

Net Section Resistance of Bolted S690 Steel Angles Subjected to Tension

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Abstract: Net section rupture is a common failure mode of bolted tension members. In particular, the net section capacity of tension angle is significantly affected by the effect of shear lag. This paper reports the tensile test results of twelve high strength steel angles and six normal steel angles of grade S690 and S275, respectively. The test parameters included steel grades, connection length (bolt number) and out-of-plane eccentricity. All the specimens were failed by net section rupture. Finite element (FE) analysis was used to simulate the structural behaviour of the test specimens and to further interpret the test results. The test and the numerical analysis results showed that the test efficiency of tension angles, which was defined by the ratio of the ultimate test load to the calculated net section resistance, was sensitive to the material ductility and the connection details (i.e. out-of-plane eccentricity and connection lengths). The effectiveness of the available design specifications for quantifying the net section resistance of S690 steel angles was evaluated. A design approach proposed by Yam and colleagues considering the influence of material mechanical characteristics and connection configurations was also revisited. It was found that the current design specifications produced inconsistent predictions of net section resistance of tension angles, whereas the method proposed by Yam and colleagues gave good predictions of net section resistance of bolted S690 steel angles.

Keywords: Shear lag; net section resistance; high strength steel; experiment; finite element model; design method

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1 Introduction

Tension members made of angles, channels and tees are often used as bracings in steel construction. In a variety of engineering applications, only part of the cross-section of a tension member is connected to the adjacent components via high-strength bolts or welds. A bolted tension angle connected to a gusset plate by one leg is illustrated in Fig. 1. In this context, the connected leg is the one effectively carrying the applied load, whereas the resistance of the outstanding leg may not be effectively mobilised. Hence, the tensile resistance of the section may not be fully developed. This phenomenon is known as “shear lag”. Note that the bolt holes may further obstruct the stress flow and produces stress concentration, aggravating the non-uniform tensile stress distribution over the section. The uneven stress distribution is generally most evident near the inner end of the bolt line, and this cross-section is defined as the “critical section”, at which fracture tends to occur. Besides, the applied load is transferred along the bolt line which does not coincide with the centroid of the section, and hence produces eccentricity to the connection. The eccentricity would cause a detrimental effect on the net section resistance of the tension member.

The behaviour and net section resistance of tension members have been examined by a number of researchers since the last century [1-4]. For instance, Chesson and Munse [3, 4] examined the behaviour of tension angles based on full-scale experimental programmes and developed an empirical design equation to compute the net section resistance of tension members. Regan and Salter [5] studied the loading carrying behaviour of welded tension angles with various welding configurations, and the authors developed design equations to compute the net section resistance of welded tension angles based on test data

of seventeen welded tension angles. Easterling and Gonzales [6] examined double angles subjected to tension, and the influence of transverse welds on the shear lag was examined. Kulak and Wu [7] studied the tensile resistance of twenty-four single and double bolted tension members and developed novel methods for predicting the resistance of tension angles. Abi-Saad and Bauer [8] proposed an analytical equation for computing the tensile resistance of tension members governed by net section failure. Paula et al. [9] provided sixty-six (66) test data of cold-formed tension angles and developed a test database based on the test programmes from the literature. Prabha et al. [10] put forth a modified design equation for predicting the tensile resistance of cold-formed steel angles failing by net section rupture. Later, Zhu et al. [11] reported more test data of welded single tension angles. Fang et al. [12] studied the behaviour and the tensile resistance of welded tension angles and tees, and the applicability of design specifications for predicting the net section resistance of angles was evaluated. Fleitas et al. [13] examined the net section resistance of bolted cold-formed steel angles using a parametric study. Note that the emphases of the studies mentioned above were generally limited to steel members with nominal yield strength below 460 MPa.

High strength steel (HSS) with a nominal yield strength equal to or over 460 MPa [14-17] has been attracting increasing attention from the academia and engineering community in recent years. Research studies on the mechanical properties of HSS [18-20], HSS connections/components [21-25] and HSS structural systems [26-29] all shed insightful lights on the promise of HSS in steel construction. In engineering practice, the use of HSS may contribute to reducing the size and weight of structures and offer significant savings

in delivery cost and material/energy consumption during steel production. However, HSS generally exhibits lower ductility and a narrower range of post-yielding strain hardening compared to those of normal steel (NS) [19, 20], which may hinder stress redistribution to occur in the vicinity of the critical section of a tension member. Research studies on net section resistance of tension member made of steel with yield strength higher than NS have been conducted by some researchers. Teh and Gilbert [30] examined the net section resistance of steel channels made of cold-reduced sheet with measured yield strength over 530 MPa, and the authors proposed design equations for practical applications. Moze et al. [31] investigated the tension resistance of grade S690 steel plate with holes and the corresponding bolted connections experimentally, and the adequacy of the Eurocode provision for predicting the net section resistance of the connection was revisited. Yam and his co-workers [32] conducted fourteen tensile tests on welded and bolted HSS angles recently. The research findings indicated that HSS material properties (limited ductility and lower tensile strength to yield strength ratio) and connection configurations may reduce the net section efficiency of the bolted angles. However, only seven bolted HSS angles covering two angle sections and one NS specimen were included in [32], which may not fully reveal the load carrying mechanism of bolted HSS angles. In addition, the influence of the connection length and the potential combined effect of this parameter and other influential factors on bolted HSS angles have not been clearly examined. In light of the above, more experimental and analytical work are needed to examine the structural behaviour and net section resistance of bolted HSS tension angles.

The current study includes eighteen (18) tensile tests on bolted steel angles failed by net

section rupture. In particular, twelve S690 HSS angles were tested, and for comparison purpose six tests of NS specimens made of grade S275 steel were conducted. The test parameters included steel grade, angle section and bolt arrangement. The new test database covered a wider range of parameters compared to the previous study [32]. The combined effect among material properties and connection details on the net section resistance of the angles, which was not examined in [32], was also studied. Finite element (FE) analysis was employed to simulate the structural behaviour of the angle specimens in order to provide further interpretation of the test observations. The design methods in current codes and a method proposed in [32] were revisited, and their feasibility for quantifying the net section resistance of HSS angles was examined by comparisons against the test results.

2 Test Programme

2.1 Specimens, test rigs and loading procedure

Eighteen (18) bolted angle specimens were tested. Twelve (12) of them were fabricated using grade S690 steel with a nominal yield stress of 690 MPa, and the remaining six (6) were the NS counterparts made of S275 steel. The steel angles were fabricated using two steel plates through groove welding. The measured thicknesses of the S690 plates were 5.94 mm and 7.88 mm on average, and the thickness of S275 steel plates was 5.75 mm. Tension angles were connected to a 10.41 mm thick gusset plates at each end using Grade 12.9 M22 high strength bolts. A typical illustration of a test specimen is shown in Fig. 2. Four angle sections (i.e. $85 \times 65 \times 6$, $65 \times 65 \times 6$, $125 \times 65 \times 6$ and $125 \times 65 \times 8$, unit: mm) were used to study the effects of out-of-plane eccentricities and angle sections. A constant

pitch of 75 mm was designed for all the specimens, whilst the number of bolt was included as one of the test parameters for examining the effect of connection length. The specimen information is summarised in Table 1. The specimen label commences by either 'A' or 'B', representing S275 or S690 steel, respectively. The following number '1', '2', '3' and '4' represents angle section $85 \times 65 \times 6$, $65 \times 65 \times 6$, $125 \times 65 \times 6$ and $125 \times 65 \times 8$ (unit: mm) sections, respectively, and the letter 'S', 'L' or 'E' refers to an angle connected by the short leg, the long leg or the equal leg, respectively. The number of bolts is indicated by the value following 'Bt'. The measured dimensions of specimens are shown in Table 1, and the definitions of the symbols are indicated in Fig. 2.

Tension coupons were extracted from the steel plates and tested according to ASTM A370 [33], and the measured material properties are summarised in Table 2. It is worth noting that although the measured yield strength of 5.94 mm thick S690 steel plate was slightly below the nominal value, the ultimate strain and the ratio of the measured tensile strength to the measured yield strength (f_u/f_y) were typical for S690 steel.

Fig. 3 schematically illustrates the test rig, which was also used in the previous study conducted by Yam and colleagues [32]. In particular, the gusset plates of the specimens were connected to the end fixtures, which were gripped by the crossheads of the testing machine. All the bolted connections were snug tightened by a wrench. The applied loads were obtained by the load cell of the machine, and the elongation of the specimens was recorded by the built-in displacement transducers. Strain gauges with a gauge length of 10 mm were mounted on the specimens to measure longitudinal strain responses at the angle's critical and mid-length section as shown in Fig. 2. In each test, a small preload was used to

147 sit and align the angle specimen and eliminate the slip in the connection. A stroke-control
148 procedure was adopted in the test with the loading rate of 0.2 mm/min exerting tension to
149 the specimen. After the specimens progressing to the inelastic stage, the stroke was
150 maintained for about 90 seconds at various load intervals to allow the specimen to reach
151 static equilibrium, and the corresponding static load values were recorded.

153 2.2 Test results

154 2.2.1 Overview

155 All the specimens were failed by net section rupture at the critical section, and the
156 typical failure modes are shown in Fig. 4. The tensile fracture of angles was initiated from
157 the toe of the connected leg and then propagated to the outstanding leg as shown in the
158 figure. The ultimate load of the specimens and the normalised net section resistance (P_{norm})
159 are shown in Table 1. The normalised net section resistance was determined by dividing
160 the static test ultimate load by $A_n f_u$, where A_n is the measured net-section area of the
161 specimen and f_u is the actual tensile strength of the material. Note that the normalised net
162 section resistance is also known as the test efficiency (i.e. U_{test}). In general, the test
163 efficiency of the grade S275 angle specimens ranged from 0.59 to 1.07, whereas U_{test} of
164 the S690 angle specimens varied from 0.61 to 1.01. It can be seen that the test efficiencies
165 of the specimens were generally lower than unity due to the combined effects of material
166 properties, eccentricity, and connection details. This observation will be further discussed
167 in the following sections.

168 2.2.2 Load-elongation responses

169 Fig. 5 gives the normalised load versus elongation curves of all the test specimens. In

general, linear load versus elongation responses were characterised initially, and nonlinear behaviour was observed when the applied load reached approximately 60% to 85% of the ultimate load. Fig. 5 shows that due to the limited deformation capability of S690 material, the normalised load-elongation responses of grade S690 angle specimens generally had a smaller total elongation at the ultimate load compared with those of the S275 counterparts with identical connection configurations. This effect was comparatively more evident in cases with a long connection (e.g. comparison group A2-E-Bt5/B2-E-Bt5 in Fig. 5b and A3-S-Bt5/B3-S-Bt5 in Fig. 5c). Note that the test efficiency of the S275 steel angle A2-E-Bt5 is higher than unity (1.07), and hence the critical section of the angle could develop full net section resistance with adequate strain hardening ($f_u/f_y = 1.52$). This might further allow yielding in the gross section of the angle before fracture of the critical section, and hence contributed to a longer elongation of the member at the ultimate load. In contrast, the lower test efficiency of the S690 steel angle indicated a less effective stress redistribution pattern in the critical section upon reaching the ultimate load due to the limited ductility of S690 steel ($\epsilon_u = 0.06$, gauge length 50 mm). Thus, yielding of the angle in the gross section might not be effectively developed upon fracture of the critical section, and the corresponding total elongation of the S690 steel angle was reduced.

After reaching the ultimate stage, the applied load deteriorated rapidly as a result of fracture initiation at the critical section. However, all the S275 angles were able to develop pronounced residual resistance in the post-fracture stage, as can be seen from the slight ascending branches in the post-ultimate equilibrium paths (Fig. 5a, Fig. 5b and Fig. 5c). The regained strength and residual ductility could be attributed to the participation of the

outstanding leg in carrying the applied load in the post-ultimate stage, recalling that fracture was firstly triggered at the toe area of the connected leg and propagated to the outstanding leg with further elongation (Fig. 4). However, this phenomenon was generally not pronounced for the S690 specimens. These observations imply that the high ductility and evident post-yielding strain hardening of S275 steel was able to effectively mobilise the unconnected leg in carrying the applied load in the post-ultimate stage, and residual strength could be achieved prior to the complete rupture of the section. On the other hand, the less ductile behaviour of S690 steel adversely affected the stress redistribution of the critical section in the post-fracture stage, and complete rupture of the section was triggered before the outstanding leg could be effectively mobilised.

2.2.3 Strain distributions

Fig. 6 presents the representative strain results of the HSS angle specimens (i.e. specimen B1-S-Bt3 and B1-L-Bt5) and the NS counterparts (i.e. specimen A1-S-Bt3 and A1-L-Bt3). Strain readings of critical and mid-length section at representative load levels (i.e. 20%, 40% and 60% of the ultimate load P_{test}) is shown in Fig. 6 to demonstrate the strain evolution of the two sections. The locations of the strain gauges and the theoretical yield strain derived from the actual material properties are also shown in the figure.

The general trend of strain distributions of the HSS and NS angle specimens at the critical section is similar, and only the HSS specimens are discussed herein. In particular, at the critical section, the connected leg was generally in tension with tensile yielding firstly triggered near the bolt hole as a result of stress concentration. However, the top edge of the outstanding leg was initially in slight compression due to the combined effects of

shear lag and secondary bending according to the strain readings of strain gauge 4. As shown in Fig. 6c, the compressive strains of the short-leg connected specimen B1-S-Bt3 kept increasing with increasing applied load. This was because the short-leg connected angle had significant out-of-plane eccentricity, thus causing more evident shear lag and secondary bending. On the contrary, the compression at the top edge of the outstanding leg of specimen B1-L-Bt5 connected by the long leg was mitigated with the applied load increased to 60% of P_{test} , as shown in Fig. 6d. This observation was due to the smaller out-of-plane eccentricity of the long-leg connected angle.

At the mid-length section, the material at the top edge of the outstanding leg was initially in compression as a result of secondary bending. As shown in Fig. 6d, specimen B1-L-Bt5 with the largest connection length and the smallest out-of-plane eccentricity reversed the compression at the top edge of the unconnected leg to tension (strain gauge 9) with increasing applied load. On the other hand, the top edge of the outstanding leg of specimen B1-S-Bt3, remained in compression with increasing applied load. Besides, the comparison between the strain responses of S275 and S690 angle specimens (i.e. group A1-S-Bt3/B1-S-Bt3) implied that yielding of the mid-length section of the NS angle might be able to be triggered more readily, as the strain of the section was closer to the yield strain at 60% of P_{test} , echoing the larger total elongation of S275 angles shown in Fig. 5. More evidence substantiating this argument will be provided in later sections based on finite element analysis of the angle specimens.

3 Discussions of test and finite element analysis results

3.1. Discussions of test results

3.1.1 Effects of type of steel

The test results showed that the limited ductility of HSS steel material adversely affected the load carrying behaviour of bolted tension angles which echoed the test observations from [32]. According to Table 1, the test efficiencies of S690 angle specimens are generally lower than those of the S275 counterparts with identical section and connection configuration. The reduction in test efficiency varied from 8% to 17%. However, the comparison group A1-S-Bt3/B1-S-Bt3 and A3-S-Bt3/B3-S-Bt3 are exceptions with the test efficiency of the S690 angle equal to or even slightly higher than that of the S275 specimens. Note that in these cases the angles generally had a significant out-of-plane eccentricity (i.e. a considerable outstanding leg length) and a short connection (i.e. three bolts). In this scenario, the influence of the connection configurations dominated the tensile behaviour of the angle specimens. The angles failed to mobilise effectively the outstanding leg in carrying the applied load. However, the influence of steel grades became more pronounced in cases with long-leg connected angles and long connections. In particular, the test efficiency of a long-leg connected S690 angle specimen B1-L-Bt3 (0.85) was lower than that of the S275 counterpart specimen A1-L-Bt3 (0.92). The test efficiency of specimen B3-S-Bt5 and A3-S-Bt5 with a long connection are 0.69 and 0.83, respectively. This phenomenon was due to the fact that the shear lag effect was reduced by a long-leg connected angle and a long connection, and therefore the effect of material ductility on the tensile behaviour and strength of the angle specimens became more

pronounced. Since the limited material ductility of S690 steel material might not allow sufficient stress redistribution to occur in mobilising the outstanding leg prior to failure, the test efficiency of the HSS angle was reduced.

3.1.2 Effects of out-of-plane eccentricity

The test results confirmed that the test efficiency decreases with increasing out-of-plane eccentricity for both S690 and S275 angle specimens. In particular, the S690 angle specimen B1-L-Bt3 connected by the long leg achieved a test efficiency of 0.85, whereas the short-leg connected counterpart (i.e. B1-S-Bt3) with a more significant out-of-plane eccentricity achieved a lower efficiency of 0.74. Similarly, specimens B1-L-Bt5 and B1-S-Bt5 produced the test efficiency of 1.01 and 0.92, respectively. The adverse effect of increasing out-of-plane eccentricity can also be seen according to the test efficiency of the comparison group B3-S-Bt5/B2-E-Bt5 with the identical connected leg and varied outstanding legs, and the test efficiency of specimen B3-S-Bt5 (outstanding leg 125 mm) is 30% lower than that of specimen B2-E-Bt5 (outstanding leg 65 mm). Similar observations were characterised for the S275 angle specimens. In general, these expected findings are consistent with those characterised from previous research works [3, 4, 9, 32].

3.1.3 Effects of connection length

The test data showed that the test efficiency of the specimens generally increases with increasing connection length. Specifically, two equal-leg connected S690 angle specimens B2-E-Bt3 (connection length 100 mm) and B2-E-Bt5 (connection length 200 mm) achieved the test efficiency of 0.80 and 0.98, respectively, which represents an increase of 23% in test efficiency with connection length increased by 100%. Similarly, the test

efficiencies of S275 angle specimens A2-E-Bt3 and A2-E-Bt5 are 0.88 and 1.07, respectively, and the corresponding increase of the test efficiency is 22%. However, the effect of connection length on the test efficiency was relatively less evident in case of short-leg connected S690 steel angles. The test efficiency of specimens B3-S-Bt3, B3-S-Bt4 and B3-S-Bt5 are 0.61, 0.69 and 0.69, respectively, representing an increase of only 13% in test efficiency with an increase in connection length of 100%. Similar findings were recorded for specimens B4-S-Bt3, B4-S-Bt4 and B4-S-Bt5. Therefore, it can be seen that a short-leg connected S690 angle, which has lower material ductility and a higher out-of-plane eccentricity, may further prohibit the effective mobilisation of the outstanding leg to resist the applied load. Thus, the beneficial effect of an increasing connection length in enhancing the net section resistance was not pronounced.

3.2 Finite element analysis

3.2.1 Modelling techniques

To facilitate further interpretation of the test results, finite element (FE) models of the specimens were developed using ABAQUS [34]. A typical FE model of the angle specimen is presented in Fig. 7. Eight-node solid elements (i.e. C3D8R) were used to model the steel angle, bolts and gusset plates. Four elements were developed in the thickness direction for all the components to avoid the “hourglass” [34] effect. A “general contact” method was employed to simulate the interaction among the components. The “hard contact” and “penalty friction” algorithm were adopted to reproduce the contact behaviour, whereas the influence of the bolt clamping force was ignored. This simplification is reasonable since snug tight condition by hand wrench was used to install

the bolts. To simulate the constraint by the end fixtures in the tests, all the degrees of freedom in the connection region of the gusset plate were coupled using “kinematic coupling”, whereas translational displacement along the angle elongation direction was allowed (U3 in Fig. 7). To model the minor elastic elongation of the test assembly during loading, elastic springs elements in the U3 direction were introduced, and a consistent stiffness was calibrated based on the initial slope of the load versus elongation responses of the specimens. “Dynamic/explicit” solver of ABAQUS was utilised to avoid convergence issues in the post-ultimate stage.

An isotropic plastic model with von Mises yield criterion was used. True stress-strain responses derived from the nominal stress-strain curves obtained from the coupon results were adopted in the modelling. Specifically, the true stress-strain relationship before necking can be expressed by the following equation.

$$\sigma_t = \sigma_{no}(1 + \varepsilon_n) \quad (1)$$

$$\varepsilon_t^p = \ln(1 + \varepsilon_n) - \frac{\sigma_t}{E} \quad (2)$$

where σ_t = true stress, σ_{no} = nominal stress (engineering stress), ε_t^p = true plastic strain, ε_n = nominal strain (engineering strain) and E = the elastic modulus. Recognising that the above correlations were valid only before necking, approximations were needed to determine the true stress-strain relationship in the post-necking branch. A trial-and-error procedure was adopted by assuming that the true stress-strain curve remains linear [35, 36] after necking. The rationale of using a trial-and-error process in simulating the post-necking behaviour of the material are supported by recent research works. The “Damage for Ductile Metals” module [34] was implemented to simulate damage evolution and

fracture of the material. The “fracture strain” and “damage evolution index” in the module quantify the strain corresponding to cracking inception and the deterioration rate of the material, respectively. To account for the influence of complex stress state on the fracture of tension angles, the classical Johnson-Cook damage function [37] was used to develop the relationship between the fracture strain (ε_f) and stress triaxiality (η) based on iterations, i.e. $\varepsilon_f = a + be^{-c\eta}$, where a , b and c are coefficients to be calibrated. Based on the available test data, $a=0.063$, $b=0.094$ and $c=2.800$ were finalised for S275 steel. For S690 steel, $a=0.040$, $b=0.800$ and $c=2.500$ were used. Since the net section resistance of all the specimens was dominated by tensile failure of the material near the bolt hole, the adopted fracture model excluding the influence of lode angle [38-40], which quantifies the influence of the shear action on the fracture behaviour, is reasonable. To determine the damage-evolution index, a linear method was assumed to simulate the material deterioration until complete stiffness loss. As the mesh property would affect the fracture prediction significantly, a refined mesh was used in the bolted connection area of the FE models where fracture was expected to occur. An element size of 2.0 mm approximately was finalised using a mesh sensitivity analysis. More information about the rationale of the adopted fracture simulation strategy in ABAQUS can be found in [34], and the adequacy and limitation of the methods was also recorded in the literature [41-45].

3.2.2 FE results and further discussions

The test-to-FE ratios computed by the ratio of the ultimate strength of the specimens (P_{test}) to the FE prediction (P_{FE}) are shown in Table 1. The test-to-FE ratio of S690 angle specimens ranged from 1.01 to 1.12, with an average $P_{\text{test}}/P_{\text{FE}}$ ratio of 1.06 and a

coefficient of variation (CoV) of 0.041. The test-to-FE ratio of S275 angles varied from 1.02 to 1.18, with an average $P_{\text{test}}/P_{\text{FE}}$ ratio of 1.09 and a CoV of 0.065. The applied load-elongation responses of typical specimen groups (A1-S-Bt3, A1-L-Bt3, A3-S-Bt3, A3-S-Bt5, B1-S-Bt3, B1-L-Bt3, B3-S-Bt3, B3-S-Bt5, B4-S-Bt3 and B4-S-Bt5) covering varied steel grades, out-of-plane eccentricities and connection lengths were compared with the corresponding FE results, as shown in Fig. 8. In general, good correlation between the load-deflection responses by tests and FE predictions is observed. The strain readings at the critical and the mid-length sections corresponding to 20%, 40% and 60% of the ultimate load were extracted from the FE models and plotted against the test results as shown in Fig. 6, which substantiated the validity of the FE models. In addition, the strain responses at the mid-length section corresponding to 95% of the ultimate load were extracted from the FE results and shown in Fig. 6. It can be seen that the S275 angles could generally develop yielding in the mid-length section when the applied load approached the ultimate, whereas this phenomenon was not evident for the S690 angles. This finding echoes the generally larger total elongation of S275 specimens as observed from the test results. Note that the damage evolution from necking to fracture obtained from the FE predictions are also included in Fig. 8 for a clearer interpretation of the structural behaviour of the specimens. The failure of the critical section was triggered by necking of the toe of the connected leg identified as “1” in the figure. Fracture of the material near the bolt hole occurred upon further loading identified as “2” in the figure. The failure modes of the test specimens compared well with those of the FE results as shown in Fig. 8.

To offer an in-depth understanding of the stress evolution, the normal stress at various loading levels (i.e. 10%, 20%, 50%, 70% and 100% of P_{FE}) from the FE results of specimen B3-S-Bt5 (S690) and specimen A3-S-Bt5 (S275) at the critical sections were examined as shown in Fig. 9. The figure shows the normal stress evolution at the connected leg and the outstanding leg, and the positive and negative values represent tensile and compressive stress, respectively. Non-uniform normal stress distribution was evident in the initial loading stages (i.e. 10% and 20% of P_{FE}) along the tensile plane of the connected leg (i.e. path “X2” in Fig. 9), and the maximum stress was seen at the edge of the bolt hole due to stress concentration. With further increase of the applied load, the angle progressed into the inelastic stage, and stress redistribution occurred across the critical section of the connected leg. At the ultimate stage, the normal stress across the critical section of the connected leg approached uniform irrespective of the steel grade as indicated by the tensile stress distribution along path “X2” in Fig. 9. On the other hand, linear normal stress distribution was characterised for the outstanding leg (i.e. path “X1” in Fig. 9) of both angles initially, and the top portion of the leg was in slight compression, echoing the strain readings from the test results. Subsequently, the normal stress distribution along path “X1” became nonlinear with increasing applied load. At the ultimate stage, the compressive stress in the outer edge of the outstanding leg was increased significantly due to the significant secondary bending effect, which was consistent with test observations. However, it should be noted that at the ultimate stage the compression area of the outstanding leg of the S275 specimen (A3-S-Bt5) was reduced almost by half whereas the corresponding compression area of the S690 specimen (B3-S-

Bt5) remained almost unchanged. This demonstrated that the limited ductility of S690 steel material did not allow sufficient deformation of the specimen to occur prior to reaching the ultimate load, and therefore prohibited the effective mobilisation of the outstanding leg to resist the applied load. These observations echoed the test result that specimen B3-S-Bt5 achieved a much lower test efficiency compared with that of A3-S-Bt5. Based on the test and the FE results, it can be seen that the limited ductility of HSS lessens the effectiveness of stress redistribution across the critical section of S690 angle specimens, and hence reduces the test efficiency.

4 Design comments

The adequacy of the design equations in major specifications CSA S16-14 [46], AS 4100 [47], Eurocode 3 [48] and AISC 360-16 [49] for predicting the net section resistance of single bolted tension angle specimens is examined in this section. The design equations documented in the specifications mentioned above are reproduced in Table 3. Although various design specifications employ different equations, they were developed based on a similar framework by considering strength reductions based on the net area of the angles.

The test-to-predicted ratios by the above design equations are summarised in Table 4. The actual material properties were used to compute the predicted resistance. Resistance factors, capacity factors and partial safety factors accounting for reliability were taken as unity. The test results of seven S690 angle specimens in [32] were also included in the discussion to enlarge the test results database. CSA S16-14 [46] produced an average test-to-predicted ratio of 1.06 with a CoV of 0.175 and an average test-to-predicted ratio of

1.27 with a CoV of 0.173 for the S690 angle specimens and the S275 angle specimens, respectively. Similarly, AS 4100 [47] produced generally conservative predictions of the net section resistance for both S275 and S690 angle specimens, whereas the conservatism of the predictions was reduced in case of S690 specimens. Eurocode 3 [48] produced an average test-to-predicted ratio of 1.78 with a CoV of 0.087 for the S690 angle specimens, and an average test-to-predicted ratio of 1.79 accompanied with a CoV of 0.154 for the S275 angle specimens, showing the overly conservative nature of the method. The average test-to-predicted ratio predicted by the AISC 360-16 [49] design equations was 0.90 with a CoV of 0.100 for the S690 angle specimens. Comparatively, the average test-to-predicted ratio of 0.98 with the CoV of 0.108 were obtained for S275 angle specimens.

Based on the available test data, it can be seen that the design equations in the specifications produced inconsistent predictions of the net section resistance of the angle specimens, and unsafe predictions were more obvious in cases of S690 steel angles. Although the average test-to-predicted ratio for the S690 angle specimens by the equations in CSA S16-14 [46] was on the conservative side, significantly unsafe predictions were recorded for some S690 specimens according to Table 4 (e.g. B4-S-Bt4 with the test-to-predicted ratio of 0.79). Also, the generally unconservative predictions by AISC 360-16 [49] in cases of S690 steel indicated that the design method may not be applicable to HSS angles. These findings might be attributed to the fact that the influence of material property of S690 steel (i.e. $f_u/f_y = 1.04 \sim 1.12$ and $\epsilon_u = 0.06$ with a gauge length of 50 mm) was not taken into account by the design equations. As revealed by the test results and the stress evolution behaviour in the FE study (Fig. 9), the outstanding leg of the S690 steel angles

may not be effectively mobilised to resist tension prior to reaching the ultimate load, and thus the above design equations developed based on normal steels are prone to overestimating the net section resistance of S690 steel angles. This could be further confirmed from the unsafe predictions by CSA S16-14 [46] and AISC 360-16 [49] in cases of S690 steel angles with a considerable outstanding leg length (e.g. B3 series and B4 series angles), in which case stress redistribution to the outstanding leg might not be effective.

Yam and his co-workers [32] developed a modified design method based on a numerical study to evaluate the net section resistance of HSS tension angles. The method considers the combined effect of the f_u/f_y ratio of the material and the configuration of the connections. In particular, the net section resistance of a single tension angle is computed by the following

$$P_{Yam} = \beta_m \beta_t \left(1 - \frac{\bar{x}}{l}\right) A_n f_u \quad (3)$$

$$\beta_m = -0.34\omega^{-1} + 1.14 \quad (4)$$

$$\beta_t = 0.4 S/S' + 0.7 \quad (5)$$

where ω = ultimate strength to the yield strength ratio of the material, S = connected leg length and S' = outstanding leg length. The definition of A_n , f_u , \bar{x} , and l are identical to those specified in Table 3, and the predictions by the method is summarised in Table 4. Employing the Yam's equation [32], an average test-to-predicted ratio of 1.06 with a CoV of 0.065 was recorded for S690 steel angles, and an average test-to-predicted ratio of 1.03 with a CoV of 0.095 was obtained for the S275 steel specimens. As can be seen, the equations proposed by Yam and co-workers [32] provided good estimates of the net

section resistances of both S275 and S690 steel angles. Based on the available test results, it is recommended that the equation proposed by Yam and co-workers to be applied to quantifying the net section resistance of bolted S690 HSS angles. However, caution should be exercised when using the Yam's equation outside the range of parameters discussed in [32] and the current study. Reliability analyses are also expected to develop a full-fledged design guideline for practical applications.

5 Conclusions

A full-scale test programme on the net section resistance of S690 high strength steel (HSS) bolted angles is reported in this study. Eighteen tests on single bolted tension angles were conducted, of which twelve specimens were S690 steel angles and the remaining six were S275 steel counterparts. The test parameters included steel grade, out-of-plane eccentricity and connection length (i.e. bolt number). The test matrix covered a broadened range of parameters compared with a previous study [32], and the comparative study between the behaviour of S690 and S275 bolted angles was conducted. The test results showed that the behaviour and failure modes of S690 HSS tension angles were similar to those made of normal steel (i.e. S275 steel) angles. The combined effect of material characteristics and connection configurations on the net section resistance of tension angles was also observed. In general, the test efficiency decreased with higher steel grade, and this trend was more obvious in cases of angles with a long-leg connection and long connection length. As expected, the test efficiency decreased with increasing out-of-plane

eccentricity for both S690 and S275 steel angles. In addition, the test efficiency of S690 and S275 steel angles generally increased with connection length, but this trend was not pronounced for S690 steel angles connected by the short leg.

To help interpret the test results, finite element (FE) models of the specimens were developed. In general, the FE predictions agreed well with the test responses, and the behaviour of tension angles from yielding inception to failure was well reproduced by the FE models. The normal stress evolution process at the critical sections of angles from the initial loading stage to the ultimate load, which could not be captured in the test, were further examined using the validated FE models. The results confirmed that the outstanding leg of the S690 steel angle might not be fully mobilised to carry the applied load prior to failure of the net section, and the reduced ductility of S690 steel would appreciably affect the net section resistance of bolted tension angles. These results echoed the test observations that the test efficiency of the S690 angle specimens was generally lower than that of the S275 angle specimens with identical connection configurations.

The test results were compared to the predictions by the design equations documented in major design specifications and to those by the equation proposed by the authors and colleagues [32]. It was observed that the design equations in CSA S16-14 [46] and AISC 360-16 [49] produced unconservative estimates of the net section resistance for S690 steel angles, particularly in cases of short-leg connected angles with a considerable outstanding leg length. AS 4100 [47] produced conservative predictions of the net section resistance for S275 and S690 steel angles, however, the coefficients of variation of the test-to-predicted ratios were significant. Eurocode 3 [48] led to overly conservative predictions of

the net section resistance of both S275 and S690 steel angles. The inconsistent predictions by the codified equations may be explained by the fact that these design methods do not consider the effect of material property on the net section resistance of tension members. In contrast, the design equation proposed by the authors and colleagues [32] accounting for the combined effect of f_u/f_y ratio and connection configurations produced good estimates of the net section resistance of both S275 and S690 angle specimens. Therefore, it is recommended to use the equation in [32] to predict the net section resistance of bolted S690 HSS angles. However, caution should be exercised when using the equation outside the range of parameters discussed in [32] and the current study.

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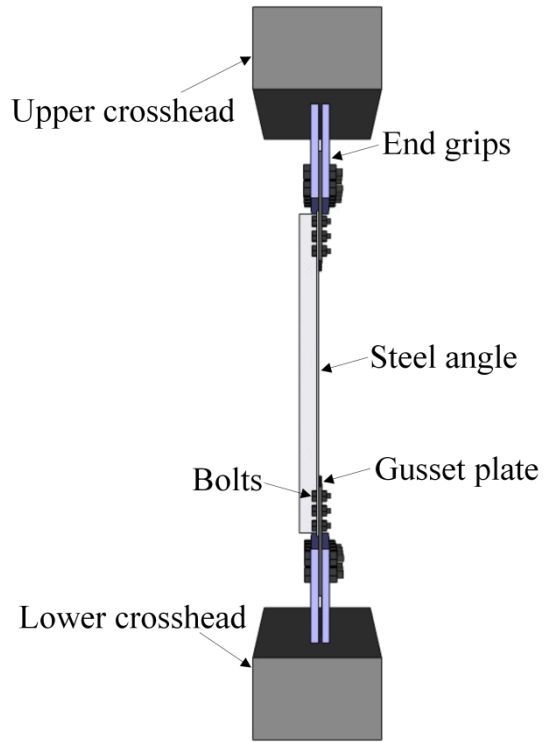
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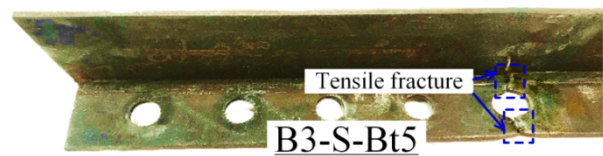
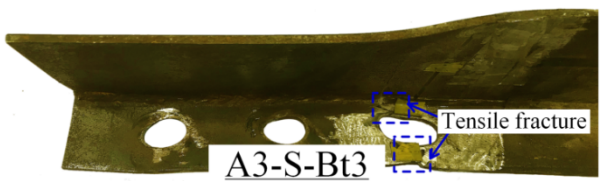
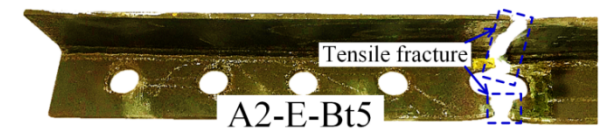
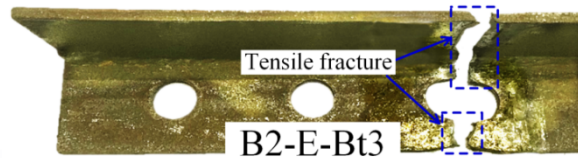
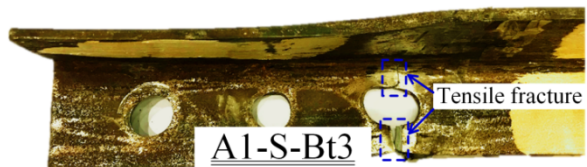
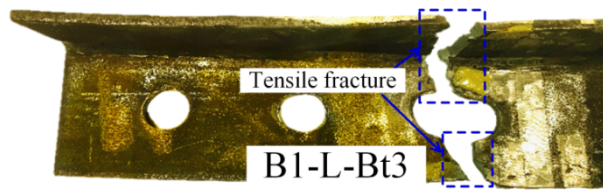
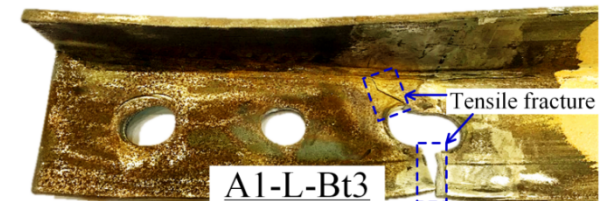


(a)



(b)

Fig. 3 Test arrangement: (a) Front view and (b) Side view.



(a)

(b)

Fig. 4 Typical failure modes of tension angles: (a) S275 angles and (b) S690 angles.

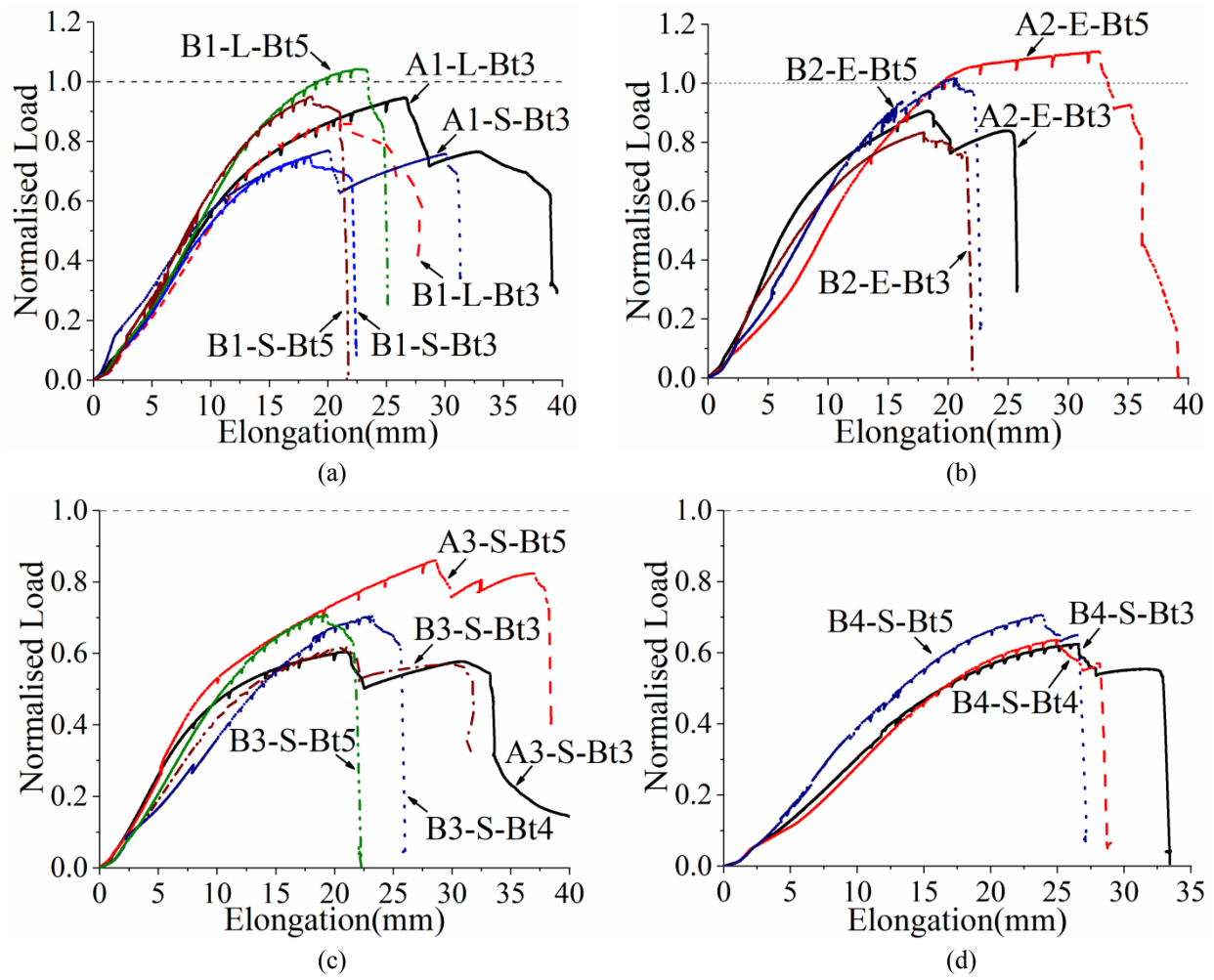
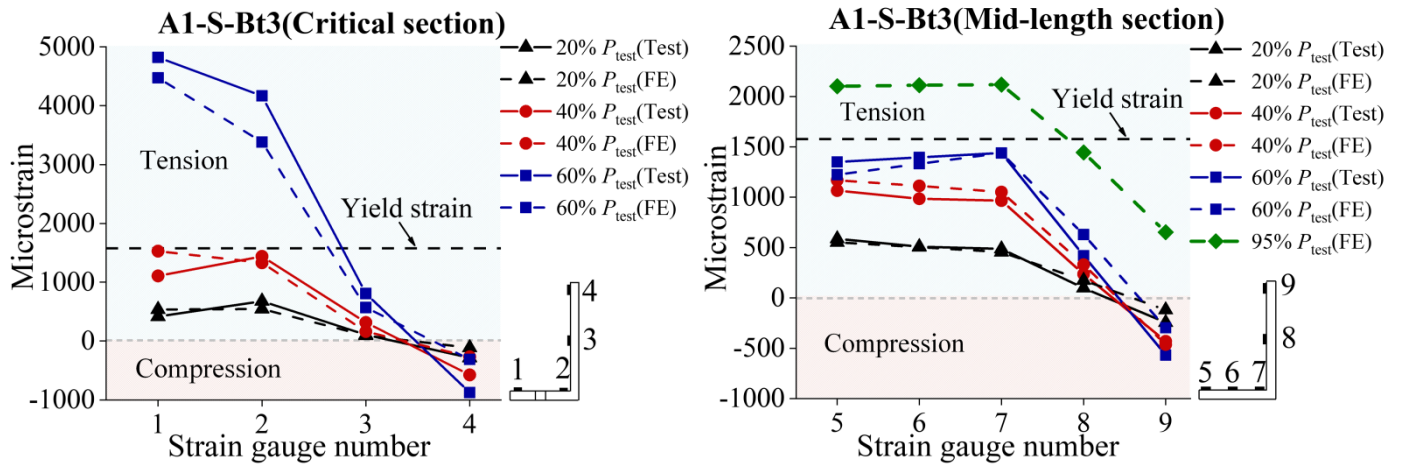
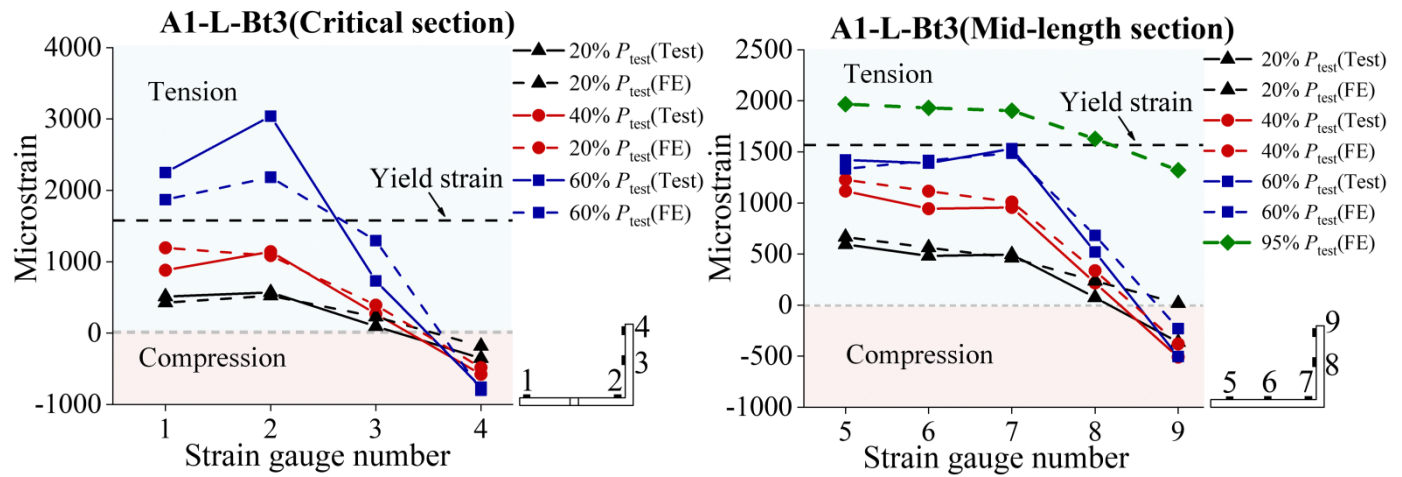


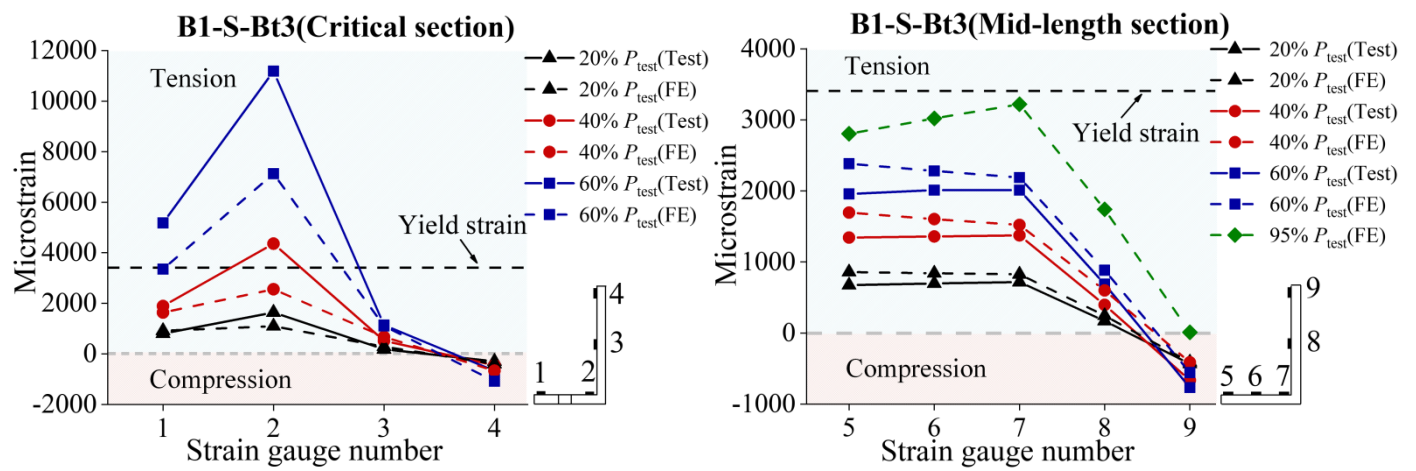
Fig. 5 Normalised load versus elongation curves: (a) A1/B1 series, (b) A2/B2 series, (c) A3/B3 series and (d) B4 series.



(a)



(b)



(c)

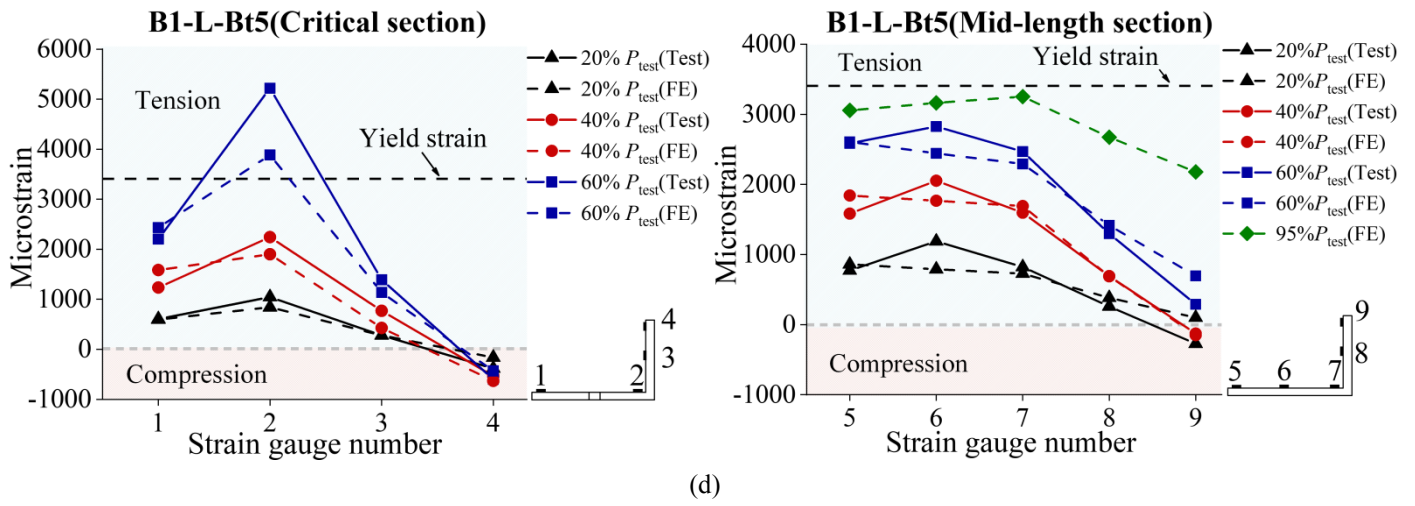


Fig. 6 Representative strain distributions: (a) A1-S-Bt3, (b) A1-L-Bt3, (c) B1-S-Bt3 and (d) B1-L-Bt5.

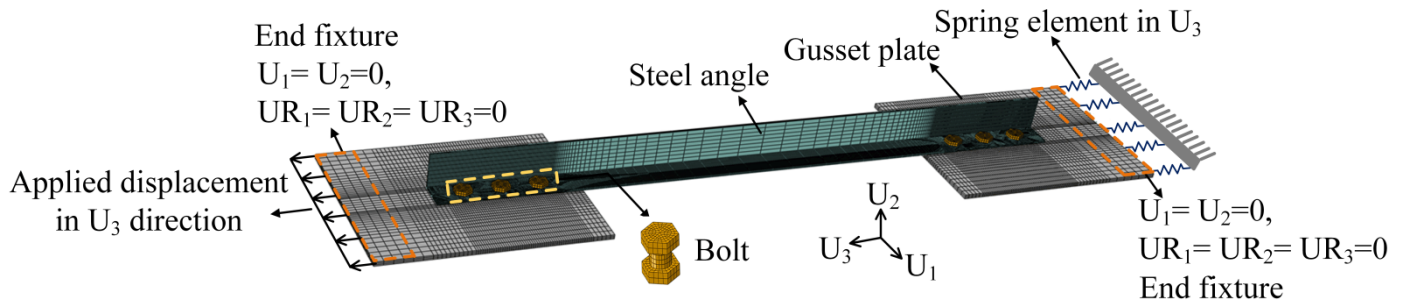
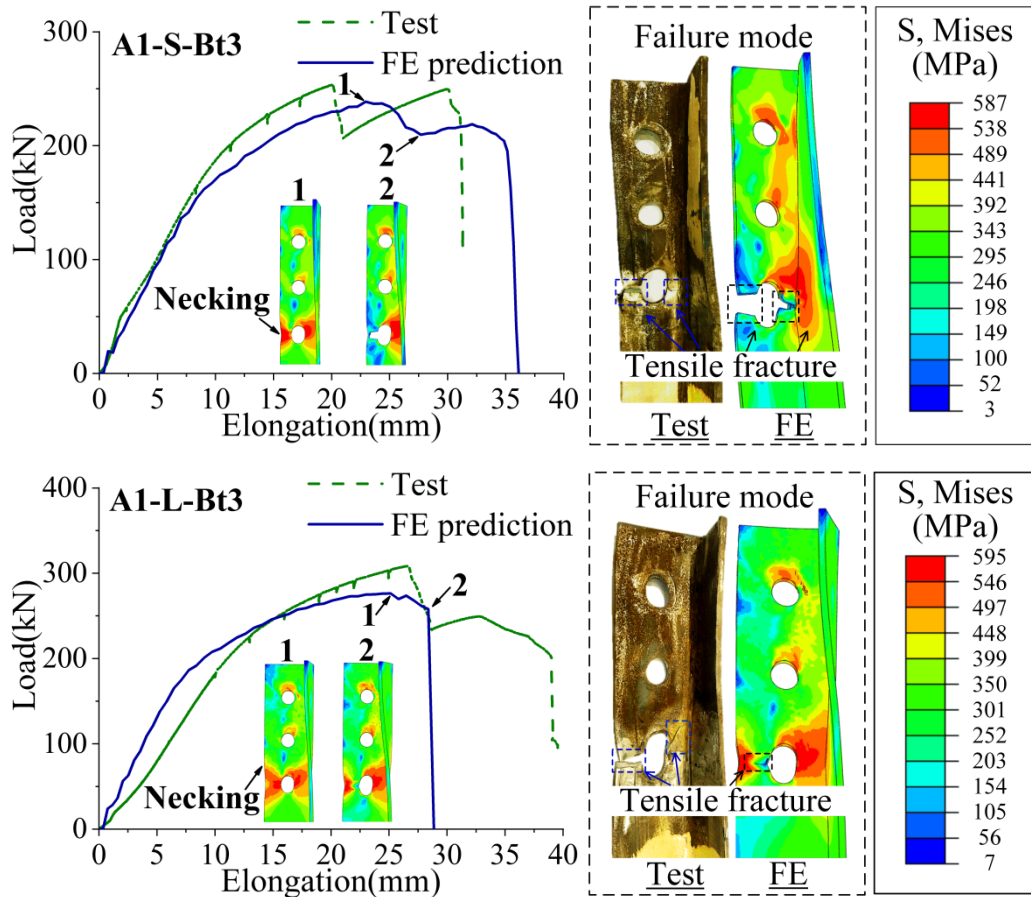
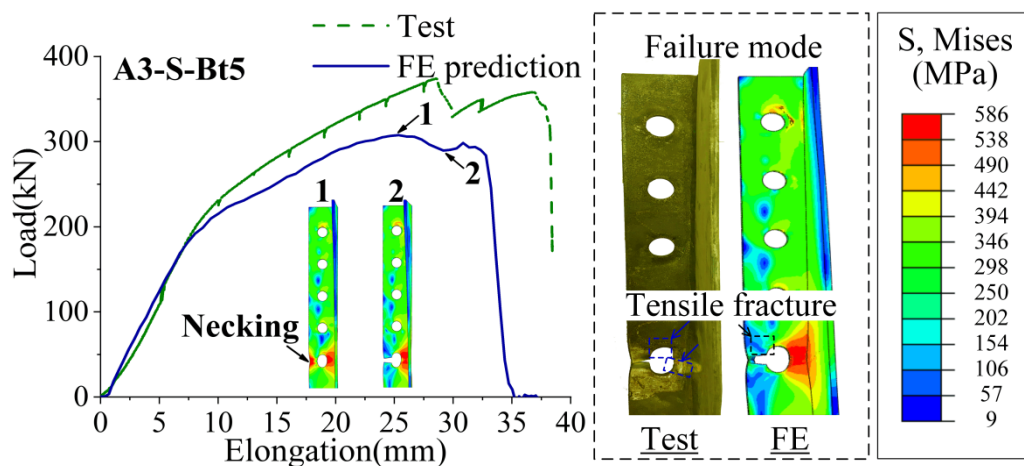
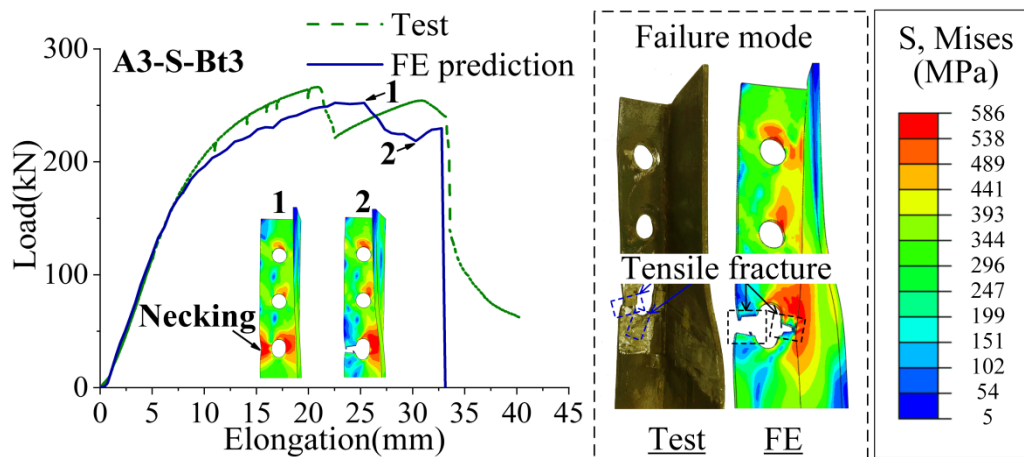


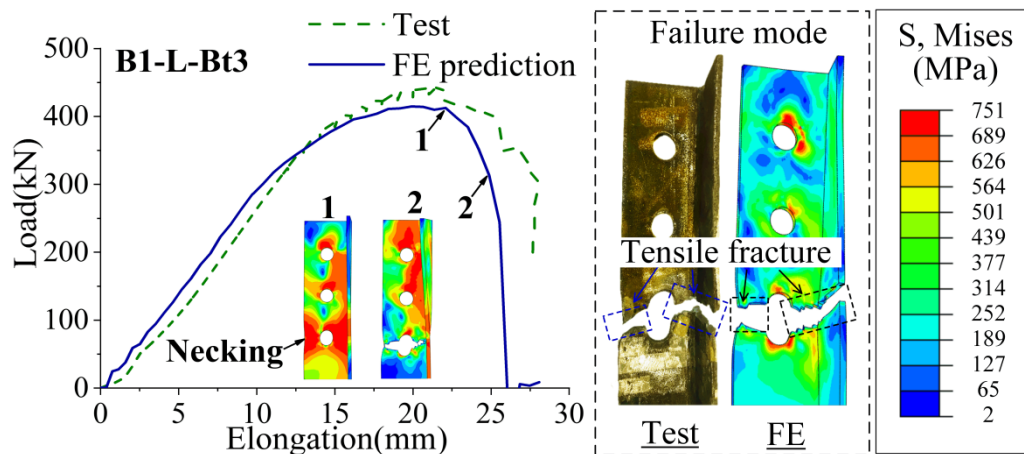
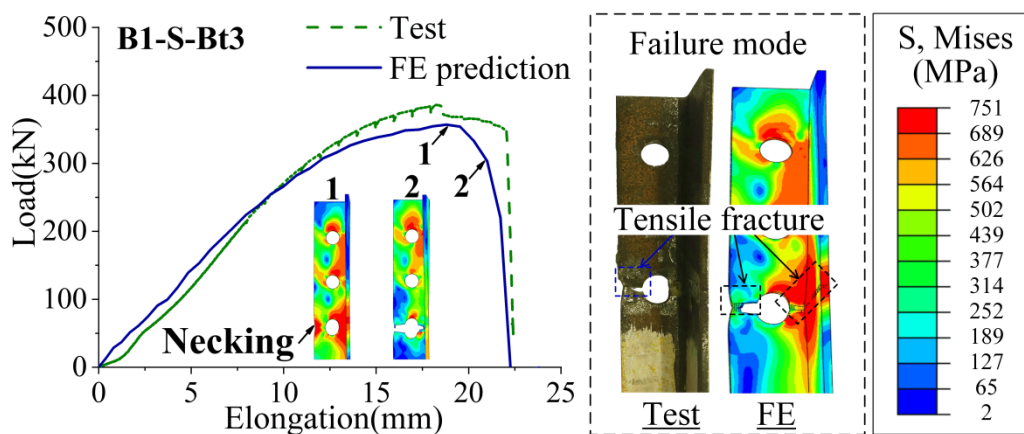
Fig. 7 Overview of finite element (FE) model.



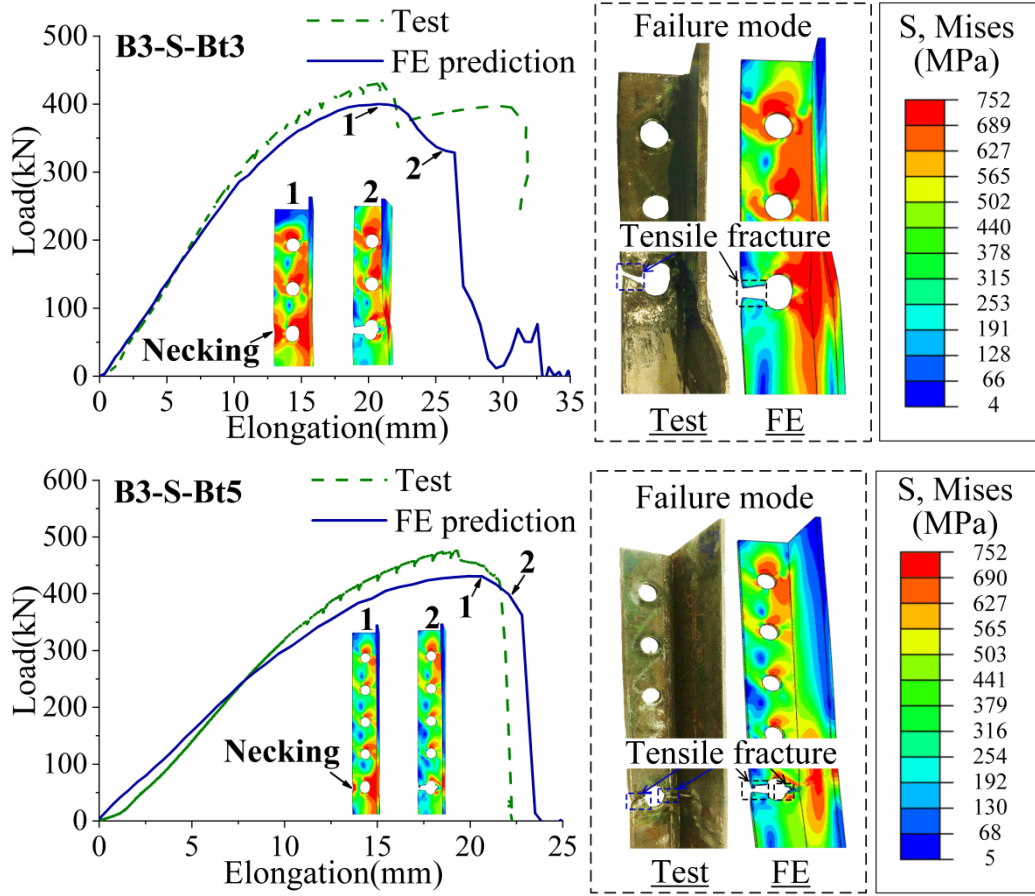
(a)



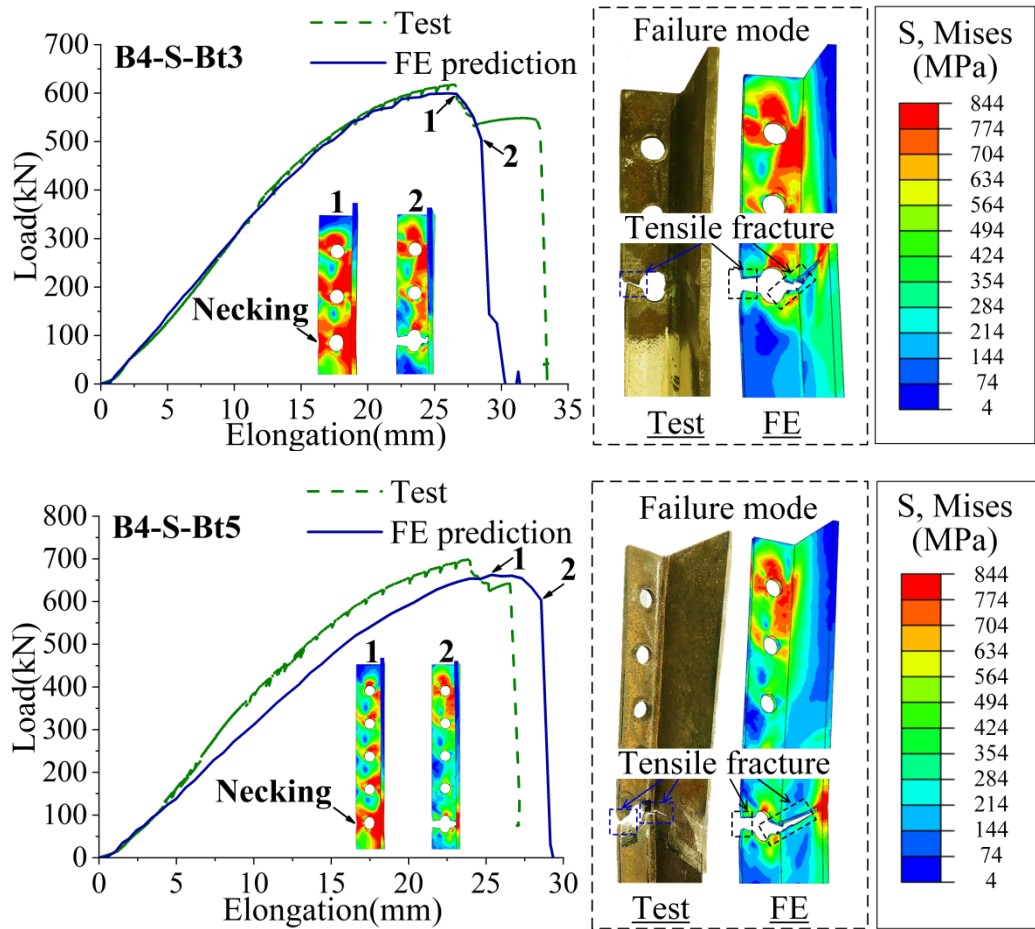
(b)



(c)



(d)



(e)

Fig. 8 Typical comparisons between test results and FE predictions: (a) A1 series, (b) A3 series, (c) B1 series, (d) B3 series and (e) B4 series.

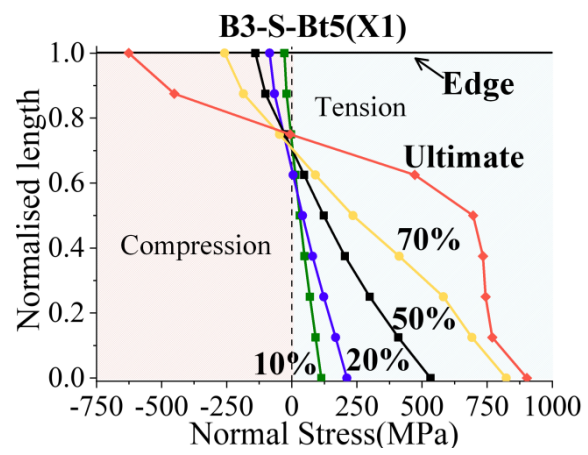
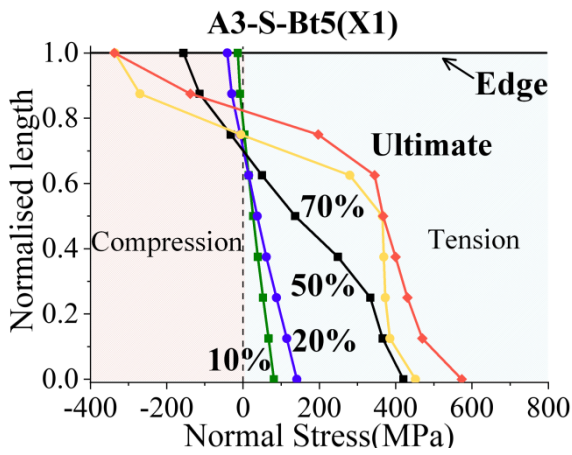
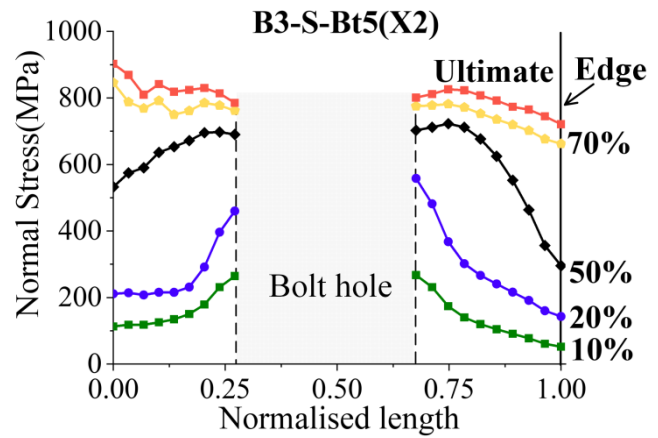
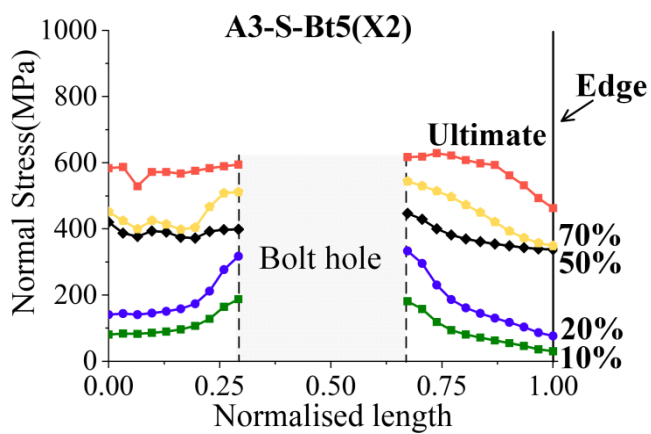
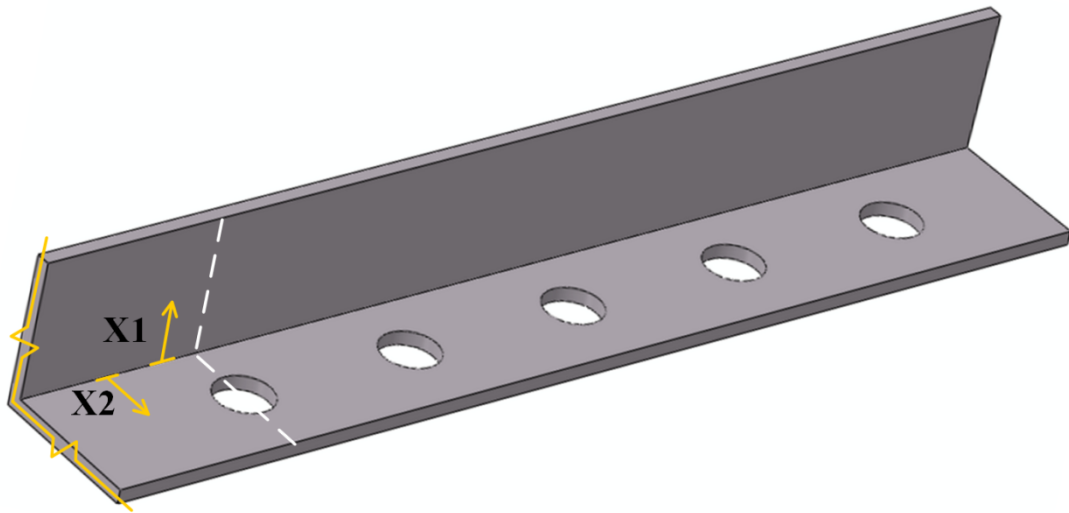


Fig. 9 Normal stress evolution at critical section of typical models.

Table 1 Specimen configurations, test resistance and predictions by finite element models

Specimen	*Dimension (mm)	Steel grade	Bolt No.	L_c (mm)	L_o (mm)	t (mm)	p (mm)	e_d (mm)	e (mm)	P_{test} (kN)	P_{norm}	P_{test}/P_{FE}
A1-L-Bt3	<u>85</u> ×65×6	S275	3	86.0	63.0	5.75	74.86	57.97	41.61	297	0.92	1.08
A1-S-Bt3	85× <u>65</u> ×6	S275	3	67.0	85.0	5.75	75.80	59.70	31.05	246	0.74	1.03
A2-E-Bt3	<u>65</u> ×65×6	S275	3	67.0	68.0	5.75	74.66	58.54	31.43	250	0.88	1.05
A2-E-Bt5	<u>65</u> ×65×6	S275	5	65.0	65.0	5.75	74.68	58.40	32.67	291	1.07	1.17
A3-S-Bt3	125× <u>65</u> ×6	S275	3	65.0	125.5	5.75	74.71	59.01	31.29	258	0.59	1.02
A3-S-Bt5	125× <u>65</u> ×6	S275	5	68.0	123.0	5.75	75.23	58.88	32.22	364	0.83	1.18
											Mean	1.09
											CoV	0.065
B1-L-Bt3	<u>85</u> ×65×6	S690	3	85.0	63.0	5.94	75.05	59.83	41.14	432	0.85	1.04
B1-L-Bt5	<u>85</u> ×65×6	S690	5	84.0	65.0	5.94	74.97	60.14	43.27	516	1.01	1.10
B1-S-Bt3	85× <u>65</u> ×6	S690	3	63.0	85.0	5.94	75.89	61.37	32.20	377	0.74	1.06
B1-S-Bt5	85× <u>65</u> ×6	S690	5	65.0	84.0	5.94	74.91	59.65	32.87	470	0.92	1.12
B2-E-Bt3	<u>65</u> ×65×6	S690	3	66.0	66.0	5.94	75.18	60.28	31.82	352	0.80	1.01
B2-E-Bt5	<u>65</u> ×65×6	S690	5	66.0	64.0	5.94	74.68	59.47	31.75	421	0.98	1.11
B3-S-Bt3	125× <u>65</u> ×6	S690	3	66.0	125.0	5.94	74.97	60.53	32.00	421	0.61	1.05
B3-S-Bt4	125× <u>65</u> ×6	S690	4	65.0	123.0	5.94	74.53	59.95	32.18	469	0.69	1.12
B3-S-Bt5	125× <u>65</u> ×6	S690	5	64.5	122.0	5.94	75.02	58.68	30.82	465	0.69	1.08
B4-S-Bt3	125× <u>65</u> ×8	S690	3	65.0	125.0	7.88	76.00	59.80	31.43	605	0.61	1.01
B4-S-Bt4	125× <u>65</u> ×8	S690	4	64.0	125.0	7.88	75.06	59.43	31.74	626	0.63	1.01
B4-S-Bt5	125× <u>65</u> ×8	S690	5	65.0	125.5	7.88	74.91	59.75	31.04	685	0.68	1.03
											Mean	1.06
											CoV	0.041

*The connected leg is underlined.

Table 2 Material properties

Material	Elastic modulus (GPa)	Yield stress f_y (MPa)	Tensile strength f_u (MPa)	Ultimate strain ϵ_u	f_u/f_y
S690 angle plate (6 mm)	185	640	715	0.061	1.12
S690 angle plate (8 mm)	200	770	800	0.060	1.04
S690 gusset plate (gusset plate)	195	705	730	0.060	1.04
S275 angle plate	195	310	470	0.163	1.52

Table 3 Design equations for net section resistance of tension members

References	Design equations
CSA S16-14 [46]	$P_{CSA} = \psi A_e f_u$ where P_{CSA} is the design rupture resistance for a tension member; ψ is the resistance factor; f_u is the ultimate tensile strength of steel and A_e is the effective area considered for shear lag. For angles connected by only one leg with four or more transverse lines of fasteners, $A_e = 0.80 A_n$, where A_n is the net area. In cases with fewer than four transverse lines of fasteners, $A_e = 0.60 A_n$.
AS4100-1998 [47]	The design resistance of a tension member is expressed as: $P_{AS} = \psi 0.85 k_t A_n f_u$ where ψ is the capacity factor; k_t is the correction factor for distribution of forces (i.e. shear lag effects), taken as 0.85 for equal leg angles and unequal leg angles connected by the long leg, or 0.75 for unequal leg angles connected by the short leg, or 0.9 for tee members; A_n is the net area of the cross-section, obtained by deducting from the gross area the sectional area of all penetrations and holes, including fastener holes and f_u is the ultimate tensile strength.
Eurocode3 Part 1-8 [48]	A single angle in tension connected by a single row of bolts in one leg may be treated as concentrically loaded over an effective net section for which the design ultimate resistance should be determined as follows: $2.0(e_2 - 0.5d_0) t f_u$ 1) with 1 bolt: $P_{EC3} = \frac{\gamma_{M2}}$ $\beta_2 A_n f_u$ 2) with 2 bolts: $P_{EC3} = \frac{\gamma_{M2}}$ $\beta_3 A_n f_u$ 3) with 3 or more bolts: $P_{EC3} = \frac{\gamma_{M2}}$ where β_2 and β_3 are reduction factors dependent on the pitch and A_n is the net area of the angle. For an unequal-leg angle connected by its short leg, A_n should be taken as equal to the net section of an equivalent equal-leg angle of leg size equal to that of the short leg; f_u is the ultimate tensile strength of the steel and γ_{M2} is the partial safety factors for resistance of bolts.
AISC 360-16 [49]	$P_{AISC} = \psi A_e f_u$ where P_{AISC} is the nominal axial strength; ψ is the resistance factor for tension rupture; f_u is the ultimate tensile strength of steel and A_e is the effective area of the member cross-section. For members with bolted connections, it is obtained from $A_e = U A_n$ where A_n is the net area of a member (i.e. the sum of the products of the thickness and the net width of each element) and U is the reduction coefficient, as given by $U = l - \bar{x} / l$ where \bar{x} is the eccentricity of the connection and l is the connection length.

Table 4 Performance of design equations

Specimen	$P_{\text{test}}/P_{\text{AISC}}$	$P_{\text{test}}/P_{\text{EC3}}$	$P_{\text{test}}/P_{\text{CSA}}$	$P_{\text{test}}/P_{\text{AS}}$	$P_{\text{test}}/P_{\text{Yam}}$
A1-L-Bt3	1.03	1.66	1.53	1.27	0.90
A1-S-Bt3	0.90	1.57	1.24	1.17	0.97
A2-E-Bt3	1.01	1.58	1.46	1.21	1.00
A2-E-Bt5	1.14	1.94	1.34	1.48	1.13
A3-S-Bt3	0.84	1.72	0.99	0.93	1.01
A3-S-Bt5	0.97	2.29	1.04	1.31	1.15
Mean	0.98	1.79	1.27	1.23	1.03
CoV	0.108	0.154	0.173	0.148	0.095
B1-L-Bt3	0.95	1.54	1.42	1.18	0.92
B1-L-Bt5	1.07	1.82	1.26	1.40	1.05
B1-S-Bt3	0.91	1.67	1.25	1.18	1.09
B1-S-Bt5	1.01	1.98	1.15	1.44	1.19
B2-E-Bt3	0.92	1.45	1.34	1.11	0.99
B2-E-Bt5	1.04	1.78	1.22	1.36	1.12
B3-S-Bt3	0.86	1.73	1.01	0.96	1.12
B3-S-Bt4	0.85	1.96	0.86	1.08	1.12
B3-S-Bt5	0.81	1.98	0.87	1.09	1.05
B4-S-Bt3	0.86	1.76	1.01	0.95	1.16
B4-S-Bt4	0.78	1.84	0.79	0.99	1.07
B4-S-Bt5	0.80	2.00	0.86	1.07	1.09
*P-A1-60L	0.96	1.79	1.12	1.24	0.95
*P-A1-75L	1.00	1.72	1.19	1.31	1.00
*P-A1-90L	0.99	1.58	1.18	1.31	0.98
*P-A1-75S	0.86	1.74	0.99	1.24	1.05
*P-A2-60S	0.82	1.95	0.88	1.10	1.05
*P-A2-75S	0.82	1.80	0.91	1.14	1.04
*P-A2-90S	0.81	1.68	0.92	1.16	1.04
Mean	0.90	1.78	1.06	1.17	1.06
CoV	0.100	0.087	0.175	0.122	0.065

*Specimens P-A1-60L, P-A1-75L, P-A1-90L, P-A1-75S, P-A2-60S, P-A2-75S and P-A2-90S refer to A1-60L, A1-75L, A1-90L, A1-75S, A2-60S, A2-75S and A2-90S in the previous test programme conducted by the authors and colleagues [32].

Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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