . Similarly, in the investigation of the effects due to the variations of  $\tau$  in each sub-series, the strengths ( $P_{FE}$ ) were normalized by the strength corresponding to  $\tau = 0.9$ . For those due to the variations of  $2\gamma$  in each sub-series, the values of  $P_{FE}$  were normalized by the strength corresponding to around  $2\gamma = 20$ . The normalized values for each sub-series are shown in the last columns of Tables 6-8.

The effects of  $\beta$ ,  $\tau$  and  $2\gamma$  on the joint strengths are plotted in Figures 20-22, respectively. In each figure, the results of the three sub-series from Series A, B and C were used. As shown Figure 20, the X-joint strengths increased as the value of  $\beta$  increased, and the increments were larger as the  $\beta$  became larger regardless of different sets of  $\tau$  and  $2\gamma$ . Furthermore, for each set of  $\tau$  and  $2\gamma$ , the trend of strength increments with increasing of  $\beta$  was similar with each other. However, the variation of  $\tau$  had little effects on the strength of the X-joints for different sets of  $\beta$  and  $2\gamma$  (see Figure 21). On the contrary to those findings in the effects due to  $\beta$ , the X-joint strengths decreased as the value of  $2\gamma$  increased, and the decrements were smaller as the  $2\gamma$  became larger regardless of different sets of  $\beta$  and  $\tau$ . For each set of  $\beta$  and  $\tau$ , the trend of strength decrements with decreasing of  $2\gamma$  was similar with each other.

## 5. Strength prediction of existing design rules

### 5.1 Design guidelines

As discussed in Section 1 of this paper, the strength ( $P$ ) for steel CHS X-joints that failed by chord plastification is function of the 0.2% proof stress (yield strength) together with the square of chord wall

348 thickness ( $f_{0.2}t_0^2$ ) based on the analytical model proposed by Togo in 1967 [57]. The design formulas  
 349 were developed based on this principle by considering the effects due to the geometrical parameters as  
 350 represented by  $Q_u$  and the preloading condition of the chord by  $Q_f$ , which is shown in Equation (3). The  
 351 angle ( $\theta$ ) between the brace and chord is considered by  $\sin\theta$ , which is equal to 1.0 for all the X-joints in  
 352 this study. The  $Q_u$  and  $Q_f$  were determined using multi-regression analyses of the experimental and  
 353 numerical results. The development of the design equations in the CIDECT and IIW were discussed in  
 354 detail by Zhao *et al.* [45] and Zhao and Tong [46].

$$355 \quad P = Q_f Q_u \frac{f_{0.2} t_0^2}{\sin \theta} \quad (3)$$

356 The CFHSS CHS X-joints in this study were designed without any preloading in the chords. Hence,  
 357 the  $Q_f$  is equal to 1.0. The determination of  $Q_u$  is related to the geometric parameters such as  $\beta$ ,  $\tau$  and  $2\gamma$ ,  
 358 and generally represented by Equation (4), where  $A$ ,  $B$ , and  $C$  are regression coefficients. The parameter  
 359 of  $\tau$  is not considered in Equation (4) as it has limited effect on the joint strengths that failed by chord  
 360 plastification, which is also illustrated in Figure 21 of this paper.

$$361 \quad Q_u = \left( \frac{A}{1-B\beta} \right) (\gamma)^C \quad (4)$$

362 The design guide in CIDECT [52] is generally based on the 3<sup>rd</sup> edition of the IIW recommendations  
 363 [49]. It updates the strength equations by considering the chord indentation limit of 3% $d_0$ . Background  
 364 of the 3<sup>rd</sup> edition of IIW recommendations [49] is explained by van der Vegte *et al.* [65]. The  
 365 determination of  $Q_u$  in CIDECT [52] is shown in Equation (5), as represented by  $Q_{CDT,f}$ .

$$366 \quad Q_{CDT,f} = 2.6 \left( \frac{1+\beta}{1-0.7\beta} \right) \gamma^{0.15} \quad (5)$$

367 The Equations (3) and (5) provided factored strength of steel CHS X-joints. This is because a safety  
 368 factor equal to 1.22 has been included [58]. Hence, the nominal strength (unfactored) of X-joints should  
 369 be determined by Equations (3) and (6).



$$Q_{CDT,n} = 3.16 \left( \frac{1+\beta}{1-0.7\beta} \right) \gamma^{0.15} \quad (6)$$

The validity ranges of the Equation (6) for the steel CHS X-joints are  $0.2 \leq \beta \leq 1.0$ ,  $2\gamma \leq 40$  and  $\theta \geq 30^\circ$ . All the CFHSS CHS X-joints in this study had the same  $\theta = 90^\circ$ , with  $0.2 \leq \beta \leq 1.0$ ,  $0.2 \leq \tau \leq 1.0$  and  $10.0 \leq 2\gamma \leq 50.0$ . The nominal strength calculations in this study, the reduction factor of 0.9 together with the material strength in the minimum of  $f_{0.2}$  and  $0.8f_u$  were used, as previous numerical studies showed that the predictions overestimated the test strengths for high strength steel CHS X-joints [37].

The  $Q_u$  for steel CHS X-joints in EN 1993-1-8 [55] is, however, mainly based on the 2<sup>nd</sup> edition of the IIW recommendations [48], which takes the peak loads as the joint strengths. The determination of  $Q_{EC,f}$  as specified in Table 7.2 of EN 1993-1-8 [55] is re-written in Equation (7) as shown below:

$$Q_{EC,f} = \frac{5.2}{1-0.81\beta} \quad (7)$$

A partial safety factor ( $\gamma_{M5}$ ) equal to 1.0 is suggested for the resistance design in EN 1993-1-8 [55]. This is because Equation (7) has implicitly adopted a safety factor of 1.28. In this sense, the nominal strength of steel CHS X-joints predicted by EN 1993-1-8 [55] should be calculated by Equation (3) together with the nominal  $Q_{EC,n}$  as determined by Equation (8).

$$Q_{EC,n} = \frac{6.67}{1-0.81\beta} \quad (8)$$

The parameter of  $\gamma$  is not shown in Equations (7) and (8). This is because they were developed based on the original Equation (9) in Wardernier [66].

$$Q_W = \frac{7.46}{1-0.812\beta} (2\gamma)^{-0.05} (f_{0.2}/f_u)^{-0.173} \quad (9)$$

The Equation (9) is simplified by adopting  $2\gamma = 40$  and  $f_{0.2}/f_u = 0.66$  as it was found that the strengths of the investigated X-joints were less sensitive under the variations of  $\gamma$  and  $f_{0.2}/f_u$  in Equation (9) [66]. The Equation (8) is applicable for steel CHS X-joints in the ranges of  $0.2 \leq \beta \leq 1.0$ ,  $10.0 \leq 2\gamma \leq 50.0$  and  $\theta \geq 30^\circ$ , as specified in EN 1993-1-8 [55]. The reduction factor of 0.9 is specified [55] for steel with

nominal yield strength exceeding 355 MPa and a further reduction factor of 0.8 is specified [2] for steel with nominal yield strength greater than 460 MPa up to 700 MPa. Hence, these two factors were used in the nominal strength calculations in this study. In addition, to make a direct comparison, the predictions by using Equation (9) were also assessed in this study, however, the reduction factors were not used for Equation (9).

It should be noted that for the above equations, the brace cross sections of the X-joints are required to be Class 1 or 2 to avoid premature of brace local buckling. In this study, the X-joints that failed by brace local buckling before reaching the chord face indentation of  $3\%d_0$  or ultimate load were excluded from the analysis regardless of the brace cross section classifications. The X-joints that failed by chord plastification having chord face indentation of not less than  $3\%d_0$  or reaching clear peak load before such indentation were used to assess the design equations regardless of cross section classifications of the braces. Those 6 specimens (see Tables 6-8) that failed by local buckling of the braces in the X-joints were not included in the analysis in this paper.

## 5.2 Design equation proposed by Lan *et al.* [38]

Numerical investigation conducted by Lan *et al.* [38] found that the predictions by CIDECT [52] are generally unconservative for the strength predictions of high strength steel CHS X-joints made up of steel members with grades of S460, S700, S900 and S1100. Hence, a reduction factor ( $Q_y$ ) was proposed in the determination of the  $Q_u$ . The  $Q_u$  proposed by Lan *et al.* [38] was represented by  $Q_L$ , as shown in Equations (10) and (11).

$$Q_L = 3.16 \left( \frac{1+\beta}{1-0.7\beta} \right) Q_y \gamma^{0.15} \quad (10)$$

$$Q_y = -62 \frac{f_{0.2}}{E} + 1.1 \quad (11)$$

The reduction factor of  $Q_y$  in Equation (11) accounts for the increased 0.2% proof stress (yield strength) due to the higher steel grades. The Equation (10) was validated for CHS X-joints made up of

415 steel members with  $f_{0.2,n}$  ranging from 700 MPa to 1100 MPa,  $0.2 \leq \beta \leq 1.0$  and  $2\gamma \leq 30.0$ . In this study,  
416 the Equations (10)-(11) suggested by Lan *et al.* [38] were also used together with Equation (3) in the  
417 nominal strength predictions of the CFHSS CHS X-joints in this study.

### 418 5.3 Comparison of test and numerical strengths with predicted strengths

419 The test strengths ( $P_t$ ) and numerical strengths ( $P_{FE}$ ) obtained in this study were compared with the  
420 nominal strengths predicted by CIDECT [52], EN 1993-1-8 [55], Wardenier [66] and Lan *et al.* [38], as  
421 represented by  $P_{CDT,n}$ ,  $P_{EC,n}$ ,  $P_W$  and  $P_L$ , respectively. It should be noted that the test strengths ( $P_t$ ) were  
422 taken as  $P_u$  for specimens of  $89 \times 4^A - 89 \times 4^*$ ,  $89 \times 4^* - 89 \times 4^*$  and  $89 \times 4^A - 89 \times 4^A$  (see Table 4) as the peak  
423 loads occurred before the 3% $d_o$  chord face indentation. Whilst, the rest of the test strengths ( $P_t$ ) were  
424 taken as  $P_{EF-0.03}$  from the verified FEM (discussed in Section 3.2). The detail comparisons of  $P_t/P_{CDT}$ ,  
425  $P_t/P_{EC}$ ,  $P_t/P_W$  and  $P_t/P_L$  are shown in Table 9; and those of  $P_{FE}/P_{CDT,n}$ ,  $P_{FE}/P_{EC,n}$ ,  $P_{FE}/P_W$  and  $P_{FE}/P_L$  are  
426 shown in Tables 10(a)-(c) for specimen Series A, B and C, respectively.

427 For the comparisons with the test results, it was found that the current predictions are unconservative,  
428 however, the equations proposed by Lan *et al.* [38] provided the least unconservative and least scattered  
429 predictions. The mean values of  $P_t/P_{CDT,n}$ ,  $P_t/P_{EC,n}$ ,  $P_t/P_W$  and  $P_t/P_L$  are 0.88, 0.91, 0.67 and 0.93, with  
430 the corresponding COVs of 0.147, 0.139, 0.136 and 0.119 (see Table 9). The reduction factors suggested  
431 in CIDECT [52] and EN 1993-1-8 [55] improved the predictions in a less unconservative manner when  
432 compared with those predicted by Wardenier [66]. Similarly, the predictions by the design rules are also  
433 unconservative when compared with the results obtained from the parametric studies except those  
434 predicted by Lan *et al.* [38] for specimens Series A (mean value of  $P_{FE}/P_L = 1.00$  as shown in Table 10(a).  
435 Generally, the predictions tended to be more unconservative as the outer diameter ( $d_o$ ) of the chords  
436 becomes larger except for those predicted by Wardenier [66]. For example, the mean values of  
437  $P_{FE}/P_{CDT,n}$  are 0.89, 0.83 and 0.72 for specimens Series A, B and C, respectively, as shown in Tables

10(a)-(c). All these comparisons by using the four design rules are further illustrated in Figures 23-26, respectively. The vertical axis of the figures plots the strength predictions while the horizontal axis plots the test and numerical results. Overall, it was found that the predictions by the current design rules are unconservative.

## 6. Proposed design rules and predictions

Efforts were made in this section to improve predictions of the CFHSS CHS X-joints. As discussed earlier, the strengths ( $P$ ) of the X-joints that failed by chord plastification are a function of the  $f_{0.2}t\sigma^2$  (see Equation (3)), and the  $Q_u$  (see Equation (4)) that are related to the geometric ratios of  $\beta$  and  $2\gamma$ , as also illustrated in Figures 20 and 22. Hence, by referring to Equation (6) and Equation (9), both the  $P_t$  and  $P_{FE}$  in this study were divided by  $f_{0.2}t\sigma^2\gamma^{0.15}$  and  $f_{0.2}t\sigma^2(2\gamma)^{-0.05}$ . In addition, the test results of high strength steel CHS X-joints subjected to compression in braces without chord preloading collected from the literature [35,36,58] were also used. Detail information of these test specimens [35,36,58] are shown in Table 11. All the results divided by  $f_{0.2}t\sigma^2\gamma^{0.15}$  and  $f_{0.2}t\sigma^2(2\gamma)^{-0.05}$  are plotted against the corresponding values of  $\beta$ , as shown in Figures 27-28, respectively.

It is shown that the values of  $P/f_{0.2}t\sigma^2\gamma^{0.15}$  and  $P/f_{0.2}t\sigma^2(2\gamma)^{-0.05}$  increased regularly as the values of  $\beta$  increased. However, the values of  $P/f_{0.2}t\sigma^2\gamma^{0.15}$  were relatively more scattered than those of  $P/f_{0.2}t\sigma^2(2\gamma)^{-0.05}$ . Hence, the relationship between  $P/f_{0.2}t\sigma^2(2\gamma)^{-0.05}$  and  $\beta$  were derived and plotted as shown in Figure 28. The relationship of  $Q_u$  (represented by  $Q_P$ ) with  $\beta$  and  $2\gamma$  was proposed as shown in the following Equation (12).

$$Q_P = (22\beta^{2.5} + 4)(2\gamma)^{-0.05} \quad (12)$$

The proposed Equation (12) was used together with Equation (3) to predict the nominal strength ( $P_P$ ) of the X-joint specimens obtained in this study, as shown in Tables 9-10. The predictions were generally improved when compared with other four predictions, as the unconservative predictions became

conservative or less unconservative. Furthermore, the predictions became less scattered, as reflected by the minimum value of COV in each table.

The test strengths obtained from the literature [35,36,58] were also used to compare with the predictions, as shown in Table 11. Overall, the existing predictions are unconservative except for those predicted by EN-1993-1-8 [55] with the mean value of  $P_t/P_{EC,n}$  equal to 1.02. The predictions by using the Equation (3) together with the newly proposed  $Q_P$  in Equations (12) provided conservative predictions as reflected in the mean value of  $P_t/P_P$  equal to 1.08 with the COV of 0.168. Table 12 further summarized all the comparisons between test and numerical strengths with predictions. Totally, 33 test results and 69 numerical results (the 6 specimens failing in local buckling of the braces but not in chord plastification were not included) were used in the comparisons. Overall, it is shown that all the existing design rules provided unconservative predictions. The EN-1993-1-8 [55] and Lan *et al.* [38] provided the least unconservative predictions with both the mean value of 0.92. However, the EN-1993-1-8 [55] provided less scattered predictions due to the smaller value of COV equal to 0.134. On the contrary, the predictions by using Equation (3) with the proposed Equation (12) provided conservative predictions, i.e., mean value and COV of 1.04 and 0.127, respectively. The test results from the literature [35,36,58] are also plotted in the comparisons as shown in Figures 23-26. The comparisons  $P_P$  against  $P_t$  and  $P_{FE}$  are shown in Figure 29.

## 7. Conclusions

Experimental and numerical investigations on cold-formed high strength steel (CFHSS) CHS X-joints have been presented. The CFHSS circular members had nominal 0.2% proof stress ( $f_{0.2,n}$ ) up to 1100 MPa. In total, 17 X-joints were tested by applying axial compression through the braces without preloading in chords. The X-joints failed by chord plastification. Non-linear finite element model (FEM) was developed for the CFHSS CHS X-joints. Parametric studies were performed by using the verified

484 FEM. The key parameters of  $\beta$ ,  $2\gamma$  and  $\tau$  were designed in the range of 0.2 to 1.0, 10 to 50 and 0.2 to 1.0,  
485 respectively. The X-joints had the outer diameter of the chord ( $d_o$ ) up to 508 mm. The chord plastification  
486 failure of the X-joints was mainly found in the numerical study, which was used in the analysis.

487 The relationship between the joint strengths and the variation of geometric ratios were investigated.  
488 It was found that as the  $\beta$  increased, the joint strengths increased in a similar manner regardless of  
489 different sets of  $\tau$  and  $2\gamma$ . On the contrary, as the  $2\gamma$  increased, the joint strengths decreased but still in a  
490 similar manner for different sets of  $\beta$  and  $\tau$ . The variation of  $\tau$  had limited effects on the joint strengths.  
491 The CHFSS CHS X-joints showed good deformation capacity and ductility, particularly for those with  
492  $d_o$  of 273 and 508 mm, as all these specimens reached the chord face indentation of  $3\%d_o$  even they did  
493 not reach the peak loads.

494 The strengths of the X-joints obtained in this study together with the test strengths collected from the  
495 literature [35,36,58] were used to compare with the predictions by using the existing design rules,  
496 including those specified in CIDECT [52] and EN-1993-1-8 [55], as well as those proposed by  
497 Wardenier [66] and Lan *et al.* [38]. It was found that the current predictions generally provided  
498 unconservative predictions, namely overestimated the CFHSS CHS X-joint strengths. The predictions  
499 by EN-1993-1-8 [55] and Lan *et al.* [38] provided the least unconservative predictions. A new equation  
500 for  $Q_P$  that considering the effects of geometric ratios on the strengths was derived based on both the test  
501 and numerical results. By adopting the newly proposed equation, the predictions were improved (at the  
502 conservative side), and provided the least scattered results when compared with the other predictions.  
503 The newly proposed  $Q_P$  is applicable to the nominal strength predictions of CFHSS CHS X-joints  
504 subjected to axial loading in braces without pre-loading in chords. The X-joints are made up of circular  
505 tubes with  $f_{0.2,n}$  from 700 MPa to 1100 MPa,  $\theta = 90^\circ$ ,  $\beta$ ,  $\tau$  and  $2\gamma$  ranged from 0.17 to 1.00, 0.20 to 2.77  
506 and 10 to 50.

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**Table 1:** Measured dimensions of CFHSS circular tubular X-joints

Specimens	Upper braces (mm)			Lower braces (mm)			Chords (mm)			Geometric ratios		
Brace - Chord	$d_l$	$t_l$	$l_l$	$d_l$	$t_l$	$l_l$	$d_o$	$t_o$	$l_o$	$\beta$	$\tau$	$2\gamma$
22×4 - 133×4	22.0	3.96	46.9	22.0	3.79	46.4	133.0	3.93	601.5	0.17	0.96	33.84
55×11 - 133×4	55.3	10.4	112.4	55.3	10.6	112.4	134.1	3.95	635.4	0.41	2.63	33.95
89×4 <sup>^</sup> - 133×4	89.3	3.94	179.8	88.6	3.91	179.2	134.5	3.93	668.3	0.66	0.99	34.22
89×4* - 133×4	89.3	3.93	179.4	89.2	3.92	179.3	134.3	3.97	669.7	0.66	0.99	33.83
22×4 - 108×4	22.0	3.79	46.2	22.0	3.83	46.2	107.7	3.91	526.5	0.20	0.97	27.54
55×11 - 108×4	55.4	10.6	112.1	55.2	10.7	112.4	107.9	3.93	559.8	0.51	2.70	27.46
89×4 <sup>^</sup> - 108×4	88.8	3.91	179.4	89.2	3.91	179.2	108.1	3.92	594.5	0.82	1.00	27.58
89×4* - 108×4	89.1	3.94	179.8	88.5	3.87	179.2	108.1	3.82	593.6	0.82	1.01	28.30
22×4 - 89×4*	22.1	3.89	45.7	22.1	3.95	46.4	88.8	3.92	470.4	0.25	0.99	22.65
55×11 - 89×4*	55.1	10.8	111.5	55.2	10.6	112.2	88.8	3.83	505.5	0.62	2.77	23.19
55×11 - 89×4*-r	55.1	10.6	111.9	55.2	10.6	111.8	89.0	3.91	503.4	0.62	2.71	22.76
89×4 <sup>^</sup> - 89×4*	89.1	3.89	180.2	88.6	3.92	179.7	88.7	3.89	537.8	1.00	1.00	22.80
89×4* - 89×4*	89.0	3.93	180.5	89.1	3.86	180.2	89.3	3.93	538.1	1.00	0.98	22.72
22×4 - 89×4 <sup>^</sup>	22.1	3.81	46.1	22.1	3.89	46.3	88.9	3.91	470.2	0.25	0.97	22.74
22×4 - 89×4 <sup>^</sup> -r	22.1	3.82	46.3	22.1	3.89	46.2	88.9	3.89	470.5	0.25	0.98	22.85
55×11 - 89×4 <sup>^</sup>	55.2	10.6	112.2	55.1	10.8	112.4	89.1	3.96	503.5	0.62	2.68	22.50
89×4 <sup>^</sup> - 89×4 <sup>^</sup>	88.6	3.90	180.3	89.1	3.90	179.8	89.0	3.93	535.9	1.00	0.99	22.65

Note: <sup>^</sup> and \* mean having nominal 0.2% proof stress of 900 MPa and 1100 MPa, respectively.

**Table 2:** Measured welding details of CFHSS circular tubular X-joint specimens

Specimens	$\Delta_1$ (mm)	$\Delta_2$ (mm)	$\Delta_3$ (mm)	$\Delta_4$ (mm)	$w$ (mm)
22×4 - 133×4	5.78	5.63	4.25	-	-
55×11 - 133×4	6.20	5.08	4.48	-	-
89×4 <sup>^</sup> - 133×4	5.68	5.53	4.54	-	-
89×4* - 133×4	5.43	5.30	4.12	-	-
22×4 - 108×4	5.93	5.28	4.77	-	-
55×11 - 108×4	5.70	4.95	3.65	-	-
89×4 <sup>^</sup> - 108×4	5.50	6.03	4.72	-	-
89×4* - 108×4	5.55	5.58	4.60	-	-
22×4 - 89×4*	6.15	5.93	4.60	-	-
55×11 - 89×4*	6.38	5.58	4.97	-	-
55×11 - 89×4*-r	6.35	4.80	4.45	-	-
89×4 <sup>^</sup> - 89×4*	5.50	6.15	4.89	19.74	1.75
89×4* - 89×4*	5.70	6.18	4.61	19.41	1.49
22×4 - 89×4 <sup>^</sup>	5.70	5.80	4.46	-	-
22×4 - 89×4 <sup>^</sup> -r	5.85	5.48	4.43	-	-
55×11 - 89×4 <sup>^</sup>	6.40	5.33	4.98	-	-
89×4 <sup>^</sup> - 89×4 <sup>^</sup>	5.35	6.43	4.61	20.77	1.35

Note: <sup>^</sup> and \* mean having nominal 0.2% proof stress of 900 MPa and 1100 MPa, respectively.

**Table 3:** Measured material properties of CFHSS circular tubes

Sections	Measured								
$D \times t$	$E$	$f_{0.01}$	$f_{0.2}$	$f_u$	$\epsilon_u$	$\epsilon_f$	$n$	$f_{0.2}/f_u$	$0.8f_u$
mm	GPa	MPa	MPa	MPa	%	%			MPa
22×4	197	501.0	755	832	1.6	5.4	7.3	0.91	665.6
55×11	204	606.0	800	919	4.4	8.6	10.8	0.87	735.2
89×4 <sup>^</sup>	212	515.0	983	1106	2.1	11.7	4.6	0.89	884.8
89×4*	207	585	1213	1313	2.4	10.6	4.1	0.92	1050.4
108×4	203	553	1155	1344	2.3	10.9	4.1	0.86	1075.2
133×4	207	535	1100	1255	2.7	10.7	4.2	0.88	1004.0

Note: <sup>^</sup> and \* mean having nominal 0.2% proof stress of 900 MPa and 1100 MPa, respectively.

**Table 4:** Test results and FE predictions of CFHSS circular tubular X-joints

Specimens	Axial shortening (mm)		Tests (kN)		FEA (kN)		Comparison	
	$\mu_{0.03}$	$\mu_u$	$P_{3\%}$	$P_u$	$P_{FE-l}$	$P_{FE-u}$	$P_{3\%}/P_{FE-l}$	$P_u/P_{FE-u}$
22×4 - 139×6	3.99	8.30	63.5	82.5	60.9	79.8	1.04	1.03
55×11 - 139×6	4.02	9.38	88.8	123.0	100.8	133.7	0.88	0.92
89×4 <sup>^</sup> - 139×6	4.04	7.61	157.8	179.0	162.5	196.0	0.97	0.91
89×4* - 139×6	4.03	7.61	161.1	182.4	164.6	198.0	0.98	0.92
22×4 - 108×4	3.23	6.45	76.7	100.1	71.3	94.5	1.08	1.06
55×11 - 108×4	3.24	7.23	120.5	147.9	130.9	166.4	0.92	0.89
89×4 <sup>^</sup> - 108×4	3.24	5.46	224.6	232.4	250.5	264.2	0.90	0.88
89×4* - 108×4	3.24	4.35	221.9	227.7	239.3	253.5	0.93	0.90
22×4 - 89×4*	2.66	6.34	86.4	112.1	83.7	108.3	1.03	1.04
55×11 - 89×4*	2.66	5.66	163.5	183.3	166.1	191.6	0.98	0.96
55×11 - 89×4*-r	2.67	5.45	152.9	173.8	-	-	-	-
89×4 <sup>^</sup> - 89×4*	2.66	1.83	431.2	441.3	447.3	480.8	0.96	0.92
89×4* - 89×4*	2.68	1.94	442.2	454.1	449.9	492.1	0.98	0.92
22×4 - 89×4 <sup>^</sup>	2.67	5.81	83.8	102.9	78.4	95.2	1.07	1.08
22×4 - 89×4 <sup>^</sup> -r	2.67	5.49	74.7	92.4	-	-	-	-
55×11 - 89×4 <sup>^</sup>	2.67	4.91	146.6	161.0	159.4	177.6	0.92	0.91
89×4 <sup>^</sup> - 89×4 <sup>^</sup>	2.67	1.84	412.3	421.9	407.1	444.0	1.01	0.95
						Mean	0.98	0.95
						COV	0.062	0.070

Note: <sup>^</sup> and \* mean having nominal 0.2% proof stress of 900 MPa and 1100 MPa, respectively.



**Table 5:** Specimens of CFHSS circular tubular X-joints in parametric studies

Series	Braces (mm)		Chords (mm)		Geometric ratios		
	$d_l$	$t_l$	$d$	$t$	$\beta$	$\tau$	$2\gamma$
Series A	[17.78~88.90]	6.30	88.9	6.30	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	1.00	14.11
	35.56	[1.26~6.30]		6.30	0.40	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	14.11
	35.56	[1.78~8.89]		1.78, 1.98, 2.22, 2.54, 2.96, 3.56, 4.45, 6.30, 8.89	0.40	1.00	10.00, 14.11, 19.98, 24.97, 30.03, 35.00, 40.05, 44.90, 49.94
Series B	[54.60~273.00]	7.50	273.0	12.50	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	0.60	21.84
	163.80	[2.50~12.50]		12.50	0.60	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	21.84
	163.80	[3.28~16.38]		5.46, 6.07, 6.83, 7.80, 9.10, 10.92, 12.50, 18.20, 27.30	0.60	0.60	10.00, 15.00, 21.84, 25.00, 30.00, 35.00, 39.97, 44.98, 50.00
Series C	[101.60~508.00]	5.00	508.0	12.50	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	0.40	40.64
	406.40	[2.50~12.50]		12.50	0.80	0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, 0.90, 1.00	40.64
	406.40	[4.06~20.32]		10.16, 11.29, 12.50, 14.51, 16.93, 20.32, 25.40, 33.87, 50.80	0.80	0.40	10.00, 15.00, 20.00, 25.00, 30.01, 35.01, 40.64, 45.00, 50.00

**Table 6:** Parametric study results and strength comparisons for X-joints Series A ( $d_0 = 88.9$  mm)

Specimens	Geometric ratios			$P_{FE}$	Normalized
Brace - Chord	$\beta$	$\tau$	$2\gamma$	(kN)	
17.78×6.30 - 88.90×6.30	0.20	1.00	14.11	211.3	0.26
26.67×6.30 - 88.90×6.30	0.30	1.00	14.11	255.2	0.31
35.56×6.30 - 88.90×6.30	0.40	1.00	14.11	306.7	0.38
44.45×6.30 - 88.90×6.30	0.50	1.00	14.11	367.4	0.45
53.34×6.30 - 88.90×6.30	0.60	1.00	14.11	440.4	0.54
62.23×6.30 - 88.90×6.30	0.70	1.00	14.11	532.4	0.65
71.12×6.30 - 88.90×6.30	0.80	1.00	14.11	653.6	0.80
80.01×6.30 - 88.90×6.30	0.90	1.00	14.11	817.2	1.00
88.90×6.30 - 88.90×6.30	1.00	1.00	14.11	1173.5	1.44
35.56×1.26 - 88.90×6.30#	0.40	0.20	14.11	-	-
35.56×1.89 - 88.90×6.30#	0.40	0.30	14.11	-	-
35.56×2.52 - 88.90×6.30	0.40	0.40	14.11	291.7	0.95
35.56×3.15 - 88.90×6.30	0.40	0.50	14.11	297.8	0.97
35.56×3.78 - 88.90×6.30	0.40	0.60	14.11	300.9	0.98
35.56×4.41 - 88.90×6.30	0.40	0.70	14.11	302.9	0.99
35.56×5.04 - 88.90×6.30	0.40	0.80	14.11	304.5	0.99
35.56×5.67 - 88.90×6.30	0.40	0.90	14.11	305.7	1.00
35.56×6.30 - 88.90×6.30	0.40	1.00	14.11	306.7	1.00
35.56×1.78 - 88.90×1.78	0.40	1.00	49.94	17.2	0.12
35.56×1.98 - 88.90×1.98	0.40	1.00	44.90	22.3	0.15
35.56×2.22 - 88.90×2.22	0.40	1.00	40.05	29.3	0.20
35.56×2.54 - 88.90×2.54	0.40	1.00	35.00	40.4	0.28
35.56×2.96 - 88.90×2.96	0.40	1.00	30.03	57.8	0.40
35.56×3.56 - 88.90×3.56	0.40	1.00	24.97	88.4	0.61
35.56×4.45 - 88.90×4.45	0.40	1.00	19.98	145.5	1.00
35.56×6.30 - 88.90×6.30	0.40	1.00	14.11	306.7	2.11
35.56×8.89 - 88.90×8.89	0.40	1.00	10.00	625.1	4.30

Note: # means brace failed by local buckling.

**Table 7:** Parametric study results and strength comparisons for X-joints Series B ( $d_0 = 273$  mm)

Specimens	Geometric ratios			$P_{FE}$	Normalized
Brace - Chord	$\beta$	$\tau$	$2\gamma$	(kN)	
54.60×7.50 - 273.00×12.50	0.20	0.60	21.84	736.0	0.23
81.90×7.50 - 273.00×12.50	0.30	0.60	21.84	902.1	0.28
109.20×7.50 - 273.00×12.50	0.40	0.60	21.84	1090.2	0.34
136.50×7.50 - 273.00×12.50	0.50	0.60	21.84	1319.3	0.41
163.80×7.50 - 273.00×12.50	0.60	0.60	21.84	1606.2	0.50
191.10×7.50 - 273.00×12.50	0.70	0.60	21.84	1973.3	0.62
218.40×7.50 - 273.00×12.50	0.80	0.60	21.84	2472.4	0.77
245.70×7.50 - 273.00×12.50	0.90	0.60	21.84	3201.3	1.00
273.00×7.50 - 273.00×12.50	1.00	0.60	21.84	4920.1	1.54
163.80×2.50 - 273.00×12.50#	0.60	0.20	21.84	-	-
163.80×3.75 - 273.00×12.50	0.60	0.30	21.84	1528.5	0.93
163.80×5.00 - 273.00×12.50	0.60	0.40	21.84	1571.8	0.96
163.80×6.25 - 273.00×12.50	0.60	0.50	21.84	1591.6	0.97
163.80×7.50 - 273.00×12.50	0.60	0.60	21.84	1606.2	0.98
163.80×8.75 - 273.00×12.50	0.60	0.70	21.84	1618.0	0.98
163.80×10.00 - 273.00×12.50	0.60	0.80	21.84	1628.7	0.99
163.80×11.25 - 273.00×12.50	0.60	0.90	21.84	1637.6	1.00
163.80×12.50 - 273.00×12.50	0.60	1.00	21.84	1645.0	1.00
163.80×3.28 - 273.00×5.46	0.60	0.60	50.00	242.6	0.15
163.80×3.64 - 273.00×6.07	0.60	0.60	44.98	311.6	0.19
163.80×4.10 - 273.00×6.83	0.60	0.60	39.97	410.5	0.26
163.80×4.68 - 273.00×7.80	0.60	0.60	35.00	557.6	0.35
163.80×5.46 - 273.00×9.10	0.60	0.60	30.00	792.2	0.49
163.80×6.55 - 273.00×10.92	0.60	0.60	25.00	1193.5	0.74
163.80×7.50 - 273.00×12.50	0.60	0.60	21.84	1606.2	1.00
163.80×10.92 - 273.00×18.20	0.60	0.60	15.00	3548.7	2.21
163.80×16.38 - 273.00×27.30	0.60	0.60	10.00	7969.2	4.96

Note: # means brace failed by local buckling.

**Table 8:** Parametric study results and strength comparisons for X-joints Series C ( $d_0 = 508$  mm)

Specimens	Geometric ratios			$P_{FE}$	Normalized
Brace - Chord	$\beta$	$\tau$	$2\gamma$	(kN)	
101.60×5.00 - 508.00×12.50	0.20	0.40	40.64	589.6	0.20
152.40×5.00 - 508.00×12.50	0.30	0.40	40.64	718.1	0.24
203.20×5.00 - 508.00×12.50	0.40	0.40	40.64	876.5	0.29
254.00×5.00 - 508.00×12.50	0.50	0.40	40.64	1075.8	0.36
304.80×5.00 - 508.00×12.50	0.60	0.40	40.64	1338.8	0.45
355.60×5.00 - 508.00×12.50	0.70	0.40	40.64	1698.1	0.57
406.40×5.00 - 508.00×12.50	0.80	0.40	40.64	2210.1	0.74
457.20×5.00 - 508.00×12.50	0.90	0.40	40.64	2978.2	1.00
508.00×5.00 - 508.00×12.50#	1.00	0.40	40.64	-	-
406.40×2.50 - 508.00×12.50#	0.80	0.20	40.64	-	0.00
406.40×3.75 - 508.00×12.50	0.80	0.30	40.64	2186.1	0.95
406.40×5.00 - 508.00×12.50	0.80	0.40	40.64	2210.1	0.96
406.40×6.25 - 508.00×12.50	0.80	0.50	40.64	2229.3	0.97
406.40×7.50 - 508.00×12.50	0.80	0.60	40.64	2247.0	0.98
406.40×8.75 - 508.00×12.50	0.80	0.70	40.64	2263.4	0.98
406.40×10.00 - 508.00×12.50	0.80	0.80	40.64	2278.1	0.99
406.40×11.25 - 508.00×12.50	0.80	0.90	40.64	2290.6	1.00
406.40×12.50 - 508.00×12.50	0.80	1.00	40.64	2300.8	1.00
406.40×4.06 - 508.00×10.16	0.80	0.40	50.00	1386.3	0.14
406.40×4.52 - 508.00×11.29	0.80	0.40	45.00	1760.0	0.18
406.40×5.00 - 508.00×12.50	0.80	0.40	40.64	2210.1	0.22
406.40×5.81 - 508.00×14.51	0.80	0.40	35.01	3071.4	0.31
406.40×6.77 - 508.00×16.93	0.80	0.40	30.01	4293.5	0.43
406.40×8.13 - 508.00×20.32	0.80	0.40	25.00	6340.5	0.63
406.40×10.16 - 508.00×25.40	0.80	0.40	20.00	10053.0	1.00
406.40×13.55 - 508.00×33.87	0.80	0.40	15.00	17421.9	1.73
406.40×20.32 - 508.00×50.80#	0.80	0.40	10.00	-	-

Note: # means brace failed by local buckling.

**Table 9:** Strength comparisons between test results obtained from this study and predictions

Specimens	$P_t/P_{CDT,n}$	$P_t/P_{EC,n}$	$P_t/P_W$	$P_t/P_L$	$P_t/P_P$
22×4 - 133×4	0.70	0.59	0.49	0.76	1.03
55×11 - 133×4	0.75	0.74	0.62	0.81	1.11
89×4 <sup>^</sup> - 133×4	0.79	0.84	0.70	0.83	0.98
89×4* - 133×4	0.78	0.83	0.69	0.83	0.96
22×4 - 108×4	0.74	0.64	0.52	0.84	1.09
55×11 - 108×4	0.79	0.80	0.66	0.89	1.07
89×4 <sup>^</sup> - 108×4	0.84	0.88	0.73	0.93	0.96
89×4* - 108×4	0.85	0.90	0.74	0.94	0.97
22×4 - 89×4*	0.86	0.69	0.57	0.93	1.15
55×11 - 89×4*	0.92	0.87	0.72	0.98	1.02
89×4 <sup>^</sup> - 89×4*	1.02	0.85	0.70	1.07	1.08
89×4* - 89×4*	1.03	0.86	0.71	1.09	1.10
22×4 - 89×4 <sup>^</sup>	0.96	0.80	0.66	0.98	1.34
55×11 - 89×4 <sup>^</sup>	0.99	0.97	0.80	1.00	1.15
89×4 <sup>^</sup> - 89×4 <sup>^</sup>	1.15	1.00	0.82	1.14	1.26
Mean	0.88	0.91	0.67	0.93	1.08
COV	0.147	0.139	0.136	0.119	0.101

Note: <sup>^</sup> and \* mean having nominal 0.2% proof stress of 900 MPa and 1100 MPa, respectively.

**Table 10:** Strength comparisons between parametric study results and predictions(a) Series A with  $d_0 = 88.9$  mm

Specimens	$P_{FE}/P_{CDT,n}$	$P_{FE}/P_{EC,n}$	$P_{FE}/P_W$	$P_{FE}/P_L$	$P_{FE}/P_P$
17.78×6.30 - 88.90×6.30	0.93	0.72	0.58	1.04	1.20
26.67×6.30 - 88.90×6.30	0.95	0.79	0.63	1.07	1.25
35.56×6.30 - 88.90×6.30 <sup>\$</sup>	0.97	0.85	0.67	1.09	1.23
44.45×6.30 - 88.90×6.30	0.98	0.89	0.71	1.10	1.16
53.34×6.30 - 88.90×6.30	0.98	0.92	0.73	1.10	1.08
62.23×6.30 - 88.90×6.30	0.98	0.94	0.75	1.10	1.02
71.12×6.30 - 88.90×6.30	0.98	0.94	0.74	1.10	0.98
80.01×6.30 - 88.90×6.30	0.98	0.90	0.72	1.10	0.97
88.90×6.30 - 88.90×6.30	1.08	0.90	0.72	1.21	1.12
35.56×1.26 - 88.90×6.30#	-	-	-	-	-
35.56×1.89 - 88.90×6.30#	-	-	-	-	-
35.56×2.52 - 88.90×6.30	0.92	0.81	0.64	1.03	1.17
35.56×3.15 - 88.90×6.30	0.94	0.82	0.65	1.06	1.19
35.56×3.78 - 88.90×6.30	0.95	0.83	0.66	1.07	1.20
35.56×4.41 - 88.90×6.30	0.96	0.84	0.66	1.07	1.21
35.56×5.04 - 88.90×6.30	0.96	0.84	0.67	1.08	1.22
35.56×5.67 - 88.90×6.30	0.97	0.84	0.67	1.08	1.22
35.56×6.30 - 88.90×6.30 <sup>\$</sup>	0.97	0.85	0.67	1.09	1.23
35.56×1.78 - 88.90×1.78	0.56	0.59	0.50	0.63	0.92
35.56×1.98 - 88.90×1.98	0.60	0.62	0.53	0.67	0.96
35.56×2.22 - 88.90×2.22	0.64	0.65	0.55	0.72	0.99
35.56×2.54 - 88.90×2.54	0.69	0.69	0.57	0.77	1.04
35.56×2.96 - 88.90×2.96	0.74	0.72	0.60	0.83	1.09
35.56×3.56 - 88.90×3.56	0.80	0.76	0.63	0.90	1.14
35.56×4.45 - 88.90×4.45	0.87	0.80	0.65	0.98	1.19
35.56×6.30 - 88.90×6.30 <sup>\$</sup>	0.97	0.85	0.67	1.09	1.23
35.56×8.89 - 88.90×8.89	1.04	0.87	0.68	1.17	1.23
Mean	0.89	0.90	0.65	1.00	1.12
COV	0.163	0.123	0.106	0.163	0.093

Note: # means brace failed by local buckling; <sup>\$</sup> means identical specimens.

(b) Series B with  $d_0 = 273$  mm

Specimens	$P_{FE}/P_{CDT,n}$	$P_{FE}/P_{EC,n}$	$P_{FE}/P_W$	$P_{FE}/P_L$	$P_{FE}/P_P$
54.60×7.50 - 273.00×12.50	0.77	0.64	0.52	0.86	1.08
81.90×7.50 - 273.00×12.50	0.80	0.71	0.58	0.90	1.15
109.20×7.50 - 273.00×12.50	0.82	0.76	0.62	0.92	1.13
136.50×7.50 - 273.00×12.50	0.84	0.81	0.66	0.94	1.08
163.80×7.50 - 273.00×12.50 <sup>\$</sup>	0.85	0.86	0.70	0.95	1.02
191.10×7.50 - 273.00×12.50	0.87	0.88	0.72	0.97	0.98
218.40×7.50 - 273.00×12.50	0.88	0.90	0.73	0.99	0.96
245.70×7.50 - 273.00×12.50	0.91	0.89	0.73	1.02	0.99
273.00×7.50 - 273.00×12.50	1.08	0.96	0.78	1.21	1.22
163.80×2.50 - 273.00×12.50#	-	-	-	-	-
163.80×3.75 - 273.00×12.50	0.81	0.81	0.66	0.91	0.98
163.80×5.00 - 273.00×12.50	0.83	0.84	0.68	0.93	1.00
163.80×6.25 - 273.00×12.50	0.84	0.85	0.69	0.95	1.02
163.80×7.50 - 273.00×12.50 <sup>\$</sup>	0.85	0.86	0.70	0.95	1.02
163.80×8.75 - 273.00×12.50	0.86	0.86	0.70	0.96	1.03
163.80×10.00 - 273.00×12.50	0.86	0.87	0.71	0.97	1.04
163.80×11.25 - 273.00×12.50	0.87	0.87	0.71	0.97	1.04
163.80×12.50 - 273.00×12.50	0.87	0.88	0.71	0.98	1.05
163.80×3.28 - 273.00×5.46	0.60	0.68	0.57	0.67	0.85
163.80×3.64 - 273.00×6.07	0.63	0.70	0.59	0.70	0.87
163.80×4.10 - 273.00×6.83	0.67	0.73	0.61	0.75	0.90
163.80×4.68 - 273.00×7.80	0.71	0.76	0.63	0.79	0.94
163.80×5.46 - 273.00×9.10	0.76	0.80	0.66	0.85	0.97
163.80×6.55 - 273.00×10.92	0.81	0.83	0.68	0.91	1.00
163.80×7.50 - 273.00×12.50 <sup>\$</sup>	0.85	0.86	0.70	0.95	1.02
163.80×10.92 - 273.00×18.20	0.94	0.89	0.71	1.05	1.05
163.80×16.38 - 273.00×27.30	1.00	0.89	0.70	1.12	1.02
Mean	0.83	0.91	0.67	0.93	1.02
COV	0.130	0.099	0.090	0.130	0.083

Note: # means brace failed by local buckling; <sup>\$</sup> means identical specimens.

(c) Series C with  $d_0 = 508$  mm

Specimens	$P_{FE}/P_{CDT,n}$	$P_{FE}/P_{EC,n}$	$P_{FE}/P_W$	$P_{FE}/P_L$	$P_{FE}/P_P$
101.60×5.00 - 508.00×12.50	0.56	0.51	0.43	0.63	0.89
152.40×5.00 - 508.00×12.50	0.58	0.56	0.47	0.65	0.94
203.20×5.00 - 508.00×12.50	0.60	0.61	0.52	0.67	0.94
254.00×5.00 - 508.00×12.50	0.62	0.66	0.56	0.70	0.91
304.80×5.00 - 508.00×12.50	0.65	0.71	0.60	0.72	0.88
355.60×5.00 - 508.00×12.50	0.68	0.76	0.64	0.76	0.87
406.40×5.00 - 508.00×12.50 <sup>\$</sup>	0.72	0.80	0.67	0.81	0.89
457.20×5.00 - 508.00×12.50	0.77	0.83	0.70	0.87	0.95
508.00×5.00 - 508.00×12.50#	-	-	-	-	-
406.40×2.50 - 508.00×12.50#	-	-	-	-	-
406.40×3.75 - 508.00×12.50	0.71	0.80	0.67	0.80	0.88
406.40×5.00 - 508.00×12.50 <sup>\$</sup>	0.72	0.80	0.67	0.81	0.89
406.40×6.25 - 508.00×12.50	0.73	0.81	0.68	0.81	0.90
406.40×7.50 - 508.00×12.50	0.73	0.82	0.69	0.82	0.90
406.40×8.75 - 508.00×12.50	0.74	0.82	0.69	0.83	0.91
406.40×10.00 - 508.00×12.50	0.74	0.83	0.70	0.83	0.92
406.40×11.25 - 508.00×12.50	0.75	0.83	0.70	0.84	0.92
406.40×12.50 - 508.00×12.50	0.75	0.84	0.70	0.84	0.92
406.40×4.06 - 508.00×10.16	0.66	0.76	0.65	0.74	0.85
406.40×4.52 - 508.00×11.29	0.69	0.79	0.66	0.78	0.87
406.40×5.00 - 508.00×12.50 <sup>\$</sup>	0.72	0.80	0.67	0.81	0.89
406.40×5.81 - 508.00×14.51	0.76	0.83	0.69	0.85	0.91
406.40×6.77 - 508.00×16.93	0.80	0.85	0.70	0.89	0.93
406.40×8.13 - 508.00×20.32	0.84	0.87	0.71	0.94	0.94
406.40×10.16 - 508.00×25.40	0.88	0.89	0.72	0.99	0.94
406.40×13.55 - 508.00×33.87	0.90	0.86	0.69	1.01	0.91
406.40×20.32 - 508.00×50.80#	-	-	-	-	-
Mean	0.72	0.86	0.65	0.81	0.91
COV	0.123	0.130	0.125	0.123	0.030

Note: # means brace failed by local buckling; <sup>\$</sup> means identical specimens.



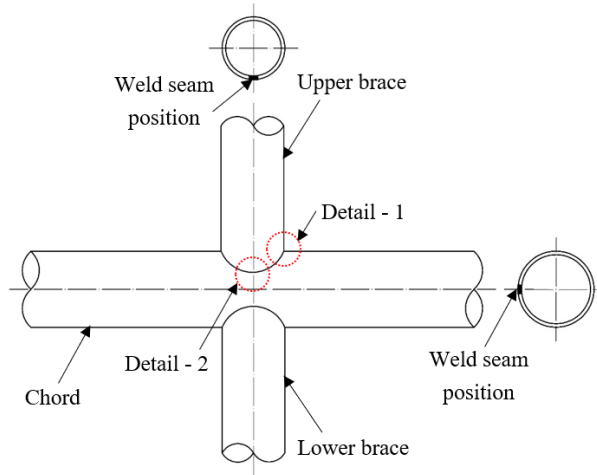
**Table 11:** Strength comparisons between test results of X-joints in literature and predictions

Specimens	$f_{0.2}$ (MPa)	$f_u$ (MPa)	$P_t/P_{CDT,n}$	$P_t/P_{EC,n}$	$P_t/P_W$	$P_t/P_L$	$P_t/P_P$
R32 <sup>a</sup>	730	800	1.23	1.15	0.95	1.11	1.45
R33 <sup>a</sup>	739	798	1.10	0.97	0.79	0.98	1.21
R42 <sup>a</sup>	727	793	1.18	0.98	0.81	1.06	1.25
R68 <sup>a</sup>	904	946	1.06	0.93	0.76	0.97	1.08
R69 <sup>a</sup>	858	879	1.18	0.93	0.76	1.04	1.38
R70 <sup>a</sup>	847	892	1.08	0.95	0.77	0.97	1.00
R71 <sup>a</sup>	854	900	1.08	0.98	0.80	0.97	1.07
R72 <sup>a</sup>	894	937	1.03	0.89	0.73	0.94	1.14
R74 <sup>a</sup>	811	863	1.11	0.93	0.75	1.00	1.04
R75 <sup>a</sup>	811	863	1.05	0.89	0.71	0.94	0.92
X90-650-0.75-16 <sup>b</sup>	764	905	1.08	1.07	0.85	1.06	1.14
X90-650-0.62-26 <sup>b</sup>	798	914	1.03	1.05	0.86	0.99	1.24
X1 <sup>c</sup>	972	1107	0.80	0.87	0.74	0.82	1.03
X2 <sup>c</sup>	972	1107	0.76	0.85	0.73	0.78	0.96
X3 <sup>c</sup>	972	1107	0.50	0.57	0.49	0.51	0.66
X4 <sup>c</sup>	972	1107	0.74	0.83	0.71	0.76	1.04
X5 <sup>c</sup>	1012	1119	0.81	0.86	0.73	0.82	0.96
X6 <sup>c</sup>	990	1114	0.77	0.85	0.72	0.77	0.95
Total 18 tests	Mean		0.98	1.02	0.76	0.92	1.08
	COV		0.202	0.132	0.121	0.159	0.168

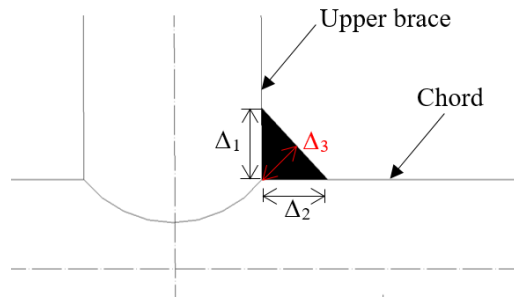
Note: <sup>a</sup>, <sup>b</sup> and <sup>c</sup> mean presented in Refs. [35], [36] and [58], respectively.

**Table 12:** Overall comparisons of test and numerical results with predictions

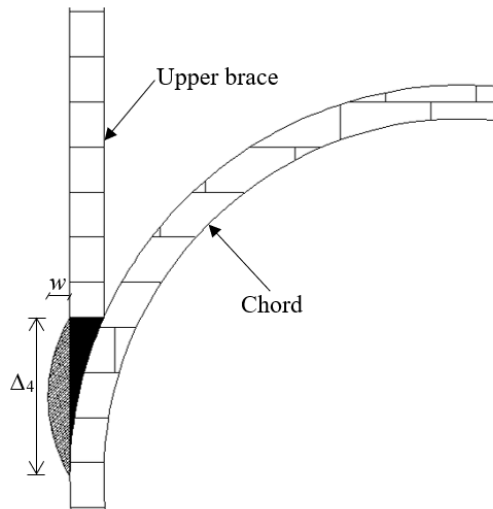
Specimens	Number		$P_t/P_{CDT,n}$ ( $P_{FE}/P_{CDT,n}$ )	$P_t/P_{EC,n}$ ( $P_{FE}/P_{EC,n}$ )	$P_t/P_W$ ( $P_{FE}/P_W$ )	$P_t/P_L$ ( $P_{FE}/P_L$ )	$P_t/P_P$ ( $P_{FE}/P_P$ )
Tests	33	Mean	0.93	0.97	0.72	0.92	1.08
		COV	0.187	0.145	0.138	0.140	0.139
Parametric studies	69	Mean	0.81	0.89	0.65	0.91	1.02
		COV	0.165	0.118	0.107	0.165	0.115
Total	102	Mean	0.85	0.92	0.68	0.92	1.04
		COV	0.185	0.134	0.127	0.156	0.127



**Fig. 1:** Schematic view of CFHSS CHS X-joint



(a) Welding "Detail 1"

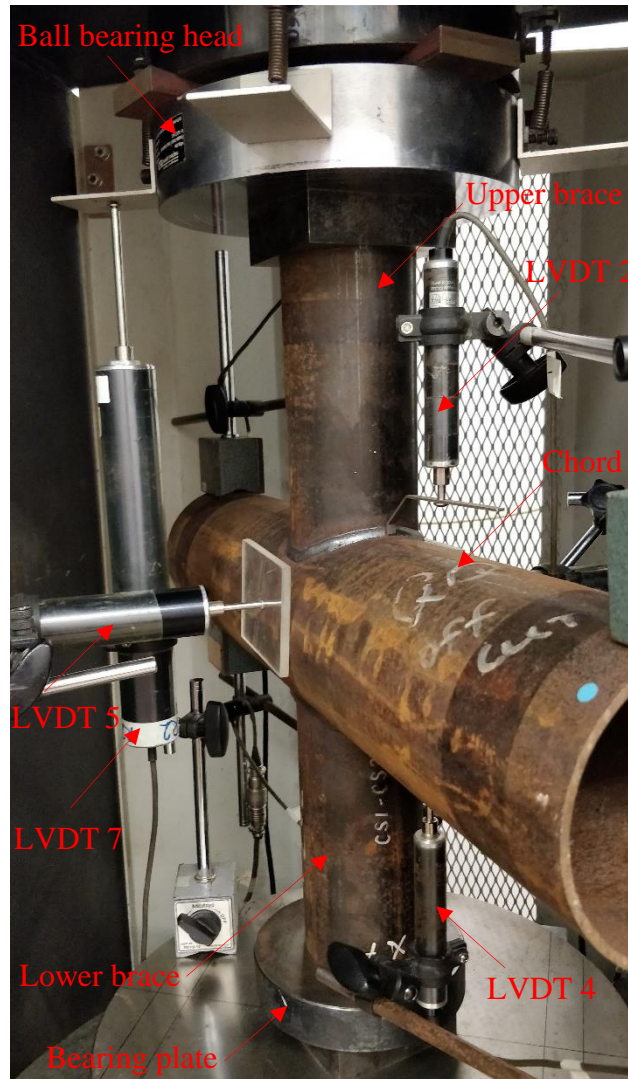


(b) Side view of welding "Detail 2" for specimens with  $\beta = 1.00$

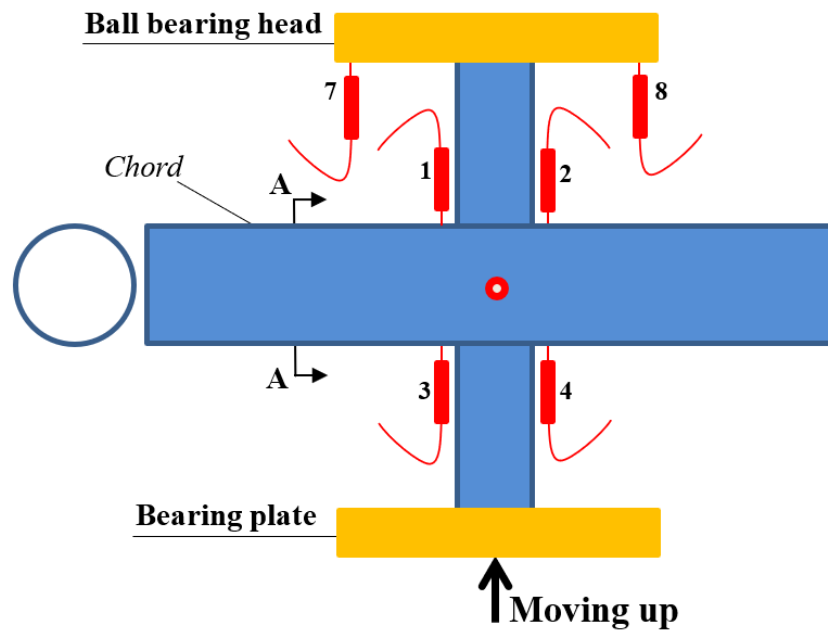
**Fig. 2:** Welding details of CFHSS CHS X-joint



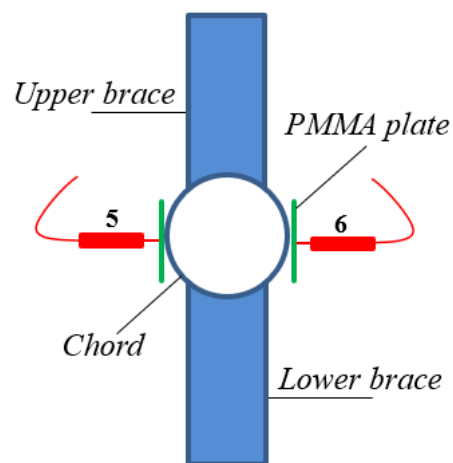
**Fig. 3:** Measurement of welding details  $\Delta_3$  at toe for specimen  $89 \times 4^* - 89 \times 4^*$



**Fig. 4:** Photo of setup for CFHSS CHS X-joint specimen 89×4\* - 108×4

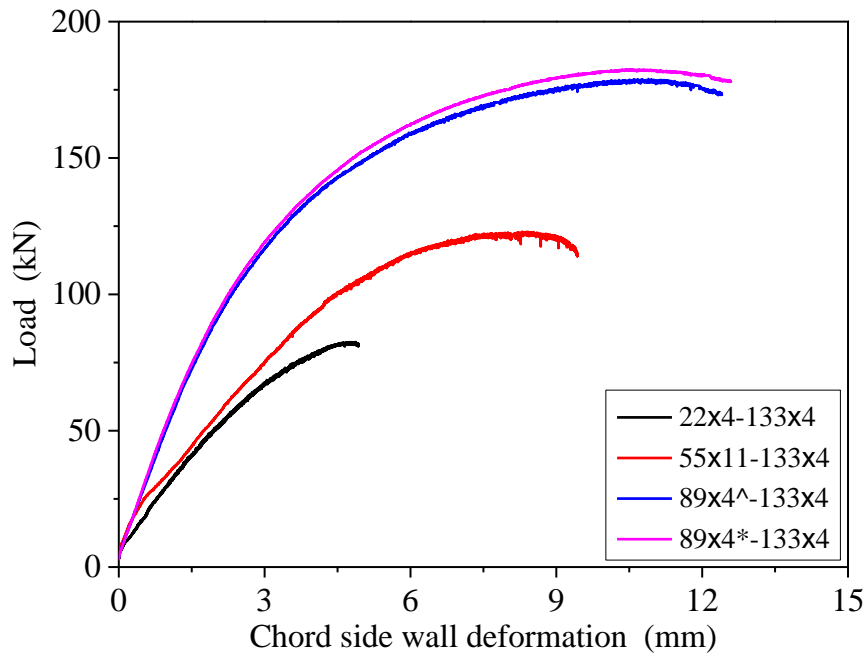


(a) Elevation view of X-joint set up

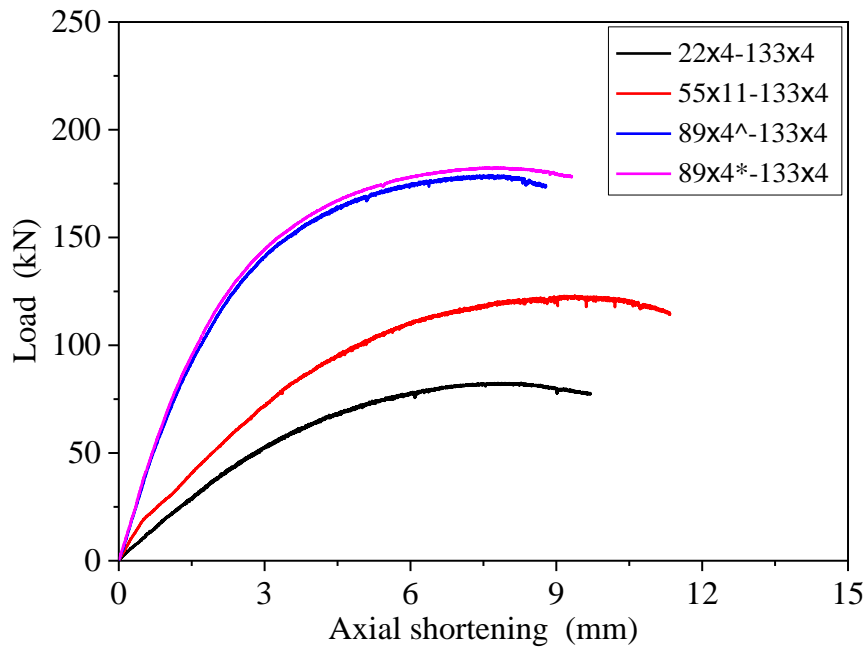


(b) Details of Section A-A

**Fig. 5:** Schematic view of test setup for CFHSS CHS X-joint

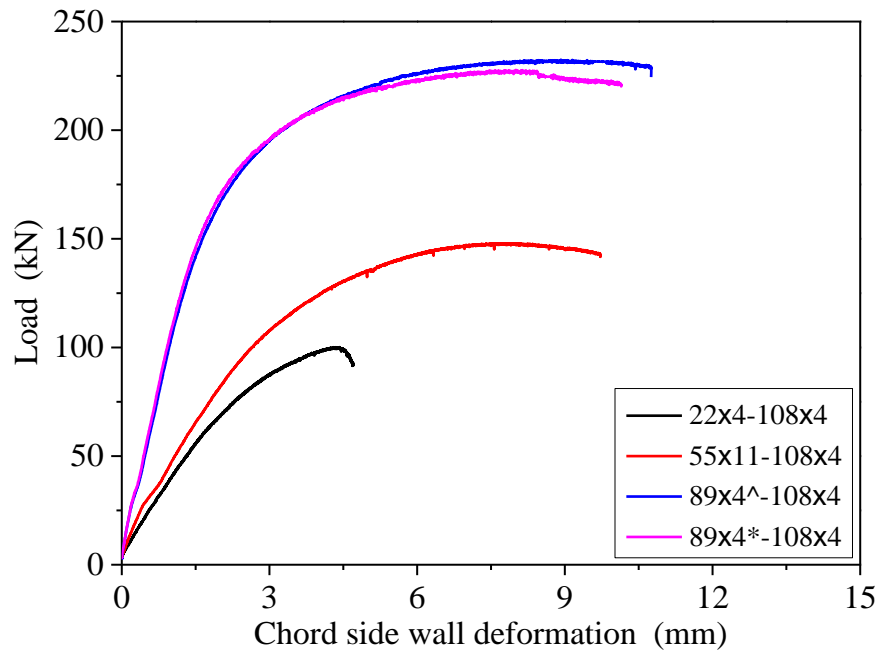


(a) Load-chord side wall deformation curves

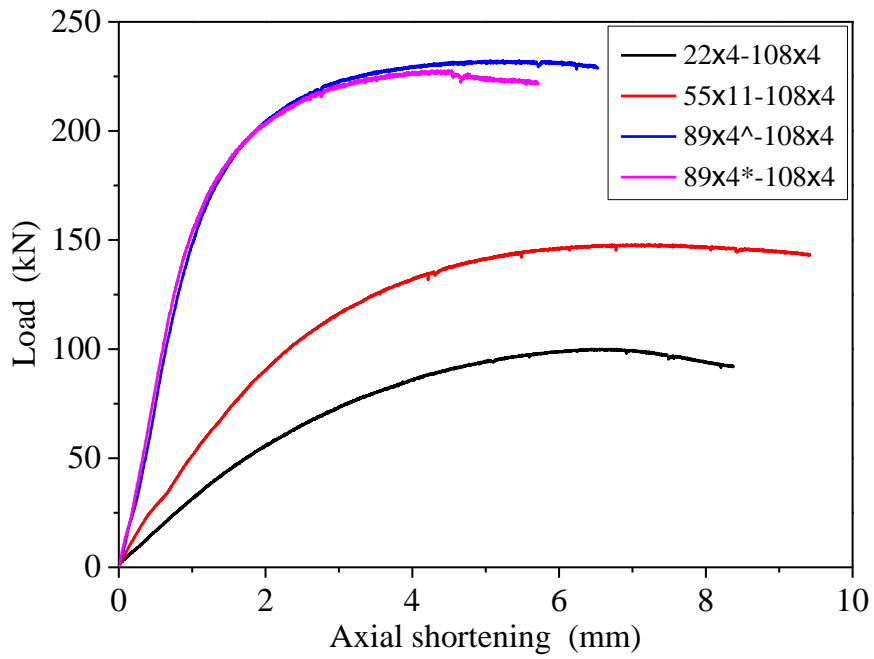


(b) Load-axial shortening curves at one side

**Fig. 6:** Test curves of X-joints with chord of 133×4 mm

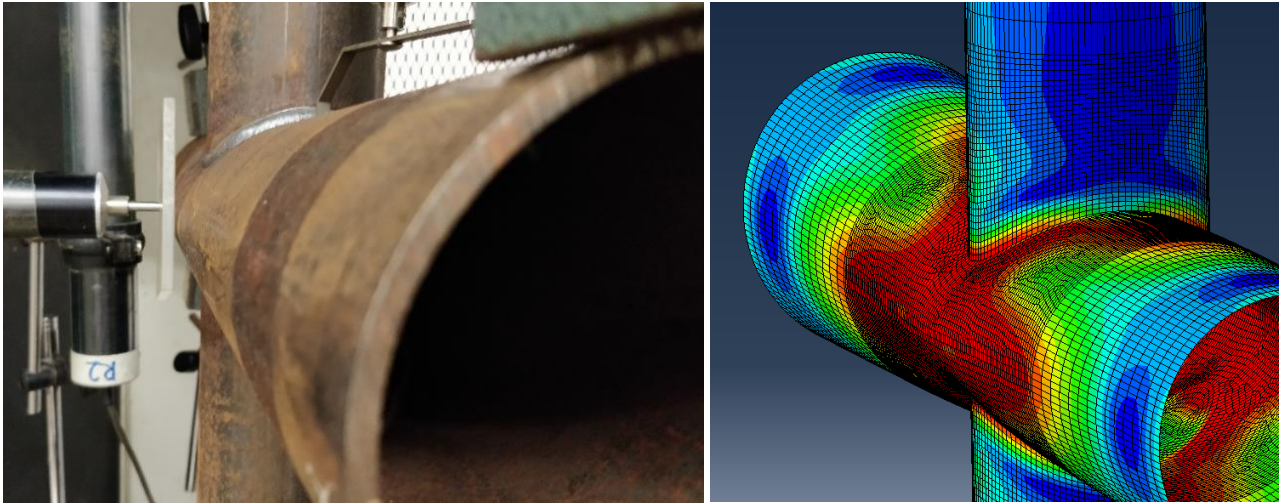


(a) Load-chord side wall deformation curves

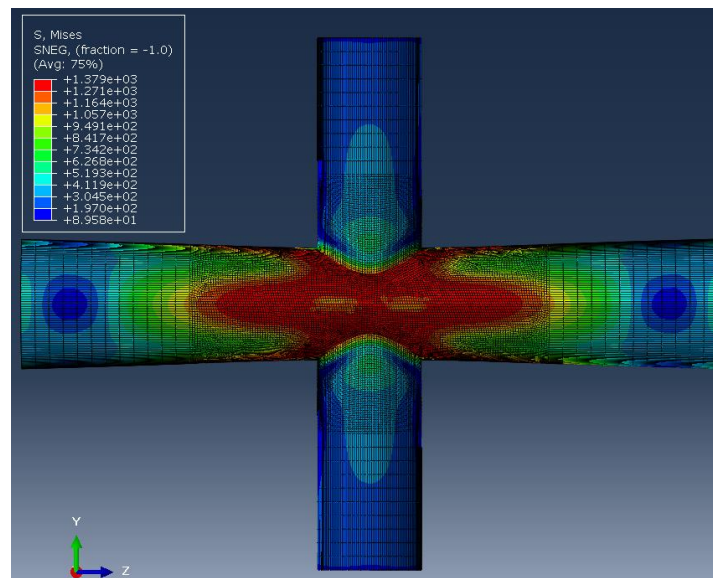


(b) Load-axial shortening curves at one side

**Fig. 7:** Test curves of X-joints with chord of 108×4 mm



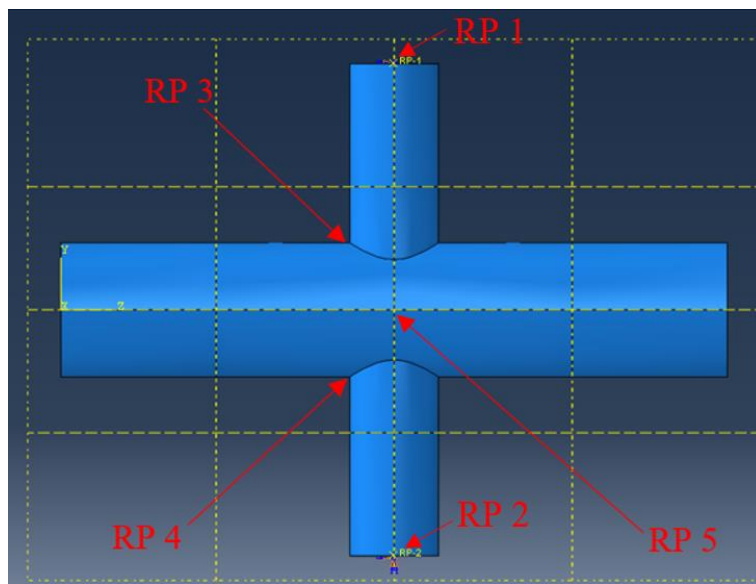
(a) Failure mode between test and FE results



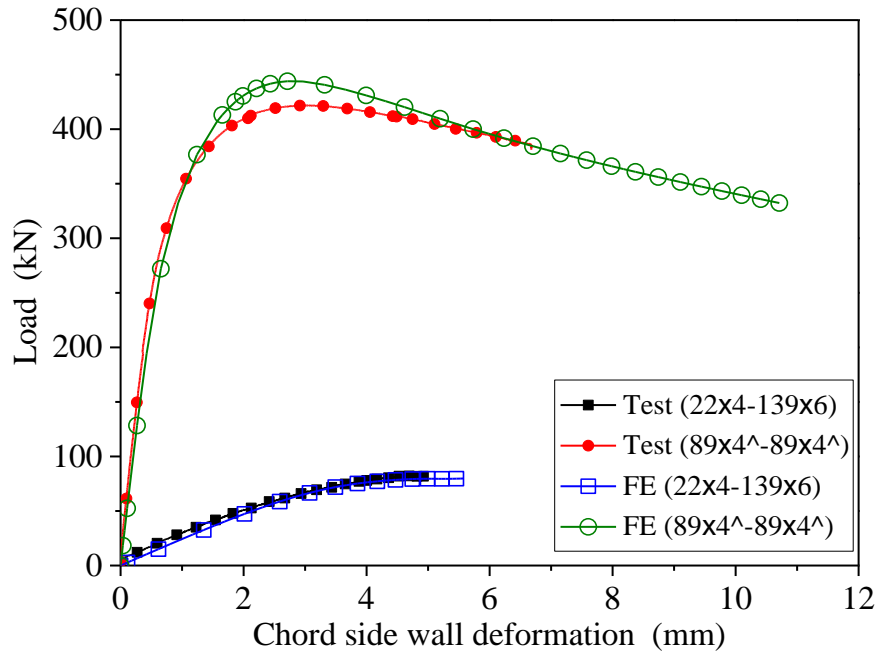
(b) Side view of FE result

**Fig. 8:** Failure mode comparison between test and FE results for specimen 89x4<sup>-</sup>-108x4

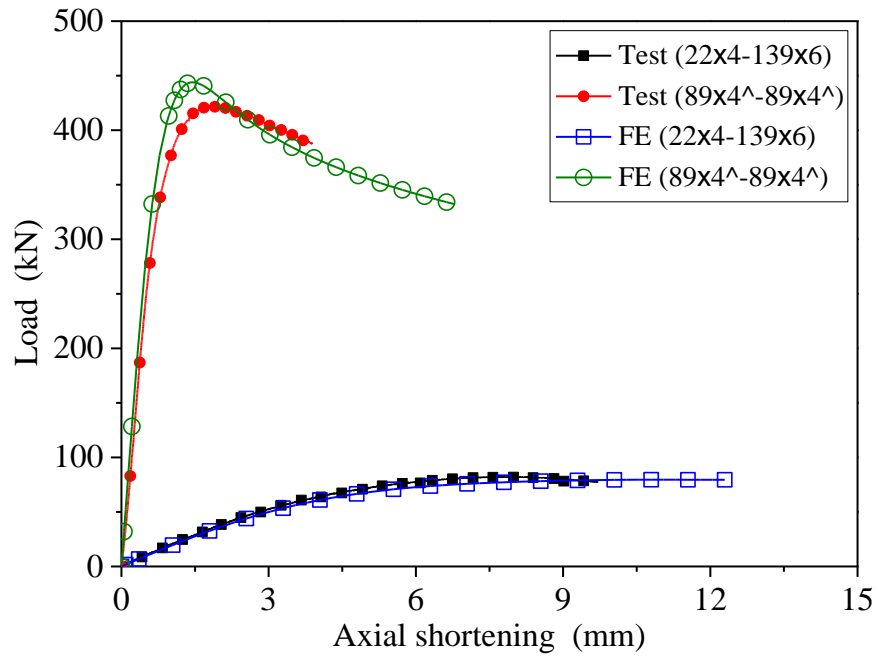




**Fig. 9:** Finite element model of CFHSS X-joint specimen 55×11 - 89×4\*

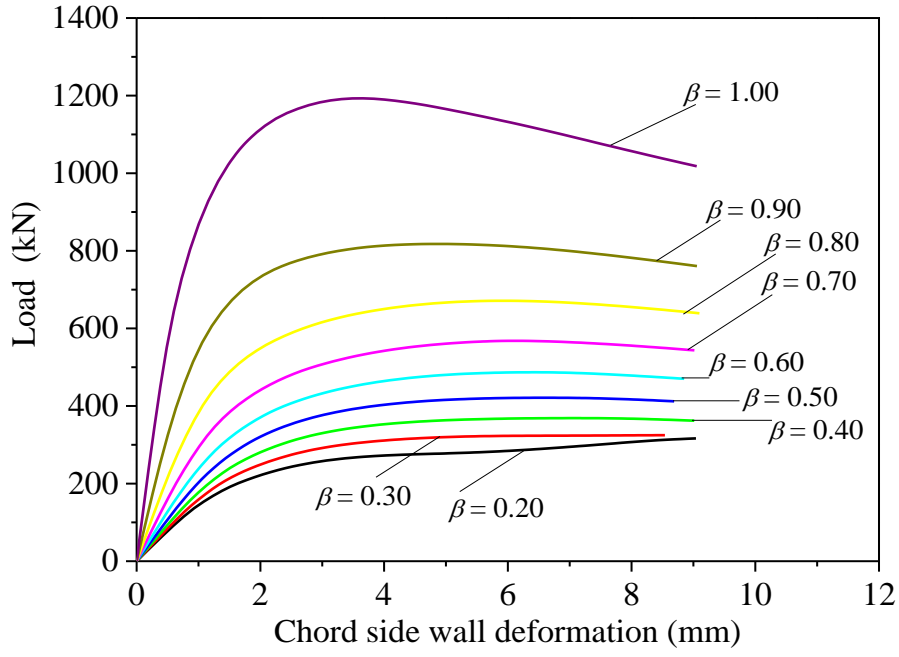


(a) Comparison of load-chord side wall deformation curves

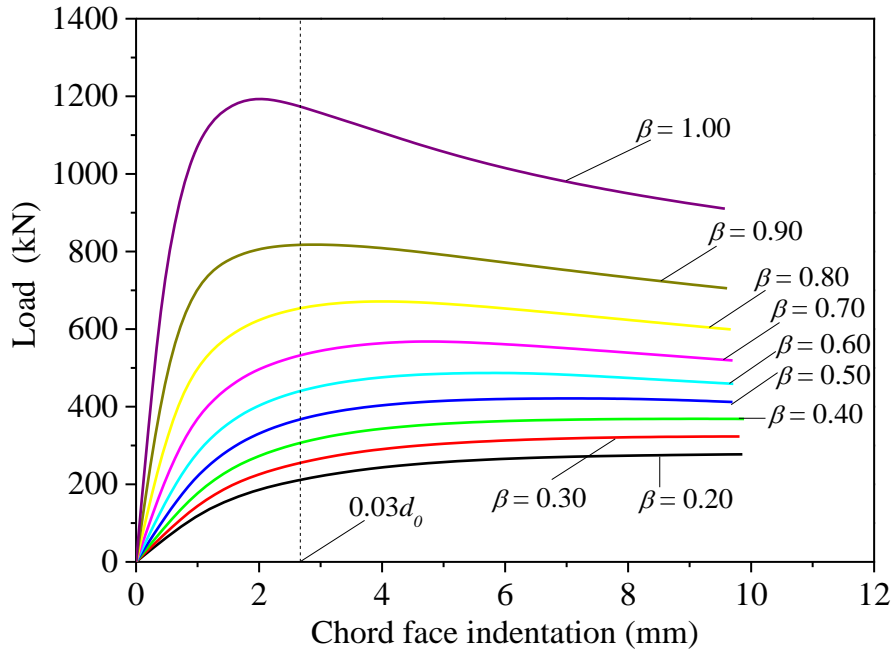


(b) Comparison of load-axial shortening curves at one side

**Fig. 10:** Comparison of load-deformation curves between test and FE results

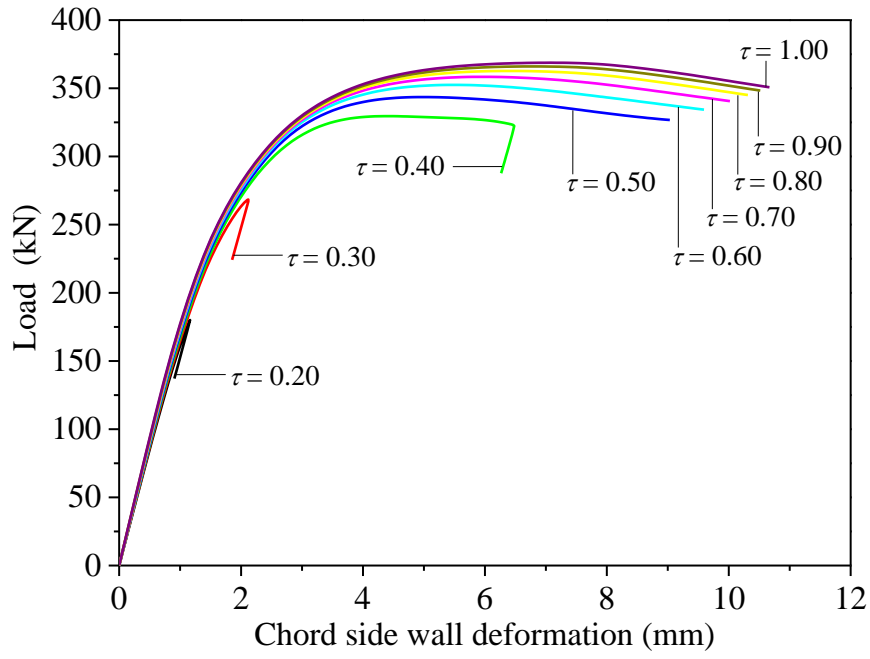


(a) Load-chord side wall deformation curves

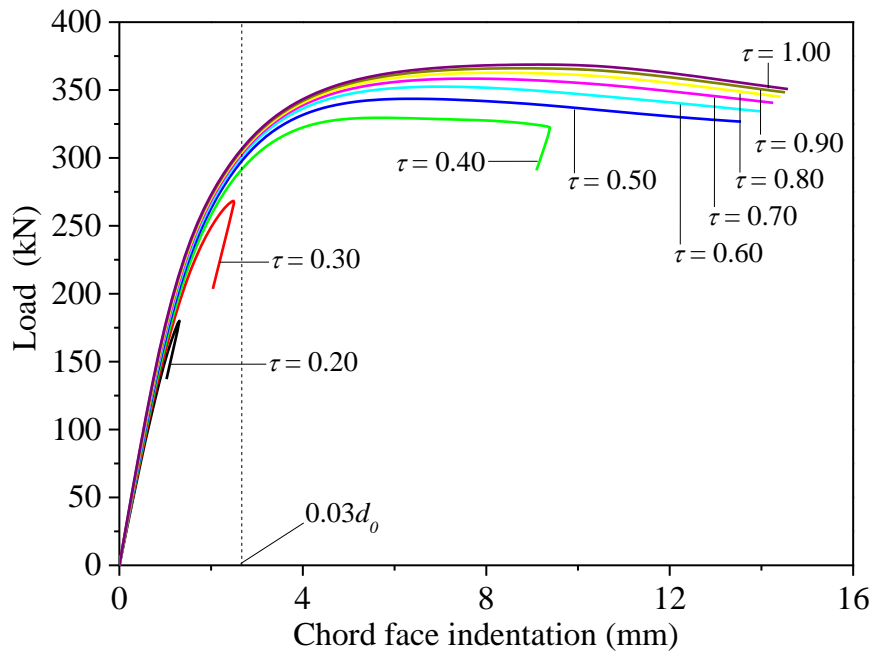


(b) Load-chord face indentation curves

**Fig. 11:** Curves of Series A with  $\tau = 1.00$  and  $2\gamma = 14.11$

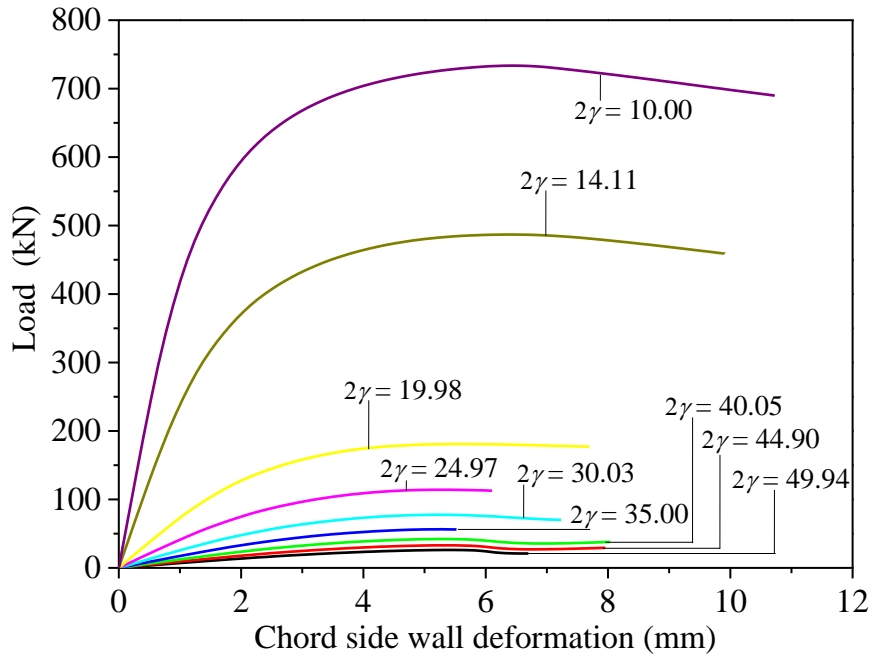


(a) Load-chord side wall deformation curves

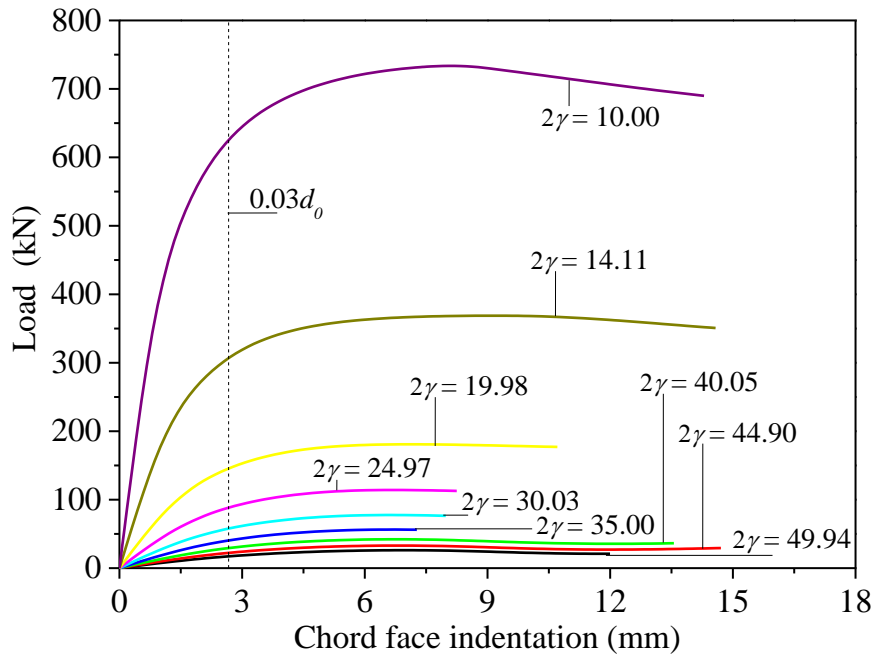


(b) Load-chord face indentation curves

**Fig. 12:** Curves of Series A with  $\beta = 1.00$  and  $2\gamma = 14.11$

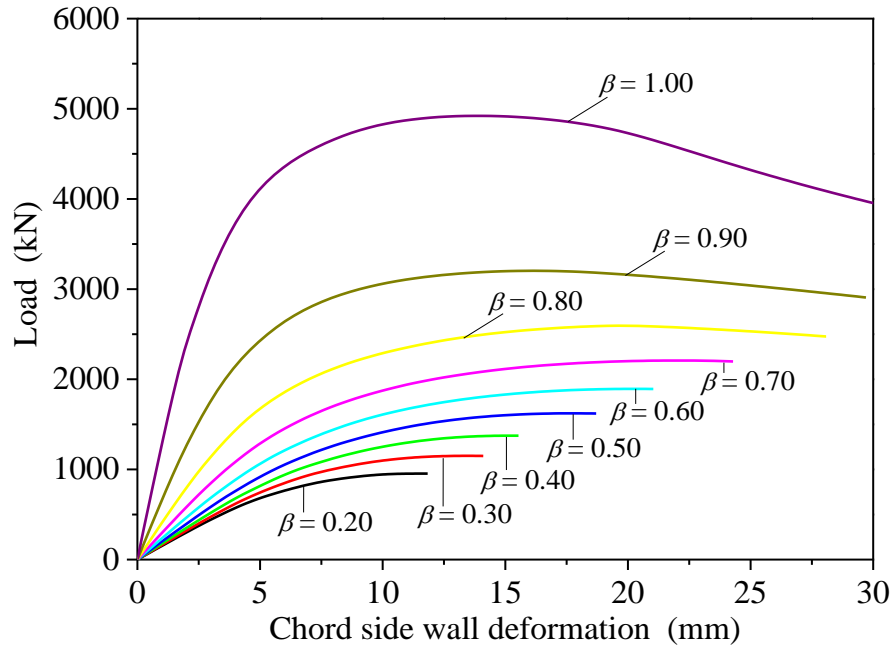


(a) Load-chord side wall deformation curves

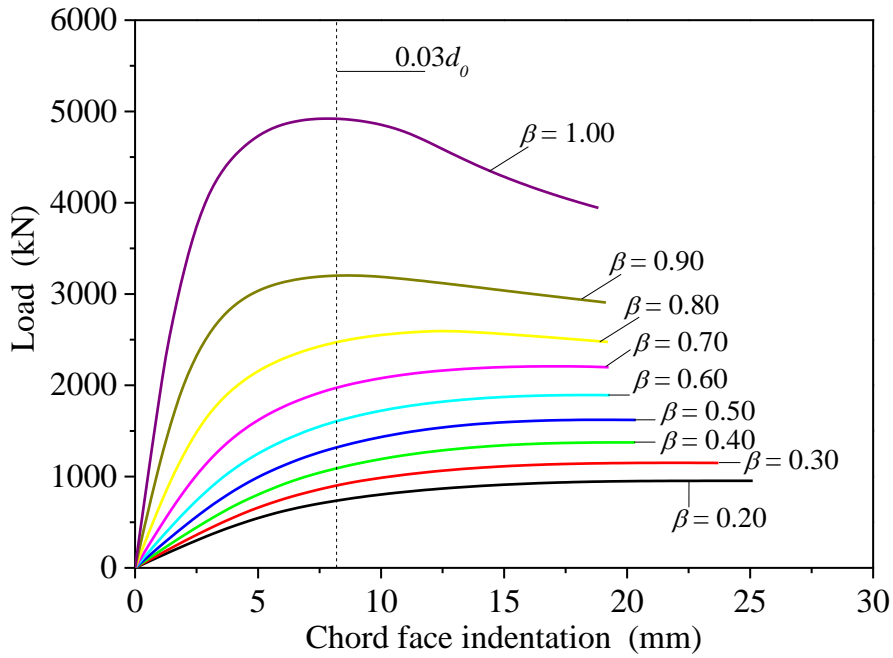


(b) Load-chord face indentation curves

**Fig. 13:** Curves of Series A with  $\beta = 1.00$  and  $\tau = 1.00$

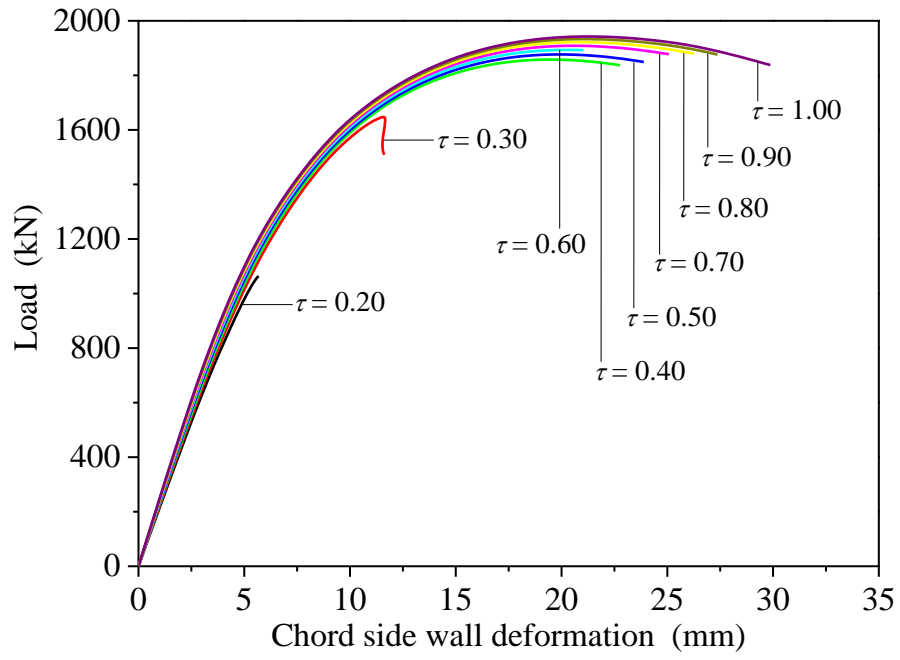


(a) Load-chord side wall deformation curves

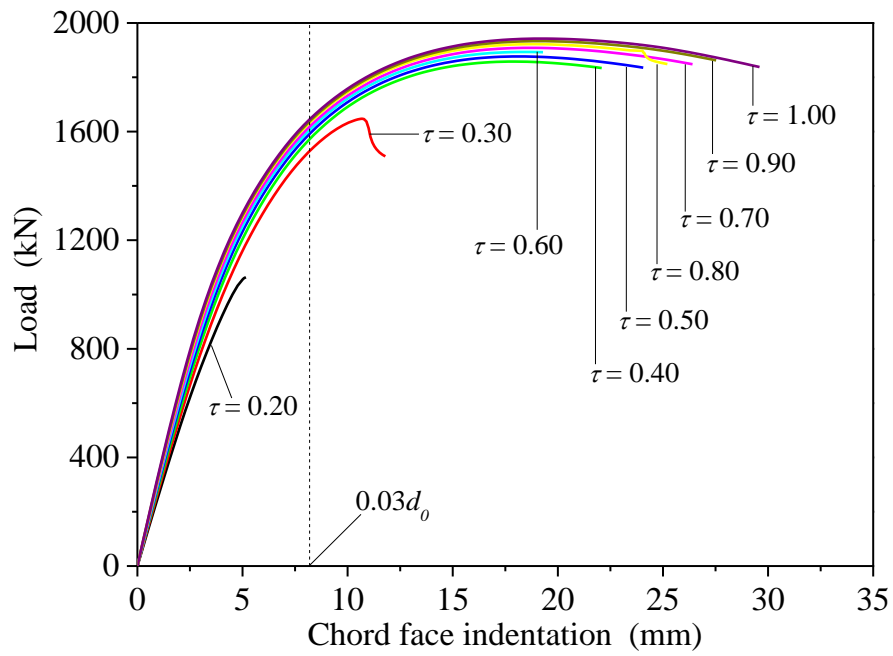


(b) Load-chord face indentation curves

**Fig. 14:** Curves of Series B with  $\tau = 0.60$  and  $2\gamma = 21.84$

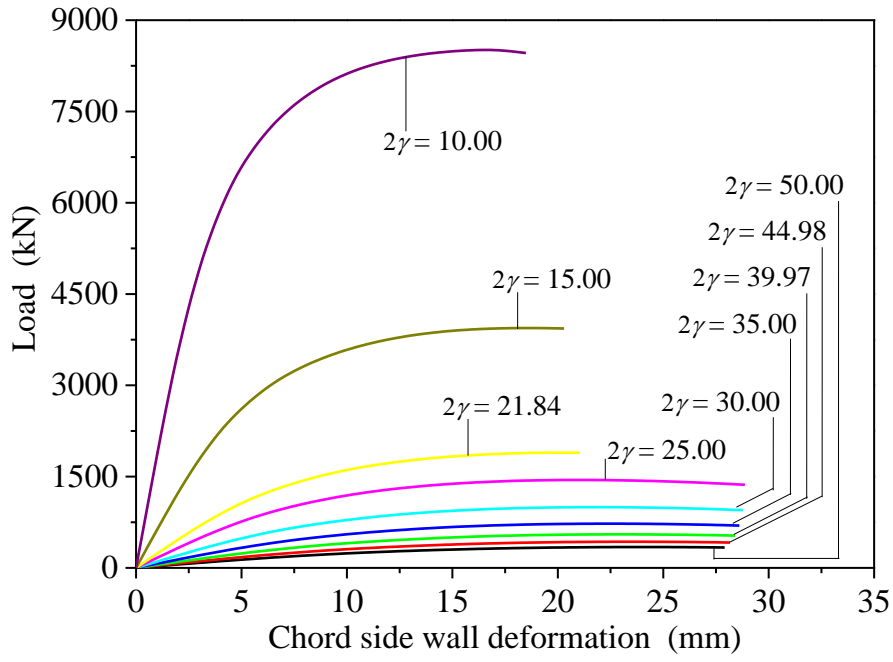


(a) Load-chord side wall deformation curves

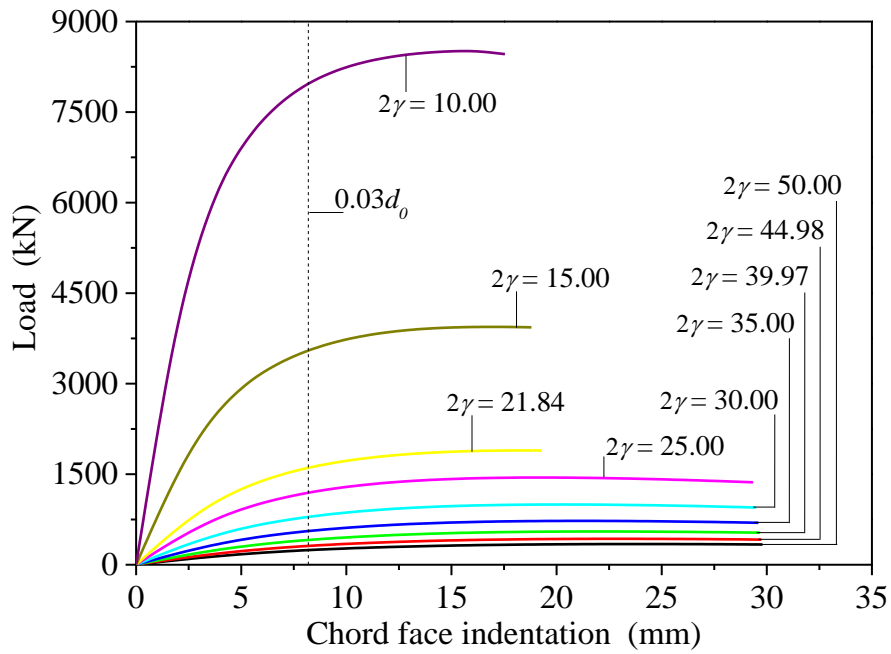


(b) Load-chord face indentation curves

**Fig. 15:** Curves of Series B with  $\beta = 0.60$  and  $2\gamma = 21.84$



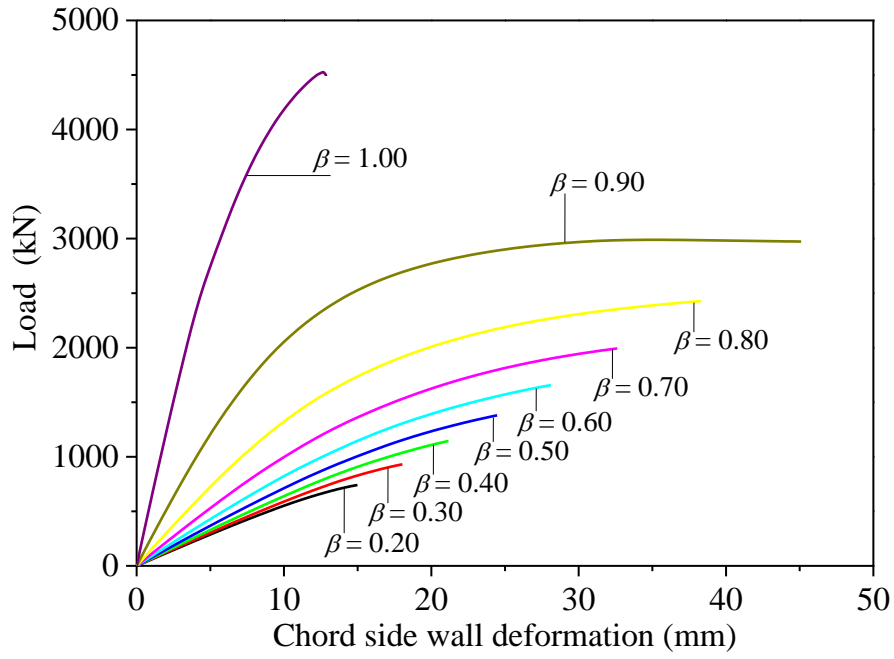
(a) Load-chord side wall deformation curves



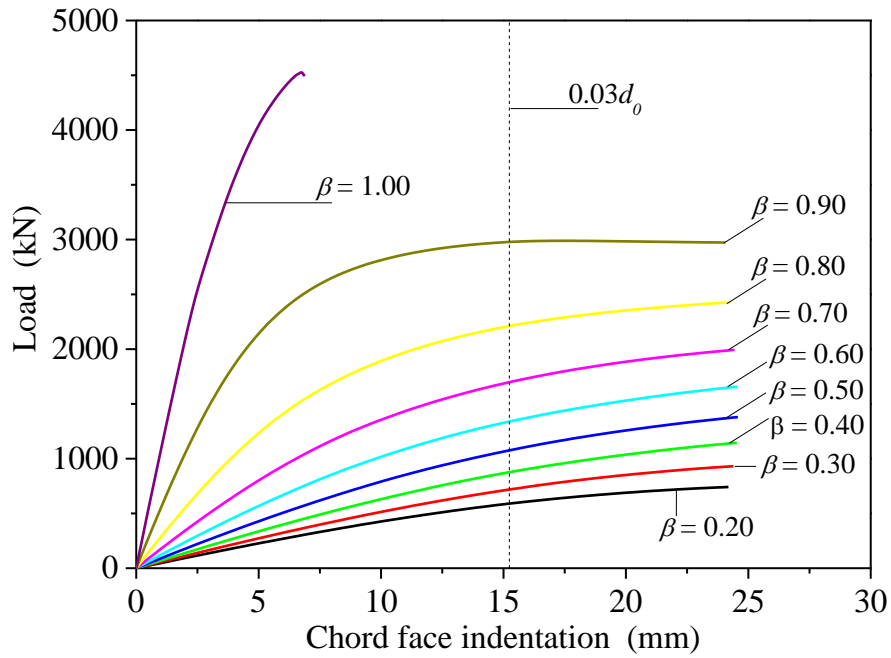
(b) Load-chord face indentation curves

**Fig. 16:** Curves of Series B with  $\beta = 0.60$  and  $\tau = 0.60$



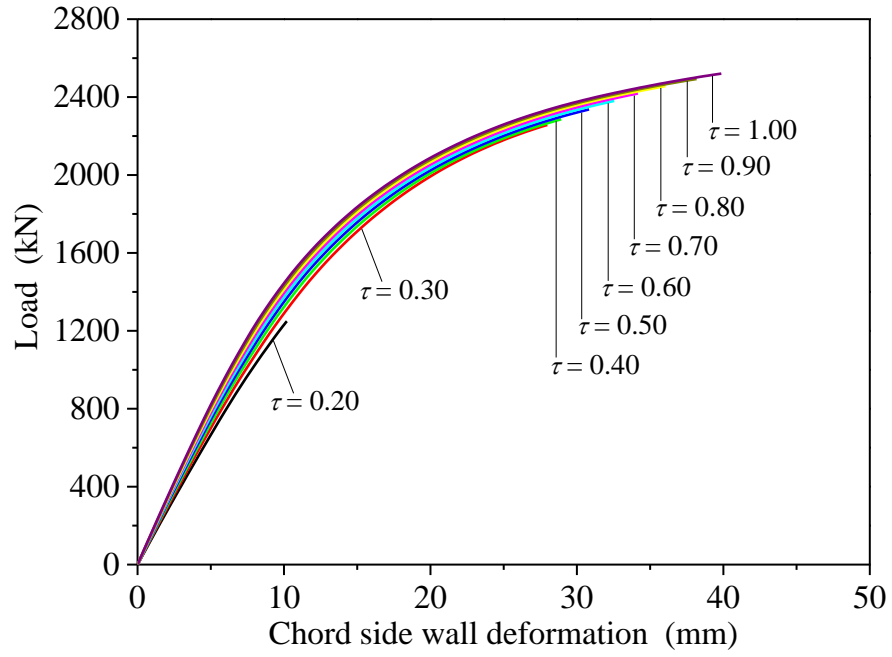


(a) Load-chord side wall deformation curves

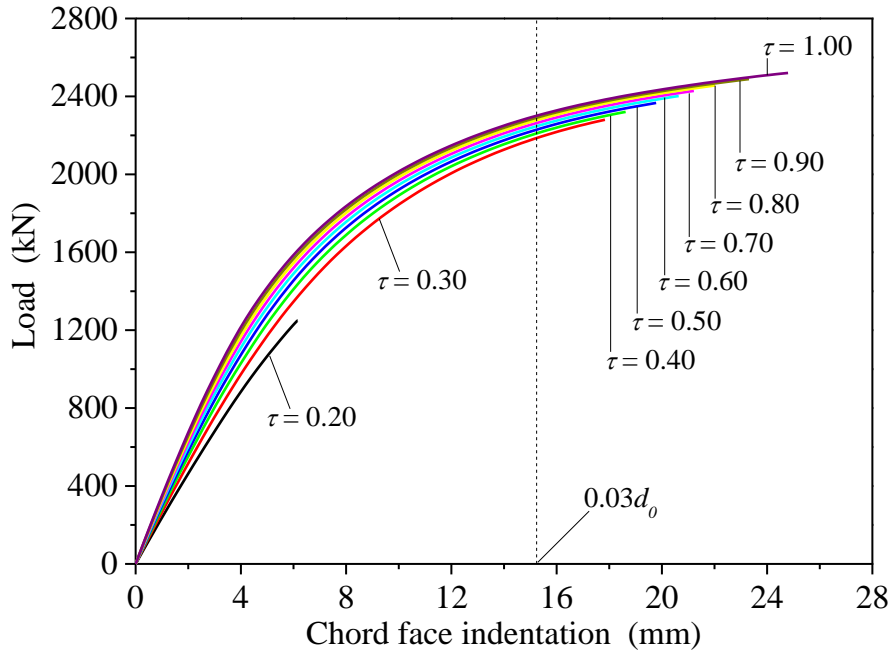


(b) Load-chord face indentation curves

**Fig. 17:** Curves of Series C with  $\tau = 0.40$  and  $2\gamma = 40.64$

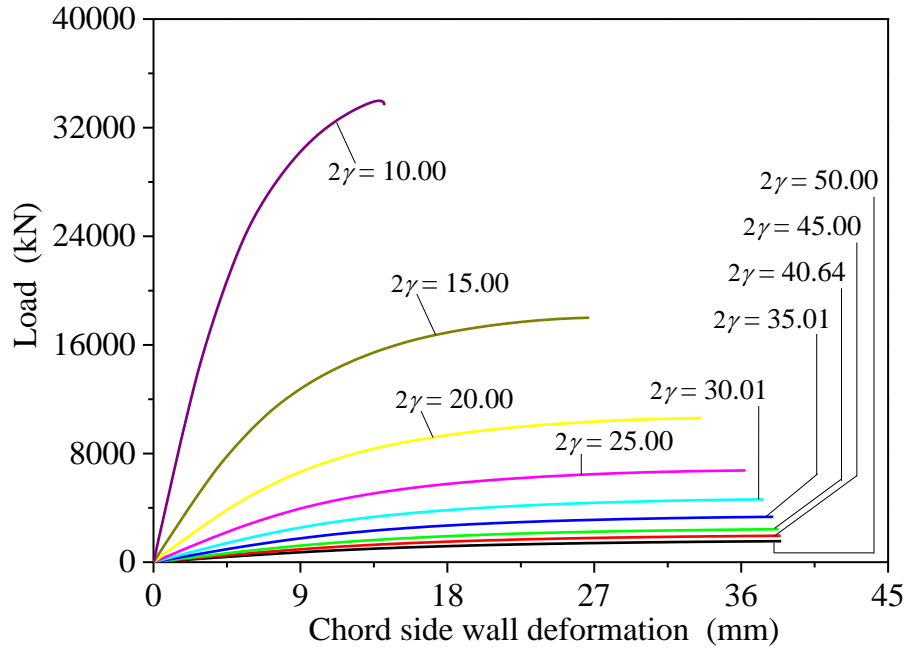


(a) Load-chord side wall deformation curves

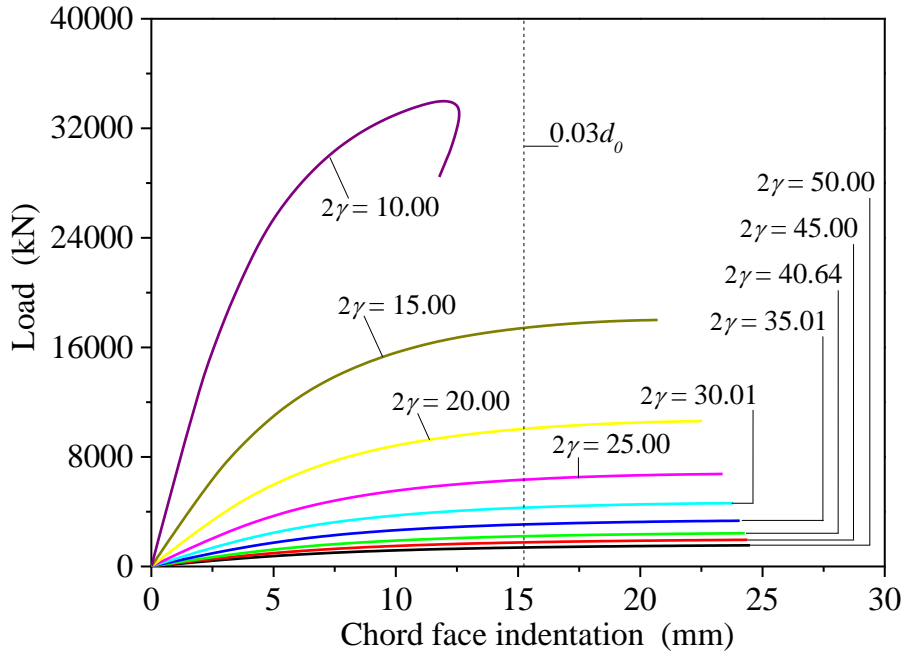


(b) Load-chord face indentation curves

**Fig. 18:** Curves of Series C with  $\beta = 0.80$  and  $2\gamma = 40.64$

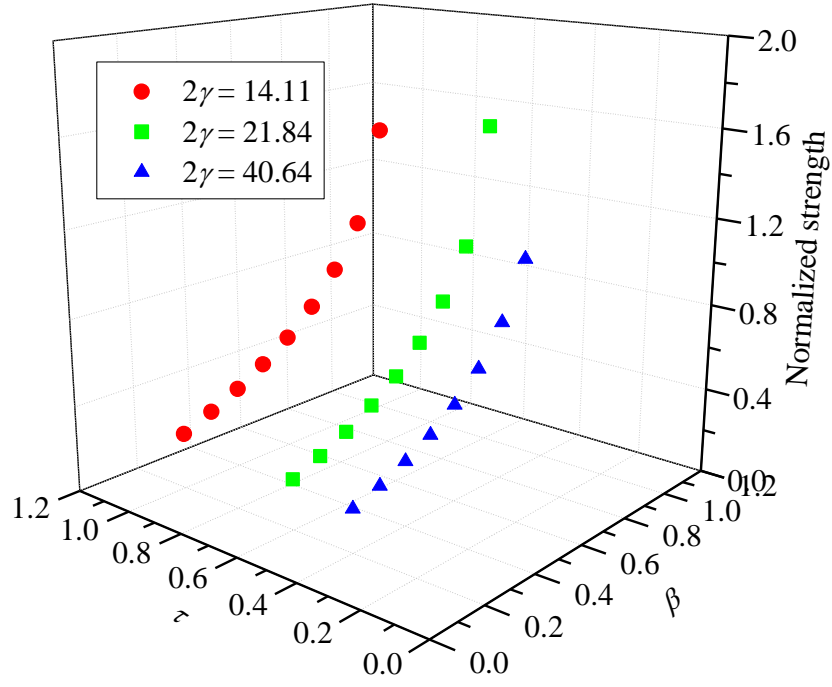


(a) Load-chord side wall deformation curves

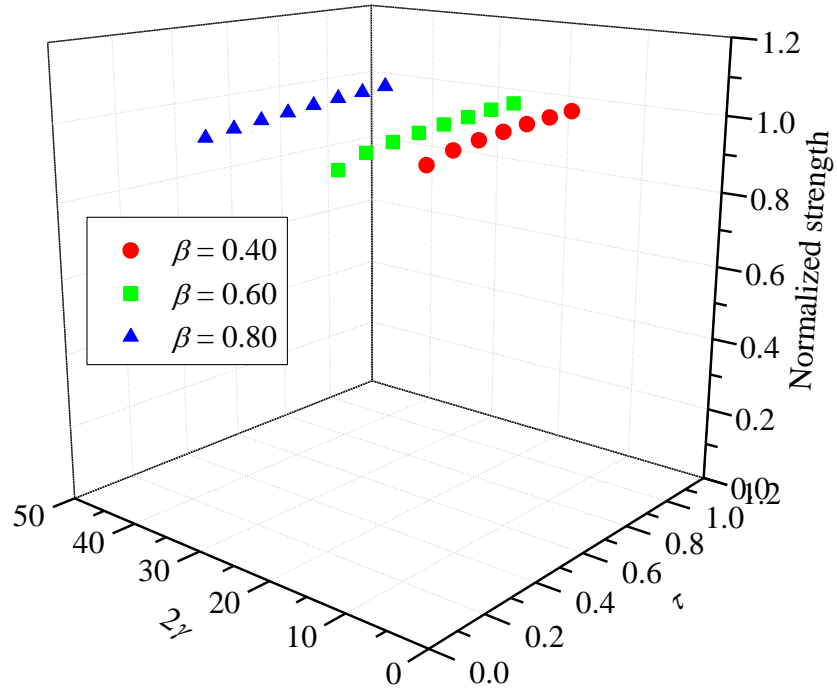


(b) Load-chord face indentation curves

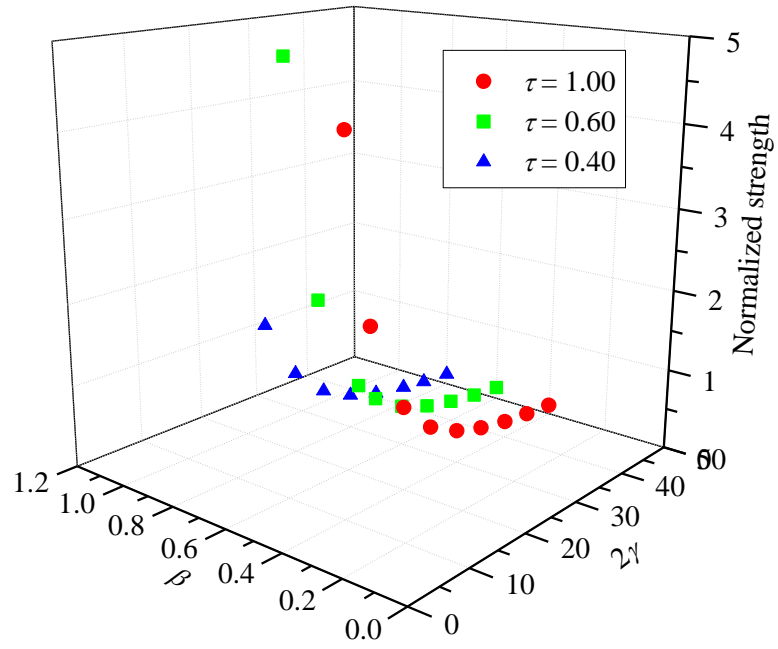
**Fig. 19:** Curves of Series C with  $\beta = 0.80$  and  $\tau = 0.40$



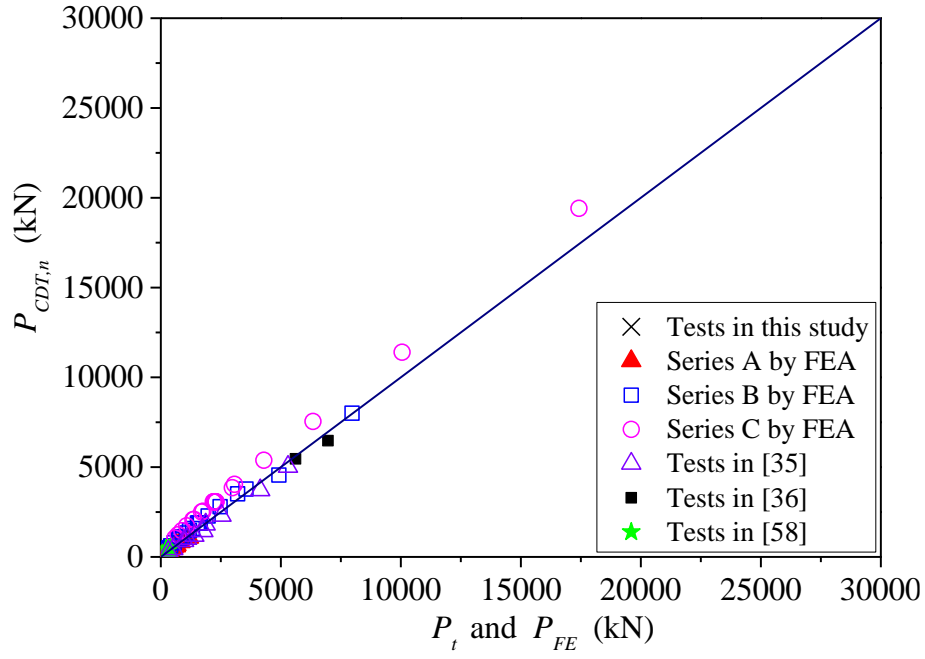
**Fig. 20:** Effects of  $\beta$  on the CFHSS circular tubular X-joint strengths



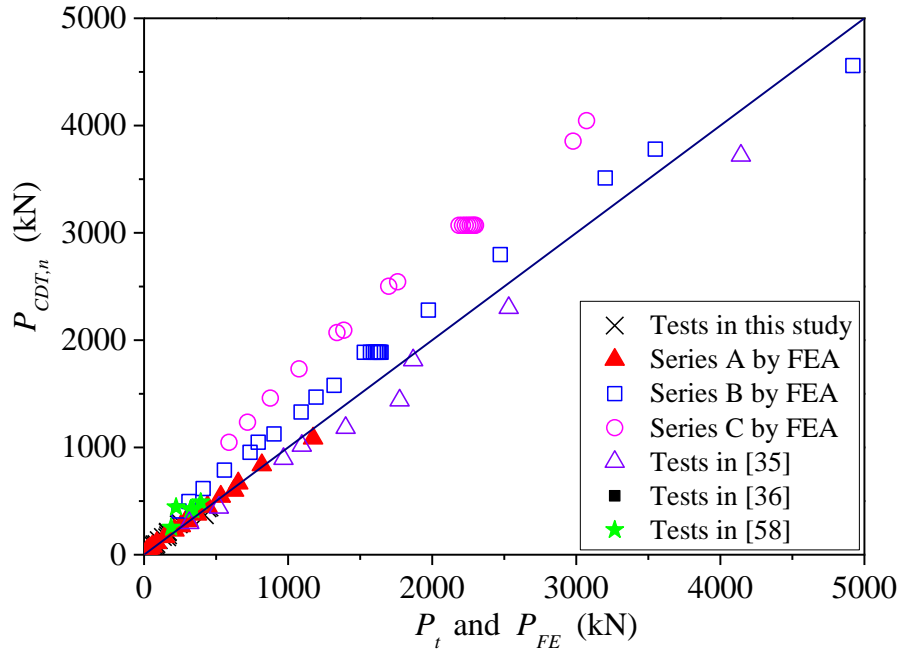
**Fig. 21:** Effects of  $\tau$  on the CFHSS CHS X-joint strengths



**Fig. 22:** Effects of  $2\gamma$  on the CFHSS CHS X-joint strengths

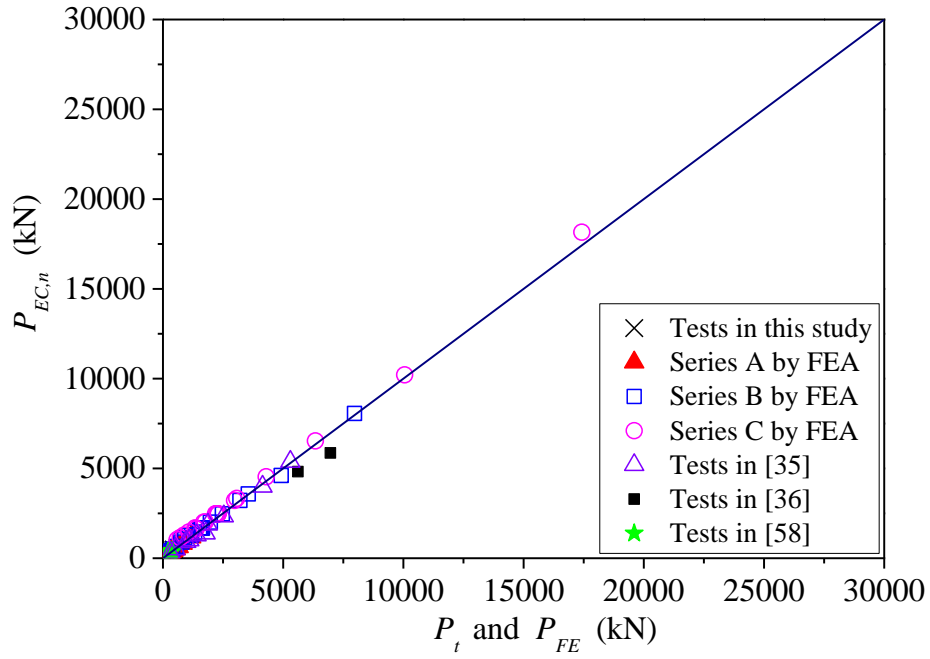


(a) Overall comparisons

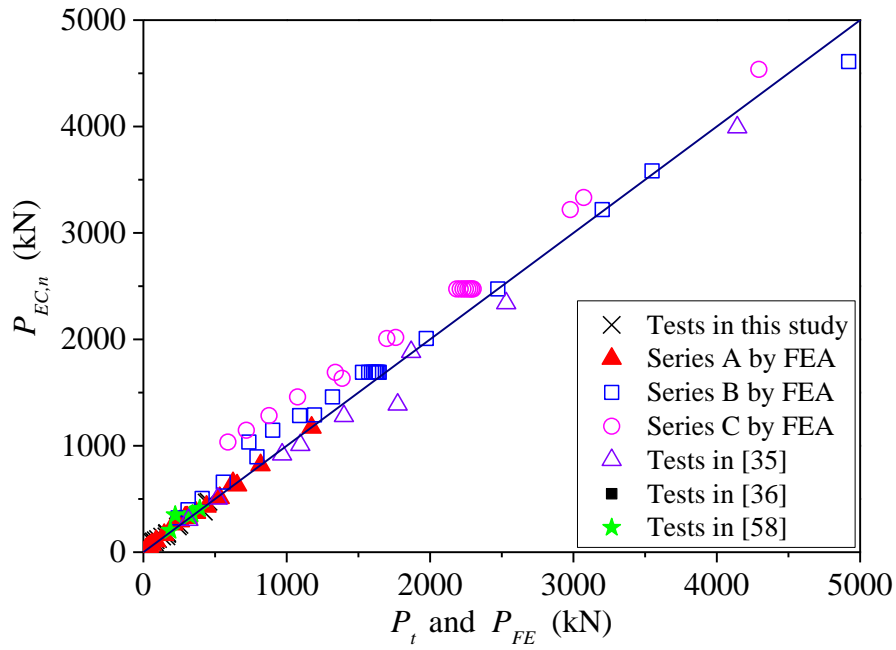


(b) Plot up to 5000 kN

**Fig. 23:** Comparison of test and FE strengths with predictions by CIDECT [52]

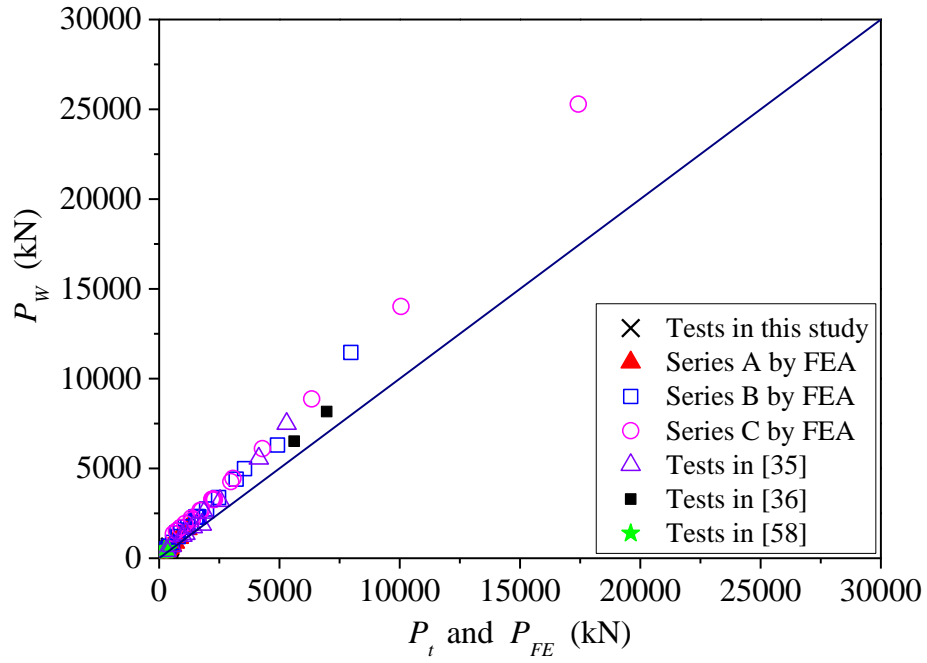


(a) Overall comparisons

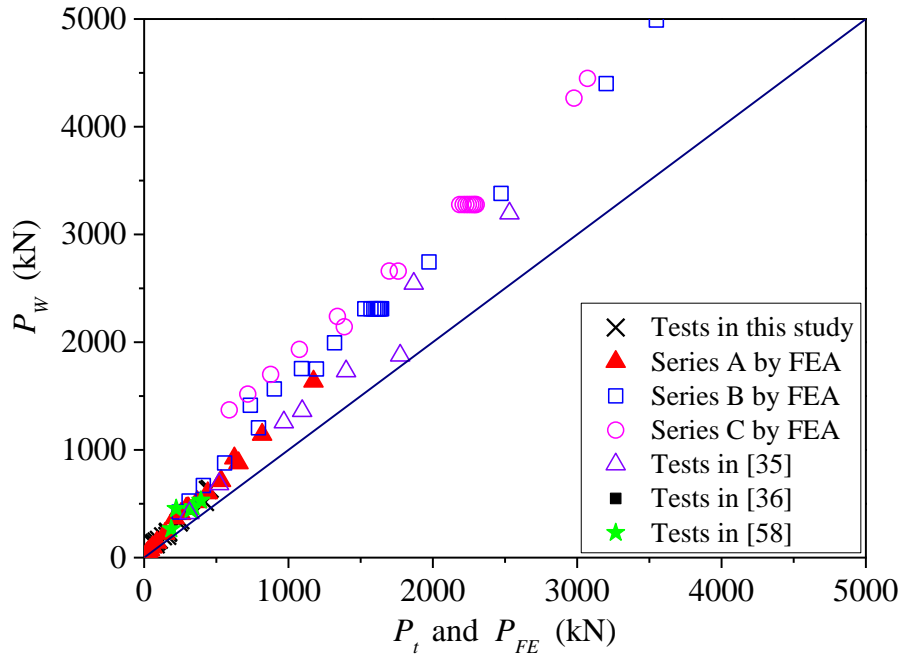


(b) Plot up to 5000 kN

**Fig. 24:** Comparison of test and FE strengths with predictions by EN-1993-1-8 [55]



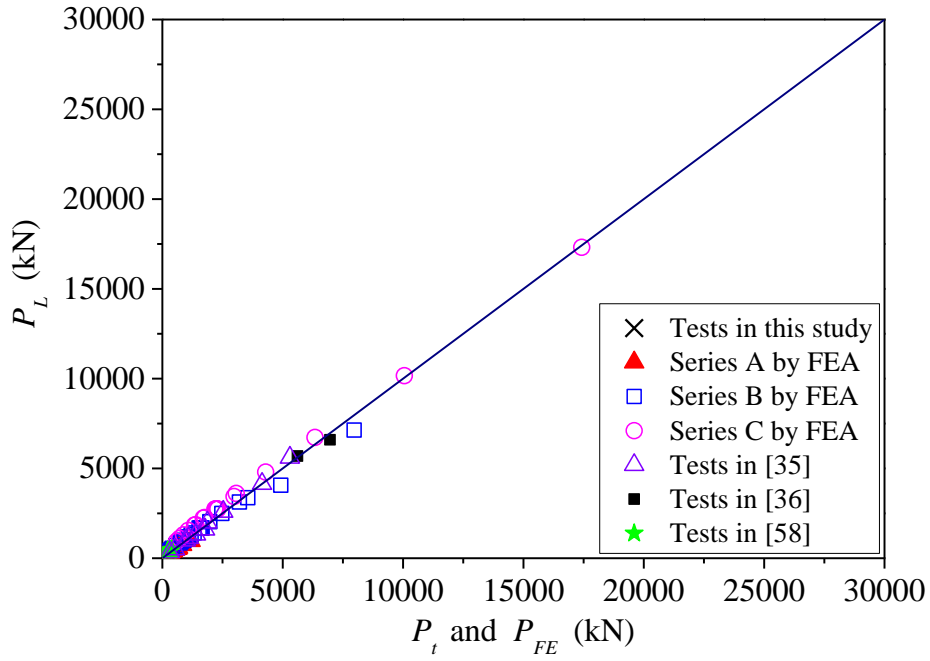
(a) Overall comparisons



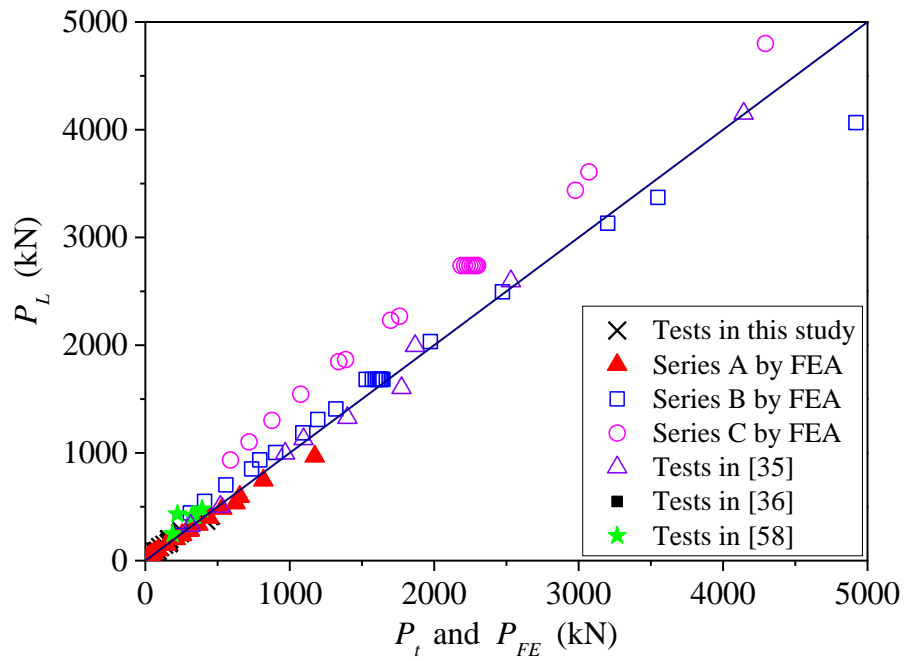
(b) Plot up to 5000 kN

**Fig. 25:** Comparison of test and FE strengths with predictions Wardenier [66]



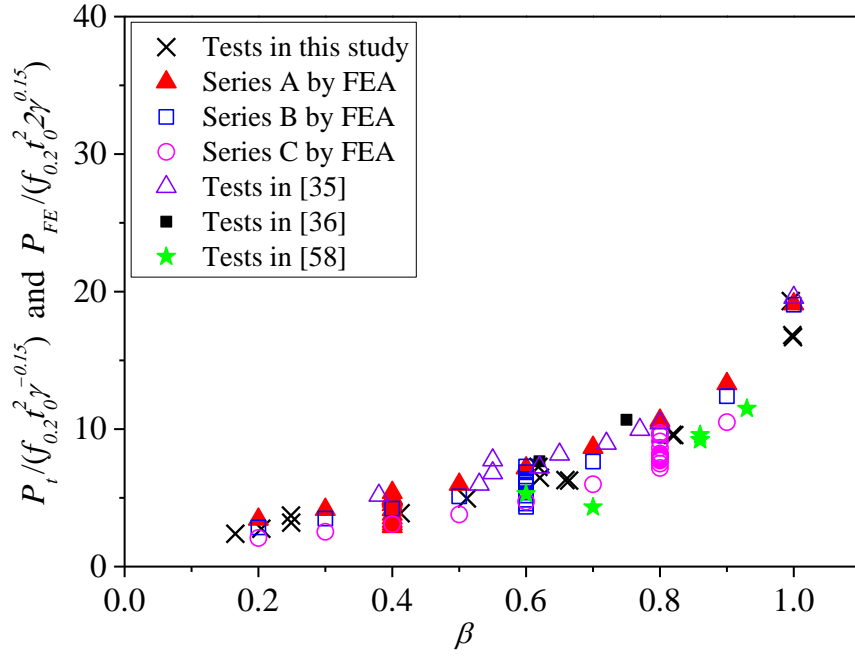


(a) Overall comparisons

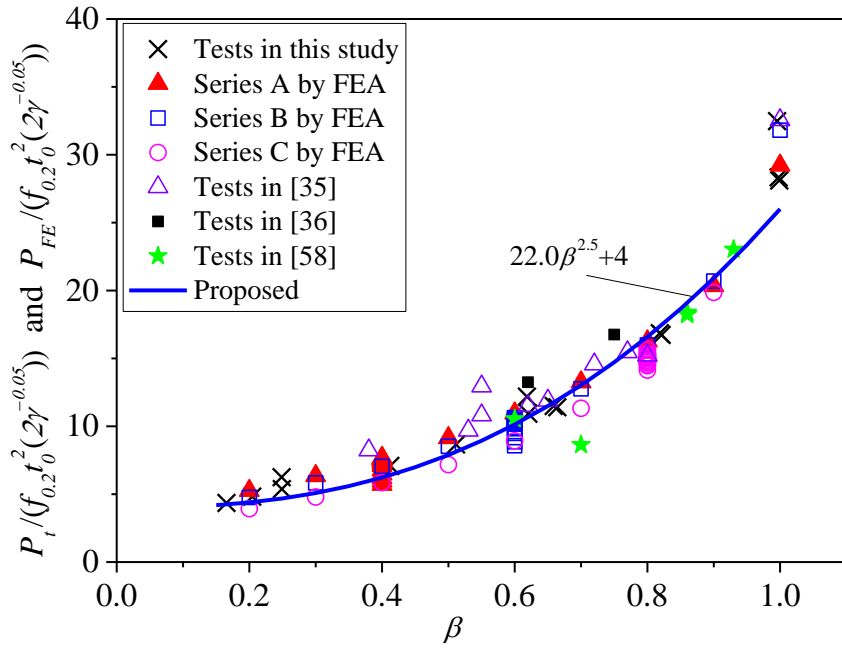


(b) Plot up to 5000 kN

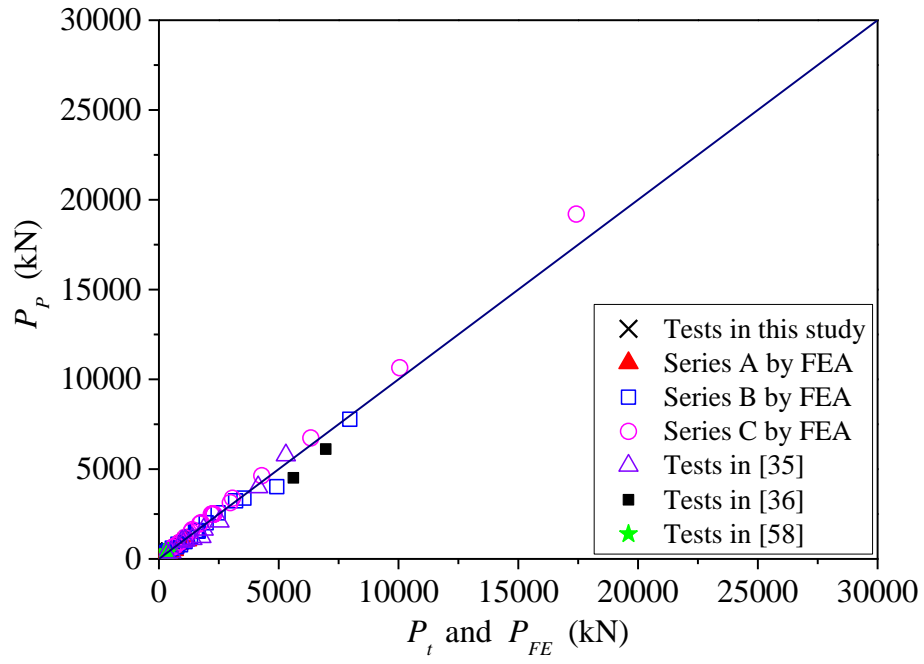
**Fig. 26:** Comparison of test and FE strengths with predictions by Lan *et al.* [38]



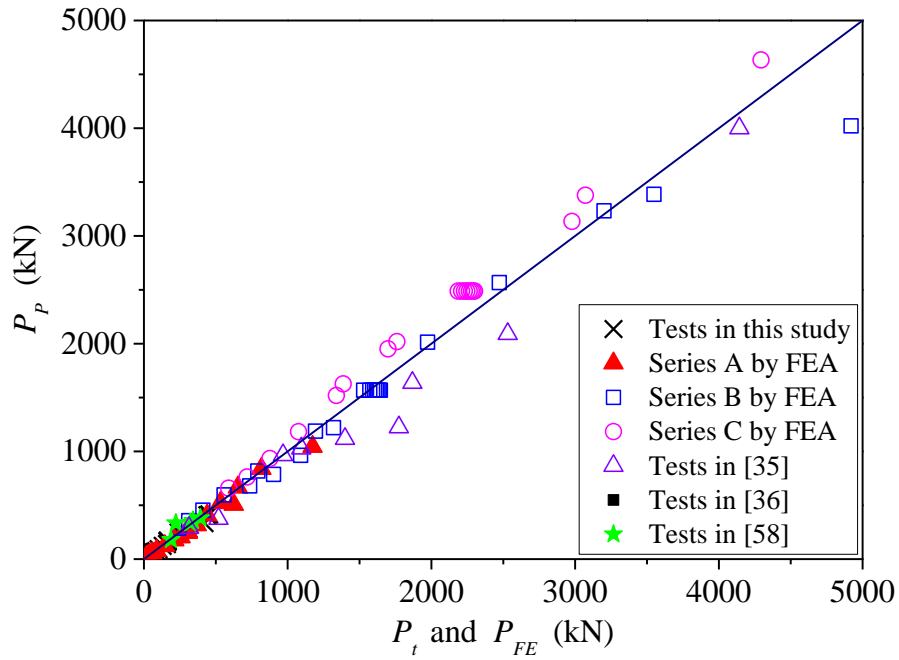
**Fig. 27:** Relationship between joint strengths divided by  $(f_{0.2} t_0^2 \gamma^{0.15})$  and  $\beta$



**Fig. 28:** Relationship between joint strengths divided by  $(f_{0.2} t_0^2 (2\gamma^{-0.05}))$  and  $\beta$



(a) Overall comparisons



(b) Scale up to 5000 kN

**Fig. 29:** Comparison of test and FE strengths with predictions by proposed equation