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# A Three-Phase Single-Stage AC-DC Wireless-Power-Transfer Converter with Power Factor Correction and Bus Voltage Control

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**Abstract**—Wireless power transfer technology has been a research and industrial hotspot with applications in many areas, such as wireless electric vehicle charging system which requires high power, high efficiency and high power factor. Usually, the power is drawn from 50/60 Hz single-phase or three-phase AC power source. For a high power application, a three-phase AC source is commonly used. In this paper, a three-phase single-stage wireless-power-transfer resonant converter with power factor correction and bus voltage control is proposed to improve efficiency and power quality of three-phase input, and reduce production cost and complexity for high power wireless-power-transfer system. A T-type topology is applied as the common part to perform both the power-factor-correction and DC-DC wireless-power-transfer functionalities simultaneously. The proposed converter is much more advantageous than conventional three-phase two-stage wireless-power-transfer converter with individual power factor corrector. Besides, three-phase single-stage topologies have better power quality than single-phase single-stage topologies because zero-sequence components can be naturally eliminated.

**Index Terms**—wireless power transfer, three-phase, single-stage, power factor correction

## I. INTRODUCTION

WIRELESS Power Transfer (WPT) is taking up more and more roles in the industrial community. WPT technology has a variety of applications with power levels ranged from several milliwatts to tens of kilowatts, including charging portable telephone [1], supplying power for biomedical implants [2] – [4], electric vehicle (EVs) battery charging [5], [6], and roadway powering moving EVs [7], [8]. Compared to conventional wired power transmission, WPT technology is

much more advantageous: convenient, safe, and reliable. Inductive coupling method [1], [2], [6] – [15], as a traditional WPT technology, has been researched for a long time and is a very efficient way to deliver power wirelessly within a short distance. However, power and efficiency drop severely if transfer distance extends or there is a misalignment between transmitter and receiver. Another efficient WPT technology for mid-range transfer, magnetic resonant coupling approach [16] – [21], proposed and demonstrated by MIT in 2007 [22], attracts much interest from researchers in recent years, due to its high efficiency and relatively longer transfer distance. This approach utilizes resonance characteristic of coupled primary and secondary resonant tanks under a specific frequency to achieve WPT efficiently.

For a three-phase isolated AC-DC converter, if power factor and THD of input current are not considered, usually a three-phase diode-bridge rectifier followed by an isolated DC-DC converter will be used, as shown in Fig. 1. However, a modern three-phase AC-DC switching-mode power supply (SMPS) is required to maintain a good power quality of input source and consists of two power conversion stages: a front-end three-phase AC-DC power-factor-correction (PFC) rectifier as the first stage, and an isolated DC-DC converter as the second stage, as shown in Fig. 2. Usually three-phase six-switch PFC rectifier [23], [24], Vienna rectifier [25], TAIPEI rectifier [26], or other type of three-phase PFC rectifier [27] – [29] is used as the first stage while the second stage can be many kinds of isolated DC-DC converters, including flyback, forward, full-bridge, half-bridge, phase-shift, and LLC resonant converters. The SMPS with such two-stage configuration is called as three-phase two-stage AC-DC topology, each stage of which has their independent active switches and control schemes. Generally, a three-phase two-stage topology needs two control strategies for both stages, which obviously increases the control complexity of the system. What's more, such two-stage topology cannot achieve its highest efficiency due to more power losses in the two-stage conversion. Moreover, it is not with the lowest cost because two-stage conversion means more components.

In recent years, three-phase single-stage AC-DC topologies [30] – [37] that integrate both AC-DC PFC rectifier and DC-DC conversion into only one power conversion stage have been proposed to overcome the drawbacks mentioned above. Such single-stage topology utilizes common active switches

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and control scheme to realize PFC and isolated DC-DC conversion functionalities simultaneously, as shown in Fig. 3 (a), and Fig. 3 (b) shows one type of three-phase single-stage AC-DC topology, the single-stage TAIPEI rectifier, proposed in [37], where active switches  $Q_1$  and  $Q_2$  are commonly used for both PFC rectification and isolated DC-DC conversion simultaneously. Because of using common active switches and one control scheme, both characteristics of PFC rectifier and isolated DC-DC converter need to be investigated in depth. Not all the PFC rectifiers and isolated DC-DC converters can be randomly integrated into a single-stage topology. In Fig. 3 (b), since the TAIPEI rectifier requires varying-frequency control scheme, the operation frequency of the full-bridge DC-DC converter is also varying in a wide range.

Most of the state-of-the-art single-stage topologies are focused on transformer-based isolated power conversion while there is few for WPT application. Two three-phase single-stage AC-AC matrix converters were proposed for WPT application [38], [39]. However, they utilized 7 and 8 active switches respectively, and their power qualities are not good enough. Also, a single-phase AC-AC matrix converter was proposed for WPT application [40], but 12 active switches are used. A single-phase single-stage AC-DC WPT converter was proposed in [41], however, since its single-phase topology, its power

quality is not as good as that of three-phase single-stage topology and its bus voltage is too high at low load condition. The reason that three-phase topology exhibits much better performance of PFC than the single-phase topology is that the former can naturally eliminate zero-sequence harmonics of input current by using an artificial neutral point of the input filter [32], especially for third-order harmonic. As shown in Fig. 3 (c), there is no path for the zero-sequence components to flow into the three-phase source. Instead, such components circulate through the capacitors of the input filter. Furthermore, single-phase topologies are not as suitable as three-phase topologies when high power WPT system is required.

In this paper, the concept of three-phase single-stage AC-DC topology is newly proposed to apply in WPT system: a three-phase single-stage AC-DC WPT resonant converter with PFC, as shown in Fig. 3 (c), where three-level T-type topology is simultaneously used for PFC rectification and DC-DC WPT conversion. Compared with the single-stage TAIPEI AC-DC converter in Fig. 3 (b) and the two-stage TAIPEI and half-bridge AC-DC converter in Fig. 2 (c), although the counts of active switches are the same, the proposed three-phase single-stage AC-DC WPT resonant converter with PFC is much more advantageous. Firstly, the topologies in Fig. 2 (c) and Fig. 3 (b) make the input EMI filter hard to design and its

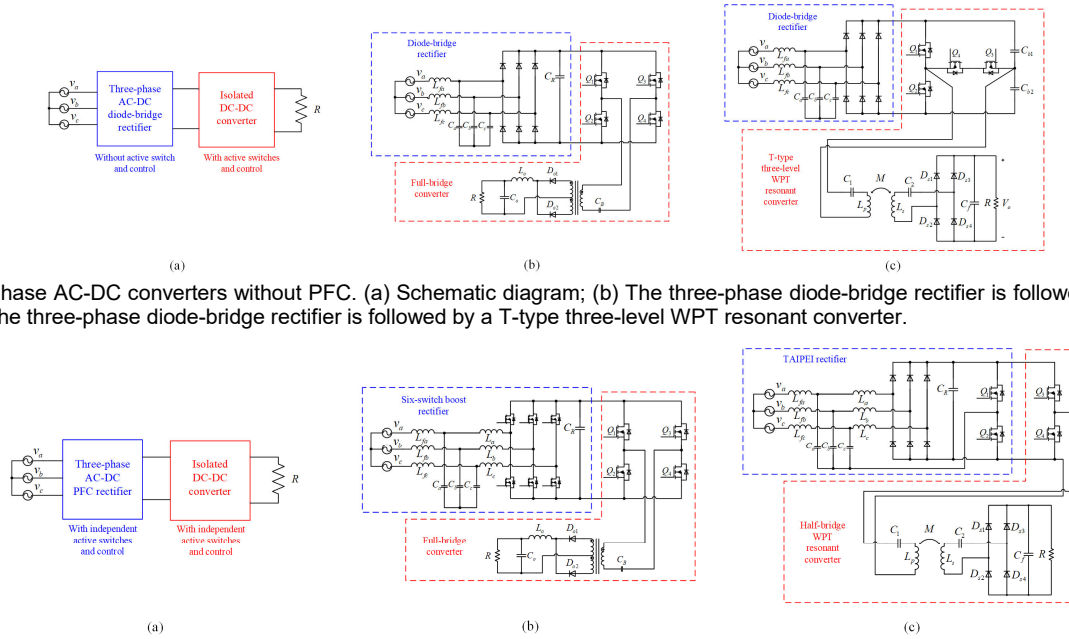


Fig. 1. Three-phase AC-DC converters without PFC. (a) Schematic diagram; (b) The three-phase diode-bridge rectifier is followed by a full-bridge converter; (c) The three-phase diode-bridge rectifier is followed by a T-type three-level WPT resonant converter.

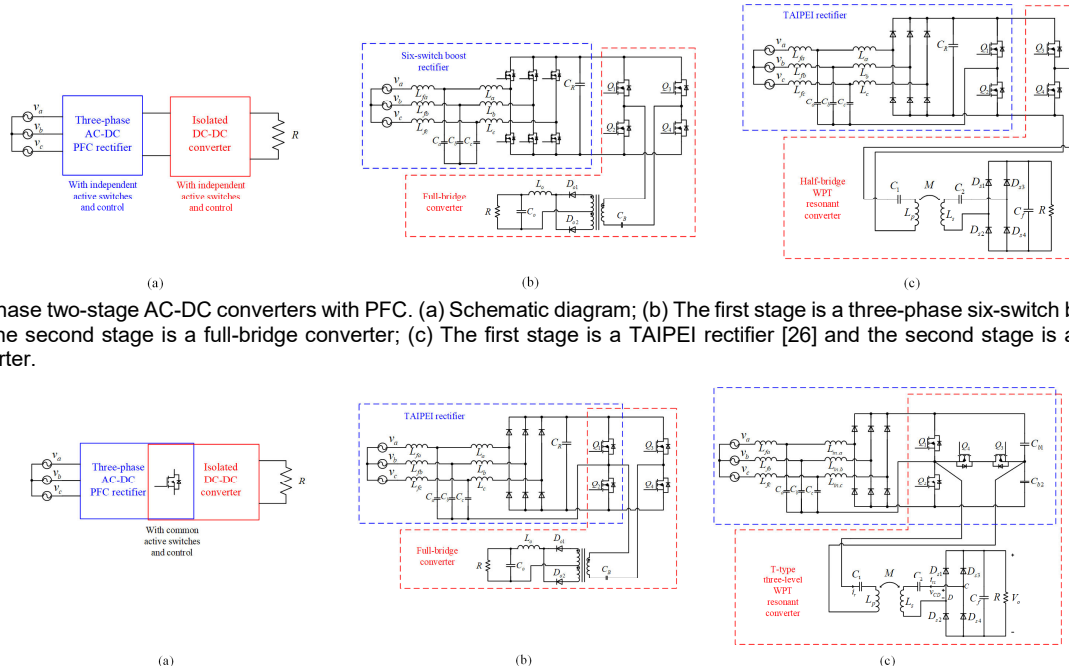


Fig. 2. Three-phase two-stage AC-DC converters with PFC. (a) Schematic diagram; (b) The first stage is a three-phase six-switch boost PFC rectifier [23], [24] and the second stage is a full-bridge converter; (c) The first stage is a TAIPEI rectifier [26] and the second stage is a half-bridge WPT resonant converter.

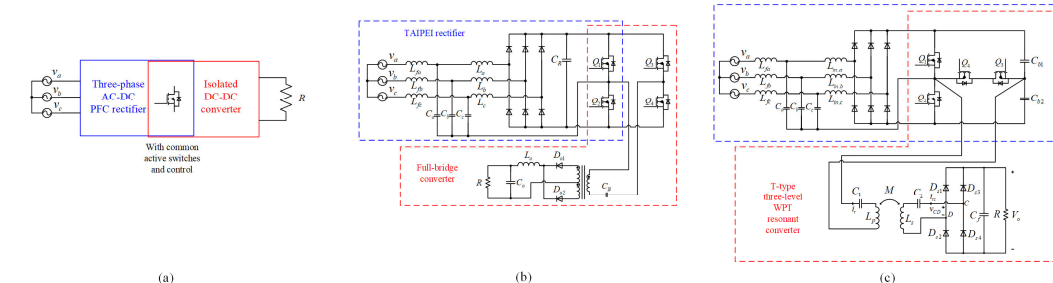


Fig. 3. Three-phase single-stage AC-DC converters with PFC. (a) Schematic diagram; (b) The single-stage TAIPEI rectifier [37]; (c) Proposed three-phase single-stage AC-DC WPT resonant converter with PFC.

volume large because of wide-range varying-frequency operation. Secondly, the second-stage half-bridge converter in Fig. 2 (c) is not so suitable for the WPT system because it generates asymmetric two-level square wave into the WPT resonant tank when the duty cycle is regulated, which brings about the even-order harmonics, increases the total harmonics and causes severer EMI problem. Thirdly, the varying-frequency control scheme of the single-stage TAPEI topology in Fig. 3 (b) cannot be applied to the WPT system since the efficiency of the WPT system is sensitive to operation frequency and will drop dramatically when operation frequency deviates from its resonant frequency. Fourthly, voltage stresses of the two middle-side switches of the proposed topology are only half of the bus voltage, and therefore the cost of switches can be reduced significantly compared with the two topologies in Fig. 2 (c) and Fig. 3 (b).

Compared with the topology without PFC in Fig. 1 (c), the proposed topology only requires three more input inductors and one line to connect the artificial neutral point with the middle point of switches  $Q_1$  and  $Q_2$ . The advantages and contributions of the proposed converter are summarized as follows:

- This work is the first time to apply three-phase single-stage AC-DC PFC topology in WPT application. Compared with two-stage topologies for WPT, the proposed converter utilizes a minimum count of power semiconductor devices and exhibits higher efficiency.
- The bus voltage is reduced and controlled constantly, which is very important because the bus voltage will not be excessively large and the effect of PFC can be optimized.
- Its operating frequency is within a small range of variation (around 6% variation during full load range), so that it can be considered as quasi-constant frequency operation, which is suitable for WPT applications and make input EMI filter design easier and with a smaller volume.
- T-type topology is used as the three-level converter, which is capable of simultaneously performing the functionalities of the AC-DC PFC rectification and the DC-DC WPT conversion. Compared with three-level NPC converter, two diodes and one flying capacitor are eliminated, and less isolated driver power supplies are used. Also, it is capable of generating a three-level symmetric square wave for the WPT resonant tank and reducing the higher-order harmonics.

In this paper, topology description and analysis, power factor (PF) and total harmonics distortion (THD) analysis, ZVS conditions, power loss analysis, control method and circuit operation of the proposed converter are presented. Then, the design procedure and example are proposed. Finally, an experimental prototype is implemented to verify the analysis and design.

## II. PROPOSED TOPOLOGY

### A. Topology description

Fig. 3 (c) shows the proposed novel topology. Firstly, a three-wire three-phase voltage source connects with an input filter for filtering the high-frequency components and zero-sequence components of three-phase currents. Followed by the input filter are three input inductors (with the same values), three diode-legs (6 diodes), and a T-type inverter (four

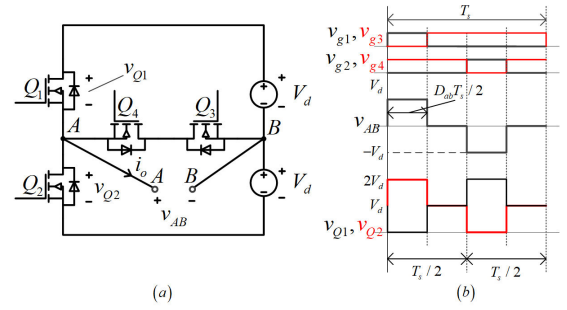


Fig. 4. (a) T-type three-level high frequency inverter; (b) Modulation waveforms of the T-type inverter, where  $V_d$  is equivalent DC voltage source.  $v_{Q1}$  and  $v_{Q2}$  are drain-source voltages of  $Q_1$  and  $Q_2$ , respectively.

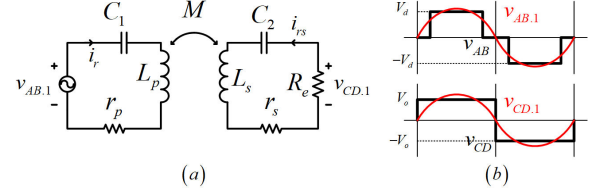


Fig. 5. (a) Equivalent circuit of series-series WPT topology; (b) input voltage and output voltage ( $v_{AB}$  and  $v_{CD}$ ) of the resonant tank and their fundamental components ( $v_{AB,1}$  and  $v_{CD,1}$ ).

switches and two bus capacitors), which are formed together to perform the three-phase PFC functionality. The T-type inverter also connects a resonant tank (resonant capacitors and inductors of primary and secondary side), a secondary-side diode rectifier bridge, an output filtering capacitor, and a load resistor, to perform DC-DC WPT conversion functionality.

### B. Wireless-power-transfer conversion stage

#### 1) T-type three-level high-frequency inverter

Fig. 4 (a) shows the T-type three-level high-frequency inverter, with high-side MOSFET  $Q_1$ , low-side MOSFET  $Q_2$ , middle-side MOSFETs  $Q_3$  and  $Q_4$ . The output voltage of this converter,  $v_{AB}$ , can be configured to be a three-level waveform. By the modulation method shown in Fig. 4 (b), the duty ratio of  $v_{AB}$ ,  $D_{ab}$  (ratio of non-zero voltage in a switching period  $T_s$ ) is adjustable and output current  $i_o$  commutates naturally despite its direction [42]. Compared to full bridge inverter, voltage stress of  $Q_3$  and  $Q_4$  reduces to half of the bus voltage while conduction loss when  $v_{AB}$  is positive or negative also reduces significantly. Compared to three-level NPC inverter, simpler modulation method, less semiconductor number, less conduction loss, and less isolated driver power supplies are the significant advantages of the T-type inverter [42].

#### 2) Analysis of the DC/DC WPT converter stage

A T-type three-level inverter, a series-series resonant tank, a secondary-side bridge rectifier, a filtering capacitor  $C_f$  and load resistor  $R$  are connected to form a DC/DC WPT converter. The resonant tank includes primary inductor  $L_p$  and capacitor  $C_1$ , secondary inductor  $L_s$  and capacitor  $C_2$ .  $M$  is the mutual inductance of  $L_p$  and  $L_s$ . Fig. 5 (a) shows the equivalent circuit of the DC/DC WPT converter for theoretical analysis, and  $r_p$  is total equivalent series resistance (ESR) of  $C_1$  and  $L_p$ , and  $r_s$  is that of  $C_2$  and  $L_s$ . To analyze the DC characteristics, First Harmonic Approximation (FHA) method [41], [43], assuming the voltage and current of the resonant tanks to be their fundamental components, is applied:

$$v_{AB} \approx v_{AB,1} = (4/\pi) \cdot V_d \sin(D_{ab} \cdot \pi/2) \cdot \sin(\omega_s t + \alpha), \quad (1)$$

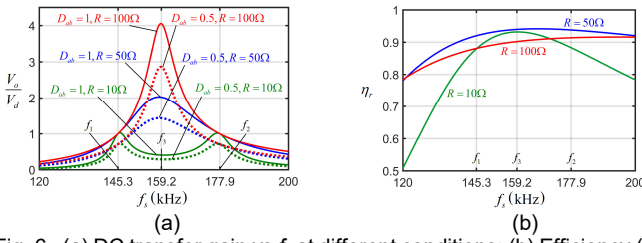


Fig. 6. (a) DC transfer gain vs  $f_s$  at different conditions; (b) Efficiency ( $\eta_r$ ) vs  $f_s$  at different load conditions. The specifications are:  $L_p=100\ \mu\text{H}$ ,  $L_s=100\ \mu\text{H}$ ,  $M=20\ \mu\text{H}$ ,  $C_1=10\ \text{nF}$ ,  $C_2=10\ \text{nF}$ ,  $r_p=0.5\ \Omega$ ,  $r_s=0.5\ \Omega$ .

$$v_{CD} \approx v_{CD,1} = (4/\pi) \cdot V_o \sin(\omega_s t + \beta), \quad (2)$$

$$i_r \approx I_{rp} \sin(\omega_s t + \theta), \quad (3)$$

$$i_{rs} \approx I_{rsp} \sin(\omega_s t + \delta). \quad (4)$$

Here  $V_d$  is half of the DC bus voltage, and  $D_{ab}$  is duty ratio of  $v_{AB}$ , as elaborated in the last section.  $V_o$  is the output voltage of the proposed topology.  $I_{rp}$  and  $I_{rsp}$  are peak values of currents through primary and secondary resonant tanks, respectively.  $\alpha$ ,  $\beta$ ,  $\theta$ , and  $\delta$  are phase angles.  $\omega_s$  is operating frequency in radian. Applying Kirchhoff's Voltage Law to the simplified equivalent circuit as shown in Fig. 5 (a), the following equations are obtained:

$$v_{AB} = [1/(j\omega_s C_1) + j\omega_s L_p + r_p] \cdot i_r + j\omega_s M \cdot i_{rs}, \quad (5)$$

$$0 = j\omega_s M \cdot i_r + [1/(j\omega_s C_2) + j\omega_s L_s + r_s] \cdot i_{rs} + R_e \cdot i_{rs}, \quad (6)$$

$$v_{CD} = -i_{rs} \cdot R_e, \quad (7)$$

where  $R_e$  is equivalent resistor:

$$R_e = (8/\pi^2) \cdot R. \quad (8)$$

Because  $r_p$  and  $r_s$  are very small compared to other impedances of the resonant tank, they can be neglected when calculating voltage transfer gain of the DC/DC WPT converter. The voltage transfer gain is calculated by (9) and (10):

$$\left| \frac{v_{AB}}{v_{CD}} \right| = \sqrt{\left( \frac{L_p - \frac{1}{\omega_s^2 C_1 M}}{M} \right)^2 + \left( \frac{\omega_s^2 L_p L_s - \frac{L_s}{C_1} - \frac{L_p}{C_2} + \frac{1}{\omega_s^2 C_1 C_2}}{R_e \omega_s M} - \frac{\omega_s M}{R_e} \right)^2}, \quad (9)$$

$$\frac{V_o}{V_d} = \sin\left(D_{ab} \cdot \frac{\pi}{2}\right) \left| \frac{v_{AB}}{v_{CD}} \right|. \quad (10)$$

Fig. 6 (a) shows the DC voltage transfer gain of the DC/DC WPT converter vs. operation frequency  $f_s$  at different conditions. Usually, the series-series resonant tank is designed assuming  $L_s = L_p \cdot k^2$  and  $C_2 = C_1/k^2$ , where  $k$  is the resonant inductance ratio. There are three resonant frequencies of the series-series resonant tank:

$$f_1 = 1/\left(2\pi\sqrt{(L_p + M/k)C_1}\right) = 1/\left(2\pi\sqrt{(L_s + M \cdot k)C_2}\right), \quad (11)$$

$$f_2 = 1/\left(2\pi\sqrt{(L_p - M/k)C_1}\right) = 1/\left(2\pi\sqrt{(L_s - M \cdot k)C_2}\right), \quad (12)$$

$$f_3 = 1/\left(2\pi\sqrt{L_p C_1}\right) = 1/\left(2\pi\sqrt{L_s C_2}\right). \quad (13)$$

The efficiency of the resonant tank,  $\eta_r$ , can be obtained as (14), its maximum point occurs at  $\omega_s = \omega_{\max}$ .  $\omega_{\max}$  can be calculated from (15). Fig. 6 (b) shows  $\eta_r$  vs.  $f_s$  at different load conditions.

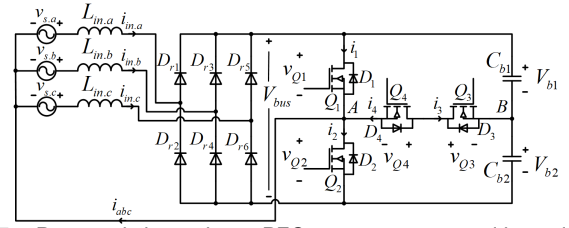


Fig. 7. Proposed three-phase PFC converter stage with equivalent three-phase voltage sources  $v_{s,a}$ ,  $v_{s,b}$ , and  $v_{s,c}$ .

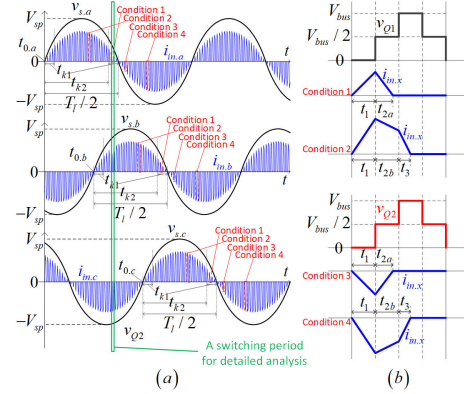


Fig. 8. Waveforms of  $v_{s,x}$  and  $i_{in,x}$  ( $x=a, b$ , and  $c$ ): (a) low frequency profile; (b) high frequency profile.

$$\eta_r = \frac{R_e}{R_e + r_s + \left( \frac{(1 - \omega_s^2 L_s C_2)^2}{\omega_s^2 M C_2} + \left( \frac{r_s + R_e}{\omega_s M} \right)^2 \right) \cdot r_p}. \quad (14)$$

$$\omega_{\max} = \left( L_s C_2 - (r_s + R_e)^2 C_2^2 / 2 \right)^{-1/2}. \quad (15)$$

### C. Three-phase power-factor-correction stage

#### 1) Working principle and analysis

Fig. 7 shows the three-phase PFC converter stage with equivalent three-phase voltage source (voltage after input filter),  $v_{s,a}$ ,  $v_{s,b}$ , and  $v_{s,c}$ . The three-phase PFC converter stage consists of three input inductors, six low-frequency diodes, two series-connected bus capacitors, and a T-type converter.  $L_{in,a}$ ,  $L_{in,b}$ , and  $L_{in,c}$  are three phase input inductors with the same inductance  $L_{in}$ .  $i_{in,a}$ ,  $i_{in,b}$ , and  $i_{in,c}$  are currents flowing through  $L_{in,a}$ ,  $L_{in,b}$ , and  $L_{in,c}$ , respectively.  $i_{abc}$  is the sum of  $i_{in,a}$ ,  $i_{in,b}$ , and  $i_{in,c}$ .  $D_{r1}$ ,  $D_{r2}$ ,  $D_{r3}$ ,  $D_{r4}$ ,  $D_{r5}$ , and  $D_{r6}$  are low-frequency diodes.  $V_{bus}$  is bus voltage of two bus capacitors  $C_{b1}$  and  $C_{b2}$  in series together.  $V_{b1}$  and  $V_{b2}$  are voltages of  $C_{b1}$  and  $C_{b2}$ , respectively, and  $V_{b1} = V_{b2} = V_{bus}/2 = V_d$ . Fig. 8 (b) gives the operation waveforms of three-phase currents  $i_{in,a}$ ,  $i_{in,b}$ , and  $i_{in,c}$ . Their operation principle is the same. In the following analysis,  $v_{s,x}$  refers to  $v_{s,a}$ ,  $v_{s,b}$ , or  $v_{s,c}$  and  $i_{in,x}$  refers to  $i_{in,a}$ ,  $i_{in,b}$  or  $i_{in,c}$ .

When  $v_{s,x}$  is at its positive cycle,  $i_{in,x}$  can behave as condition 1 or 2, where voltage across  $L_{in,x}$  is  $v_{s,x} - v_{Q1}$ ; when  $v_{s,x}$  is at its negative cycle,  $i_{in,x}$  can behave as condition 3 or 4, where voltage across  $L_{in,x}$  is  $v_{s,x} + v_{Q2}$ , as shown in Fig. 8 (b).  $i_{in,x}$  as conditions 1, 2, 3, and 4 are all working in discontinuous current mode (DCM), which is capable of reducing higher harmonics and performing PFC functionality. Firstly,  $v_{s,x}$  is expressed as:

$$v_{s,x} = V_{sp} \sin(\omega_l t - \varphi_x), \quad x = a, b, c, \quad (16)$$

where  $V_{sp}$  is peak value,  $\omega_l$  is line frequency in radian, and  $\varphi_x$  is



the initial phase ( $\varphi_a=0, \varphi_b=2\pi/3, \varphi_c=4\pi/3$ ). The limitation of  $i_{in,x}$  working in DCM is:

$$V_{sp} \leq V_{bus}/2. \quad (17)$$

Note  $V_{sp}/V_{bus}$  as  $m$ , and the limitation is:

$$m \leq 0.5. \quad (18)$$

When  $i_{in,x}$  working in condition 1, current increases from zero to peak value during  $t_1$  and then decreases from the peak value to zero during  $t_{2a}$ . Therefore,

$$\frac{v_{s,x}}{L_{in}} \cdot t_1 + \frac{v_{s,x} - V_{bus}/2}{L_{in}} \cdot t_{2a} = 0. \quad (19)$$

When in condition 2, current increases from zero to peak value during  $t_1$  and then decreases from the peak value to zero during  $t_{2b}$  and  $t_3$  with two different slopes. Therefore,

$$\frac{v_{s,x}}{L_{in}} \cdot t_1 + \frac{v_{s,x} - V_{bus}/2}{L_{in}} \cdot t_{2b} + \frac{v_{s,x} - V_{bus}}{L_{in}} \cdot t_3 = 0. \quad (20)$$

When in condition 3, current decreases from zero to negative peak value during  $t_1$  and then increases from the negative peak value to zero during  $t_{2a}$ . Therefore,

$$\frac{v_{s,x}}{L_{in}} \cdot t_1 + \frac{v_{s,x} + V_{bus}/2}{L_{in}} \cdot t_{2a} = 0. \quad (21)$$

When in condition 4, current decreases from zero to negative peak value during  $t_1$  and then increases from the negative peak value to zero during  $t_{2b}$  and  $t_3$  with two different slopes. Therefore,

$$\frac{v_{s,x}}{L_{in}} \cdot t_1 + \frac{v_{s,x} + V_{bus}/2}{L_{in}} \cdot t_{2b} + \frac{v_{s,x} + V_{bus}}{L_{in}} \cdot t_3 = 0, \quad (22)$$

where  $t_1$  and  $t_{2b}$  are determined by  $D_{ab}$ :

$$t_1 = D_{ab} T_s / 2, \quad t_{2b} = (1 - D_{ab}) T_s / 2. \quad (23)$$

The boundary of condition 1 and 2 is  $v_{s,x} = V_{bus}(1 - D_{ab})/2$  and the boundary of condition 3 and 4 is  $v_{s,x} = -V_{bus}(1 - D_{ab})/2$ . From (16) – (22), the average value of  $i_{in,x}$ ,  $i_{avg,x}$  is expressed as:

$$i_{avg,x} = \begin{cases} \frac{V_{sp} T_s}{L_{in}} \cdot \frac{D_{ab}^2 \sin(\omega t - \varphi_x)}{8(1 - 2m \sin(\omega t - \varphi_x))}, & 0 \leq \sin(\omega t - \varphi_x) \leq \frac{(1 - D_{ab})}{2m} \\ \frac{V_{sp} T_s}{L_{in}} \cdot \frac{-(1/m)(1 - D_{ab})^2 + 2(1 + D_{ab}^2) \sin(\omega t - \varphi_x)}{32(1 - m \sin(\omega t - \varphi_x))}, & \sin(\omega t - \varphi_x) > \frac{(1 - D_{ab})}{2m} \\ \frac{V_{sp} T_s}{L_{in}} \cdot \frac{D_{ab}^2 \sin(\omega t - \varphi_x)}{8(1 + 2m \sin(\omega t - \varphi_x))}, & 0 > \sin(\omega t - \varphi_x) \geq -\frac{(1 - D_{ab})}{2m} \\ \frac{V_{sp} T_s}{L_{in}} \cdot \frac{(1/m)(1 - D_{ab})^2 + 2(1 + D_{ab}^2) \sin(\omega t - \varphi_x)}{32(1 + m \sin(\omega t - \varphi_x))}, & \sin(\omega t - \varphi_x) < -\frac{(1 - D_{ab})}{2m} \end{cases} \quad (24)$$

If  $m \leq (1 - D_{ab})/2$ ,  $i_{in,x}$  always works in condition 1 or 3. Because of the symmetrical characteristic of  $i_{in,x}$  when  $v_{s,x}$  in the positive or negative cycle, the input power of a phase can be calculated by average power in half a line period ( $T/2$ ):

$$P_{in,x} = \frac{2}{T_l} \int_{t_{0,x}}^{t_{0,x} + T_l/2} i_{avg1,x} \cdot v_{s,x} dt. \quad (25)$$

If  $m > (1 - D_{ab})/2$ ,  $i_{in,x}$  works in all condition 1, 2, 3, and 4. Because of the symmetrical characteristic of  $i_{in,x}$  when  $v_{s,x}$  in the positive or negative cycle, the input power of a phase can be calculated by average power in half a line period ( $T/2$ ):

$$P_{in,x} = \frac{2}{T_l} \left[ \int_{t_{0,x}}^{t_{0,x} + t_{k1}} i_{avg1,x} v_{s,x} dt + \int_{t_{0,x} + t_{k1}}^{t_{0,x} + t_{k2}} i_{avg2,x} v_{s,x} dt + \int_{t_{0,x} + t_{k2}}^{t_{0,x} + T_l/2} i_{avg1,x} v_{s,x} dt \right], \quad (26)$$

where  $t_{0,x} = \varphi_x / \omega_l$  ( $x=a, b, \text{ or } c$ ) and

$$t_{k1} = \frac{1}{\omega_l} \arcsin \left( \frac{V_{bus}}{2V_{sp}} (1 - D_{ab}) \right), \quad (27)$$

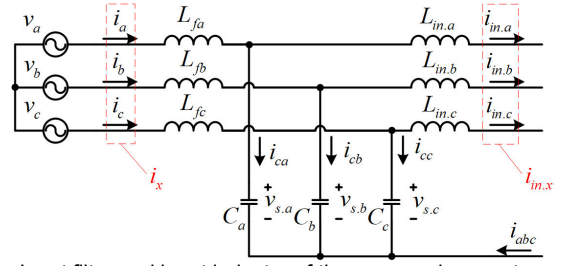


Fig. 9. Input filter and input inductor of the proposed converter

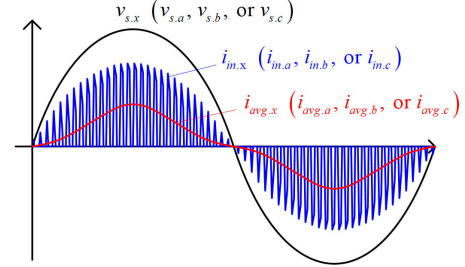


Fig. 10. Waveforms of  $v_{s,x}$ ,  $i_{in,x}$ ,  $i_{avg,x}$ .

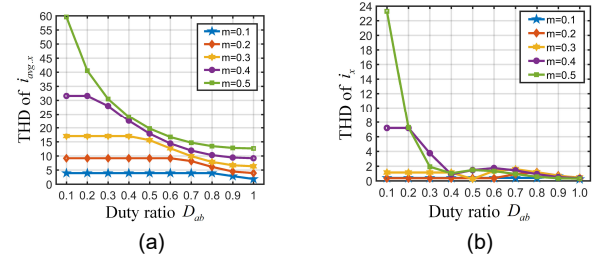


Fig. 11. THD (%) under different  $m$  conditions: (a) THD of  $i_{avg,x}$ ; (b) THD of  $i_x$ .

$$t_{k2} = \frac{1}{\omega_l} \left[ \pi - \arcsin \left( \frac{V_{bus}}{2V_{sp}} (1 - D_{ab}) \right) \right]. \quad (28)$$

Therefore, the total input power is

$$P_{in} = P_{in,a} + P_{in,b} + P_{in,c}. \quad (29)$$

## 2) Analysis of THD and PF

From Fig. 3 (c) and Fig. 9, before the three-phase PFC converter stage is the input filter. The input filter eliminates high-frequency components of input inductance current  $i_{in,x}$  (representing  $i_{in,a}$ ,  $i_{in,b}$ , or  $i_{in,c}$ ), as well as the zero-sequence components because of using an artificial neutral point of the input filter [32]. Note the average current of input inductance current  $i_{in,x}$  in a switching period  $T_s$  as  $i_{avg,x}$  (representing  $i_{avg,a}$ ,  $i_{avg,b}$ , or  $i_{avg,c}$ ), called as average input inductance current, as shown in Fig. 10, which can be transformed to Fourier series and then its THD (only related to  $D_{ab}$  and  $m$  value) is obtained by calculation. Because zero-sequence components (including third harmonic and its odd multiples) are eliminated, THD of line current  $i_x$  (representing line current  $i_a$ ,  $i_b$ , or  $i_c$ ) is much smaller than that of  $i_{avg,x}$ .

True PF is the result that displacement PF ( $PF_{dp}$ ) multiplied with distortion PF ( $PF_{dt}$ ). It can be analyzed that displacement PF is 1 theoretically and then true PF can be calculated by:

$$PF = PF_{dp} \cdot PF_{dt} = PF_{dt} = 1 / \sqrt{1 + THD_i^2}. \quad (30)$$

Fig. 11 shows the THD of average input inductance current  $i_{avg,x}$  and line current  $i_x$  at different  $m$  conditions. It is obvious that THD of  $i_x$  is much lower than that of  $i_{avg,x}$ .

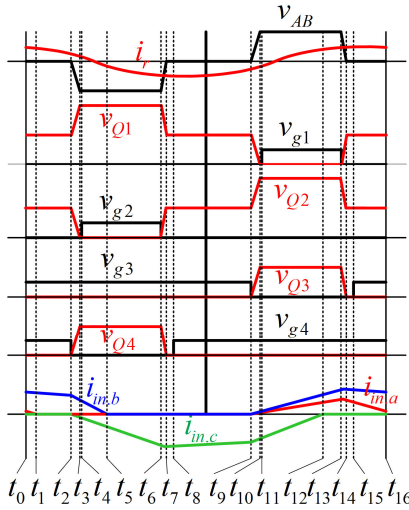


Fig. 12. Operation waveforms during a switching period

#### D. Single-stage operation and analysis

Input power can be obtained from (24) – (28), and output power  $P_o$  can be derived from (8) – (10). If the converter is designed with constant output voltage  $V_o$ , then  $P_o$  is:

$$P_o = \frac{V_o^2}{R} = \frac{8V_o^2}{\pi^2} \sqrt{\left( \frac{V_{sp} \cdot \sin(D_{ab} \pi/2)}{2mV_o} \right)^2 - \left( \frac{L_p}{M} - \frac{1}{\omega_s^2 C_1 M} \right)^2} \cdot \sqrt{\left( \frac{\omega_s^2 L_p L_s - \frac{L_s}{C_1} - \frac{L_p}{C_2} + \frac{1}{\omega_s^2 C_1 C_2}}{\omega_s M} - \omega_s M \right)^2}. \quad (31)$$

For single-stage operation, ideally,  $P_{in}$  is equal to  $P_o$  at all times. Once  $P_{in}$  is not equal to  $P_o$ ,  $V_{bus}$  will change in order to make them equal to realize steady-state condition.

By FHA method, the resonant tank and secondary side can be equivalent to an impedance  $Z_r$ , then the detailed operation analysis is illustrated in Fig. 12 and Fig. 13. The waveforms of Fig. 12 are taken from a switching period of Fig. 8 (a). In the following analysis,  $i_{abc}$  is defined as the sum of  $i_{in.a}$ ,  $i_{in.b}$ , and  $i_{in.c}$ , as shown in Fig. 14.

**Stage 1 ( $t_0 - t_2$ ):** From  $t_0$  to  $t_2$ ,  $Q_3$  and  $Q_4$  are ON, whereas  $Q_1$  and  $Q_2$  are OFF. At  $t_1$ ,  $i_{in.a}$  decreased to zero. Current paths of  $t_0 - t_1$  and  $t_1 - t_2$  are shown in Fig. 13 (a) and (b), respectively.

**Stage 2 ( $t_2 - t_4$ ):** At  $t_2$ ,  $Q_4$  is turned OFF.  $C_{s4}$  and  $C_{s1}$  start to be charged, and  $C_{s2}$  starts to be discharged by  $i_r$  and  $i_{abc}$ . At  $t_3$ ,  $C_{s4}$  and  $C_{s1}$  is charged to  $V_{bus}/2$  and  $V_{bus}$  respectively while  $C_{s2}$  is discharged to zero. At this instant,  $D_2$  starts to conduct. At  $t_4$ ,  $v_{Q2}$  has been zero and  $Q_2$  is turned ON.  $Q_4$ 's turning OFF and  $Q_2$ 's turning ON realize zero voltage switching (ZVS). Current paths of  $t_2 - t_3$  and  $t_3 - t_4$  are shown in Fig. 13 (c) and (d), respectively.

**Stage 3 ( $t_4 - t_6$ ):** From  $t_4$  to  $t_6$ ,  $Q_2$  and  $Q_3$  are ON, whereas  $Q_1$  and  $Q_4$  are OFF. At  $t_5$ ,  $i_{in.b}$  decreased to zero. Current paths of  $t_4 - t_5$  and  $t_5 - t_6$  are shown in Fig. 13 (e) and (f), respectively.

**Stage 4 ( $t_6 - t_8$ ):** At  $t_6$ ,  $Q_2$  is turned OFF.  $C_{s4}$  and  $C_{s1}$  start to be discharged, and  $C_{s2}$  starts to be charged by  $i_r$  and  $i_{abc}$ . At  $t_7$ ,  $C_{s4}$  and  $C_{s1}$  are discharged to zero and  $V_{bus}/2$  respectively while  $C_{s2}$  is charged to  $V_{bus}/2$ . At this instant,  $D_4$  starts to conduct. At  $t_8$ ,  $v_{Q4}$  has been zero and  $Q_4$  is turned ON.  $Q_2$ 's turning OFF and  $Q_4$ 's turning ON realize ZVS. Current paths of  $t_6 - t_7$  and  $t_7 - t_8$  are shown in Fig. 13 (g) and (h), respectively.

**Stage 5 ( $t_8 - t_9$ ):** From  $t_8$  to  $t_9$ ,  $Q_3$  and  $Q_4$  are ON, whereas  $Q_1$

and  $Q_2$  are OFF. The current path of this stage is shown in Fig. 13 (i).

**Stage 6 ( $t_9 - t_{11}$ ):** At  $t_9$ ,  $Q_3$  is turned OFF.  $C_{s3}$  and  $C_{s2}$  start to be charged, and  $C_{s1}$  starts to be discharged by  $i_r$  and  $i_{abc}$ . At  $t_{10}$ ,  $C_{s3}$  and  $C_{s2}$  are charged to  $V_{bus}/2$  and  $V_{bus}$  respectively while  $C_{s1}$  is discharged to zero. At this instant,  $D_1$  starts to conduct. At  $t_{11}$ ,  $v_{Q1}$  has been zero and  $Q_1$  is turned ON.  $Q_3$ 's turning OFF and  $Q_1$ 's turning ON realize ZVS. Current paths of  $t_9 - t_{10}$  and  $t_{10} - t_{11}$  are shown in Fig. 13 (j) and (k), respectively.

**Stage 7 ( $t_{11} - t_{13}$ ):** From  $t_{11}$  to  $t_{13}$ ,  $Q_1$  and  $Q_4$  are ON, whereas  $Q_2$  and  $Q_3$  are OFF. At  $t_{12}$ ,  $i_{in.c}$  decreased to zero. Current paths of  $t_{11} - t_{12}$  and  $t_{12} - t_{13}$  are shown in Fig. 13 (l) and (m), respectively.

**Stage 8 ( $t_{13} - t_{15}$ ):** At  $t_{13}$ ,  $Q_1$  is turned OFF.  $C_{s3}$  and  $C_{s2}$  start to be discharged, and  $C_{s1}$  starts to be charged by  $i_r$  and  $i_{abc}$ . At  $t_{14}$ ,  $C_{s3}$  and  $C_{s2}$  is discharged to zero and  $V_{bus}/2$  respectively while  $C_{s1}$  is charged to  $V_{bus}/2$ . At this instant,  $D_3$  starts to conduct. At  $t_{15}$ ,  $v_{Q3}$  has been zero and  $Q_3$  is turned ON.  $Q_1$ 's turning OFF and  $Q_3$ 's turning ON realize ZVS. Current paths of  $t_{13} - t_{14}$  and  $t_{14} - t_{15}$  are shown in Fig. 13 (n) and (o), respectively.

**Stage 9 ( $t_{15} - t_{16}$ ):** This stage is the same with stage 1.

#### E. ZVS conditions

As shown in Fig. 14, the critical point of ZVS operation is node A because  $i_1$ ,  $i_2$ ,  $i_4$  ( $i_3$ ),  $i_{abc}$ , and  $i_r$  flow and collect here.  $i_{abc}$  is defined as the sum of  $i_{in.a}$ ,  $i_{in.b}$ , and  $i_{in.c}$ . There are three necessary conditions for a switch to achieve ZVS: dead time, a snubber capacitor, and an appropriate current flowing through the switch. At the instant of turning-OFF, the current flowing through the switch (from Drain to Source) is required to be positive and relatively large enough. In the proposed topology,  $i_{abc}$  and  $i_r$  determine the directions and magnitudes of  $i_1$ ,  $i_2$ ,  $i_3$ , and  $i_4$  ( $Q_1$ ,  $Q_2$ ,  $Q_3$ , and  $Q_4$ 's drain currents) at the turning-OFF instants of  $Q_1$ ,  $Q_2$ ,  $Q_3$ , and  $Q_4$ . By analysis, operation at stage 4 or 8 can achieve ZVS definitely at any load conditions because the sum of  $i_{abc}$  and  $i_r$  is always negative or positive respectively ( $i_{abc}$  and  $i_r$  both collect at or diverge from node A) and large enough. Operation of stage 2 or stage 6 can also achieve ZVS when the sum of  $i_{abc}$  and  $i_r$  is positive or negative respectively. However, at  $t_2$  or  $t_9$ , the sum of  $i_{abc}$  and  $i_r$  is not always positive or negative respectively. Assume all the snubber capacitors ( $C_{s1}$ ,  $C_{s2}$ ,  $C_{s3}$ , and  $C_{s4}$ ) of  $Q_1 - Q_4$  are with the same capacitance value  $C_s$ , then the ZVS conditions of stage 2 are obtained as:

$$\begin{cases} I_{zvs} > 0 \\ \frac{3C_s V_{bus}}{2I_{zvs}} \leq T_{dt} \end{cases}, \quad (32)$$

where  $T_{dt}$  is the switching dead time between  $Q_2$  and  $Q_4$  (also is the switching dead time between  $Q_1$  and  $Q_3$ );  $I_{zvs}$  is the ZVS current of stage 2, defined as the minimum sum of  $i_{abc}$  and  $i_r$  at  $t_2$ , which is calculated by (44) of Appendix. The dead time is considered small enough compared with the switching period that during the dead time  $i_r$  and  $i_{abc}$  are considered to be constant. Because of symmetry the switching characteristics, the ZVS conditions of stage 6 is the same as that of stage 2. It can be analyzed that ZVS operation of stage 2 or stage 6 cannot be achieved when  $D_{ab}$  is relatively small (at low load conditions). The critical and specific conditions of ZVS operations can be obtained only when the operation and design

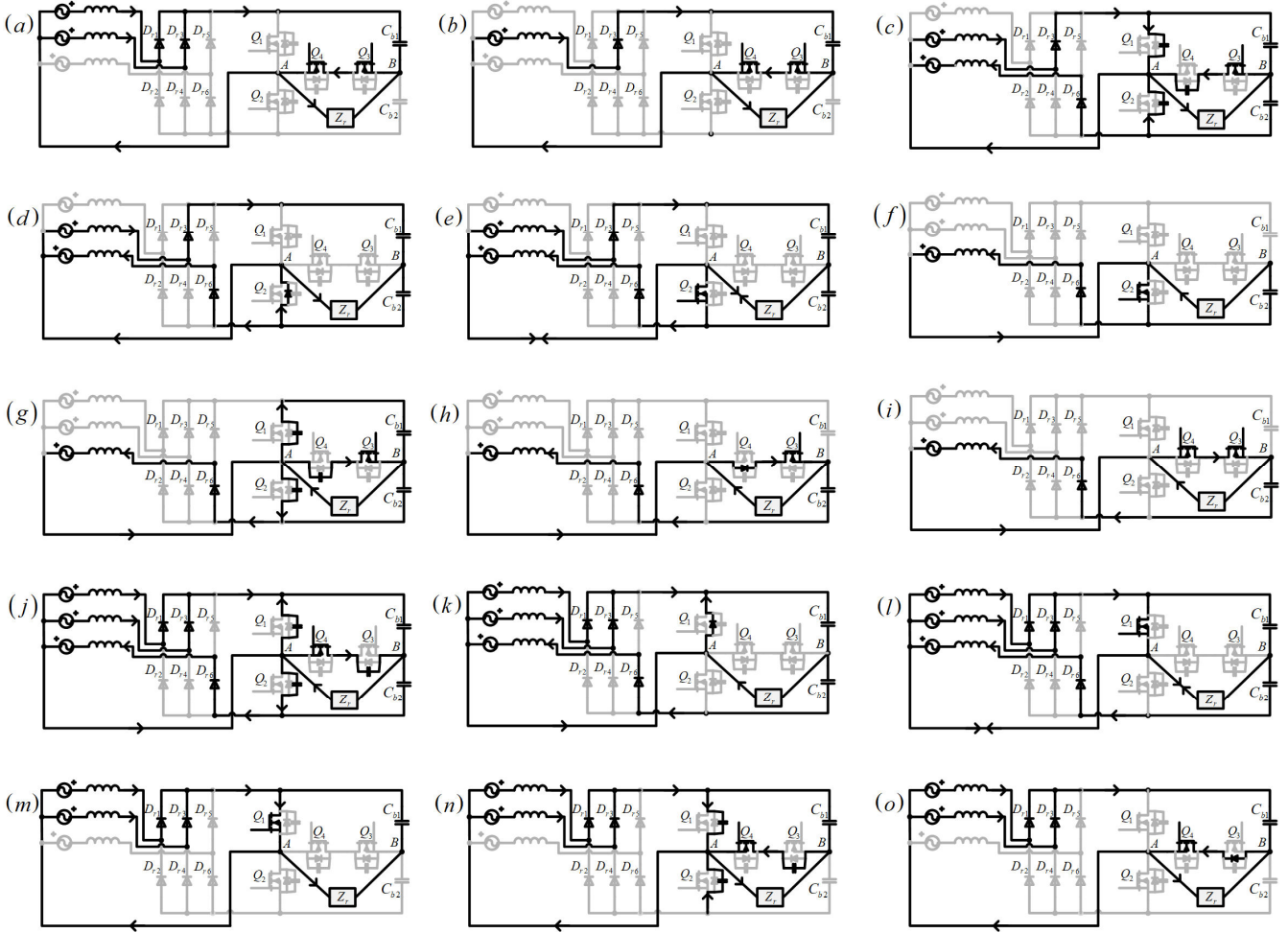


Fig. 13. Operation modes during a switching period: (a)  $t_0 - t_1$ ; (b)  $t_1 - t_2$ ; (c)  $t_2 - t_3$ ; (d)  $t_3 - t_4$ ; (e)  $t_4 - t_5$ ; (f)  $t_5 - t_6$ ; (g)  $t_6 - t_7$ ; (h)  $t_7 - t_8$ ; (i)  $t_8 - t_9$ ; (j)  $t_9 - t_{10}$ ; (k)  $t_{10} - t_{11}$ ; (l)  $t_{11} - t_{12}$ ; (m)  $t_{12} - t_{13}$ ; (n)  $t_{13} - t_{14}$ ; (o)  $t_{14} - t_{15}$ .

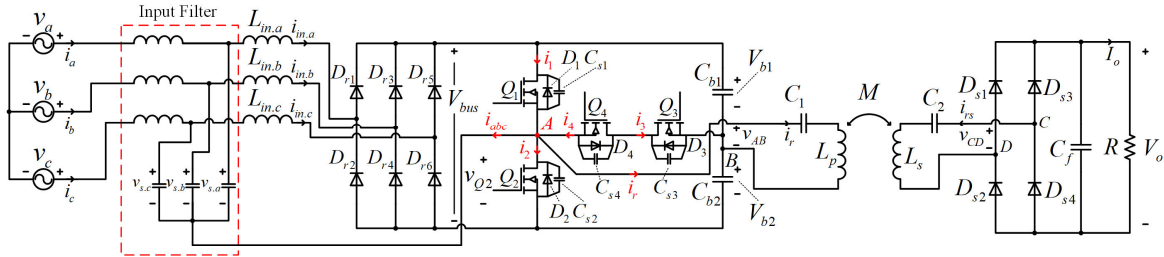


Fig. 14. Proposed converter with marked critical currents

parameters of the proposed converter are confirmed. Generally speaking, when the load condition is larger than 50%, ZVS operations can be achieved. In chapter IV, table II implies whether ZVS operations are achieved or not at different load conditions according to (32). The details can be found in section A of Appendix.

## F. Control method

### 1) Description

The bus voltage ( $V_{bus}$ ) of the topology is very significant as it decides the maximum voltage ratings of diodes  $D_{r1} - D_{r6}$ , switching devices  $Q_1 - Q_4$ , and bus capacitors  $C_{b1}$  and  $C_{b2}$ . Usually, for single-stage topologies, bus voltage fluctuates with load variations and could be very high at light load condition [32], [41]. Too high bus voltage is unacceptable and therefore

many single-stage topologies cannot work at light load condition or standby (zero-load) condition. In this paper, a bus voltage control method is proposed to control  $V_{bus}$  stably within a wide load range. In this analysis, the input voltage is assumed to be constant (constant  $V_{sp}$ ). If allowable maximum bus voltage  $V_{bus,max}$  is confirmed, then minimum  $m$  value ( $m_{min}$ ) will be obtained. From Fig. 11, generally THD of  $i_x$  decreases with  $m$  value decreases ( $V_{bus}$  increases). Therefore,  $V_{bus}$  is controlled to be equal to  $V_{bus,max}$  stably to obtain the best THD performance.

$D_{ab}$  and  $f_s$  are two control parameters used for regulating output voltage  $V_o$  and bus voltage  $V_{bus}$ . Fig. 15 shows the curves of  $P_{in}$  (dotted lines) and  $P_o$  (solid lines) under different  $D_{ab}$  and  $f_s$  conditions, with constant  $m$  value and  $V_o$ . At specific  $D_{ab}$  and  $f_s$  condition, when  $P_{in}$  is equal to  $P_o$ ,  $V_o$  and  $V_{bus}$  will be stable.

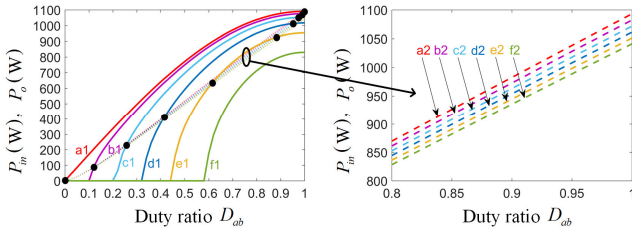


Fig. 15. An example of  $P_{in}$  and  $P_o$  vs  $D_{ab}$  under different operation frequency with parameters:  $L_m=73.5 \mu\text{H}$ ;  $L_p=L_s=246 \mu\text{H}$ ;  $C_1=C_2=10.3 \text{ nF}$ ;  $M=46 \mu\text{H}$ ;  $m=0.5$ ;  $V_{sp}=110\sqrt{2} \text{ V}$ ;  $V_o=250 \text{ V}$ . There are six sets of curves with operation frequency: a1 and a2 ( $\omega_s=\omega_3$ ); b1 and b2 ( $\omega_s=1.01*\omega_3$ ); c1 and c2 ( $\omega_s=1.02*\omega_3$ ); d1 and d2 ( $\omega_s=1.03*\omega_3$ ); e1 and e2 ( $\omega_s=1.04*\omega_3$ ); f1 and f2 ( $\omega_s=1.05*\omega_3$ ).

However, when  $P_{in}$  is larger than  $P_o$ ,  $V_{bus}$  will increase, and therefore  $V_o$  will increase and vice versa. Increasing  $f_s$  will decrease both  $P_{in}$  and  $P_o$ . However, the decrement of  $P_o$  is much larger than that of  $P_{in}$ , which means that increasing  $f_s$  can increase  $V_{bus}$ .

$D_{ab}$  is mainly for  $V_o$  control, and  $f_s$  is mainly for  $V_{bus}$  control. When  $V_o$  is detected to be higher,  $D_{ab}$  will be decreased; simultaneously, when  $V_{bus}$  is detected to be higher,  $f_s$  will be decreased, and vice versa. Black dots of Fig. 15 are the real operation points at different load conditions. Such a method can realize a wide load range operation and bus voltage control. From Fig. 15, the operation range of  $f_s$  within the full load range is very small (around 6% of  $f_3$ ), so it is easy to design input EMI filter and efficiency of resonant tanks is kept high.

### 2) Limitation of resonant coils design

There is a limitation of the proposed control method that characteristics of input and output power are required to be similar to those of Fig. 15, which means that the output power should be smaller than the input power at the conditions of  $f_s$  larger than  $f_3$  when  $D_{ab}$  is equal to 1, resulting in the limitation expressed as:

$$\frac{V_o}{n} \geq \frac{V_{bus}}{\sqrt{2}}. \quad (33)$$

Therefore, when bus voltage  $V_{bus}$  and output voltage  $V_o$  are confirmed, there will be a restriction for the design of the resonant coils: the square root of the ratio of  $L_s$  and  $L_p$  are required to fulfill (33). The details can be found in section B of Appendix.

### 3) Control block diagram

Fig. 16 shows the block diagram of the proposed control method. There are three control loops including an output voltage loop, a bus voltage loop, and a bus voltage balance loop. The output signal of the output voltage loop is duty cycle  $D_{ab}$ , while those of bus voltage loop and bus voltage balance loop are frequency  $f_s$  and phase difference  $P_h$ , respectively. The upper and lower bus voltages and output voltage ( $V_{b1}$ ,  $V_{b2}$ , and  $V_o$ ) are three signals measured and sampled from the power circuit. The balance of the  $V_{b1}$  and  $V_{b2}$  (voltages of  $C_{b1}$  and  $C_{b2}$ ) are controlled automatically by regulating the phase difference of driving PWM signals of  $Q_1$  and  $Q_2$ . Ideally, when the phase difference is 180 degree, the current flowing through the middle path ( $Q_3-Q_4$  path) in a switching period is zero, and the bus voltages will be in balance. However, due to the practical difference of the middle switches with different leakage current and parasitic parameters, the current flowing through the middle path ( $Q_3-Q_4$  path) in a switching period is not zero

TABLE I  
PARAMETERS OF THE LABORATORY PROTOTYPE

Components	Details
$L_{in,a}, L_{in,b}, L_{in,c}$	102.8 $\mu\text{H}$ , 103.9 $\mu\text{H}$ , and 103.3 $\mu\text{H}$
$D_{r1} - D_{r6}$	STTH6010
$Q_1, Q_2$	CREE C2M0080120D
$Q_3, Q_4$	CREE C3M0065090D
$C_{b1}, C_{b2}$	1080 $\mu\text{H}$ , 450 V (electrolytic capacitors)
$C_{s1}, C_{s2}$	1 nF, 1 kV (polypropylene capacitors)
$L_p, L_s, M$	330.2 $\mu\text{H}$ ; 150.9 $\mu\text{H}$ ; 48.5 $\mu\text{H}$
$C_1, C_2$	10.66 nF; 23.34 nF (10 kV polypropylene capacitors)
$D_{s1}, D_{s2}, D_{s3}, D_{s4}$	Vishay VS-30EPH06PbF
$C_f$	220 $\mu\text{F}$ , 450 V (electrolytic capacitor)
$L_{lf}, C_{lf}$	(1.97 mH, 1.98 mH, 1.98 mH), (0.92 $\mu\text{F}$ , 0.91 $\mu\text{F}$ , 0.89 $\mu\text{F}$ )
$f_s$	Min: 85.0 kHz; Max: 90.5 kHz
$D_{ab}$	0 – 1

when the phase difference is 180 degree, resulting in bus voltages imbalance. Therefore, in practical, the phase difference needs to be fine-tuned by the controller automatically all the time to ensure the balance of bus voltages.

## III. DESIGN PROCEDURE AND CONSIDERATIONS

### A. Design procedure

To verify the design and control of the proposed topology, a 3.3-kW laboratory prototype with constant  $V_o$  is designed and implemented. The design procedures are given as follows:

1) *Requirements of input and output*: Phase voltage  $v_x$  of the three-phase voltage source is designed to be 220 V<sub>rms</sub>, 50 Hz. Maximum output power  $P_{o,max}$  is 3.3 kW, with constant output voltage  $V_o$  to be 330 V and hence maximum output current  $I_{o,max}$  is 10 A (minimum load resistance  $R_{min}$  being 33  $\Omega$ ).

2) *Requirements of bus voltage*:  $V_{bus,max}$  is designed to be 640 V and hence  $V_{bus}$  is kept to be  $V_{bus,max}$  during wide load variation. Then,  $m$  value is obtained as  $220\sqrt{2}/640 = 0.486$ .

3) *Minimum operation frequency  $f_{s,min}$  and mutual inductance  $M$* : From Fig. 12, maximum output power condition occurs at the condition with  $D_{ab}$  being 1 and  $f_s$  being  $f_3$ , and  $P_{o,max}$  is expressed as:

$$P_{o,max} = \frac{2V_o V_{sp}}{\pi^3 m f_3 M}. \quad (34)$$

According to SAE J2954 for wireless EV charging, operation frequency is suggested to be 81.39 – 90 kHz. Therefore,  $f_{s,min}$  is selected to be around 85.0 kHz. When  $f_3$  ( $f_{s,min}$ ) is set as 85.0 kHz, then mutual inductance  $M$  is calculated to be 48.6  $\mu\text{H}$ .

4) *Design of resonant tank*: From (33), the square root of the ratio of  $L_s$  and  $L_p$ ,  $n$ , is limited as:

$$n \leq \frac{\sqrt{2}V_o}{V_{bus}} = \frac{\sqrt{2} \times 330}{640} = 0.73. \quad (35)$$

Therefore, the ratio of self-inductance values of primary-side and secondary-side coils is required to be smaller than 0.53. For mid-range wireless power transfer, the coupling coefficient  $k_{ps}$



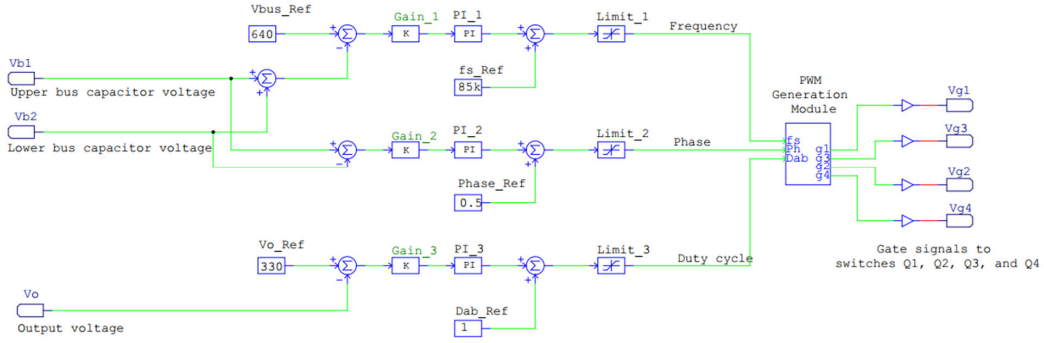


Fig. 16. Block diagram of the proposed control method

of two resonant coils ranges from 0.1 to 0.3 [11], [44]. And considering for EV charging application, air gap distance  $d_{ag}$  of two coils is designed to be 150 mm. Therefore, integrating the known parameters of  $k_{ps}$ ,  $M$ , and  $d_{ag}$ , the two resonant coils are designed in a spiral shape with the average diameter  $d$  to be 400 mm. Their coils numbers are designed to be 25 and 15 respectively. To reduce AC resistance of resonant coils, litz wire with 1000 strands (each strand's diameter is 0.1 mm) are used. The strand's diameter is smaller than two times of skin depth  $d_{sk}$ , which is obtained as:

$$d_{sk} = \sqrt{\rho / (\pi f_s \mu)} \approx 0.23 \text{ mm}, \quad (36)$$

where  $\rho$  and  $\mu$  are resistivity and permeability of copper litz wire. Therefore, the skin effect can be significantly reduced. Finally, the measured values of the  $L_p$ ,  $L_s$ , and  $M$  are 330.2  $\mu\text{H}$ , 150.9  $\mu\text{H}$ , and 48.5  $\mu\text{H}$ , respectively. Values of  $L_p$  and  $L_s$  fulfill the requirement of (35). According to (13), assuming  $f_3$  to be 85.0 kHz, then  $C_1$  and  $C_2$  are calculated as 10.62 nF and 23.23 nF respectively. Practically, the measured values of  $C_1$  and  $C_2$  are 10.66 nF and 23.34 nF.

5) *The Inductance of input inductors  $L_{in}$* : Ideally, maximum input power ( $P_{in,max}$ ) is equal to  $P_{o,max}$ , and also occurs when  $D_{ab}=1$  and  $f_s=f_3$ . With known  $m$  value (0.486) and  $V_{sp}$  ( $220\sqrt{2}$  V),  $L_{in}$  can be calculated from (23) – (29), which is 112.0  $\mu\text{H}$ .

6) *Maximum operation frequency  $f_{s,max}$* : By analysis and calculation, at operation frequency  $f_s$  equal to  $1.065f_3$ ,  $P_{in}$  and  $P_o$  curves have only one intersection point. Hence,  $f_{s,max}$  is confirmed to be  $1.065f_3$ , which is 90.5 kHz.

7) *Input filter design*: To design the input filter, input resistance of the proposed converter need to be confirmed. Because the input filter configuration of each phase is the same, input resistance of one phase ( $v_x$ ) is calculated. Here only half-positive cycle of  $v_x$  are considered. When  $0 \leq v_x \leq (1-D_{ab})V_{bus}/2$ , input resistance  $R_i$  is:

$$R_i = \frac{8L_{in}f_s(V_{bus} - 2v_x)}{D_{ab}^2V_{bus}}, \quad (37)$$

and when  $v_x > (1-D_{ab})V_{bus}/2$ ,  $R_i$  is:

$$R_i = \frac{32L_{in}f_s v_x (V_{bus} - v_x)}{2v_x V_{bus} (1 + D_{ab}^2) - V_{bus}^2 (1 - D_{ab})^2}. \quad (38)$$

It can be analyzed that minimum input resistance  $R_{i,min}$  occurs when  $D_{ab}=1$  (100% load) and  $v_x=220\sqrt{2}$  V. And  $R_{i,min}$  is calculated to be 39  $\Omega$ . Note inductance and capacitance of the input filter of each phase as  $L_{if}$  and  $C_{if}$ , then  $\omega L_{if} \ll R_{i,min}$  should

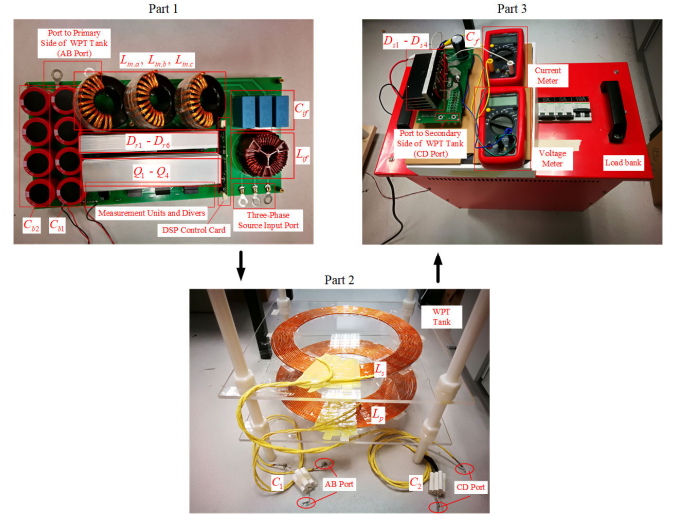


Fig. 17. Setup of the laboratory prototype.

be fulfilled. Therefore,  $L_{if}$  is designed to be 1.8 mH first. Because  $f_s$  is around 85.0 kHz, the cutoff frequency is designed to be smaller than 8.5 kHz. Therefore,  $C_{if}$  is designed to be around 1.0  $\mu\text{F}$ . In practice,  $L_{if}$  is measured to be 1.97 mH, 1.98 mH, 1.98 mH (three-phase common mode choke Wurth Elektronik 744837018220) and  $C_{if}$  is measured to be 0.92  $\mu\text{F}$ , 0.91  $\mu\text{F}$ , and 0.89  $\mu\text{F}$  (three polypropylene capacitors).

#### B. Design summary and laboratory prototype

Setup of the laboratory prototype is shown in Fig. 17 and Table I gives the detailed design parameters of the laboratory prototype. Input inductor  $L_{in,a}$ ,  $L_{in,b}$ , and  $L_{in,c}$  are designed to be the same; however, they are a little different due to manufacturing errors and their values are measured to be 102.8  $\mu\text{H}$ , 103.9  $\mu\text{H}$ , and 103.3  $\mu\text{H}$  respectively. Kool M $\mu$  magnetic core in toroid shape (with 125 relative permeability, 62.0 mm outer diameter, 32.6 mm inner diameter, and 25.0 mm height) is used as the core of input inductors and the values of  $k$ ,  $\alpha$ , and  $\beta$  are 1.18, 1.63, and 2.2 respectively. A three-phase auto-transformer is used to output 220 V<sub>rms</sub> three-phase voltage. CREE discrete SiC MOSFETs are used as the switches  $Q_1 - Q_4$  in order to reduce switching loss. Measured ESRs of primary-side and secondary-side coils of WPT tank are 0.41  $\Omega$  and 0.29  $\Omega$  respectively.

#### IV. EXPERIMENTAL RESULTS

According to the proposed design procedure, the laboratory

TABLE II  
IDEAL OPERATION PARAMETERS AND ZVS CONDITIONS AT DIFFERENT LOAD CONDITIONS

Load conditions	Load resistance $R$	Duty ratio $D_{ab}$	Operation frequency $f_s$	$Q_1, Q_2$ 's turning off and $Q_3, Q_4$ 's turning on	$Q_1, Q_2$ 's turning on and $Q_3, Q_4$ 's turning off
100% load (3300 W)	33 $\Omega$	1.00	85.0 kHz	ZVS	ZVS
82.5% load (2722.5 W)	40 $\Omega$	0.88	90.3 kHz	ZVS	ZVS
66% load (2178 W)	50 $\Omega$	0.72	90.2 kHz	ZVS	ZVS
50% load (1650 W)	66 $\Omega$	0.58	89.6 kHz	ZVS	ZVS
33% load (1089 W)	100 $\Omega$	0.41	88.6 kHz	ZVS	ZVS
16.5% load (544.5 W)	200 $\Omega$	0.25	87.5 kHz	ZVS	non-ZVS

TABLE III  
COMPARISONS WITH STATE-OF-THE-ART AC-DC OR AC-AC TOPOLOGIES FOR WPT

Topologies	Efficiency (%)		Count of power devices		PF	THD <sub>i</sub> (%)	Ratio of bus voltage and input phase voltage	Power level (W)	Soft switching techniques	Three- or single-phase
	AC-AC Part	Overall	AC-AC Part	Overall						
Proposed topology	95.4	89.2	6 diodes + 4 MOSFETs	10 diodes + 4 MOSFETs	1.0	3.5	640/220	3300	ZVS	three-phase
Single-stage AC-AC matrix converter [38]	89.4	not reported	6 diodes + 7 MOSFETs	not reported	0.67	110.8	not reported	267	ZCS	three-phase
Single-stage AC-AC matrix converter [39]	not reported	85	8 MOSFETs	not reported	<0.95	>20.0	not reported	300	no soft switching	three-phase
Single-stage Bidirectional AC-AC matrix converter [40]	92.0	not reported	8 MOSFETs	12 MOSFETs	0.98	19.0	not reported	95	ZCS	single-phase
Single-stage AC-DC converter [41]	93.5	90.1	2 diodes + 4 MOSFETs	6 diodes + 4 MOSFETs	0.99	15.4	745/220	2560	ZVS	single-phase
Two-stage AC-DC converter [45]	not reported	< 85%	7 diodes + 5 MOSFETs	11 diodes + 5 MOSFETs	<0.98	>5.0	180/38	850	not reported	three-phase
Two-stage AC-DC converter [46]	not reported	91.0	12 MOSFETs	4 diodes + 12 MOSFETs	not reported	not reported	750/220	25000	ZVS	three-phase
Two-stage AC-DC wireless charger [47]	95.4	85.2	not reported	not reported	0.93	>20.0	324/221	6600	not reported	single-phase
Two-stage AC-AC converter [48]	91.7	not reported	8 MOSFETs	not reported	0.99	4.5	200/120	100	ZVS	single-phase

prototype is implemented with rated 3300 W output power. In the experiments, due to the limitation of load bank, operations at 16.5%, 33%, 50%, 66%, 82.5%, and 100% load conditions (544.5 W – 3300 W) are tested to verify the functionalities and advantages of the proposed topology. Table II gives the ideal operation parameters and ZVS conditions at different load conditions. It should be noted that the ideal operating parameters are obtained by simulation results without considering power losses.

Fig. 18 (a) shows the measured overall efficiency and partial efficiencies of different parts (part 1: from three-phase ac line input to input port (AB) of WPT tank; part 2: from input port (AB) to output port (CD) of WPT tank; part 3: from output port (CD) of WPT tank to load, as shown in Fig. 17) at different load

conditions. Fig. 18 (b) shows the measured power factor and THD of input current at different load conditions. At full load condition, efficiency, power factor, and THD of input current achieve the best performances (89.2%, 1.0, and 3.5%, respectively). Part 1 of the system can be considered as the AC-AC converter for the WPT tank, which can achieve 95.4% efficiency at full load condition. The efficiency of part 2 (WPT tank) drops when load resistance deviates from the optimum load resistance of the WPT tank. Fig. 19 presents the power loss distributions by theoretical analysis and calculation at 100% and 50% load conditions. The detailed calculation of power losses can be found in section D of Appendix. Power losses of input inductors, of which 99% are the core losses, are the most dominant among total power losses. Such losses can be

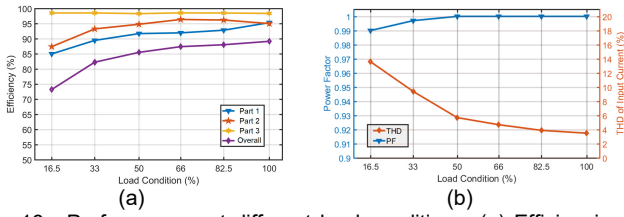


Fig. 18. Performances at different load conditions: (a) Efficiencies of different parts; (b) Power factor and THD of the three-phase input current.

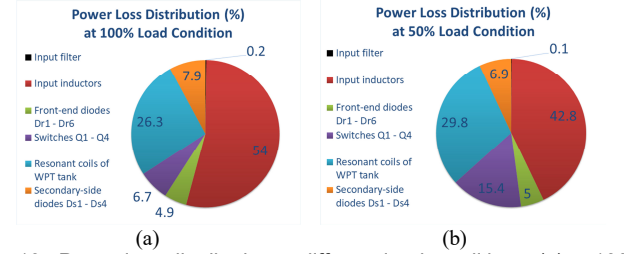


Fig. 19. Power loss distribution at different load conditions: (a) at 100% load condition; (b) at 50% load condition.

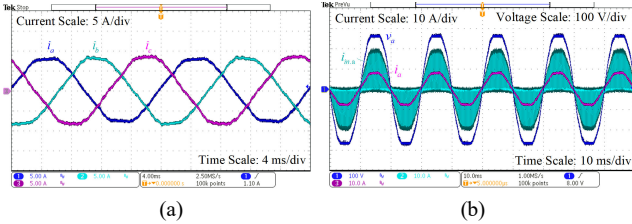


Fig. 20. (a) Three-phase input current at 100% load condition; (b) Phase voltage and input inductor current of one phase of 100% load condition.

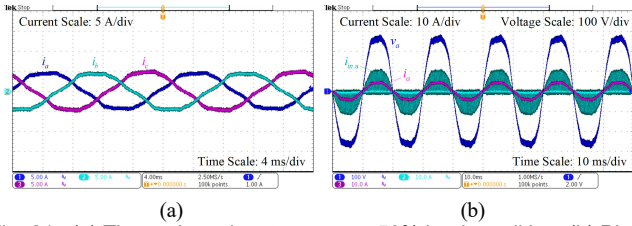


Fig. 21. (a) Three-phase input current at 50% load condition; (b) Phase voltage and input inductor current of one phase of 50% load condition.

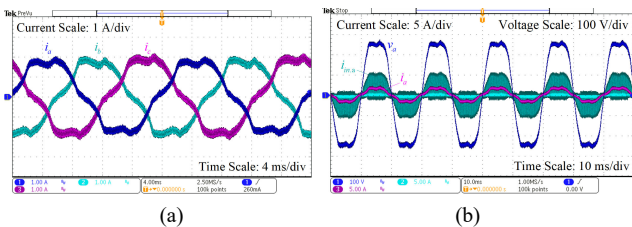


Fig. 22. (a) Three-phase input current at 16.5% load condition; (b) Phase voltage and input inductor current of one phase of 16.5% load condition.

minimized further by choosing a proper magnetic core with relatively low permeability. Power losses of  $Q_1 - Q_4$  are small because ZVS is achieved so that there are only conduction losses. At 50% load condition, the inductive current resulting from the WPT tank is relatively larger, and conduction of  $Q_3$  and  $Q_4$  are remarkable, hence, the ratio of power losses of  $Q_1 - Q_4$  is obviously larger than that at 100% load condition.

Table III presents comparisons of the proposed topology with other state-of-the-art AC-DC or AC-AC topologies for WPT in terms of efficiency, count of power devices, power quality, power level, and soft-switching technique. Compared with the three-phase single-stage AC-AC matrix converters for WPT

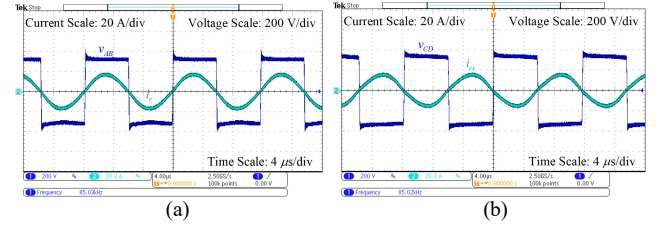


Fig. 23. Waveforms of resonant tank at 100% load condition: (a)  $v_{AB}$  (in blue) and  $i_r$  (in cyan); (b)  $v_{CD}$  (in blue) and  $i_{rs}$  (in cyan).

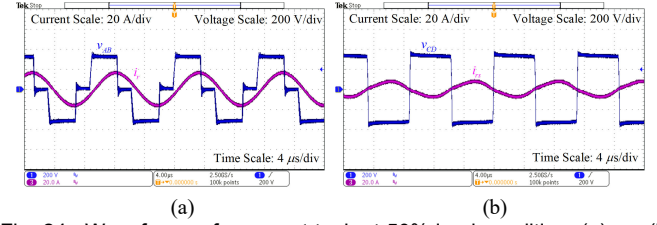


Fig. 24. Waveforms of resonant tank at 50% load condition: (a)  $v_{AB}$  (in blue) and  $i_r$  (in purple); (b)  $v_{CD}$  (in blue) and  $i_{rs}$  (in purple).

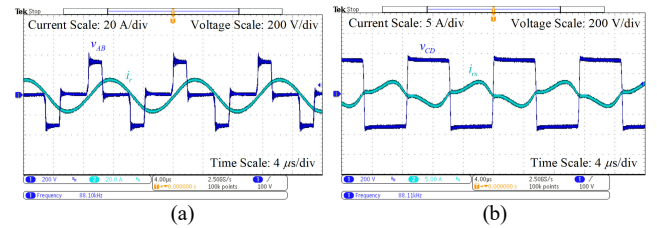


Fig. 25. Waveforms of resonant tank at 16.5% load condition: (a)  $v_{AB}$  (in blue) and  $i_r$  (in cyan); (b)  $v_{CD}$  (in blue) and  $i_{rs}$  (in cyan).

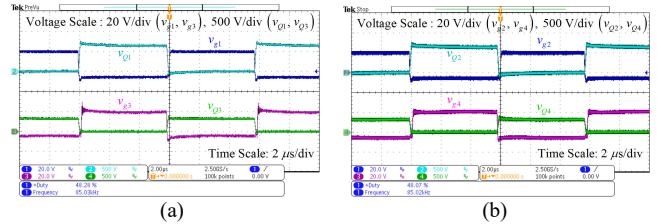


Fig. 26. Switching waveforms at 100% load condition: (a) GS voltages ( $v_{g1}$  and  $v_{g3}$ ) and DS voltages ( $v_{Q1}$  and  $v_{Q3}$ ) of  $Q_1$  and  $Q_3$ ; (b) GS voltages ( $v_{g2}$  and  $v_{g4}$ ) and DS voltages ( $v_{Q2}$  and  $v_{Q4}$ ) of  $Q_2$  and  $Q_4$ .

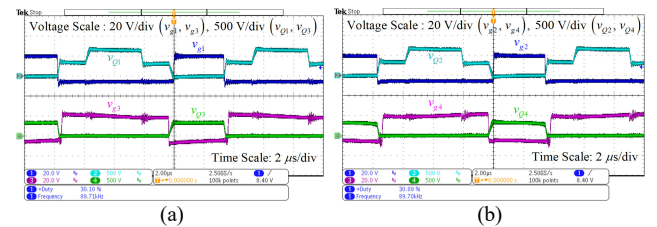


Fig. 27. Switching waveforms at 50% load condition: (a) GS voltages ( $v_{g1}$  and  $v_{g3}$ ) and DS voltages ( $v_{Q1}$  and  $v_{Q3}$ ) of  $Q_1$  and  $Q_3$ ; (b) GS voltages ( $v_{g2}$  and  $v_{g4}$ ) and DS voltages ( $v_{Q2}$  and  $v_{Q4}$ ) of  $Q_2$  and  $Q_4$ .

[38], [39] and three-phase two-stage AC-DC topologies for WPT [45], [46], the proposed topology performs remarkably better efficiency (except for the topology of [46]) and power quality and uses less count of power MOSFETs. Throughout the wide load-varying range, bus voltage is maintained to be stable (640 V) as designed previously, which is lower than that of single-phase single-stage topology [41]. Compared to the single-phase single-stage and two-stage topologies for WPT [40], [41], [47], [48], the power quality of the proposed topology is also much better. In general, the proposed topology exhibits significant and dominant advantages considering the integrated performances of power quality, efficiency, count of

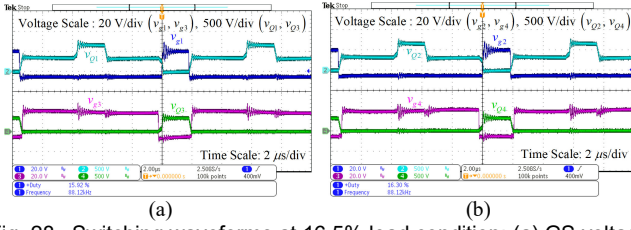


Fig. 28. Switching waveforms at 16.5% load condition: (a) GS voltages ( $v_{g1}$  and  $v_{g3}$ ) and DS voltages ( $v_{Q1}$  and  $v_{Q3}$ ) of  $Q_1$  and  $Q_3$ ; (b) GS voltages ( $v_{g2}$  and  $v_{g4}$ ) and DS voltages ( $v_{Q2}$  and  $v_{Q4}$ ) of  $Q_2$  and  $Q_4$ .

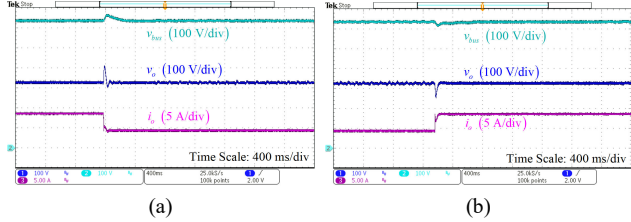


Fig. 29. Step responses of  $V_{bus}$  and  $V_o$ : (a) from 82.5% to 41.25% load condition; (b) from 41.25% to 82.5% load condition.

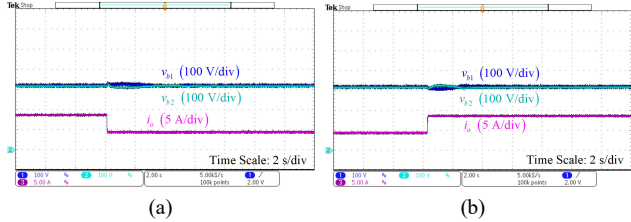


Fig. 30. Step responses of  $V_{b1}$  and  $V_{b2}$ : (a) from 82.5% to 41.25% load condition; (b) from 41.25% to 82.5% load condition.

power devices, and power capability compared with existing topologies for WPT.

Fig. 20 – Fig. 22 show the input current, phase input voltage, and input inductor current at 100%, 50%, and 16.5% load conditions respectively. Fig. 23 – Fig. 25 show the voltages and currents of the WPT tank at 100%, 50%, and 16.5% load conditions respectively. Fig. 26 – Fig. 28 show the switching waveforms of  $Q_1 - Q_4$  at 100%, 50%, and 16.5% load conditions respectively. It is evident that at 100% and 50% load conditions,  $Q_1 - Q_4$  can realize soft-switching at both turn-on and turn-off instants. However, when load condition is lower than 30%, such as 16.5% load condition, soft-switching cannot be totally realized due to insufficient inductive resonant current and therefore the efficiency of part 1 drops remarkably. Fig. 29 and Fig. 30 show the dynamic responses of the proposed converter with the proposed control method. Both bus voltage and output voltage are controlled stable and constant with good dynamic performances and voltages of upper and lower bus capacitors are also controlled in balance stably when the load changes.

## V. CONCLUSIONS

A three-phase single-stage AC-DC WPT resonant converter with PFC is firstly proposed, studied, and developed in this paper. The proposed topology combines a three-phase rectifier bridge and a T-type three-level inverter together to realize the functionalities of AC-DC power factor correction and DC-DC WPT simultaneously. The proposed three-phase topology can improve efficiency and reduce control complexity compared to three-phase two-stage AC-DC WPT converters. In addition, bus voltage is also maintained to be a relatively low level when

the load condition varies. Detailed description and analysis, design procedure, and a laboratory prototype are presented. The experimental results verify the functionalities and performances of the proposed topology.

## APPENDIX

### A. Derivation of the ZVS conditions

Here operation of stage 2 is taken to analyze the ZVS conditions. At  $t_2$ ,  $i_{in,c}$  is zero to ensure DCM operation, and hence  $i_{abc}$  is equal to the sum of  $i_{in,a}$  and  $i_{in,b}$ , expressed as:

$$i_{in,a}|_{t_2} = \begin{cases} \frac{v_{s,a}}{L_{in,a}} \cdot \frac{D_{ab}T_s}{2} - \frac{V_{bus}/2 - v_{s,a}}{L_{in,a}} \cdot \frac{(1-D_{ab})T_s}{2}, & v_{s,a} \geq \frac{V_{bus}}{2}(1-D_{ab}) \\ 0, & v_{s,a} < \frac{V_{bus}}{2}(1-D_{ab}) \end{cases} \quad (39)$$

$$i_{in,b}|_{t_2} = \begin{cases} \frac{v_{s,b}}{L_{in,b}} \cdot \frac{D_{ab}T_s}{2} - \frac{V_{bus}/2 - v_{s,b}}{L_{in,b}} \cdot \frac{(1-D_{ab})T_s}{2}, & v_{s,b} \geq \frac{V_{bus}}{2}(1-D_{ab}) \\ 0, & v_{s,b} < \frac{V_{bus}}{2}(1-D_{ab}) \end{cases} \quad (40)$$

By analysis, minimum  $i_{abc}$  at  $t_2$  is expressed as (input inductors  $L_{in,a}$ ,  $L_{in,b}$ , and  $L_{in,c}$  are assumed to be the same, equal to  $L_{in}$ ):

$$(i_{abc}|_{t_2})_{\min} = \begin{cases} \frac{T_s}{4L_{in}} [\sqrt{3}V_{sp} - (1-D_{ab})V_{bus}], & D_{ab} \geq 1 - \frac{\sqrt{3}V_{sp}}{V_{bus}} \\ 0, & D_{ab} < 1 - \frac{\sqrt{3}V_{sp}}{V_{bus}} \end{cases} \quad (41)$$

At  $t_2$ , the current of the primary side of WPT tank,  $i_r$ , is expressed as:

$$i_r|_{t_2} = \frac{-(2V_{bus}/\pi) \sin(D_{ab}\pi/2) \sin[(1-D_{ab})\pi/2 - \angle Z_r]}{|Z_r|}, \quad (42)$$

where  $Z_r$  is defined as the equivalent impedance of the resonant tank and secondary side:

$$Z_r = j\omega_s L_p - \frac{j}{\omega_s C_1} + \frac{\omega_s^2 M^2}{j\omega_s L_s - j/(\omega_s C_2) + R_e}. \quad (43)$$

Therefore, the ZVS current of stage 2, defined as the minimum sum of  $i_{abc}$  and  $i_r$  at  $t_2$ , is obtained as:

$$I_{zvs} = \begin{cases} \frac{T_s}{4L_{in}} [\sqrt{3}V_{sp} - (1-D_{ab})V_{bus}] + \frac{-(2V_{bus}/\pi) \sin(D_{ab}\pi/2) \sin[(1-D_{ab})\pi/2 - \angle Z_r]}{|Z_r|}, & D_{ab} \geq 1 - \frac{\sqrt{3}V_{sp}}{V_{bus}} \\ \frac{-(2V_{bus}/\pi) \sin(D_{ab}\pi/2) \sin[(1-D_{ab})\pi/2 - \angle Z_r]}{|Z_r|}, & D_{ab} < 1 - \frac{\sqrt{3}V_{sp}}{V_{bus}} \end{cases} \quad (44)$$

### B. Derivation of the limitation of resonant coils design

From Fig. 15, the output power should be smaller than the input power at the conditions of  $f_s$  larger than  $f_3$  when  $D_{ab}$  is equal to 1; hence, the following expression is obtained:

$$P_{in}(\omega_s)|_{D_{ab}=1} = P_{in,max} \frac{\omega_s}{\omega_s} \geq P_o(\omega_s)|_{D_{ab}=1}, \quad (45)$$

which means that:

$$[\omega_s P_o(\omega_s)|_{D_{ab}=1}]_{\max} = \omega_s P_o(\omega_s)|_{D_{ab}=1}. \quad (46)$$

When  $D_{ab}$  is set as 1, output power  $P_o$  can be transformed as:

$$P_o|_{D_{ab}=1} = \frac{8(V_o/n)^2}{\pi^2} \frac{1}{\omega_s (M/n)} \sqrt{\frac{\left[ \frac{V_{bus}}{2(V_o/n)} \right]^2 - \left[ \frac{(\omega_s L_p - 1/(\omega_s C_1))}{\omega_s (M/n)} \right]^2}{\left[ \left( \frac{(\omega_s L_p - 1/(\omega_s C_1))}{\omega_s (M/n)} \right)^2 - 1 \right]^2}}, \quad (47)$$



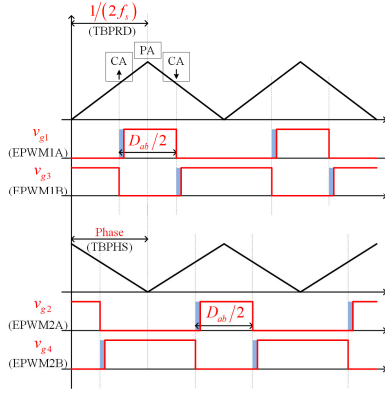
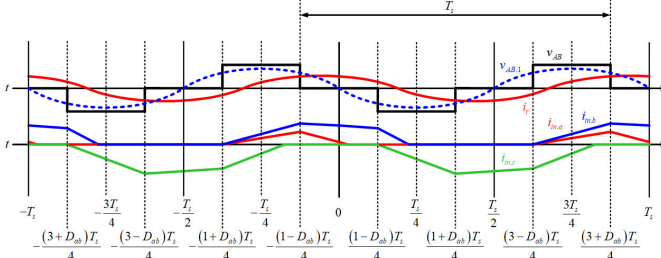


Fig. 31. PWM generation scheme

Fig. 32. Ideal waveforms of  $v_{AB}$ ,  $v_{AB,1}$ ,  $i_r$ ,  $i_{in,a}$ ,  $i_{in,b}$ ,  $i_{in,c}$  for analysis and calculation

where  $n$  is defined as the square root of the ratio of  $L_s$  and  $L_p$  and resonant frequencies ( $\omega_3$ ) of primary and secondary sides are assumed as the same:

$$n = \sqrt{\frac{L_s}{L_p}}, \quad (48)$$

$$\omega_3 = \frac{1}{\sqrt{L_p C_1}} = \frac{1}{\sqrt{L_s C_2}}. \quad (49)$$

Hence, from (46) and (47), the following inequality is obtained:

$$\omega_3 P_o|_{D_{ab}=1} = \frac{8(V_o/n)^2}{\pi^2} \cdot \frac{1}{(M/n)} \cdot \sqrt{\frac{\left[ \frac{V_{bus}}{2(V_o/n)} \right]^2 - \left[ \frac{\left( \omega_s L_p - \frac{1}{\omega_s C_1} \right)}{\omega_s (M/n)} \right]^2}{\left[ \left( \frac{\omega_s L_p - \frac{1}{\omega_s C_1}}{\omega_s (M/n)} \right)^2 - 1 \right]}} \quad (50)$$

$$\leq \frac{8(V_o/n)^2}{\pi^2} \cdot \frac{1}{(M/n)} \cdot \frac{V_{bus}}{2(V_o/n)},$$

which is solved with the result of (33).

### C. PWM generation scheme

TI DSP28335 control card is used as the controller of the proposed topology and Fig. 31 shows its PWM generation scheme. Two EPWM modules (EPWM1 and EPWM2) are used to provide driving signals for switches  $Q_1 - Q_4$ : EPWM1A for  $v_{g1}$ ; EPWM1B for  $v_{g3}$ ; EPWM2A for  $v_{g2}$ ; and EPWM2B for  $v_{g4}$ . The modules' registers TBPRD, CMPA, and TBPHS are control variables corresponding to frequency  $f_s$ , duty cycle  $D_{ab}$ , and phase difference  $P_h$ .

### D. Power loss analysis

The overall power loss of the proposed topology mainly consists of power losses of the input filter, input inductors, front-end diodes  $D_{r1} - D_{r6}$ , switches  $Q_1 - Q_4$ , resonant coils of WPT tank, and secondary-side diodes  $D_{s1} - D_{s4}$ , which are

analyzed and calculated in details as follows:

#### 1) Input filter

The power loss of the input filter mainly results from its inductors. Due to the current flowing through them is 50 Hz, the core loss is very small and can be ignored compared to the copper loss. Therefore, the power loss of the input filter is calculated as:

$$P_{if} = \begin{cases} \frac{6R_{if}}{\pi} \int_0^{\arcsin\left(\frac{1-D_{ab}}{2m}\right)} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta + \int_{\arcsin\left(\frac{1-D_{ab}}{2m}\right)}^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{-(1/m)(1-D_{ab})^2 + 2(1+D_{ab}^2) \sin \theta}{32(1-m \sin \theta)} \right)^2 d\theta, & D_{ab} > 1-2m \\ \frac{6R_{if}}{\pi} \int_0^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta, & D_{ab} \leq 1-2m \end{cases}, \quad (51)$$

where  $m$  is defined as the ratio of  $V_{sp}$  and  $V_{bus}$ , and  $R_{if}$  is the equivalent series resistance (ESR) of the inductors of the input filter.

#### 2) Input inductors

From [49] – [51], the formula to calculate core loss with DCM boost inductor current waveform can be derived, and the core loss of input inductors is given by:

$$P_{L_{in}} = \begin{cases} 3V_{if} f_s \cdot \frac{2}{\pi} \int_0^{\arcsin\left(\frac{1-D_{ab}}{2m}\right)} k_i \left( \frac{\mu_r N V_{sp} \sin \theta D_{ab}}{L_m} \right)^2 \frac{D_{ab}}{2f_s} d\theta + \int_{\arcsin\left(\frac{1-D_{ab}}{2m}\right)}^{\frac{\pi}{2}} k_i \left( \frac{\mu_r N V_{sp} \sin \theta D_{ab}}{L_m} \right)^2 \frac{D_{ab}}{2f_s} \left( \frac{(V_{bus}/2) - V_{sp} \sin \theta}{2f_s (V_{bus}/2 - V_{sp} \sin \theta)} \right)^2 d\theta, & D_{ab} > 1-2m \\ 3V_{if} f_s \cdot \frac{2}{\pi} \int_0^{\frac{\pi}{2}} k_i \left( \frac{\mu_r N V_{sp} \sin \theta D_{ab}}{L_m} \right)^2 \frac{D_{ab}}{2f_s} d\theta, & D_{ab} \leq 1-2m \end{cases}, \quad (52)$$

where  $A_e$  and  $V_e$  stand for the cross-sectional area and the volume of the magnetic core respectively.  $N$  is the number of coils,  $\mu_r$  is relative permeability, and  $\mu_0$  is the permeability constant.  $k_i$  is the constant related to  $k$ ,  $\alpha$ ,  $\beta$ , defined as:

$$k_i = \frac{k}{2^{\beta+1} \pi^{\alpha-1} \left( 0.2761 + \frac{1.7061}{\alpha+1.354} \right)}, \quad (53)$$

where constants  $k$ ,  $\alpha$ ,  $\beta$  (constants to calculate core loss) can be found from the relevant datasheet.

Copper loss of input inductors is given by:

$$P_{L_{in, copper}} = \begin{cases} \frac{6R_{Lin}}{\pi} \int_0^{\arcsin\left(\frac{1-D_{ab}}{2m}\right)} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta + \int_{\arcsin\left(\frac{1-D_{ab}}{2m}\right)}^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{-(1/m)(1-D_{ab})^2 + 2(1+D_{ab}^2) \sin \theta}{32(1-m \sin \theta)} \right)^2 d\theta, & D_{ab} > 1-2m \\ \frac{6R_{Lin}}{\pi} \int_0^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta, & D_{ab} \leq 1-2m \end{cases}, \quad (54)$$

where  $R_{Lin}$  is the ESR of input inductors.

#### 3) Diodes $D_{r1} - D_{r6}$

By analyzing the operation of the proposed topology, each front-end diode conducts for a half-cycle of the line period. Hence, the total losses of diodes  $D_{r1} - D_{r6}$  are calculated by:

$$P_{Dr} = \begin{cases} \frac{6V_{fr}}{\pi} \int_0^{\arcsin\left(\frac{1-D_{ab}}{2m}\right)} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta + \int_{\arcsin\left(\frac{1-D_{ab}}{2m}\right)}^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{-(1/m)(1-D_{ab})^2 + 2(1+D_{ab}^2) \sin \theta}{32(1-m \sin \theta)} \right)^2 d\theta, & D_{ab} > 1-2m \\ \frac{6V_{fr}}{\pi} \int_0^{\frac{\pi}{2}} \left( \frac{V_{sp} T_s}{L_m} \frac{D_{ab}^2 \sin \theta}{8(1-2m \sin \theta)} \right)^2 d\theta, & D_{ab} \leq 1-2m \end{cases}, \quad (55)$$

4) *Switches*  $Q_1 - Q_4$

$$P_{Q_i,con} = \frac{6R_{ds,on}.12}{T_I T_s} \int_0^{\frac{T_I}{6}} \left[ \int_{\frac{3-D_{ab}T_s}{4}}^{\frac{3+D_{ab}T_s}{4}} (i_{abc} + i_r)^2 dt \right] dt, \quad (56)$$

$$P_{Q_2.con} = \frac{6R_{ds.on.12}}{T_I T_s} \int_0^{\frac{T_I}{6}} \left[ \int_{\frac{1-D_{ab}T_s}{4}}^{\frac{1+D_{ab}T_s}{4}} (i_{abc} + i_r)^2 dt \right] dt, \quad (57)$$

$$P_{Q_s, con} = P_{Q_s, con} = \frac{6R_{ds, on} 34}{T_l T_s} \int_0^{\frac{T_l}{6}} \left[ \int_{-\frac{1-D_{ab}}{4} T_s}^{\frac{1-D_{ab}}{4} T_s} (i_{abc} + i_r)^2 dt + \int_{\frac{1+D_{ab}}{4} T_s}^{\frac{3-D_{ab}}{4} T_s} (i_{abc} + i_r)^2 dt \right] dt, \quad (58)$$

If ZVS can be achieved for switches  $Q_1 - Q_4$ , there will be no switching loss theoretically. However, as analyzed in section II.E, ZVS cannot be fully achieved for the switches at relatively low load conditions. At the instant of  $Q_2$ 's turning-ON and  $Q_4$ 's turning-OFF, when  $i_{abc}$  reaches zero and  $i_r$  is negative, hard-switching will occur instead of ZVS. Due to the symmetry of operation, power losses of  $Q_1$ 's turning-ON and  $Q_3$ 's turning-OFF are equal to those of  $Q_2$ 's turning-ON and  $Q_4$ 's turning-OFF respectively and can be calculated as:

$$P_{Q_1, SW} = P_{Q_2, SW} = \frac{1}{2} \cdot \frac{V_{bus}}{2} \cdot \left( i_r \Big|_{t=\frac{(3-D_{ab})T_s}{4}} \right) \cdot t_{r,12} \cdot f_s, \quad (59)$$

$$P_{Q_3,sw} = P_{Q_4,sw} = \frac{1}{2} \cdot \frac{V_{bus}}{2} \cdot \left( i_r \left|_{t=\frac{(3-D_{ab})T_s}{4}} \right. \right) \cdot t_{f,34} \cdot f_s, \quad (60)$$

### 5) Resonant coils of WPT tank

Copper losses of primary-side and secondary-side coils of WPT tank are calculated as:

$$P_{L_p} = \left[ \frac{\sqrt{2}V_{bus} \sin(D_{ab}\pi/2)}{\pi|Z_r|} \right]^2 \cdot R_{l_p}, \quad (61)$$

$$P_{LS} = \left[ \frac{2\sqrt{2}V_o}{\pi R_e} \right]^2 \cdot R_{ls}, \quad (62)$$

where  $Z_r$  and  $R_e$  can be obtained from (43) and (8) respectively.

6) *Diodes  $D_{s1} - D_{s4}$*

The total losses of secondary-side diodes  $D_{s1} - D_{s4}$  are calculated as:

$$P_{Ds} = 4 \cdot \frac{1}{\pi} \cdot \frac{4V_o}{\pi R_o} \cdot V_{fs} = \frac{16V_o V_{fs}}{\pi^2 R_o}, \quad (63)$$

where  $V_{fs}$  is the forward drop voltage of diodes  $D_{s1} - D_{s4}$ .

### E. Other expressions

Fig. 32 shows the ideal waveforms of the proposed converter for analysis and calculation, where  $v_{AB,1}$  is the fundamental component of  $v_{AB}$ , calculated as:

$$v_{AB,1} = -(2V_{bus}/\pi) \sin(D_{ab}\pi/2) \sin(\omega_s t). \quad (64)$$

$Z_r$  is defined as the equivalent impedance of the WPT resonant

tank and the secondary-side circuit, calculated as (43). Therefore, the current flowing through the primary side of the WPT resonant tank,  $i_r$ , is calculated as:

$$i_r = \frac{v_{AB,1}}{Z_r} = \frac{-(2V_{bus}/\pi)\sin(D_{ab}\pi/2)\sin[\omega_s t - \angle Z_r]}{|Z_r|}, \quad (65)$$

In the following calculations,  $v_{s,x}$  ( $x=a, b$ , or  $c$ ) means equivalent phase voltage  $v_{s,a}$ ,  $v_{s,b}$ , or  $v_{s,c}$ :

$$v_{s.a} = V_{sp} \sin(\omega_l t), \quad (66)$$

$$v_{s,b} = V_{sp} \sin\left(\omega_l t - \frac{2}{3}\pi\right), \quad (67)$$

$$v_{s.c} = V_{sp} \sin\left(\omega_l t - \frac{4}{3}\pi\right), \quad (68)$$

$i_{in,x}$  means input inductor current  $i_{in,a}$ ,  $i_{in,b}$ , or  $i_{in,c}$ .  $i_{abc}$  is the sum of  $i_{in,a}$ ,  $i_{in,b}$ , and  $i_{in,c}$ :

$$i_{abc} = i_{in,a} + i_{in,b} + i_{in,c}, \quad (69)$$

where  $i_{in,a}$ ,  $i_{in,b}$ , and  $i_{in,c}$  are calculated as (70):

$$\begin{aligned}
& \left. \begin{aligned} & \frac{v_{i,2} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \left( i + \frac{(1-D_{i,2}) T_i}{4} \right) & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4} \\ & \frac{v_{i,2} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \frac{(1-D_{i,2}) T_i}{2} & \frac{(1-D_{i,2}) T_i}{4} \leq t < t_{i,2} \\ & -\frac{v_{i,2} - v_{i,1}}{L_{i,2}} \left( i - \frac{(1-D_{i,2}) T_i}{4} \right) & v_{i,2} > \frac{(1-D_{i,2})}{2} v_{i,1} \end{aligned} \right\} \\
& \quad \begin{aligned} & 0 & t_i \leq t < \frac{(3-D_{i,2}) T_i}{4} \\ & \frac{v_{i,2}}{L_{i,2}} \left( i - \frac{(3-D_{i,2}) T_i}{4} \right) & \frac{(3-D_{i,2}) T_i}{4} \leq t \leq \frac{(3+D_{i,2}) T_i}{4} \\ & \frac{v_{i,2} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \left( i + \frac{(1-D_{i,2}) T_i}{4} \right) & \frac{(1-D_{i,2}) T_i}{4} \leq t < t_i \end{aligned} \\
& \quad \begin{aligned} & 0 & t_i \leq t < \frac{(3-D_{i,2}) T_i}{4}, \quad 0 \leq v_{i,1} \leq \frac{(1-D_{i,2})}{2} v_{i,2} \\ & \frac{v_{i,1}}{L_{i,1}} \left( i - \frac{(3-D_{i,2}) T_i}{4} \right) & \frac{(3-D_{i,2}) T_i}{4} \leq t \leq \frac{(3+D_{i,2}) T_i}{4} \\ & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4}, & \end{aligned} \\
& \quad \begin{aligned} & 0 & t_i \leq t < \frac{(3+D_{i,2}) T_i}{4} \\ & \frac{v_{i,1}}{L_{i,1}} \left( i - \frac{(1-D_{i,2}) T_i}{4} \right) & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4}, \quad 0 > v_{i,1} \geq -\frac{(1-D_{i,2})}{2} v_{i,2} \\ & \frac{v_{i,1} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \left( i - \frac{(1+D_{i,2}) T_i}{4} \right) & \frac{(1+D_{i,2}) T_i}{4} \leq t < t_i \end{aligned} \\
& \quad \begin{aligned} & 0 & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4}, \\ & \frac{v_{i,1}}{L_{i,1}} \left( i - \frac{(1-D_{i,2}) T_i}{4} \right) & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4} \\ & \frac{v_{i,1} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \left( i - \frac{(1+D_{i,2}) T_i}{4} \right) & \frac{(1+D_{i,2}) T_i}{4} \leq t < t_i \end{aligned} \\
& \quad \begin{aligned} & 0 & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4}, \\ & \frac{v_{i,1}}{L_{i,1}} \left( i - \frac{(1-D_{i,2}) T_i}{4} \right) & \frac{(1-D_{i,2}) T_i}{4} \leq t < \frac{(1+D_{i,2}) T_i}{4} \\ & \frac{v_{i,1} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \left( i - \frac{(1+D_{i,2}) T_i}{4} \right) & \frac{(1+D_{i,2}) T_i}{4} \leq t < \frac{(3-D_{i,2}) T_i}{4}, \quad v_{i,1} < -\frac{(1-D_{i,2})}{2} v_{i,2} \\ & \frac{v_{i,1} D_{i,2} T_i}{L_{i,2}} - \frac{v_{i,2} f_{i,2} - v_{i,1}}{L_{i,2}} \frac{(1-D_{i,2}) T_i}{2} & \frac{(3-D_{i,2}) T_i}{4} \leq t < t_i \end{aligned}
\end{aligned}$$

where  $t_w, t_x, t_y, t_z$  are calculated as:

$$t_w = \frac{2v_{s,x} - V_{bus}(1 - D_{ab})}{V_{bus} - v_{s,x}} \cdot \frac{T_s}{4} + \frac{(1 - D_{ab})T_s}{4}, \quad (71)$$

$$t_x = \frac{v_{s,x}}{V_{\text{bus}}/2 - v_{s,x}} \cdot \frac{D_{ab}T_s}{2} - \frac{(1-D_{ab})T_s}{4}, \quad (72)$$

$$t_y = \frac{-v_{s,x}}{V_{bus}/2 + v_{s,x}} \cdot \frac{D_{ab}T_s}{2} + \frac{(1+D_{ab})T_s}{4}, \quad (73)$$

$$t_z = \frac{-2v_{s,x} - V_{bus}(1 - D_{ab})}{V_{bus} + v_{s,x}} \cdot \frac{T_s}{4} + \frac{(3 - D_{ab})T_s}{4}. \quad (74)$$

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