

The following publication Lau, P. K. W., Cheung, B. W. Y., Lai, W. W. L., & Sham, J. F. C. (2021). Characterizing pipe leakage with a combination of GPR wave velocity algorithms. *Tunnelling and Underground Space Technology*, 109, 103740 is available at <https://doi.org/10.1016/j.tust.2020.103740>.

1 ***Identifying Pipe Leakage with a combination of***
2 ***GPR Wave Velocity Algorithms***

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8

9 **Abstract**

10 Moisture content contained in any dielectric media is the most influential factor
11 reducing Ground Penetrating Radar (GPR) wave velocity, which can be measured
12 by the gradients of diffractive hyperbolas as a result of any round-shaped object,
13 such as water carrying utilities. Such characteristic were then used to estimate
14 location of pipe leak where moisture content is higher in localized area compared
15 to the neighbouring no-leak dry area (Cheung & Lai, 2019). However, depth of
16 utilities is required as a known input in the algorithms based on multiple triangular
17 ray paths using common offset antenna (Sham and Lai, 2016). In this paper, we
18 proposed a combination of velocity algorithm for estimation of velocity, followed
19 by water leak location where wave velocity is reduced compared to non-leak
20 location, without priori information of utility depth. The combination of velocity
21 algorithm was validated firstly using high-frequency 2GHz antenna in air, where
22 wave velocity is equal to speed of light. The second validation is two full-scale
23 studies of water leakage detection by the proposed velocity analytical approach
24 using a 600MHz GPR. Results of both studies substantiate the validity of a
25 combination of few velocity algorithms. It reveals the accurate estimation of pipe
26 seepage and leak location, as a result of 5-10% and 20-30% wave velocity
27 reduction, respectively. The algorithms and validation experiments are believed to
28 pave the way for large-scale applications.

29

1. Introduction

30 Hong Kong is one of the most densely populated cities in the world. It has a
31 complex underground utility network to support the daily life of seven million
32 citizens. Since rapid urbanization from earlier 1980s, various types of pressurized
33 pipes were buried including water main, rising main, cooling main and foul drain.
34 The condition of pipe was like most cities, an unknown mystery causing frequent
35 pipe burst. Water leakage accidents were brought to the attention of the public
36 because of its high frequency of appearance in media. According to water supplies
37 department (WSD, 2019), the leakage rate of government mains in underground
38 utilities is approximately 15%. Therefore, a comprehensive leak detection method
39 is essential to locate the leakage from a complex network of underground utilities
40 not only to achieve the sustainable use of water but also prevent the underground
41 hazards like the land subsidence.

42 Acoustic methods are traditional survey approach applied for locating water
43 leakage in pipe while Leak Noise Correlator (LNC) is an efficient way to determine
44 the leak position (Hunaidi et al, 2004). After the survey by LNC, mechanical leak
45 detector (MLD) can be used to confirm the leak point. The listening stick thus acts
46 as a waveguide to search for the high-pitch leak sound, but this method requires
47 specific experienced personnel to identify the actual leak point. Noting that
48 effectiveness of LNC is restricted by the pipe material like plastic pipe leaks since
49 plastic is a poor conductor of sound wave (Cabrera, 2003). Acoustic methods are
50 always interfered by the environmental and cultural noises which share the same
51 frequency bandwidths.

52 Apart from mapping the underground utilities, GPR, one of the widely used non-
53 destructive testing (NDT) technologies, is also considered as an effective way to

54 locate leak point of underground utilities with the use of various radar data
55 processing and visualization strategies (Cataldo et al., 2014; Cheung & Lai, 2018;
56 De Coster et al., 2019; Demirci, Yigit, Eskidemir, & Ozdemir, 2012; Hao et al.,
57 2011; Ocaña-Levario, Carreño-Alvarado, Ayala-Cabrera, & Izquierdo, 2018). It is
58 because water content is a dominant factor among nonmetallic materials which
59 attenuates GPR reflected signal amplitude and reduces wave's velocity particularly
60 the high-frequency (Lai et al., 2016). As the electromagnetic waves propagate
61 towards the materials, its velocity and amplitude are a function of relative dielectric
62 properties and electric conductivity (Milsom and Eriksen, 2011).

63 As water content slows down GPR wave propagation velocity and weakens its
64 amplitude, it can be used as a decisive indicator that depicts abnormal reflection
65 from water content along different GPR survey traverse. Thus, location of water
66 seepage or water leakage by GPR survey can be identified for further open-up
67 action. In this study, a novel velocity estimation combining three velocity
68 estimation equations has been developed by taking complicated triangular ray-
69 paths into account. The method was validated in a control experiment with air as a
70 homogeneous medium of wave velocity and applied in two case studies of water
71 leak detection.

72 **2. Methodology**

73 **2.1 Velocity measurement algorithm from diffractive hyperbola in** 74 **radargram**

75 The diffractive hyperbolas obtained in a radargram is a result of the spread of
76 downward conical footprint (or First Fresnel Zone) of the GPR wave penetrating
77 through a dielectric media and reach a round-shape target with significant dielectric

78 contrast with the host media. When the GPR dipoles/E-field direction is parallel to
79 the alignment of the utility, or the antenna traverse is perpendicular to the
80 alignment of utility in most ordinary common offset configuration, the utility will
81 appear as a diffractive hyperbola described by the equations in later section of this
82 paper. Gradient of the hyperbola carries the important information of wave velocity
83 that relates spatial and lateral position (x) to travel time (t) as shown in figure 1,
84 modeling the hyperbolic reflections accurately is essential in velocity analysis.
85 Most importantly, it indicates material wetness directly affiliated to pipe leak.

86 For common offset configuration of velocity estimation,

87 (a) Velocity measurement by stationary single point

88 The most simplified equation considers two-way travel time for estimating the
89 GPR wave velocity. It is only applicable when the depth of the object point or any
90 flat continuous surface is known.

$$91 \quad v = \frac{2D_0}{t} \quad (1)$$

93 where:

94 t = two-way travel time of the signal reflected from the object,

95 D_0 = depth of the reflected object.

96 (b) Velocity algorithm by single trilaterated method with a round-shaped reflector
97 as point-source target (ASTM D6432-2011)

98 This equation is being widely used in commercial software for hyperbolic fitting,
99 based on an assumption that pair of transmitting and receiving antennae, and the

100 target utility are all point sources. It follows that both antenna separation and size
101 of objects are not taken into account.

$$v(x_i) = \left(\frac{2}{t_0}\right) \left[\frac{x_i}{\sqrt{\left(\frac{t_i}{t_0}\right)^2 - 1}} \right] \quad (2)$$

104 where:

105 x_i = horizontal distance between the antenna at an oblique position 'i' to the
106 apex of hyperbola if the GPR traverse is perpendicular to the alignment of the
107 studied linear object,

108 t_i = two-way travel time of a reflection from an interface at antenna position 'i',

109 t_0 = two-way travel time of a reflection from an interface when the antenna is
110 directly on top of the utility.

111 (c) Velocity algorithm by multi-trilaterated ray-path method (only target as point
112 source)

113 Point-source assumption in method (b) is for the purpose of simplicity. In reality,
114 actual ray-path is more complicated and requires more understanding of the actual
115 geometry of the antennae (i.e. separation of transmitter and receiver), as well as
116 the second triangle (on-plane) existed between the GPR traverse and utility
117 alignment creating a non-right angle on plan. Therefore, by taking antenna
118 separation '2B' and oblique angle θ between traverse and utility alignment into
119 consideration, equation (3) is developed.

$$v(x_i) = \sqrt{\frac{2(x_i \sin \theta)^2 t_i \pm 2x_i \sin \theta ((x_i \sin \theta)^2 t_i^2 - 4B^2 t_i^2 + 4B^2 t_0^2)^{0.5}}{t_i^3 - t_0^2 t_i}} \quad (3)$$

122 where:

123 x_i = horizontal distance between the antenna at an oblique position ‘ i ’ to the
 124 apex of hyperbola,

125 θ = oblique angle between the pipe alignment and GPR traverse,

126 B = half of the antenna separation distance,

127 t_i = two-way travel time when GPR is oblique to object,

128 t_0 = two-way travel time when GPR is normal to object.

129 (d) Velocity algorithm by multi-trilaterated ray-path method and estimated cover
 130 depth D_0 and radius (Sham and Lai, 2016)

131 For even more accurate measurement of velocity, known depth (D_0) and radius (r)
 132 of the object are further considered according to Sham & Lai, (2016); Xie et al.
 133 (2018), in addition to the factor of antenna separation and angle in equation (3) as
 134 shown in the programming platform in figure 2 and figure 3.

135

$$v(x_i) = \sqrt{\frac{\left[\left[(D_0+r) - \frac{(D_0+r)r}{\sqrt{(D_0+r)^2 + (x_i \sin \theta)^2}} \right]^2 + \left[x_i - \frac{r(x_i \sin \theta)}{\sqrt{(D_0+r)^2 + (x_i \sin \theta)^2}} - B \right]^2 + \left[(D_0+r) - \frac{(D_0+r)r}{\sqrt{(D_0+r)^2 + (x_i \sin \theta)^2}} \right]^2 + \left[x_i - \frac{r(x_i \sin \theta)}{\sqrt{(D_0+r)^2 + (x_i \sin \theta)^2}} + B \right]^2}{t_{x_i}}}$$

137 (4)

138 where:

139 x_i = horizontal distance between the antenna at an oblique position 'i' to the
140 apex of hyperbola

141 θ = oblique angle between the pipe alignment and GPR traverse,

142 D_0 = estimated depth of the object from equation (1) & (3),

143 r = radius of object

144 B = half of the antenna separation distance,

145 t_{x_i} = two-way travel time when GPR is oblique to object,

146 t_0 = two-way travel time when GPR is normal to object.

147 Table 1 summarizes the parameters for velocity measurement method which is
148 discussed in this section. Whilst object size (radius 'r') can be obtained in record
149 drawings, antenna separation (two times 'B') is known in manufacturer's menu
150 and angle (' θ ') can be measured after observing the grid direction and utility
151 alignment in 3D imaging, depth (' D_0 ') is not available most of the time. It is also
152 a paradox for estimating velocity through known depth, while depth of the utility
153 is, in itself, the purpose of the survey. The combination of algorithms solves this
154 problem by combining the above few equations so that the both velocity and depth
155 can be estimated. Note that the outlier of velocity data are all filtered by setting a
156 standard deviation limit to 0.01m/ns (10% of normal velocity in soil, i.e. 0.1m/ns)
157 and velocity data points larger than 0.2998 m/ns (speed of light) are treated as
158 invalid outlier. The reason of doing this is to eliminate the velocity outlier
159 calculated due to the relatively unreasonable small difference of time of flight
160 between the apex and location close to the apex of the hyperbola. In other words,
161 the setting of the limit was made purposely for calculating velocity profiles on the

162 locations much away from the apex of the hyperbola, or the diffractive and
163 relatively linear part of the hyperbola. Note also that the process of elimination was
164 done separately on the left and the right side of the hyperbola. Therefore if velocity
165 values between the left and right side of the hyperbola are different, the overall
166 reported standard deviation will exceed the 0.01 m/ns threshold.

167 As shown in figure 4, the proposed combination of velocity measurement method
168 is a new approach for estimating GPR wave velocity by substituting mean of $v(x_i)$
169 in equation (3) into V in equation (1) to estimate D_0 then substitute the estimated
170 D_0 in equation (4) to re-calculate $v(x_i)$ and D_0 . Not also in this paper, the effect of
171 oblique angle ($\sin \theta$) does not affect velocity estimation in equation (3) and (4)
172 because the GPR traverse is always perpendicular to the alignment of the buried
173 linear object, which makes $\sin(90^\circ)$ is always equal to 1.

174 **2.2 Velocity validation in air**

175 Validation test in a known environment and controllable manner is crucial for any
176 new proposed algorithm. As GPR wave travels in speed of light (0.2998m/ns) in
177 homogeneous medium - air, the air-steel verification test can evaluate the
178 constituency of the proposed velocity analytical method combining equation (1),
179 (3), (4) by comparing the percentage error of resulted velocity with the velocity
180 from equation (3) standalone only and equation (4) using model answer of known
181 object depth. As shown in figure 5, a 2GHz antenna was used for the calibration of
182 wave velocity in air as the media for radar signal transmission. A wooden board
183 (for running GPR traverse) and a Y25 steel bar were placed inside a rack so that
184 the distance between the GPR antenna and the Y25 steel bar could be adjusted (i.e.
185 300mm and 400mm). The GPR antenna was moved perpendicularly to the Y25

186 steel bar and the radargram of the traverse was used for velocity analysis (Sham
187 and Lai, 2016). The analysis was done by measuring the velocity of the reflected
188 wave at different depths with a 2GHz antenna using the proposed GPR wave
189 velocity analytical method.

190 As shown in figure 6, the calculated discrete velocity using the proposed
191 combination of velocity algorithms involving equation (1), (3), (4) are more
192 consistent than those obtained from only equation (3). It is evident in Table 2, that
193 the velocity from equation (1), (3), (4) are more concentrated in the range of 0.29
194 - 0.3m/ns which is an ideal wave velocity in the air with reference to the constant
195 line of the speed of light.

196 In 300mm target depth, result from equation (3) underestimates the GPR wave
197 velocity by 10% compared to the speed of light, while result from the combination
198 of velocity algorithms yields only 1% less than the speed of light, and equation (4)
199 with model answer of object depth measured by tape as input can give a zero-error
200 result. In 400mm target depth, the estimated velocity from equation (3) is still
201 underestimated by 9%, but the combination of velocity algorithms can give a zero-
202 error result, and the equation (4) underestimates the velocity by 1%.

203 Concerning the standard deviation of the velocity data points, in 300mm depth, the
204 proposed velocity algorithm with 0.0009m/ns is smaller than 0.0500m/ns from the
205 equation (3) but larger than 0.0007m/ns from equation (4). In 400mm depth, the
206 proposed velocity analytical method with 0.0003m/ns is smaller than both
207 0.0481m/ns from equation (3) and 0.0011m/ns from equation (4). Such small errors
208 suggest that the velocity algorithms give highly accurate estimation of GPR wave
209 velocity in the validation test.

210 **2.3 Validation in two field experiments**

211 Before using the datasets for further velocity analysis as case studies. All datasets
212 should be post-processed to enhance the overall image quality of the
213 radargram. After standard data processing according to LSGI (2019), the
214 radargrams are processed by the new velocity algorithm programmed in the
215 inhouse LabVIEW program shown in figure 2 (Sham & Lai, 2016). Then, the 2D
216 velocity profiles were generated afterwards after applying a moving average filter.

217 **Case study 1 - controlled field experiment in Shek Mun, Hong Kong**

218 The first case study makes use of datasets collected in a controlled-water leakage
219 experiment. Cheung & Lai (2019) makes use of only equation (4) to validate the
220 proposed velocity algorithm. This paper makes use of the same set of data but adopt
221 equation (1), (3) and (4) for velocity estimation. The experiment setup simulates a
222 controllable progression pattern of water-leak scenario from smaller seepage to
223 leak given that the location of the pre-defined drill hole and displaced joint were
224 known, and the same datasets surveyed by IDS RIS MF HiMod 600MHz central
225 frequency GPR with profile spacing of 0.5 m , were used to check whether the
226 same leak point can be pinpointed by the combination of velocity algorithms and
227 its consistency of measurement.

228 The field experiment was set up in On Muk Street, Shek Mun, Hong Kong where
229 the site is divided into two parts: reinforced concrete slab and block paver
230 constructed as shown in figure 7 according to construction guideline of pedestrian
231 walkways from Highways department, HKSAR Government (Highways Standard
232 Drawing H1102B, 2014; Highways Standard Drawing H1103F, 2014; Highways
233 Standard Drawing H6168, 2014). A 200mm ductile iron pipe was buried with

234 0.59m depth in a relatively flat ground without change of depth. (Lai et al.,2018;
235 Cheung & Lai, 2019)

236 According to Figure 7, a total of four leak point was predefined on site. When water
237 being injected into the pipe, water leak from these points and spread out to the
238 surrounding soil. Since the depth of the pipe (D_0) in this case study was measured
239 from on-site measurement. The following velocity analysis implemented equation
240 (4) which required a given D_0 as input (Cheung & Lai, 2019). Figure 8 shows the
241 level of velocity drop across the two paving materials which is concrete paving and
242 block paving. In concrete paving, the velocity drops are 14% and 22% in leak point
243 X2 and X14, respectively. While in block paving, the velocity drops are 5% and
244 2% in leak point X26 and X37, respectively.

245 By implementing the proposed combination of velocity algorithms which
246 combines equation (1), (3), (4), D_0 is not required for the velocity analysis. The
247 results show a 9% of velocity drop and 4% of velocity increase in leak point X2
248 and X14. While for block paving, 7% of velocity increase in leak point X26 and
249 velocity drop of 6% in leak point X37 as shown in figure 8. In Figure 9, it is evident
250 that the range of standard deviation (i.e. the error) of each velocity measurement
251 after leak is higher than that before the leak. It is because of the increasingly
252 heterogenous environment causing more scattering and absorption of GPR wave,
253 hence distorting the original intact shape of hyperbolic tails in the case before leak.
254 In addition, there is no significant difference between the use of the two algorithms,
255 i.e. equation 3 alone and combined equation 1, 3 and 4.

256

257 **Case study 2: real case in Island Road, Hong Kong**

258 The site is located in Island Road, Deep Water Bay, Hong Kong (Figure 10), where
259 a 300m long ductile iron and pressurized rising main with 450mm diameter was
260 reported that the pressure of upstream pump station dropped from 3 bars to 1.5 bars.
261 The drop of pressure indicated that there is potential leak point along the pipe. All
262 acoustic methods including leak noise correlator and listening stick had been used
263 but were in vain. In this study, IDS RIS MF HiMod 600MHz central frequency
264 GPR with profile spacing of 1m and GPR velocity analysis method was used to
265 detect the water leakage point of raising main in Island Road, after both secondly
266 2D radargram velocity analysis and firstly 3D GPR time slice visualization and
267 finally the leak point was successfully found and confirmed by open up.

268 Firstly, 3D time slice imaging was conducted according to the 3D process flow in
269 Luo et al. (2019) and shown in Figure 11. A continuous reflection of the rising
270 main had been observed from the top view of the 3D time slice, but it is obvious
271 that there is weaker amplitude at point A (811562m Northing in Hong Kong 1980
272 coordinates system) as reflected energy is mostly absorbed by the water content
273 surrounded the leak point. Secondly, based on the same set of data processed with
274 time slice, the combination of velocity algorithms was used to give velocity profile
275 across the hilly terrain.

276 The result shows that GPR wave velocity dropped significantly around the actual
277 leak point (818562m northing) confirmed by open-up trial pit, as shown in figure
278 12. The profile of velocity forms a cave shape. By comparing lateral wave velocity
279 from individual radargram with the mean velocity throughout the whole GPR
280 traverse, obvious percentage difference of wave velocity was observed. The high
281 percentage of velocity drop compared to the mean velocity, indicates that a
282 significant accumulation of water slows down the wave velocity up to 30% as

283 shown in top of figure 12. It is an important indicator which shows the water
284 content around the leak point slows down the GPR wave velocity and explicitly
285 suggests the location of leak point.

286

287 **3 Discussion**

288 **3.1 30% velocity changes as leak indicator**

289 By measuring the velocity of the host material velocity analysis of host material
290 (i.e. soil) on top of the target object (i.e. pipe), the overall velocity distribution
291 should be a constant with relatively stable velocity profile in a no-leak pipeline. As
292 reduction of velocity is a common indicator to prove the increase of water content
293 in the soil as the GPR wave propagation was retarded, leak points can be identified
294 by pinpointing the area that shows around 30% of velocity drop as shown in figure
295 12 in case study 2. The only unresolved matter is how to measure it correctly. This
296 work provides a reliable algorithms and data collection methods in this regard.

297 **3.2 Constituency of the combination of velocity algorithms**

298 The study reveals the consistency of the proposed velocity algorithm in identifying
299 water leakage by GPR. In case study 2, it is worthwhile to note the standard
300 deviation of velocity data points along the pipe drops from 0.013m/ns to 0.002m/ns
301 which is 88% less than equation (3) standalone after implementing the proposed
302 combination of velocity algorithms involving equation (1), (3) and (4) as
303 mentioned. The smaller standard deviation of the proposed method implies that the
304 mathematical model for estimating the velocity is more consistent and it can result
305 in a more consistent velocity profile.

306

4 Limitations

307 There are still three limitations in the analysis for pinpointing water leak due to
308 the selected region of interest (ROI) and assumption of constant wave velocity.

309 **4.1 Scattering effect on wave velocity estimation**

310 From case study 1, the error bars show that the overall standard deviation of wave
311 velocity after water leak is much larger than that before water leak. This can be
312 explained by scattering effect of various grain sizes in soil of inhomogeneity. Since
313 distribution of water content further intensifies the original inhomogeneity of the
314 host environment resulting in change of the triangular ray-paths. Thus, the resulted
315 hyperbolas are further distorted which affected the overall standard deviation of
316 the estimated velocity in the measurement.

317 **4.2 Incomplete hyperbolas within region of interest (ROI)**

318 The proposed algorithm relies on the selection of the region of interest (ROI)
319 containing the full targets' hyperbolic reflections. Any distortion of the hyperbola
320 caused by deviation of ray-paths results in a significant standard deviation of the
321 estimated velocity. In some cases, even only one side of the symmetric hyperbola
322 is available. As a result, a single side of hyperbola does not work as the algorithm
323 requires a good definition of the location of hyperbolic apex. As the peak time is
324 designed to be automatically picked by comparing the two-way travel time of each
325 independent data points on the two sides of the hyperbola, single-sided hyperbola
326 requires manual picking of hyperbolic apex. Such pick can be an arbitrary and
327 operator-dependent process.

328 In reality, the scattering effect and attenuations of the GPR signal will distort the
329 target hyperbola. Those noises and disturbances can be caused by:

- 330 i) The neighboring underground utilities including those metallic and
331 non-metallic pipes, similar to the limitation 4.1
- 332 ii) Individual scatterers such as gravels and pebbles whose sizes are
333 comparable to the GPR wavelength
- 334 iii) Attenuation of the radar pulse reducing signal to noise ratio for
335 recognition of the hyperbolas

336 **4.3 Assumption of constant wave velocity**

337 All velocity algorithms mentioned assume constant GPR wave velocity within the
338 medium between the GPR antenna and the target objects. In reality, the engineering
339 structure of the ground is always in different layers and are likely subject to uneven
340 compaction of the back-fill materials affecting wave velocity. Therefore, the
341 estimated GPR wave velocity is subject to variation between concrete, block paver
342 and soil layers at different depths, but it is assumed homogeneous in the algorithms.

343 **5 Conclusion**

344 This paper provides solutions in two aspects. Firstly, it has been well-known that
345 GPR wave velocity is dependent on material properties like water content. This
346 paper modifies the algorithm by combining the computation of diffractive
347 hyperbolas. Advantage is on one hand, taking into account the complicated
348 trilaterated ray-path due to antenna separation, object size, angles between antenna
349 B-field polarization and object alignment. On the other hand, object's cover depth
350 is no longer required as an input parameter. Secondly, such algorithm can be used
351 to locate water leak point with high level of confidence. It is believed that these
352 two aspects will benefit the scientific and engineering committees, that GPR is not
353 only an object mapping tool, but also an useful diagnostic tool of city underground.

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