

Thermodynamic modeling of CO₂ solubility in saline water using NVT flash with the Cubic-Plus-Association equation of state

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Abstract

1 The accurate estimation of CO₂ sequestration potential in deep saline aquifers
2 requires the knowledge of CO₂ solubility in brine, thus placing importance
3 on reliable thermodynamic models that account for the effect of different
4 salts and their mixtures over wide ranges of pressure, temperature and
5 salt concentration. Most literature investigated CO₂ solubility in a single-
6 salt solution as a replacement of real saline water, which may significantly
7 overestimate CO₂ sequestration potential through solubility trapping. In
8 order to accurately estimate CO₂ sequestration potential over geological
9 conditions, the Peng-Robinson Cubic-Plus-Association (PR-CPA) equation
10 of state (EOS) is used in this study to model both aqueous and nonaque-
11 ous phases. A promising flash technique at given moles, volume and tem-
12 perature, known as NVT flash, is employed and the salting-out effect is
13 reproduced by correcting the chemical potential of aqueous nonelectrolyte
14 components. To represent real saline environments, five salts are considered,

1 including sodium chloride (NaCl), potassium chloride (KCl), calcium chlo-
2 ride (CaCl_2), magnesium chloride (MgCl_2) and sodium sulfate (Na_2SO_4).
3 With taking into account the electrostatic contribution caused by salts, the
4 combination of the salt-based PR-CPA EOS and NVT flash accurately mod-
5 els the solubility behavior of CO_2 in mixed-salt solutions and the numerical
6 results agree with experimental data very well. Moreover, the proposed
7 CPA model exhibits neck-to-neck accuracy to the more sophisticated elec-
8 trolyte CPA EOS, thus making it promising to accurately estimate carbon
9 sequestration potential in saline aquifers through solubility trapping.

Keywords:

CO_2 sequestration, Saline water, Thermodynamic modeling, NVT flash,
Cubic-Plus-Association equation of state

1. Introduction

10 Nowadays, among various environmental problems, global warming is
11 an extensively concerned issue, since the anthropogenic emission of CO_2
12 is imperiling the earth ecosystem and will threaten human civilization if
13 not controlled in time. It has been reported that the Paris Agreement
14 climate goals are being challenged due to committed emissions from existing
15 energy infrastructure [1]. Unfortunately, fossil fuels are still believed to
16 occupy the dominant position of the world's energy supply in the foreseeable

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1 future, due to their inherent advantages, such as large reserves, competitive
2 cost and easy storage and transportation [2, 3]. It is imperative to find
3 an immediately available and technologically feasible approach to reduce
4 enormous CO₂ emissions from fossil fuel combustion, thus giving birth to
5 the idea of CO₂ sequestration.

6 One economic disposal approach is injecting CO₂ into oil reservoirs to
7 enhance oil recovery (EOR) and meanwhile sequesters CO₂ underground
8 [4–6]. When CO₂ contacts with oil, hydrocarbon components are extracted
9 into the less viscous CO₂ phase and, on the other hand, the dissolved CO₂
10 makes oil swelling so that oil can be displaced more easily [7, 8]. However,
11 since a considerable amount of CO₂ is "lost" to the oil phase for recovery
12 enhancement, the carbon sequestration potential in this EOR process is less
13 than expectation. Another promising geological site for CO₂ sequestration
14 is deep saline aquifers, which provide substantial storage capacity due to
15 its large pore volume and wide distribution [2, 9, 10]. Most of the injected
16 CO₂ is trapped in saline water by dissolution and such a mechanism is
17 called solubility trapping [11, 12]. However, saline water usually has a
18 considerable salt content and the presence of salts could significantly reduce
19 CO₂ solubility, which is known as the salting-out effect.

20 Clearly, a better understanding of CO₂ solubility in saline water plays
21 a critical role in the success of CO₂ sequestration projects [13–15]. Such a
22 knowledge is important to design CO₂ flooding [16–19] as well since water is
23 injected either alternately or simultaneously with the CO₂ slug [20]. More-

1 over, unlike other gases, the dissolution of CO_2 into aqueous phase often
 2 causes a density increase, which can induce natural convection and facilitate
 3 CO_2 mixing with water [10, 21, 22]. Therefore, it is necessary to accurately
 4 describe the aqueous-phase density when modeling CO_2 sequestration and
 5 migration in saline aquifers, making the fugacity-fugacity (ϕ - ϕ) model ad-
 6 vantageous over the fugacity-activity (γ - ϕ) model even though the latter has
 7 been successfully applied to estimate CO_2 solubility in water/brine [23–27].
 8 Another distinct advantage of the ϕ - ϕ approach is all fluid phases can be
 9 modeled by a single consistent equation of state (EOS) [28–31]. Popular cu-
 10 bic EOSs, such as Peng-Robinson (PR) EOS [32] and Soave-Redlich-Kwong
 11 (SRK) EOS [33], were used to deal with gas-water or gas-brine equilibria
 12 in combination with complicated mixing rules, improved α -term or non-
 13 symmetric binary interaction coefficients (BICs) [34–38], but these semiem-
 14 pirical cubic EOSs were originally designed for hydrocarbons only. As a
 15 result, they are essentially inapplicable to associating and highly polar flu-
 16 ids [39], e.g. water, which exhibits unusual thermodynamic behaviors due
 17 to strong hydrogen bonding interactions. There is also evidence that CO_2
 18 can form weak hydrogen bonds in the presence of associating species [40].
 19 As can be seen, such behaviors cannot be easily captured by conventional
 20 thermodynamic models that only take into account the physical interactions
 21 between molecules.

22 The establishment of Wertheim’s thermodynamic perturbation theory
 23 [41] contributes to CPA EOS [42], which explicitly accounts for hydrogen

1 bonding interactions and takes advantage of a cubic EOS to describe phys-
2 ical interactions. Despite of its simple physical term, CPA EOS exhibits
3 high computational efficiency and accuracy so that it has been extensively
4 applied to various phase equilibria problems. During the past decade, nu-
5 merous efforts have been made to accurately estimate CO_2 solubility by
6 CPA-type models either in fresh water [43–48] or NaCl solution [49–51],
7 both of which are far from the composition of real saline environments. In
8 reality, saline water consists of a variety of salts, including NaCl, KCl, CaCl_2 ,
9 MgCl_2 , Na_2SO_4 , etc. Unfortunately, no representative salinity composition
10 has been reported so far since it is highly dependent on the local geological
11 condition of saline water. Despite this, the salting-out effect of different
12 salts cannot be fully represented by a single salt. Thus, accurate evaluation
13 of CO_2 sequestration potential heavily relies on modeling of CO_2 solubility
14 behavior in mixed-salt solutions. Just recently, Sun et al. [52] applied their
15 electrolyte CPA EOS, also called e-CPA EOS, to estimate CO_2 solubility
16 in both single- and mixed-salt solutions. The electrostatic contributions in
17 their model has two sources, the ion-ion long range interactions described by
18 the Debye-Hückel (DH) theory and the solvation interactions represented by
19 the Born term. By tuning ion-based parameters to the experimental data,
20 they successfully modeled CO_2 solubility behaviors in single- and mixed-salt
21 solutions, which exhibited satisfactory agreement with experimental data.

22 Despite the fact that most of CPA models use SRK EOS as the phys-
23 ical term, recently PR-CPA (Peng-Robinson Cubic-Plus-Association) EOS

1 has gained popularity and achieved great success in various engineering
2 problems, such as inhibition of gas hydrate formation [53], removal of acid
3 gas [54, 55], as well as production of bitumen [56]. However, it has not
4 been extended to phase behavior modeling of CO₂-brine systems. Thus, in
5 this study, PR-CPA EOS is used to estimate CO₂ solubility in mixed-salt
6 solutions, which comprise the five salts mentioned above. The salting-out
7 effect is reproduced by correcting the chemical potential of aqueous nonelec-
8 trolyte components. More importantly, the distinct difference between this
9 work and all the other works is phase equilibria modeling is performed at
10 given moles, volume and temperature (the so-called NVT flash), instead of
11 the conventional NPT flash framework. The new variable specification ex-
12 hibits inherent advantages, such as well-posed formulation, unique pressure-
13 volume relation, as well as promising potential in compositional flow simu-
14 lation [57]. The NVT flash also has appealing properties for both implicit
15 flow simulation [58] and semi-implicit flow simulation [59, 60]. Numerous
16 efforts have been made to enhance computational performance of NVT flash
17 calculations [61–66] and extend its applications [67–72]. It is worth men-
18 tioning that Jindrová and Mikyška [73] previously modeled phase equilibria
19 of CO₂-H₂O mixture under the NVT flash framework with their PR-CPA
20 EOS to estimate the potential of CO₂ sequestration. However, they neither
21 considered the effect of salts nor compare their results with experimental
22 data. To the best of our knowledge, this is the first time that the combi-
23 nation of NVT flash and salt-based PR-CPA EOS is applied to deal with

1 phase equilibria for CO₂-brine systems over geological storage conditions.
 2 Numerical results demonstrate that the proposed thermodynamic model
 3 can accurately estimate CO₂ solubility in saline water and it exhibits neck-
 4 to-neck accuracy in comparison to the more sophisticated e-CPA model
 5 proposed by Sun et al. [52].

6 The remainder of this paper is organized as follows. In the following
 7 section, we first formulate the NVT flash problem to model two-phase equi-
 8 librium between CO₂ and brines. Next, data and parameter optimization
 9 are elaborated. In Section 4, we present numerical results for single- and
 10 mixed-salt solutions and discuss the results. At the end, we make our con-
 11 clusions in Section 5.

2. Thermodynamic modeling

2.1. Phase equilibria between CO₂ and H₂O

12 PR-CPA EOS takes advantage of PR EOS to describe the physical in-
 13 teractions between CO₂ and H₂O while the thermodynamic perturbation
 14 theory models associating interactions. Thus, the Helmholtz free energy
 15 density $f(\mathbf{n})$ has two components

$$f(\mathbf{n}) = \frac{F(\mathbf{n})}{V} = f^{\text{PR}}(\mathbf{n}) + f^{\text{assoc}}(\mathbf{n}) \quad (1)$$

16 where F is Helmholtz free energy, V is the volume of fluid mixture and
 17 \mathbf{n} is the vector of molar concentrations. The physical contribution f^{PR} is
 18 formulated based on PR EOS

$$f^{\text{PR}} = RT \sum_i n_i (\ln n_i - 1) - nRT \ln(1 - bn) + \frac{a(T)n}{2\sqrt{2}b} \ln \left(\frac{1 + (1 - \sqrt{2})bn}{1 + (1 + \sqrt{2})bn} \right), \quad (2)$$

1 where R is the universal gas constant, T is the temperature, $n = \sum_i n_i$
2 is the overall molar concentration. $a(T)$ and b represent the energy and
3 co-volume parameter of the fluid mixture, which can be computed by the
4 classical Van der Waals mixing rule

$$a(T) = \sum_i \sum_j x_i x_j (a_i a_j)^{1/2} (1 - k_{ij}) , \quad b = \sum_i x_i b_i , \quad (3)$$

5 where $a_i = a_i^0 \left[1 + c_i \left(1 - \sqrt{T/T_{c,i}} \right) \right]^2$, x_i is the mole fraction of compo-
6 nent i , and k_{ij} is the BIC between component i and j . For nonwater species,

$$a_i^0 = 0.45724 \frac{R^2 T_{c,i}^2}{P_{c,i}} , \quad (4)$$

$$b_i = 0.07780 \frac{R T_{c,i}}{P_{c,i}} , \quad (5)$$

$$c_i = \begin{cases} 0.37464 + 1.54226\omega_i - 0.26992\omega_i^2 , & \text{if } \omega_i < 0.5 \\ 0.3796 + 1.485\omega_i - 0.1644\omega_i^2 + 0.01667\omega_i^3 , & \text{if } \omega_i \geq 0.5 \end{cases} \quad (6)$$

7 where $P_{c,i}$, $T_{c,i}$ and ω_i denote the critical pressure, critical temperature and
8 acentric factor of component i , respectively.

9 According to the Wertheim's perturbation theory, the association con-
10 tribution to Helmholtz free energy density is given by

$$f^{\text{assoc}} = RT \sum_i n_i \sum_{A_i} \left(\ln X_{A_i} - \frac{1}{2} X_{A_i} + \frac{1}{2} \right) , \quad (7)$$

11 where X_{A_i} is the unbonded site fraction of site A on component i , which
12 can be solved from the following nonlinear equation system

$$X_{A_i} = \frac{1}{1 + \sum_j n_j \sum_{B_j} X_{B_j} \Delta^{A_i B_j}}, \quad (8)$$

1 with association strength

$$\Delta^{A_i B_j} = g \beta^{A_i B_j} \left[\exp \left(\frac{\varepsilon^{A_i B_j}}{RT} \right) - 1 \right] b_{ij}. \quad (9)$$

2 In Eq. (9), $\beta^{A_i B_j}$ and $\varepsilon^{A_i B_j}$ are the association volume and association en-
 3 ergy parameter between site A on component i and site B on component j .
 4 $b_{ij} = (b_i + b_j)/2$ is the cross co-volume parameter. The radial distribution
 5 function is approximated by $g = 1/(1 - 1.9\eta)$ [74], where $\eta = bn/4$ is the
 6 reduced density. Clearly, it is not straightforward to directly solve X_{A_i} from
 7 Eq. (8). Instead, the iterative algorithm proposed by Michelsen [75] is em-
 8 ployed here to efficiently compute X_{A_i} with no worry about the association
 9 scheme of CO₂ and H₂O molecules.

10 Similarly, chemical potential and pressure consist of both physical and
 11 association components as well

$$\begin{aligned} \mu_i &= \mu_i^{\text{PR}} + \mu_i^{\text{assoc}} + \Delta\mu_i^{\text{DH}}, \\ P &= P^{\text{PR}} + P^{\text{assoc}}. \end{aligned} \quad (10)$$

12 In addition, the expression of chemical potential includes an additional con-
 13 tribution in the presence of salts, which is denoted as $\Delta\mu_i^{\text{DH}}$. For the CO₂-
 14 H₂O system, $\Delta\mu_i^{\text{DH}} = 0$. Details on modeling of $\Delta\mu_i^{\text{DH}}$ will be described
 15 in subsection 2.2. The physical contributions to chemical potential and
 16 pressure are

$$\mu_i^{\text{PR}} = RT \ln n_i - RT \left(\ln(1 - bn) - \frac{nb_i}{1 - bn} \right) + \frac{2 \left(\sum_{j=1}^M x_j a_{ij} \right) b - ab_i}{2\sqrt{2}b^2} \times \ln \left(\frac{1 + (1 - \sqrt{2})bn}{1 + (1 + \sqrt{2})bn} \right) + \frac{a(T)n}{2\sqrt{2}b} \left(\frac{(1 - \sqrt{2})b_i}{1 + (1 - \sqrt{2})bn} - \frac{(1 + \sqrt{2})b_i}{1 + (1 + \sqrt{2})bn} \right), \quad (11)$$

$$P^{\text{PR}} = \frac{nRT}{1 - bn} - \frac{a(T)n^2}{1 + 2bn - (bn)^2}, \quad (12)$$

1 where $a_{ij} = (a_i a_j)^{1/2} (1 - k_{ij})$. On the other hand, the association contribu-
 2 tions can be computed by taking advantage of the stationary point of the
 3 well-defined Q function in [76], which yields

$$\mu_i^{\text{assoc}} = RT \left[\sum_{A_i} \ln X_{A_i} - \frac{1}{2} \sum_{i=1}^M n_i \sum_{A_i} (1 - X_{A_i}) \frac{\partial \ln g}{\partial n_i} \right], \quad (13)$$

$$P^{\text{assoc}} = -\frac{1}{2} RT \left(1 + \eta \frac{\partial \ln g}{\partial \eta} \right) \sum_{i=1}^M n_i \sum_{A_i} (1 - X_{A_i}). \quad (14)$$

4 Note that the NVT flash requires the chemical equilibrium condition ($\mu_i^{\text{naq}} =$
 5 μ_i^{aq}) and mechanical equilibrium condition ($P^{\text{naq}} = P^{\text{aq}}$) are simultaneously
 6 satisfied at the equilibrium state. The superscript naq and aq represent the
 7 nonaqueous and aqueous phase. Chemical potential and pressure in each
 8 phase can be calculated from Eq. (10) to (14).

2.2. Modeling of electrolyte solutions

9 Real formation water or saline water usually has a considerable salt
 10 content and could significantly inhibit the dissolution of CO₂ in water, which
 11 is known as the salting-out effect. Thus, it is of vital importance to take
 12 into account the effect of salts on phase equilibria modeling of CO₂-brine
 13 systems. In this study, we assume salts only exist in the aqueous phase.

1 The chemical potential of each nonelectrolyte component in the aqueous
 2 phase is corrected by introducing the DH activity coefficient [77]

$$\ln \gamma_i^{\text{DH}} = \frac{2AM_m h_{is}}{B^3} f(BI^{\frac{1}{2}}), \quad (15)$$

3 with

$$f(BI^{\frac{1}{2}}) = 1 + BI^{\frac{1}{2}} - \frac{1}{(1 + BI^{\frac{1}{2}})} - 2 \ln(1 + BI^{\frac{1}{2}}), \quad (16)$$

4 where M_m is the molecular weight of salt-free mixture, h_{is} is the interac-
 5 tion parameter between nonelectrolyte component and salt, and the ionic
 6 strength

$$I = \frac{1}{2} \sum_j m_j z_j^2, \quad (17)$$

7 where m_j and z_j is the molality and ionic charge of ion j for a given salt,
 8 respectively. The coefficient A and B in Eq. (15) have the following form

$$A = 1.327757 \times 10^5 \frac{\rho_m^{\frac{1}{2}}}{(\eta_m T)^{\frac{3}{2}}}, \quad B = 6.35969 \frac{\rho_m^{\frac{1}{2}}}{(\eta_m T)^{\frac{1}{2}}}, \quad (18)$$

9 where ρ_m is the mass density, $\eta_m = x_w \eta_w$ is the dielectric constant of the
 10 salt-free mixture, x_w is the mole fraction of water and η_w is the dielectric
 11 constant of pure water at given density and temperature.

12 It can be seen from Eq (15) that the interaction parameter h_{is} plays a
 13 critical role in accurate modeling of CO₂ solubility in brines. In particular,
 14 the interaction parameter h_{ws} , between water and salts, is considered as a
 15 function of salt concentration and temperature [78]

$$h_{ws} = \frac{A_{ws}}{W} + B_{ws}W^2 + \frac{C_{ws}}{W^2} + D_{ws} + E_{ws}(T - 273.15), \quad (19)$$

16 while the interaction parameter between CO₂ and salts, h_{cs} , is assumed to

1 depend on temperature only [79],

$$h_{cs} = A_{cs}T^2 + B_{cs}T + C_{cs}, \quad (20)$$

2 where W is salt concentration in weight percent and T is temperature in
 3 Kelvin. Since the excess chemical potential follows $\mu_i^E = RT \ln \gamma_i$, the DH
 4 electrostatic contribution to chemical potential can be modeled by $\Delta\mu_i^{\text{DH}} =$
 5 $RT \ln \gamma_i^{\text{DH}}$. For a mixed-salt solution, the overall electrostatic contribution
 6 to chemical potential of a nonelectrolyte component is modeled based on
 7 the relationship proposed by [80]

$$\Delta\mu_i = \sum_{j=1}^{N_s} w_j \Delta\mu_{i,j}^0, \quad w_j = \frac{I_j}{\sum_j I_j} \quad (21)$$

8 where N_s is the number of salts, w_j is the ionic strength fraction of salt j ,
 9 and $\mu_{i,j}^0$ is the chemical potential of component i in the single-salt solution
 10 j at the overall ionic strength.

11 Similar to confined phase equilibria problems that take into account
 12 capillary effect, the additional chemical potential contribution converts the
 13 original optimization problem into an equation-solving problem [66] where
 14 the symmetric Jacobian matrix, commonly used to design efficient numerical
 15 algorithm, no longer exists. To enhance the convergence performance, a
 16 VT-based successive substitution iteration (SSI) [66, 81] is used to initialize
 17 Newton iterations. Moreover, the two-stage line search scheme is applied to
 18 ensure the computed variables sit inside their physically meaningful ranges
 19 and Helmholtz free energy constantly dissipates over iterations. If energy
 20 dissipation stops before it reaches the stopping criterion, we switch back to

1 SSI and continue phase equilibria calculation at the given condition. It is
 2 also worth mentioning that CPA EOS has a near-cubic behavior [42]. In
 3 other words, typically there are three real roots when solving the volume
 4 equation under the NPT flash framework. As a result, root selection has
 5 to be performed in certain rules, which may result into slow convergence or
 6 even incorrect solution for NPT flash if roots are improperly selected at the
 7 early stage. In contrast, this can be avoided in NVT flash calculation since
 8 each pressure corresponds to a unique volume.

3. Parameter optimization

9 To accurately model phase behavior using the CPA-type EOS, it is cru-
 10 cial to optimize parameters by fitting the experimental data. Moreover, the
 11 success of any association model depends on the association scheme and as-
 12 sociation approach of the investigated molecules, which could heavily affect
 13 the fitted parameters. A large amount of literature investigated which com-
 14 bination of association scheme and approach works best for the CO₂-H₂O
 15 system. Unfortunately, the optimal combination remains unclear [82]. In
 16 this study, both H₂O and CO₂ are assumed as 4-site molecules with two
 17 proton donors and two proton acceptors. Such association schemes have
 18 been extensively used in the literature. We consider CO₂ as a solvating
 19 molecule, which is only allowed to cross associate with H₂O. In the rest
 20 of this section, the shuffled complex evolution method proposed by Duan
 21 et al. [83] is used for parameter optimization. In addition, instead of using
 22 the sum of squared errors as the objective function, the absolute average

1 deviation (AAD), often used to indicate fitting errors, is directly minimized
 2 in our fitting process, which could help us avoid overfitting those outliers
 3 that are incorrectly or improperly measured in experiments [82]

$$\text{AAD}\% = \frac{1}{N_p} \sum_{i=1}^{N_p} \left| \frac{x_i^{\text{cal}} - x_i^{\text{exp}}}{x_i^{\text{exp}}} \right| \times 100, \quad (22)$$

4 where N_p is the number of data points, x_i^{cal} and x_i^{exp} represent the computed
 5 result and experiment data of the given property, respectively.

3.1. Physical and association parameters for water

6 To reproduce phase behavior of H_2O , all five pure-compound parame-
 7 ters, including a_i^0 , b_i , c_i , $\varepsilon^{A_i B_j}$ and $\beta^{A_i B_j}$, are tuned by fitting experimental
 8 data of saturated vapor pressure and liquid density [84, 85], obtained from
 9 DIPPR database. The fitting process is performed over the temperature
 10 range $0.42 < T_{r,w} < 0.95$, where $T_{r,w}$ denotes the reduced temperature of
 11 water. Figure 1 compares the computed vapor pressure and liquid density
 12 using the optimized parameters with the experiment data. It can be seen the
 13 computed saturation pressures agree with the measurements very well but
 14 the computed liquid density is slightly overestimated at low temperature.
 15 On the other hand, since saturation vapor pressures and liquid densities of
 16 CO_2 can be accurately estimated using the critical pressure, temperature
 17 and acentric factor (shown in Table 1), it is decided to use Eq. (4), (5) and
 18 (6) to compute a_i^0 , b_i and c_i rather than re-estimate these parameters for
 19 CO_2 . In addition, thanks to the introduction of the cross association factor,
 20 it is unnecessary to parameterize $\varepsilon^{A_i B_j}$ and $\beta^{A_i B_j}$ for CO_2 . Table 2 shows

- 1 the pure-compound parameters of H₂O and CO₂ and the corresponding
- 2 AAD of saturated vapor pressure and liquid density.

Table 1: Compositional properties of H₂O and CO₂.

Component	$T_{c,i}$ [K]	$P_{c,i}$ [Pa]	ω_i	$M_{w,i}$ [kg · mol ⁻¹]
H ₂ O	647.29	2.209×10^7	0.3440	0.01802
CO ₂	304.14	7.375×10^6	0.2390	0.04401

Table 2: Physical and association parameters of H₂O and CO₂.

Component	a_0 [Pa · (m ³ /mol) ²]	b [m ³ /mol]	c_1	ε [Pa · m ³ /mol]	β	AAD %	
						P_{vapor}	ρ_{liquid}
H ₂ O	0.1405	1.4759×10^{-5}	1.2088	1.4159×10^4	0.1134	0.20	1.06
CO ₂	0.3962	2.6652×10^{-5}	0.7060	-	-	0.78	2.55

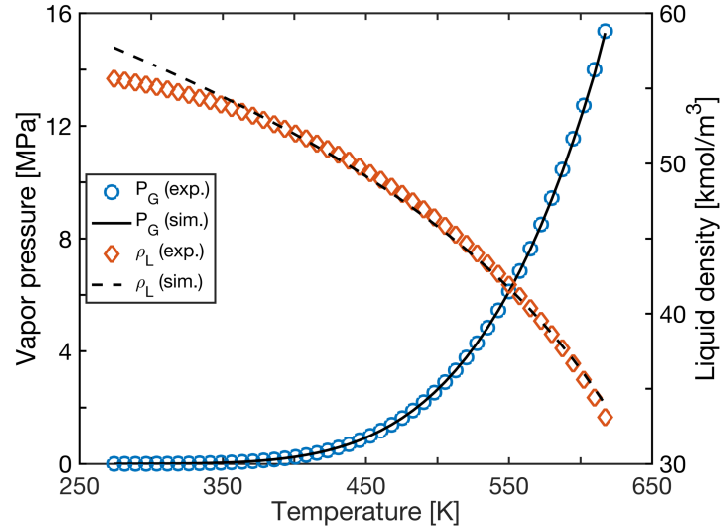


Figure 1: Fitting experimental vapor pressure and liquid density data for H₂O. The experimental data are obtained from DIPPR database.

3.2. Binary interaction coefficient and cross-association factor

Another two important parameters for phase equilibria modeling of CO₂-H₂O system are BIC, k_{ij} , and the cross association factor, s_{ij} , which describes the cross-association strength between CO₂ and H₂O. Essentially, tuning the cross-association factor is equivalent to tuning the cross-association volume in the modified CR-1 combining rule proposed by Folas et al. [86]. The cross-association strength is computed by the product of self-association strength of H₂O and s_{ij} [87]. To better represent k_{ij} and s_{ij} , most literature considers they are strongly temperature-dependent. By extensively testing the performance of published expressions, we adopt $k_{ij} = a_1 T_{r,\text{CO}_2} + a_2$ where T_{r,CO_2} denote the reduced temperature of CO₂, and $s_{ij} = b_1 T_{r,\text{CO}_2}^3 + b_2 T_{r,\text{CO}_2}^2 + b_3 T_{r,\text{CO}_2} + b_4$. Six coefficients a_1 , a_2 , b_1 , b_2 , b_3 and b_4 are fitted to the experimental solubility data of CO₂-H₂O mixtures. In order to obtain the most accurate and reliable data, Aasen et al. [82] conducted an exhaustive literature review to evaluate published experimental data. Here we use all the available data that we can ensure their accuracy and reliability from the suggested publications [37, 46, 88–96] to tune the six coefficients mentioned above, which yields

$$k_{ij} = 0.6546 T_{r,\text{CO}_2} - 0.6165, \quad (23)$$

$$s_{ij} = -0.4254 T_{r,\text{CO}_2}^3 + 1.6922 T_{r,\text{CO}_2}^2 - 1.9815 T_{r,\text{CO}_2} + 0.7380, \quad (24)$$

with the AAD of 4.91 % for CO₂ solubility in the H₂O-rich phase and AAD of 9.79 % for H₂O solubility in the CO₂-rich phase. Figure 2 shows the

1 values of k_{ij} and s_{ij} over the temperature range $T \in [278, 478]$ K.

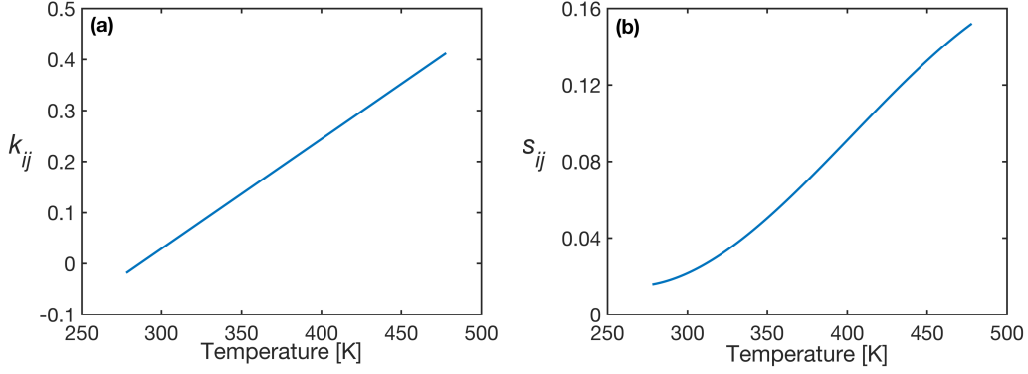


Figure 2: Binary interaction coefficient k_{ij} (a) and cross-association factor s_{ij} (b) as a function of temperature at $T \in [278, 478]$ K for CO₂-H₂O system.

3.3. Interaction paramters between nonelectrolyte component and salt

2 Accurate description of CO₂ solubility behavior in saline water places
3 importance on the optimization of the H₂O-salt interaction parameter, h_{ws} ,
4 and CO₂-salt interaction parameter, h_{cs} . For this purpose, the five coef-
5 ficients in h_{ws} , see Eq. (19), are fitted to the experimental freezing point
6 depression data by modeling phase equilibria between the aqueous single-
7 salt solution and its ice phase at the ice vapor pressure. We collect all
8 the available experimental data for NaCl [78, 97–101], KCl [97, 99, 101],
9 CaCl₂ [78, 97, 100–103], MgCl₂ [78, 97, 98, 101, 102, 104] and Na₂SO₄
10 [101, 104, 105] from the publications suggested in [78]. The optimized coef-
11 ficients of h_{ws} are shown in Table 3. Figure 3 displays the computed melting
12 temperatures together with the experimental data. It can be seen the fitted
13 coefficients accurately predict the melting temperature of each single-salt so-

1 lution as the salt concentration increases. In addition, the three coefficients
 2 in h_{cs} , see Eq. (20), are optimized using the experimental solubility data
 3 of CO₂ in the NaCl [93, 106–109], KCl [110–112], CaCl₂ [112–114] MgCl₂
 4 [112, 114], and Na₂SO₄ [112, 115] solution, respectively. Table 4 shows the
 5 investigated temperature and molality ranges where the coefficients of h_{cs}
 6 are applicable and the AAD of CO₂ solubility in each single-salt solution.
 7 Overall, the optimized coefficients yield satisfactory accuracy, of which the
 8 CO₂-CaCl₂ interaction parameter exhibits a little higher AAD than others.

Table 3: Optimized coefficients for the H₂O-salt interaction parameter h_{ws} .

	A	B	C	D	E/K	AAD %
NaCl	−9.4875	−0.0011	−0.1569	−7.7593	0.1998	0.011
KCl	−11.7708	−0.0018	−0.0336	−7.8928	0.0495	0.010
CaCl ₂	−2.1142	−0.0035	−0.0380	−4.3097	0.1768	0.036
MgCl ₂	−1.7205	−0.0173	−0.0499	−4.7829	0.0100	0.040
Na ₂ SO ₄	−7.6939	−0.0014	−0.0074	−2.3803	0.0067	0.036

Table 4: Optimized coefficients for the CO₂-salt interaction parameter h_{cs} .

	T [K]	M [mol/kg]	$A \times 10^{-5}$	B	C	AAD %
NaCl	293.08 - 433.08	0.25 - 6.00	−1.9837	−0.1334	85.2549	4.26
KCl	313.1 - 433.1	0.50 - 4.50	1.3679	−0.0236	26.1853	4.72
CaCl ₂	298.15 - 424.64	0.18 - 5.00	−21.475	0.0872	27.7695	5.81
MgCl ₂	309.52-424.68	0.333 - 5.00	59.180	−0.4799	125.4637	4.70
Na ₂ SO ₄	286.97 - 423	0.25 - 2.00	0	−0.2498	130.3604	4.54

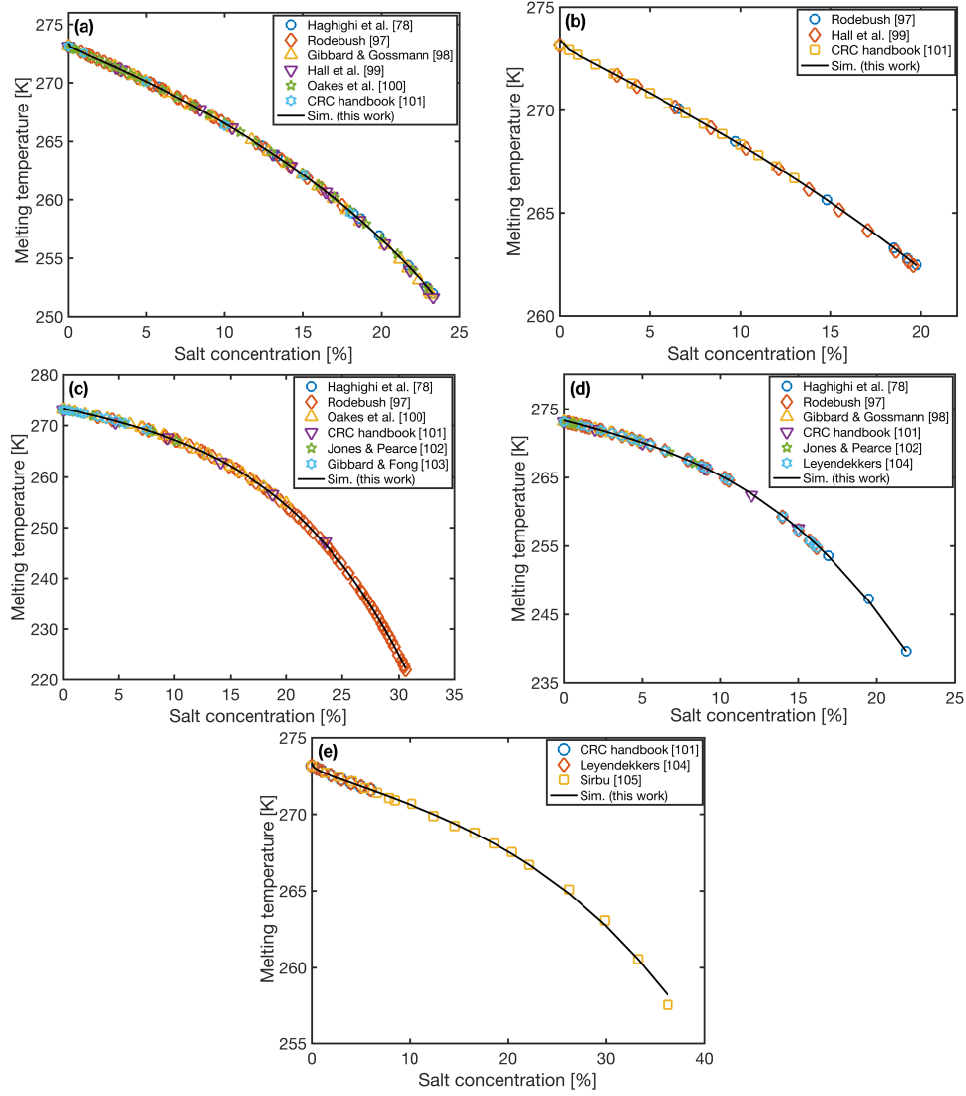


Figure 3: Fitting experimental freezing point depression data of single-salt solutions: (a) NaCl [78, 97–101]; (b) KCl [97, 99, 101]; (c) CaCl₂ [78, 97, 100–103]; (d) MgCl₂ [78, 97, 98, 101, 102, 104]; (e) Na₂SO₄ [101, 104, 105].

4. Results and discussion

4.1. Model validation

1 To validate the proposed model, we first compare the computed CO₂
2 solubility in single-salt solutions with experimental data. Figure 4 shows
3 the mole fraction of CO₂ dissolved in NaCl solution at $T = 323$ K. The circle,
4 diamond and square symbol represents measured CO₂ solubility data in the
5 NaCl solution with molality of 1, 3 and 5 mol/kg water, respectively. It
6 can be seen the computed results agree with the experimental data very
7 well, while the CO₂ solubility is slightly overestimated in the NaCl solution
8 of 1mol/kg water when pressure is greater than 20 MPa. Moreover, we
9 compare our results with Sun et al. [52]’s results, which are shown as dash
10 lines in the following figures. As can be seen, their electrolyte CPA model
11 estimates CO₂ solubility at low salt molality (1 mol/kg water) better than
12 ours, but it overestimates CO₂ solubility a little at high salt molality (5
13 mol/kg water). Both models exhibit the salting-out effect becomes more
14 significant as the salt concentration increases.

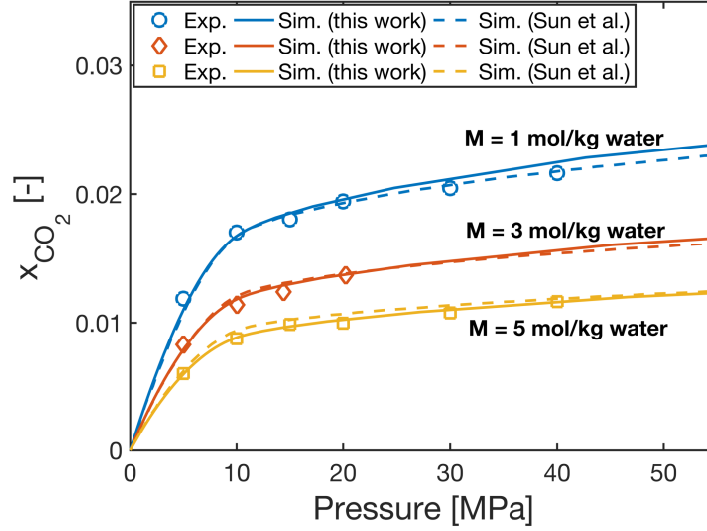


Figure 4: CO_2 solubility in the NaCl solution at $T = 323$ K with molality of 1 mol/kg (blue) , 3 mol/kg (red) and 5 mol/kg (yellow) water, respectively. The experimental data are obtained from [93] and [107].

Figure 5 displays the computed CO_2 solubility in the CaCl_2 solutions of 1.01 and 2.28 mol/kg water together with experimental data. At lower molality, Sun et al. [52] e-CPA EOS slightly outperforms the proposed model at $T = 349$ K. Both models can predict CO_2 solubility behavior in the 2.28 m CaCl_2 solution well, although the proposed model slightly underestimates while the e-CPA model overestimates the amount of CO_2 dissolved in CaCl_2 solution. By plotting the computed results together, as shown in Figure 6, we find CO_2 solubility at $T = 349$ K intersects with CO_2 solubility at $T = 374$ K, which was also observed by [52]. Interestingly, at a fixed salt concentration, CO_2 solubility at $T = 374$ K is not always lower than that at $T = 349$ K, which is contradictory to the general knowledge. The salting-

- 1 out effect at $T = 374$ K gets weakened as pressure exceeds around 35 MPa,
- 2 implying the high-temperature CaCl_2 solution could provide extra storage
- 3 capacity at high pressures.

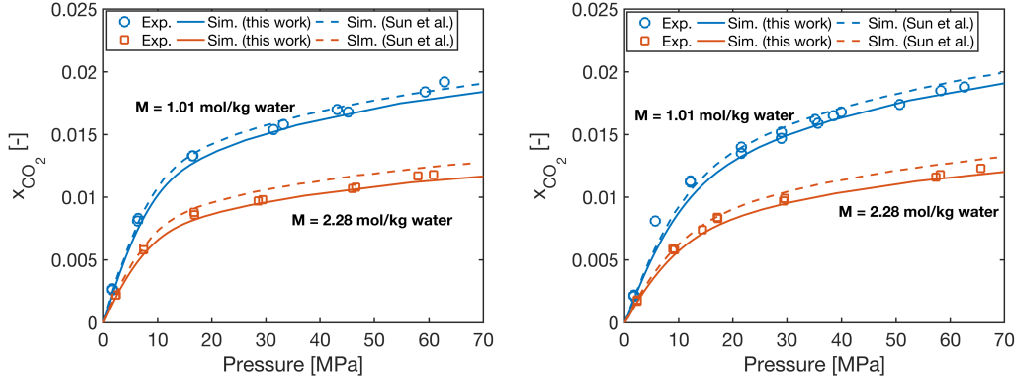


Figure 5: CO_2 solubility in the CaCl_2 solution at $T = 349$ K (left) and $T = 374$ K (right). All the experimental data are obtained from [113].

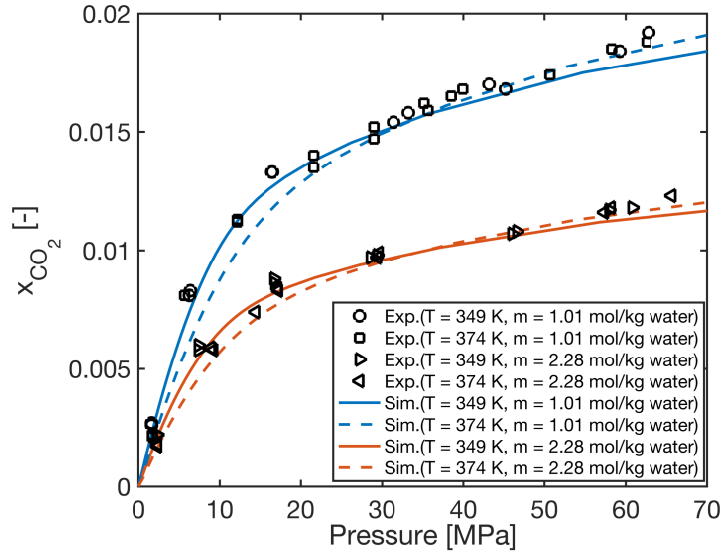


Figure 6: CO_2 solubility in the CaCl_2 solution. The experimental data [113] and computed results are represented by symbols and lines, respectively.

1 The last example for model validation compares the experimental data,
2 obtained from [106], with computed CO_2 solubility in Na_2SO_4 solutions
3 with molality of 1 and 2 mol/kg water at two different temperatures, as
4 shown in Figure 7. At $T = 313$ K, the proposed CPA model has the same
5 accuracy with the e-CPA EOS [52]. Clearly, CO_2 solubilities in two salinity
6 solutions are underestimated, even though the e-CPA EOS accounts for the
7 ion solvation by an additional Born term. On the other hand, the e-CPA
8 model yields higher prediction accuracy at $T = 333$ K. Several reasons
9 may account for the poor performance of the proposed model for Na_2SO_4
10 solutions. Above all, the measured CO_2 solubility data in Na_2SO_4 solutions
11 are much less than in NaCl and CaCl_2 solutions. A smaller number of
12 experimental data are used to tune the interaction parameter between CO_2
13 and Na_2SO_4 so that the prediction accuracy is somewhat unsatisfactory.
14 Moreover, the fitting data used for parameter optimization in this study is
15 partially inconsistent with the experimental data used by Sun et al. [52].
16 Some data in their work are unavailable for us and thereby we have to use
17 other data as a replacement. Also, experimental measurements may have
18 errors, which is another reason for the poor performance that cannot be
19 ignored. It is worth mentioning that the proposed model doesn't take into
20 account the effect of ion size on CO_2 solubility behavior, which may play an
21 important role in Sun et al. [52]'s model to accurately estimate the amount
22 of dissolved CO_2 in Na_2SO_4 solutions. In addition, we also compare the

1 estimated CO_2 solubility in 1, 2 and 3 m^1 Na_2SO_4 solutions at $T = 348$ K
2 with the experimental data [116] in Figure 8, which are recently found and
3 not used to tune the interaction parameter between CO_2 and Na_2SO_4 . The
4 computed results match up with the new experimental data very well. It
5 is worth mentioning that the CO_2 - Na_2SO_4 interaction parameter is tuned
6 up to $M = 2$ mol/kg water. The yellow dash line in Figure 8 is predicted
7 outside the molality range, see Table 4, and it shows great accuracy and
8 consistency with the experimental data.

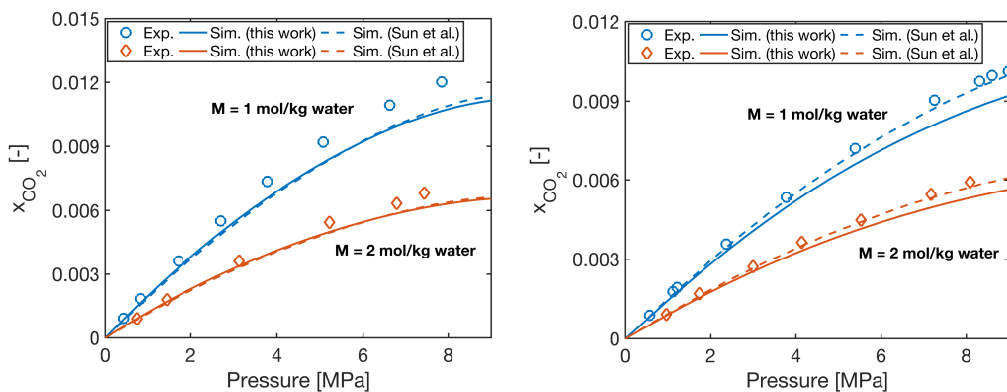


Figure 7: CO_2 solubility in the Na_2SO_4 solution at $T = 313$ K (left) and $T = 333$ K (right). Experimental data are obtained from [106].

¹A solution with molality of X mol/kg is often denoted as X m. Here m is the abbreviation of molality unit rather than length unit.

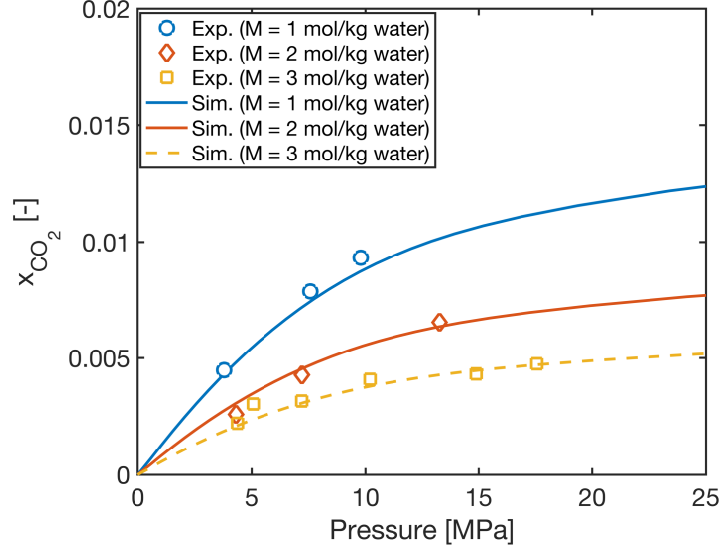


Figure 8: CO_2 solubility in the Na_2SO_4 solution at $T = 348$ K with molality of 1, 2 and 3 mol/kg water. The dash line is predicted beyond the molality range $M \in [0.25, 2.00]$ mol/kg where $h_{\text{CO}_2-\text{Na}_2\text{SO}_4}$ is tuned. All the experimental data are obtained from [116].

4.2. CO_2 solubility prediction in mixed-salt solutions

Figure 9 displays the mole fraction of CO_2 dissolved in the NaCl-KCl, NaCl- CaCl_2 and KCl+ CaCl_2 solution at $T = 318$ K with the total salt concentration of 10 wt.%. The weight ratio of NaCl : KCl, NaCl : CaCl_2 and KCl : CaCl_2 is 1 : 1. Similar to the results of [52], the proposed CPA model predicts CO_2 solubility in the NaCl- CaCl_2 solution much better than the NaCl-KCl and KCl- CaCl_2 solutions. Although the experimental data [117] present that the 10 wt.% NaCl-KCl and KCl- CaCl_2 solutions have close salting-out effect on CO_2 solubility above 10 MPa, both models

1 exhibit the salting-out effect of KCl-CaCl₂ solution is stronger than NaCl-
 2 KCl solution, since the combination of KCl and CaCl₂ at the 10 wt.% salt
 3 concentration yields larger ionic strength. Overall, the prediction accuracy
 4 is still acceptable.

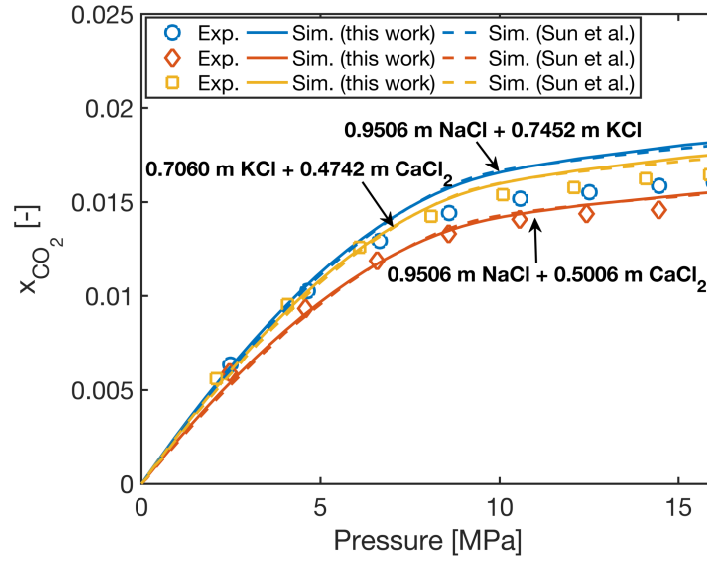


Figure 9: CO₂ solubility in the NaCl+KCl solution (blue), NaCl+CaCl₂ solution (red) and KCl+CaCl₂ solution (yellow) at $T = 318$ K with the total salt concentration of 10 wt.%. All the experimental data are obtained from [117].

5 The solubility behavior of CO₂ in the NaCl-KCl, NaCl-CaCl₂ and KCl+CaCl₂
 6 solutions, shown in Figure 9, can be qualitatively explained from the per-
 7 spective of kosmotrope and chaotrope. With the same anion, it mainly
 8 depends on the effect of cations on the structure of water. Overall, the
 9 presence of salt reduces CO₂ solubility in the aqueous solution since wa-

1 ter molecules aggregate around ions and consequently less H₂O associates
 2 with CO₂. However, a kosmotropic (structure-breaking) cation, e.g. Ca²⁺,
 3 contributes to the stability and structure of water-water interaction, and
 4 instead, a chaotropic (structure-making) cation, e.g. K⁺, disrupts the hy-
 5 drogen bonding interactions between water molecules. Considering the in-
 6 teraction strength between CO₂ and H₂O is much weaker than the hydrogen
 7 bonding interactions between H₂O, the introduction of chaotropic ions could
 8 increase the potential of CO₂ associating with H₂O through their weak hy-
 9 drogen bonding interactions. It is worth noting that Na⁺ can be categorized
 10 as a borderline ion due to its neutral effect on the structure of water [118].
 11 Thus, it is easy to find that CO₂ solubility in the NaCl-CaCl₂ solution
 12 should be smaller than in the NaCl-KCl at the same salt concentration.
 13 Even though the structure-making effect of Ca²⁺ could compensate for the
 14 structuring-breaking effect of K⁺, the interaction strength of K⁺-H₂O is
 15 stronger than that of Ca²⁺-H₂O. With the salt content of KCl higher than
 16 CaCl₂, CO₂ solubility in the KCl+CaCl₂ solution should be smaller than
 17 NaCl-KCl solution but greater than in the NaCl-CaCl₂, which agree with
 18 the prediction given by both models as shown in Figure 9.

19 Figure 10 displays CO₂ solubility in the NaCl-KCl-CaCl₂ solution at
 20 $T = 308$ K with the total salt concentration of 5 wt.%, 10 wt.% and 14.3
 21 wt.%, respectively. The weight ratio of NaCl, KCl and CaCl₂ is 1 : 1 : 1
 22 and detailed molarity compositions are shown in the figure. As the total
 23 salt concentration increases, the salting-out effect becomes more significant.

1 The proposed model gives the best estimation of CO₂ solubility at 5 wt.%
2 salt concentration and it slightly underestimates the amount of dissolved
3 CO₂ with the total salt concentration increasing. Moreover, we investigate
4 the effect of temperature on CO₂ solubility behavior in the 10 wt.% NaCl-
5 KCl-CaCl₂, shown in Figure 11. The 10 wt.% NaCl-KCl-CaCl₂ solution
6 contains 0.6338 m NaCl, 0.4968 m KCl and 0.3337 m CaCl₂ under the
7 identical weight ratio. The increasing temperature aggravates molecular
8 motion, thus making it more difficult to trap CO₂ in water. As a result,
9 the mole fraction of dissolved CO₂ continues to decrease. Even though
10 the computed results increasingly deviate from the experimental data with
11 an increase of temperature, the proposed model successfully capture the
12 decreasing CO₂ solubility behavior with good accuracy.

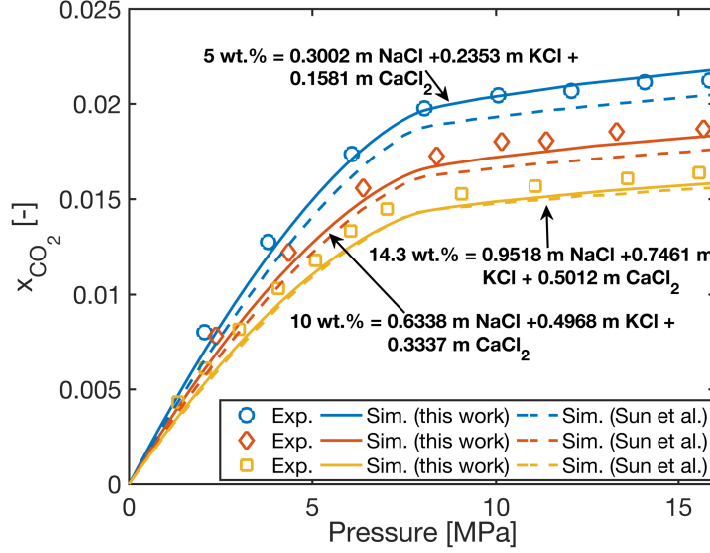


Figure 10: CO₂ solubility in NaCl + KCl + CaCl₂ solution with salt concentration of 5 wt.% (blue), 10 wt.% (red) and 14.3 wt.% (yellow) at $T = 308$ K. All the experimental data are obtained from [117].

1 In Figure 12, we compute CO₂ solubility in a quaternary-salt solution,
2 consisting of 1.4006 m NaCl, 0.0474 m KCl, 0.3405 m CaCl₂ and 0.0615 m
3 MgCl₂ at $T = 297$ K, and compare our results with the experimental
4 data [119], which is an approximation of the high-salinity brine in the Ap-
5 palachian Basin . The molality of each salt is close to the value used by Sun
6 et al. [52]. Both models capture CO₂ solubility behavior in such a complex
7 mixed-salt solution. Up to 6 MPa, the mole fraction of dissolved CO₂ in-
8 creases in the NaCl + KCl + CaCl₂ + MgCl₂ solution and then it reaches
9 a "plateau", indicating the sequestration potential is hardly increased any
10 more in this saline water sample after 6 MPa.

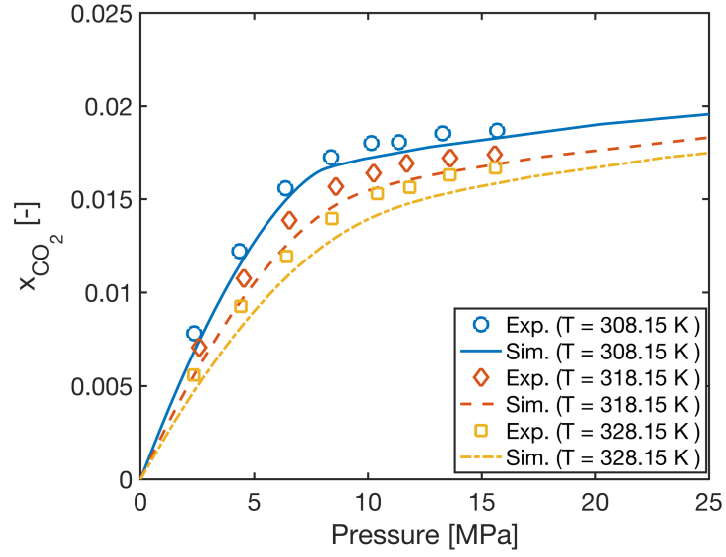


Figure 11: CO₂ solubility in NaCl + KCl + CaCl₂ solution of 10 wt.% salt concentration at $T = 308.15$, 318.15 and 328.15 K. All the experimental data are obtained from [117].

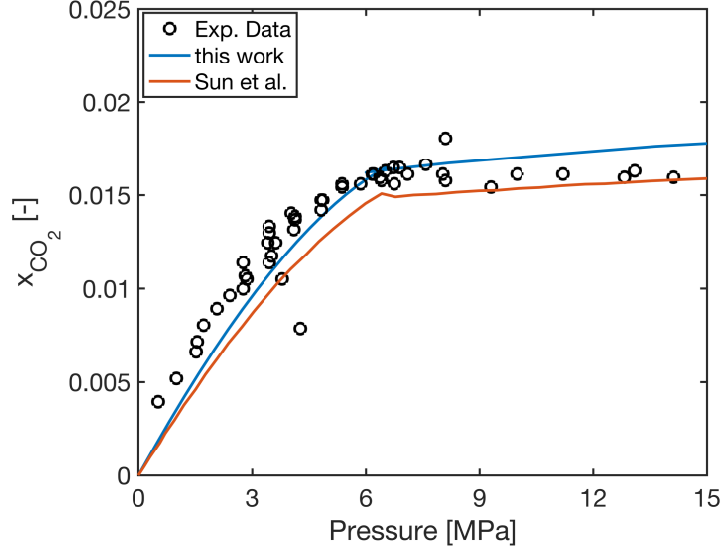


Figure 12: CO₂ solubility in mixed-salt solution consisting of 1.4006 m NaCl, 0.0474 m KCl, 0.3405 m CaCl₂ and 0.0615 m MgCl₂ at $T = 297$ K. The experimental data are obtained from [119].

1 At the end, the salting-out effects of all the five salts are compared.
 2 Figure 13 shows the CO₂ solubility in each single-salt solution with mo-
 3 lality of 1 mol/kg water. The blue, red, yellow, purple and green color
 4 represents NaCl, KCl, CaCl₂, MgCl₂ and Na₂SO₄ solution respectively, and
 5 corresponding experimental data are represented by the circle [93, 107], di-
 6 amond [112], square [112, 117, 120], triangle [112] and pentagram [112, 115]
 7 symbol. It can be seen the salting-out effect follows the order KCl < NaCl <
 8 CaCl₂ \approx MgCl₂ < Na₂SO₄, similar to the observation of [52]. Due to the
 9 distinct salting-out effect of different salts, real saline environments cannot
 10 be fully represented by a single salt. However, a lot of literature used single

1 NaCl solution as a surrogate of saline water, to estimate CO₂ sequestration
2 potential. As NaCl solution exhibits much larger solvent capacity at high
3 pressures, this can result into overestimation of carbon sequestration poten-
4 tial and cause considerable economic loss due to the incorrect evaluation.

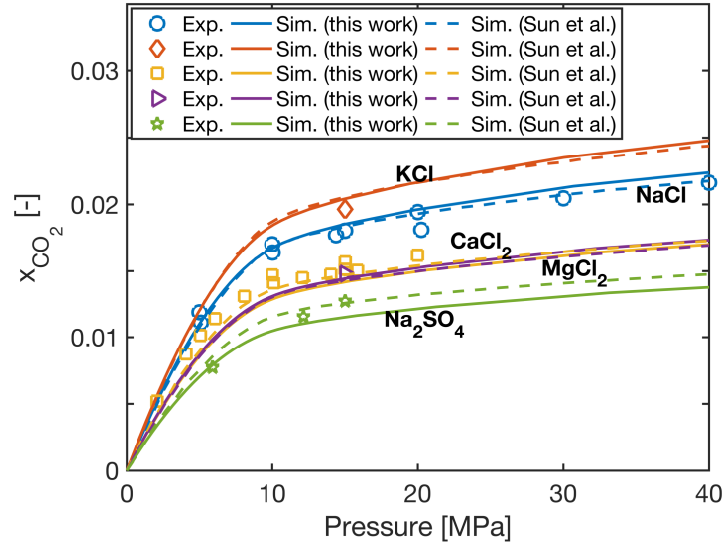


Figure 13: Comparison of CO₂ solubility in single NaCl (blue), KCl (red), CaCl₂ (yellow), MgCl₂ (purple) and Na₂SO₄ (green) solutions at $T = 323.15$ K. Each single-salt solution has molality of 1 mol/kg water.

5 In Figure 13, the single CaCl₂ solution and the MgCl₂ solution exhibit
6 very close salting-out effect. However, if strictly abiding by the influence
7 of ion charge and ion size on the salting-out effect, our results yield a little
8 discrepancy that the salting-out effect of CaCl₂ is slightly stronger than
9 that of MgCl₂ while the opposite is true. This may be one advantage of the
10 electrolyte CPA EOS with ion-specific parameters. Despite this, the effect
11 of ion charge and size is not the main focus of this work and the proposed

1 model gives reasonable predictions with satisfactory accuracy. If we analyze
2 the results from the perspective of ions, or rather cations which are believed
3 to play a dominant role in adjusting the capacity of solvent to trap dissolved
4 gas molecules [121], it may explain why the salting-out effect follows such
5 an order. Under the same molality, Na_2SO_4 presents the strongest salting-
6 out effect because it has the largest cation concentration. Compared to the
7 NaCl and KCl solution, CO_2 is less soluble in the CaCl_2 and MgCl_2 solution,
8 implying the cation charge has a more significant impact than the cation
9 size when comparing the salting-out effect of a divalent-cation salt with a
10 monovalent-cation salt. Due to the larger ion size, the salting-out effect of
11 KCl is weaker than NaCl at the same ion charge.

12 It can be seen the combination of NVT flash and PR-CPA EOS success-
13 fully estimate CO_2 solubility in single- and mixed-salt solutions over wide
14 range of pressures, temperatures and salt concentrations with satisfactory
15 accuracy. In comparison to Sun et al. [52]’s e-CPA EOS with ion-specific
16 parameters, the PR-CPA EOS in this study may be considered as a salt-
17 based model since interactions between nonelectrolyte component and salt
18 are considered rather than ion and corresponding interaction parameters are
19 tuned by fitting experimental data. Similarly, the interaction parameters of
20 single H_2O -salt and single CO_2 -salt are employed to estimate CO_2 solubility
21 in mixed-salt solutions and no additional parameters are needed. Such a
22 treatment significantly simplifies the complexity of phase behavior modeling
23 of CO_2 -brine systems and meanwhile preserves satisfactory accuracy.

5. Conclusions

1 In this study, the combination of NVT flash and PR-CPA EOS is suc-
2 cessfully applied to model CO₂ solubility behavior in single- and mixed-
3 salt solutions. The salting-out effect is reproduced by introducing the
4 Debye-Hückel electrostatic contribution to chemical potential of nonelec-
5 trolyte components in the aqueous phase. Five common salts, including
6 NaCl, KCl, CaCl₂, MgCl₂ and Na₂SO₄ are considered to represent real
7 saline environments. To enhance the prediction accuracy, a large number
8 of reliable experimental data are used to tune binary interaction coefficient,
9 cross-association factor and interaction parameter between nonelectrolyte
10 components and salts. It is shown that the combination of NVT flash and
11 salt-based CPA model gives accurate estimation of CO₂ solubility in single-
12 and mixed-salt solutions over wide ranges of pressure, temperature and salt
13 concentration. More importantly, the proposed model exhibits neck-to-neck
14 prediction accuracy with the more sophisticated e-CPA model, making it
15 confident to accurately estimate carbon sequestration potential in saline
16 aquifers through solubility trapping.

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