

A context-aware concept evaluation approach based on user experiences for smart product-service systems design iteration

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Abstract

With the trend of ‘digitalization’ and ‘servitization’ in the manufacturing industry, numerous product-service systems fail to seize a market share and encounter an imbalance between digital investments and expected revenues. This phenomenon is probably caused by the insufficient evaluation on user experience and by the lag between user requirement changes and the offered solutions. Both limitations can be mitigated via automatic Smart PSS evaluation based on broader concerns on user experience information that collected from either product-service bundles or user behavior. In this paper, a context-aware concept evaluation approach is proposed for Smart PSS design iteration, aiming to satisfy users in a more timely and automatic manner. Derived from the conventional information axiom method, the proposed approach introduces a context-aware evaluation indicator identification module and an automatic system range identification procedure based on natural language processing techniques, and eventually return the most robust concepts during the usage phase. With less human intervention in the design process, it relieves the lag between user requirement changes and the solutions, and reduces the prescriptive instructions in the conventional information axiom method. A case study of a 3D printer company’s design iteration is conducted, which proves the proposed approach’s feasibility. It is hoped that this work provides practical guidance for achieving a more context-aware Smart PSS development.

Keywords: *smart product-service systems; concept evaluation; user experience; information axiom; context-awareness*

Notations and Abbreviations

| | |
|-------------------------|--|
| AI | Artificial Intelligence |
| ANP | Analytic Network Process |
| c | Context feature |
| C_i | Closeness to the best solution (from TOPSIS) |
| CBOW | Continuous-Bag of Words |
| CNC | Computerized Numerical Control |
| CPS | Cyber-physical systems |
| d_i^+ | Distance between the PSB candidate i and the best PSB candidate b (from TOPSIS) |
| d_i^- | Distance between the PSB candidate i and the worst PSB solution w (from TOPSIS) |
| dr_{ij} | PSB_i 's design range on evaluation indicator j |
| $evSet$ | Event set that identify the patterns of usage scenario s |
| I_i^j | Information content of PSB_i on evaluation indicator j |
| I_i | Total information content of PSB_i |
| ICT | Information and Communication Technologies |
| IoT | Internet of Things |
| KPI | Key Performance Indicator |
| p_{ij} | Ratio of common range and system range of PSB_i on aspect j |
| $pr_{i,j}(\hat{y} = 1)$ | Probability of a PSB_i 's performance belongs to a usage scenario aspect j |
| pr_{ijt} | Probability of the positive label of PSB_i on aspect j from the PSB_i 's t -th comment |
| pr_{ij} | Probability of total positive user perception pr_{ij} of PSB_i on aspect j |
| PSB | Product-service Bundle |
| PSS | Product-service systems |
| QFD | Qualify Function Deployment |
| R | Semantic relations between context features |
| RBF | Radial Basis Function |
| s | Usage scenario |
| sr_{ij} | PSB_i 's system range on evaluation indicator j |
| SVM | Support vector machine |
| TF-IDF | Term Frequency-Inverse Document Frequency |
| TOPSIS | Technique for Order of Preference by Similarity to Ideal Solution |

1 **1 Introduction**

2 With the dramatic transformation of manufacturing servitization, product-service systems
3 (PSS) have been globally accepted by manufacturing companies in recent years [1]. As an
4 inherently dynamic and multi-dimensional system including multiple stakeholders and product-
5 service bundles, PSS delivers user-required functionalities in a way that reduces the impact on
6 the environment [2-4]. Since 2014, a novel business paradigm called Smart PSS [5] appears along
7 with many cutting-edge information and communication technologies (ICT), such as Internet-of-
8 Things (IoT), Cyber-Physical Systems (CPS), and Artificial Intelligence (AI) [6]. Those new
9 techniques enable even more massive accessible data from multiple parties, much more flexible
10 interactive modes, and proper decision supports throughout the product lifecycle [7-10]. From
11 this perspective, the appearance of Smart PSS denotes a further transformation from servitization
12 into digitalization, making the manufacturing business an ever-evolving and much more flexible
13 manner that can be examined and then upgraded even after launching to the market [11, 12].

14 However, according to an investigation [13], only a small proportion of companies
15 succeeded in their digitalization transformation to obtain the expected economic returns [14]. The
16 imbalance between the digital servitization investments and the expected economic returns, the
17 so-called ‘*digitalization paradox*’, has been discovered in many firms [14, 15]. For example,
18 Michelin has launched a comprehensive tire management solution called Michelin Fleet Solution
19 for the large European transportation companies in 2000, but received far below-expected
20 contracts and profits [16]. Another example is that General Electric has reached \$ 3.9 billion in
21 digital revenue in 2018, but it is still nowhere approaching its goal of \$15 billion in digital revenue
22 in 2020 [15].

23 Demonstrating the inherent unsustainability in the economic aspect and some non-linear
24 effects on company performance [17], the traps of digitalization paradox in Smart PSS
25 development are commonly regarded to be caused by (1) the excessive attention on technical
26 possibilities rather than customer experiences [15]; (2) the frequent change of user experience due
27 to the insufficient satisfaction on user requirements and the influence of fashion trend/public
28 media [18]; and (3) the lag between the changes of user experience and the solutions [19].

29 Facing the above challenges, several strategies are taken to comprehensively and wisely
30 evaluate Smart PSS and pursue a win-win situation for both companies and customers [20].
31 Firstly, the product-service bundles (PSBs) evaluation should be conducted comprehensively
32 based on user experience indicators, rather than only on technical attributes. Secondly, service
33 providers are expected to offer a quick approach to explore user-concerned indicators to the PSBs.
34 Since the user experience changes can be reflected in both their behavior physically [21] and their
35 attitude cognitively [22], a context-aware concept evaluation approach for Smart PSS design

36 iteration is expected. Thirdly, service providers should select the most robust PSB concepts to
37 relieve the lag effect between the customer experience changes and the solutions [23]. To achieve
38 it, the information axiom in axiomatic design is one of the effective methods for robust concept
39 evaluation [13].

40 Although the above strategies have been separately discussed in numerous product
41 development studies [13, 24-26], in the big and content-rich world that is encoded by massive
42 user-generated data and sensed-data in Smart PSS design iteration [8, 27], the PSB concept
43 evaluation approach still needs to be further enhanced in automation perspective and rapid
44 reaction capability. Therefore, the primary focus of this paper is on (1) how to identify evaluation
45 indicators automatically and (2) how to rapidly evaluate the current design concepts considering
46 user experience.

47 The remaining sections are organized as follows. Related studies on concept evaluation and
48 context awareness are reviewed in Section 2. Section 3 expounds on the proposed context-aware
49 Smart PSS evaluation method in detail. Subsequently, in Section 4, an example of a 3D printing
50 company's concept evaluation is demonstrated for the feasibility of the proposed method. Finally,
51 we discuss the primary results and then summarize the main academic contributions in Section 5
52 and Section 6, respectively.

53 **2 Literature review**

54 To have a whole picture on the concept evaluation in Smart PSS, evolutions towards Smart
55 PSS, current studies on concept evaluation of Smart PSS, and the context-awareness in Smart
56 PSS are summarized and discussed.

57 **2.1 Evolutions towards Smart PSS**

58 PSS, a system that develops and offers integrated product and service bundles, was coined
59 by Goedkoop [28] in 1999. Thereafter, PSS has been examined by both academia and industries
60 in the recent two decades [2, 29-32]. According to the innovations on system architecture of PSS
61 paradigms, the evolutions of PSS can be grouped into three phases, namely conventional PSS,
62 Industrial PSS, and Smart PSS. Table 1 lists their systematic innovations.

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69 Table 1.
70 Systematic features of PSS paradigms

| PSS paradigm | Systematic innovations |
|-----------------------------------|--|
| Conventional PSS [2, 28] | <ul style="list-style-type: none"> • Servitization of products/productization of services, • Separately developed add-on values • Manufacturer-dominant |
| Industrial PSS [1, 33] | <ul style="list-style-type: none"> • Seamless integration between products and service • For industrial applications |
| Smart PSS [34] (Similar terms: | <ul style="list-style-type: none"> • Integration of physical space and cyber space (i.e., a digital-based ecosystem) |
| Digitalized PSS [35] and | <ul style="list-style-type: none"> • Mutual interactions among stakeholders |
| Cyber-physical PSS [36]) | <ul style="list-style-type: none"> • Value co-creation (i.e., ever-evolving PSB design iterations) |

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72 In conventional PSS, the attached products/services perform as add-on values, but they are
73 still separately developed. Besides, conventional PSS is still a manufacturer-dominant system.
74 Although customers have been involved in the value generation process during usage, customers
75 still do not participate in the PSS value proposition stage.

76 Industrial PSS [1] (also called Technical PSS [33]) arose with seamless integration of
77 Industrial PSS results, associated resources, and stakeholders during each PSS lifecycle stage. For
78 example, Meier, Roy and Seliger [1] underlined the potentials of integrating tangible products
79 and intangible services in industrial production applications. Associated resources, including
80 flexible production scheduling [37], installation planning [32], and IPSS purchasing actions [38,
81 39] were highlighted by numerous scholars with a more comprehensive insight for IPSS
82 development. Besides, the integration of customers was also studied to promote mutual
83 interaction among stakeholders [40]. All the studies imply that the data/information from
84 downstream scenarios has great values and can facilitate the design of Industrial PSS.

85 Along with digital servitization, Smart PSS emerged by integrating physical space and
86 cyberspace, making it a digital-based ecosystem [34, 41, 42]. It is widely accepted that Smart PSS
87 is a multipartite system fundamentally consisting of multiple stakeholders, intelligent systems,
88 smart connected products and their generated digital services [11]. At the same time, Smart PSS
89 is also a value-co-creation business paradigm for industry digitalization, where both the customers
90 and the service providers exchange information with each other and further generate values
91 together.

92 Unlike conventional PSS and industrial PSS, the smartness of Smart PSS is reflected in the
93 *online smartness* and the *offline smartness* [27, 43]. Online smartness refers to the capability of
94 making proper and personalized decisions by intelligent algorithms and analytic tools based on
95 multi-source and heterogeneous data. Meanwhile, achieved by smart connected products, offline
96 smartness refers to the capability of perceiving a specific usage scenario with context-awareness.
97 It can adjust the product itself by leveraging the embedded hardware and the self-learning
98 software [8, 44, 45].

99 These two types of smartness drive the Smart PSS development up to a much more flexible
100 and ever-evolving manner [34]. Specifically, the design activities in Smart PSS, including
101 requirement identification, solution selection, and reconfiguration, can be agilely conducted with
102 automatic decision supports based on user-generated content. In contrast, conventional PSS
103 design activities are knowledge-intensive and manufacturer-dominant, which is time-consuming
104 and costly [46].

105 Although the academic community has recognized the unique features of Smart PSS and has
106 attempted to develop design frameworks for Smart PSS, there is still a far long way to a mature
107 and comprehensive Smart PSS development methodology. One typical gap is the excessive
108 emphasis on technical possibilities but insufficient attention on user experience [10], which
109 somehow appears in the non-comprehensive concept evaluation in Smart PSS.

110 **2.2 Concept evaluation in Smart PSS**

111 Concept evaluation, one of the critical tasks in the Smart PSS development process,
112 dominates the success of concepts. Only the concepts comprehensively and periodically evaluated
113 by the users can retain their competitiveness in the fierce market. According to Mourtzis et al.'s
114 study [47], the Smart PSS concept evaluation can be measured via Key Performance Indicators
115 (KPIs) from the perspective of customer perceptions, sustainability, and risks.

116 Considering that this research emphasizes the concept evaluation based on user experience,
117 only the customer perception-related methods are discussed. The related studies mainly focus on
118 concept evaluation in the early design stage before the market launch and under the PSS paradigm.
119 Kimita, Shimomura, and Arai [48] proposed a non-linear satisfaction-attribute function to
120 estimate customer satisfaction based on the PSS features, wherein the PSS features consist of the
121 customer state changes and function parameters such as cost, physical interference and provider
122 feasibility. Lee et al. [49] concentrated on assessing the probability of new PSS concepts being
123 accepted by users using the analytic network process (ANP) and niche theory.

124 Although many researchers, such as Lan, Zhang, Zhong and Huang [50], Turkyilmaz,
125 Oztekin, Zaim and Demirel [51] and Wang, Hazen Benjamin and Mollenkopf Diane [52],
126 suggested that this method effectively evaluates customer satisfaction, the limitations can still be

127 found in three folds. Initially, it is engineers/experts rather than customers themselves to decide
128 the evaluation indicators, which cannot straightforwardly reflect the users' perception. Secondly,
129 even if some approaches encourage users to identify the evaluation indicators, the methods to
130 extract the indicators are manually determined instead of automatically extracted. Thirdly, the
131 concept evaluation process is conducted before the market launch once for all without any other
132 reappraisals, which cannot fulfil the requirement of agile reaction in Smart PSS's development
133 manner.

134 **2.3 Context-awareness in Smart PSS**

135 In an effort to automatically detect customer perceptions, a context-aware approach is
136 expected in this article. According to Dey's definition, a system is context-aware if it uses context
137 to provide relevant information and/or services to the user, where relevancy depends on the user's
138 task [53]. Here, the context follows its broad definition that "*any information that can be used to*
139 *characterize the situation of an entity*" [54], specifically containing the current usage scenarios
140 characterized by sensors and the users' attitude characterized by their satisfaction/sentiments.

141 To establish context-aware applications, it is critical to ensure the potential context features
142 can be collected and interpreted in a context-aware system. Several context-aware computing
143 techniques are adopted to monitor the end-user's usage contexts [55], which can be divided into
144 three phases, namely *context acquisition*, *context processing*, and *context usage* [56].

145 As the first phase, *context acquisition* intends to identify and then collect the context
146 information via sensors or user interfaces. Context information collected via sensors is mainly the
147 elementary and physical contexts, such as location information from GPS, time information from
148 the computers' built-in clock, and luminance information from the photosensitive diode. The ones
149 identified from user interfaces will be more advanced, which usually indicates users' current
150 activities or their feedbacks. They can be obtained from computer logs, user schedules, and other
151 artificial intelligence techniques. Then in the *context processing* phase, context processing will
152 systematically transform the context information into useful information for further analysis
153 [57]. Finally, during the *context usage* phase, the context-aware system will apply the context
154 information to adjust itself or give relevant responses. The applications of context information
155 vary based on the task purpose. In this study, the usage of contextual information aims to set up
156 the evaluation indicators and collaborate with information axiom to assess the PSBs' performance.

157 The significance of contexts has been recognized in a Smart PSS survey that context plays a
158 significant role during Smart PSS development [5]. Specifically, end-users expect personalized
159 functionalities rather than generalized ones. Hence, the service providers are expected to give
160 rapid reactions once the end-user's contexts change, in which the context-aware feature should
161 be considered during the usage stage. However, the implementation of using context-aware

162 systems in Smart PSS concept evaluation has yet to be fully explored. To bridge the gap, two
163 prerequisites of the context-aware system in Smart PSS should be implemented. One is the
164 application of multi-sourced and heterogeneous data. The data that is multi-sourced from users
165 and service providers and is heterogeneous with different data formats from user behavior and
166 user perceptions offer a comprehensive analysis towards the Smart PSS's performance. A unified
167 representation format should fuse those data for the ease of machine readability and processing.
168 The other prerequisite is the application of intelligent algorithms that have automatic learning
169 capability from the datasets unless the rapid evaluation and reaction will be hardly realized. In
170 this study, they are the rationales to uniform the heterogeneous user-behavioral data and user
171 perception data and further to collaborate with information axiom and SVM method.

172 **3 Methodology**

173 The information axiom in axiomatic design is a classic and effective method for concept
174 evaluation in PSS, which demonstrates strong effectiveness and extendibility in multiple
175 scenarios [58-60]. Inspired by it, a context-aware concept evaluation framework is proposed for
176 Smart PSS design iteration. This framework takes user experience information into account and
177 integrates natural language processing techniques to fulfil the requirement of comprehensively
178 and automatically evaluating designs in Smart PSS.

179 As shown in Figure 1, the proposed framework comprises three phases, namely, Phase I:
180 Identify evaluation indicators for Smart PSS concept evaluation (Context acquisition), Phase II:
181 Identify design ranges and system range based on context information (Context processing), and
182 Phase III: Compute information content (Context usage). The uppermost contribution lies in the
183 hybrid evaluation manner that considers both behavior and perceptual perspectives under an
184 environment that user experiences count the final success but hard to perceive rapidly.

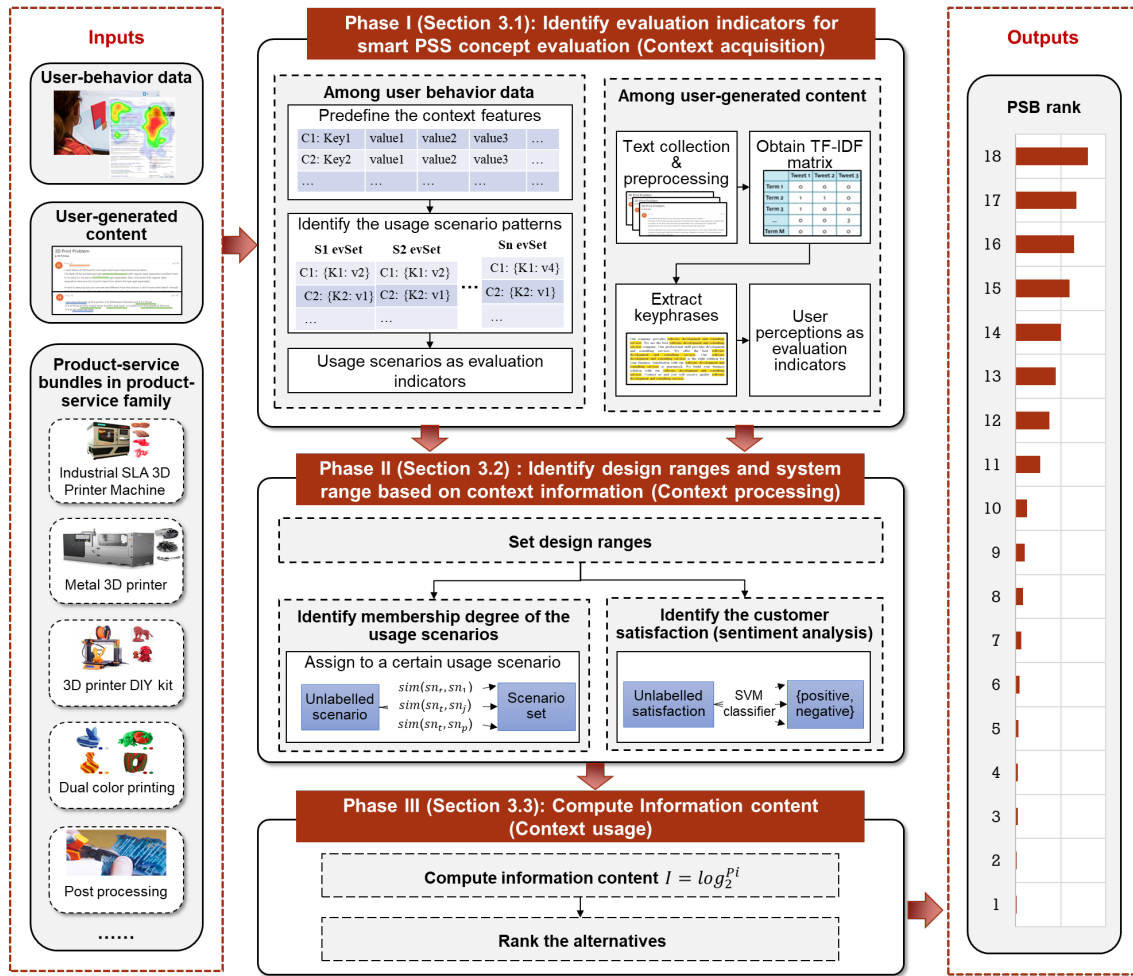


Figure 1. An overview of the proposed context-aware Smart PSS evaluation method

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Three inputs are deployed in the proposed Smart PSS concept evaluation framework: PSBs in the product-service family, user behavior data, and user-generated comments. PSBs refer to the customized solutions characterized by different technical parameters, functions, or usage scenarios for user segments/groups in Smart PSS. For instance, industrial SLA 3D printers suit for the manufacturing in the small or medium enterprises; metal 3D printer is valuable for mechanical equipment production; 3D printer DIY kits apply to the novices who want to experience 3D printing with relatively low price; and finally, the dual-colour printers might be required by the creative designers for rapid prototyping. Besides PSBs, user-behavior data denotes the digits/values collected via sensors or IT platforms during the usage process, such as printing speed and layer height set by users. Those values are usually numerical and crisp. Additionally, with the explosive increase of social media, individuals and organizations have widely accepted to express their ideas/perceptions online [61], which is so-called user-generated content. Although the user-generated contents have a broad scope containing text, figure, videos, and other media formats, it refers explicitly to textual customer comments in this study. They are often linguistic and rough.

203 Phase I aims to identify the user-concerned evaluation indicators based on user-behavior data
204 and user-generated data. On the one hand, the predefined context features, such as selected
205 printing material, and printing speed, will form usage scenarios, reflecting to what extent a user's
206 behavior patterns conform to the typical usage scenarios. Those contextual features establish the
207 behavior-level evaluation model, as addressed in subsection 3.1.1. On the other hand, the user-
208 mentioned features in customer comments, such as quality, delivery, and customer service, will
209 build up the perceptual-level evaluation model, as illustrated in subsection 3.1.2. The extracted
210 indicators will be further applied for the following phases, thus serving as the framework's
211 foundation.

212 In Phase II, both the design ranges and each PSB alternative's system ranges will be
213 determined for each indicator in Smart PSS. The design ranges mean the user-expected value
214 ranges for the functions/features, which are set by users by default. Nowadays, many methods
215 can be used for design range identification, such as Qualify Function Deployment (QFD), Likert
216 scales, or identifying from explicit descriptions in the initial configuration orders. Considering
217 the different data formats of user-behavior data and user-generated content, two methods for
218 system range identification will also be addressed in this phase, as explained in subsection 3.2.
219 To solve the mentioned problem of time-consuming on perceiving user satisfaction, we extended
220 the information axiom in axiomatic design by automatically identifying the system ranges on user
221 satisfaction.

222 Finally, each PSB alternative's information content can be calculated and ranked, which is
223 reported in subsection 3.3. The PSB alternatives are ranked in terms of the sum of all criteria'
224 information content. The higher the information content, the more robust the alternatives will be.

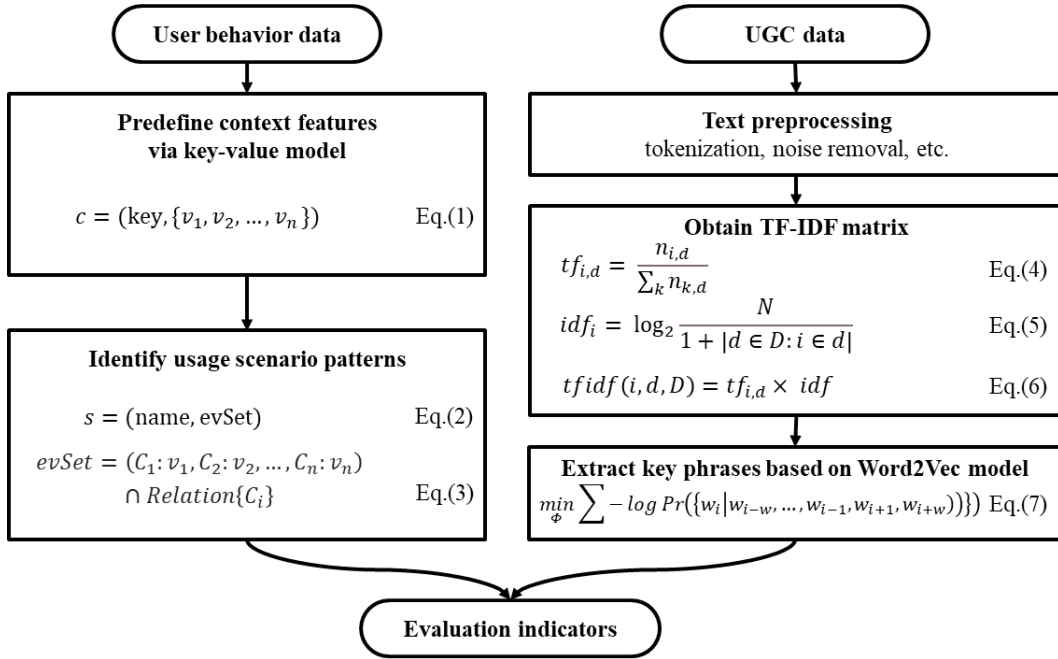
225 **3.1 Phase I: Identify evaluation indicators for Smart PSS concept evaluation (Context** 226 **acquisition)**

227 To make the evaluation process context-aware, we need to clarify the contexts' scope in the
228 initial. Considering the functional basis of designs and the interactions among product, services,
229 and users in Smart PSS, the contexts for PSB design evaluation can be categorized into four
230 groups [62]: (1) physical context (i.e., information about the surrounding environment, such as
231 time and room temperature); (2) social context (i.e., information about the nearby products or
232 services, e.g., a coffee grinder is a nearby product for a coffee machine; additional filament and
233 sandpaper are the nearby products for a 3D printer); (3) user context (i.e., the information about
234 users and user-PSS interactions, such as user demographics, user habit, user preference, user
235 knowledge and so on); and (4) operation context (i.e., information related to the operational status
236 of the Smart PSS, such as power/energy, lifespan and software version). In this study, only PSB-
237 related data (e.g., room temperature or historical purchase log) instead of personal data (e.g., home
238 address or user facial data) is defined to be collected. Contrary to the personal data applied to

239 identify a person [63], the PSB-related data focuses on the interactions with the PSBs.
 240 Furthermore, those contextual data can be collected only after the users agree with the data
 241 collection regulation offered by the service providers.

242 As discussed, the user experience will be reflected in their behavior and perceptions. To
 243 evaluate the current PSS designs, user-concerned evaluation indicators should be identified from
 244 two perspectives: user-behavior data and user-generated data. Figure 2 shows the evaluation
 245 identification process.

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Figure 2. Flowchart of evaluation indicator identification

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250 3.1.1 From user behavior data

251 (1) Predefine the context features

252 Key-value modelling [64] is selected in this study due to its simple representation format and
 253 fast processing capability. More importantly, to integrate with the information axiom, the PSB
 254 evaluation indicators (i.e., the context features related to user experience) should be represented
 255 as key attributes with corresponding values. Key-value modelling is applied owing to its strength
 256 on solid compatibility with the information axiom as well. Based on key-value modelling, a
 257 context feature can be defined as a set that has a key and set of possible values, denoted as follows:

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$$c = (\text{key}, \{v\}) \quad (1)$$

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For example, a 3D printer will have the context feature of *printing speed* and its values set.

260 However, key-value modelling alone cannot represent the relationships between the context
 261 features, so the semantic relations R [65] between context features should also be defined. They
 262 are represented as triples $\langle E_s, P, E_o \rangle$, where E_s is the entity for subjects and E_o is the entity for
 263 objects.

264 (2) Identify the usage scenario patterns

265 After defining the context models, the scenarios of interest in a Smart PSS can be identified.
 266 A scenario refers to the current situation of the product-service bundle and its involved
 267 environment, which can be represented as a tuple with its name and a set of events [66]. The
 268 mathematical expression of a scenario is given as follows:

$$269 \quad s = (\textit{scenario name}, \textit{evSet}) \quad (2)$$

270 , where \textit{evSet} refers to the set of predefined contexts with their values, and

$$271 \quad \textit{evSet} = (C_1: v_1, C_2: v_2, \dots, C_n: v_n) \cap \textit{Relation}\{C_i\}. \quad (3)$$

272 In this way, a set of usage scenarios are determined by the engineers or experts, and are set
 273 as the evaluation indicators from the behavioral aspect.

274 3.1.2 From user-generated content

275 Another input data for design evaluation is the user-generated content; it is used to extract
 276 the perceptual evaluation indicators.

277 (1) Text pre-processing

278 After collecting the raw textual user reviews, two pre-processing steps, tokenization and
 279 noise removal (e.g. HTML tags, extra whitespaces), are conducted to clean the raw texts.
 280 Considering that sentiment analysis will be conducted in the following steps, stopwords are not
 281 removed since they could contain users' sentiments.

282 (2) Obtain TF-IDF matrix

283 Words in the cleaned sentences will then be transformed into a critical matrix, i.e., Term
 284 Frequency-Inverse Document Frequency (TF-IDF) matrix. Term frequency (TF) is the number
 285 of a term occurs in a document, denoted as

$$286 \quad \textit{tf}_{i,d} = \frac{n_{i,d}}{\sum_k n_{k,d}} \quad (4)$$

287 , where $n_{i,j}$ refers to the frequency of term i occurring in document d . Inverse document
 288 frequency (IDF) is defined as the number of documents containing a specific word, reflecting the
 289 importance of a word in a series of documents. IDF is denoted as

$$290 \quad \textit{idf}_i = \log_2 \frac{N}{1 + |\{d \in D: i \in d\}|} \quad (5)$$

291 , where $N = |D|$ represents the number of documents, $|d \in D: t \in d|$ is the number of documents
 292 where the term i appears. Then $tf-idf$ is calculated as the multiply of term frequency and inverse
 293 document frequency, written as

$$294 \quad \quad \quad tfidf(i, d, D) = tf_{i,d} \times idf \quad (6)$$

295 (3) Extract key phrases

296 To extract the keywords or key phrases as the evaluation indicators, a keyword extraction
 297 approach, i.e., TextRank [67], can be applied based on the trained Word2Vec model [68].

298 Word2Vec model is used to generate word embeddings as the feature presentation. It
 299 considers the co-occurrence information of the same contexts in sentences, hence keeping the
 300 semantic meanings of words. The Word2Vec generally has two algorithms: Skip-Grams and
 301 Continuous-Bag of Words (CBOW). In this article, CBOW is selected because of its better
 302 performance on the relatively small data. Its rationale is to learn a function which can predict the
 303 word based on the given context words (i.e., the former words and latter words in a window),
 304 whose objective function is:

$$305 \quad \quad \quad \min_{\phi} \sum -\log Pr(\{w_i | w_{i-w}, \dots, w_{i-1}, w_{i+1}, w_{i+w}\}) \quad (7)$$

306 , where w_i is the predicted word and $w_{i-w}, \dots, w_{i-1}, w_{i+1}, w_{i+w}$ are the context words.

307 TextRank was chosen since it can be extended for phrases and short sentences extraction.
 308 Some extracted phrases with the same/similar meanings are integrated to keep the total key
 309 phrases concise.

310 Following these steps, both usage scenario patterns and user-concerned phrases can be
 311 extracted for further evaluation.

312 **3.2 Phase II: Identify design ranges and system range based on context information** 313 **(Context processing)**

314 Based on the extracted evaluation indicators, PSBs' design range dr_{ij} and system range sr_{ij}
 315 can be identified, as shown in Figure 3.

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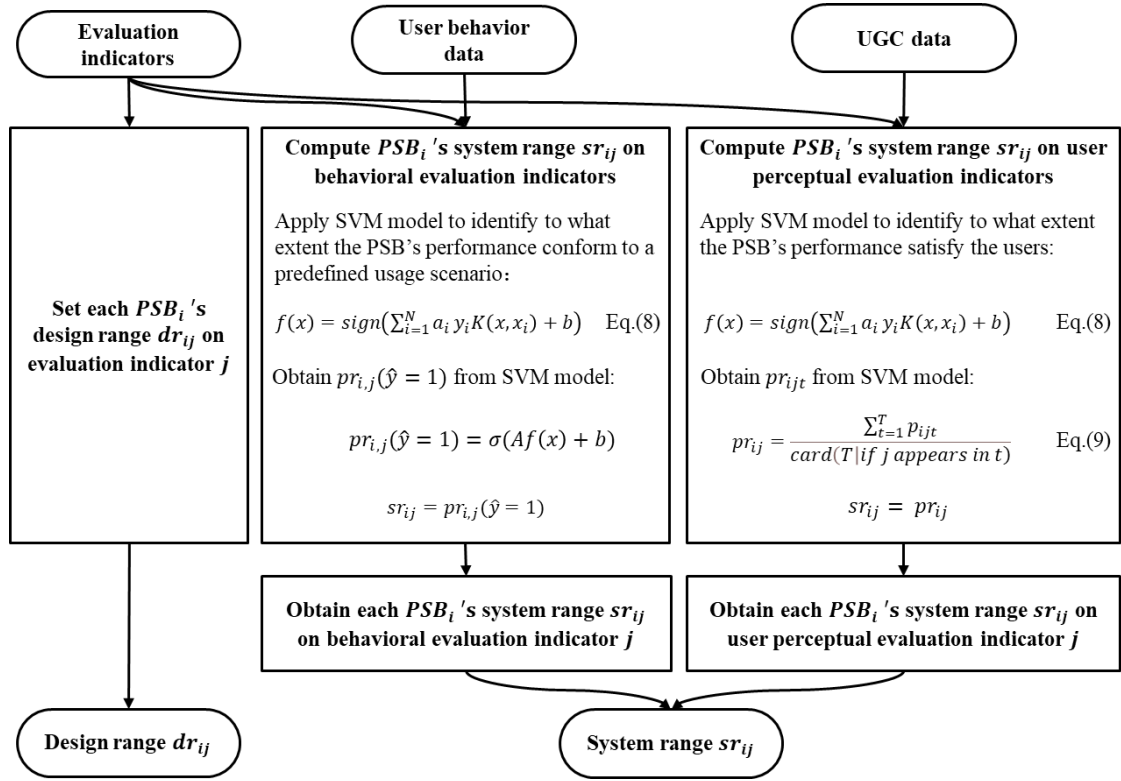


Figure 3. Flowchart of design range and system range identification

(1) Set design ranges

According to axiomatic design theory, the design ranges indicate what the users want. They are all normalized within the range of (0,1), where 1 represents the perfect user experience. Under the situation of design iteration, the design ranges from users can be collected and pre-processed from the recent design iterations. The design range of a PSB candidate PSB_i on an evaluation indicator j can be denoted as dr_{ij} .

(2) Identify the membership degree of the usage scenarios

The membership degree of each usage scenario can be regarded as the system ranges of an alternative. Specifically, we hope to monitor to what extent a usage scenario conforms to the typical ones, which is essentially a classification task. The scenarios in the Smart PSS are domain-specific and can be linearly non-separable in many cases. Support vector machine (SVM) [69] is a well-known classification algorithm to deal with non-linear problems and has already been proved to have better generalization performance than other traditional learning techniques like neural networks [70]. Hence, SVM is adopted in this study to assign the scenarios.

Specifically, given a training dataset S with N scenarios, i.e., $S = \{(\mathcal{X}_i, y_i), i = 1, 2, \dots, N\}$, $\mathcal{X}_i \in \mathbb{R}^P$, $y_i \in \{+1, -1\}$ in the binary classification, where \mathcal{X}_i is a feature vector and y_i indicates whether \mathcal{X}_i belongs to a specific scenario group. The non-linear SVM model is

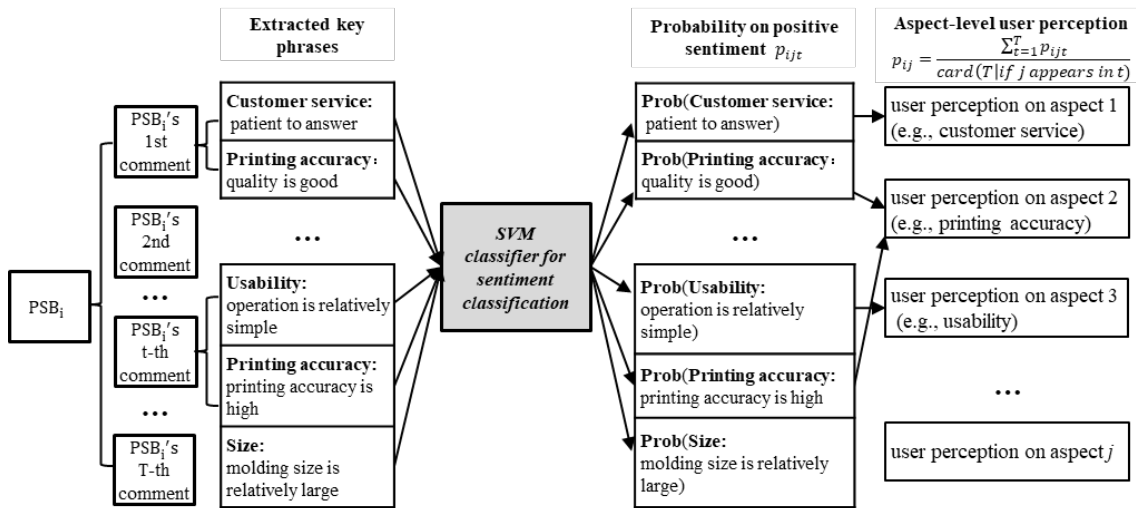
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$$f(x) = \text{sign}(\sum_{i=1}^N a_i y_i K(x, x_i) + b) \quad (8)$$

338 , where $K(x, x_i)$ is the kernel function, which maps the inputs into a high-dimensional feature
 339 space to make them linear-separable [70]. Several frequently-used kernel functions can be tested,
 340 including linear function, polynomial function, Gaussian radial basis function (RBF), and sigmoid
 341 function. The one with the best classification performance will be selected.

342 (3) Identify customer satisfaction

343 Besides evaluating usage scenarios, user's satisfaction can be regarded as the system ranges
 344 on perceptual indicators, it indicates to what extent a PSB can fulfill the users' expectations.
 345 Customer satisfaction is reflected in different aspects among the user comments [71], such as
 346 positive in quality, positive on customer service, and negative on price. As illustrated in Figure 4,
 347 a sentiment analysis approach based on another SVM classifier [72] is used to predict customers'
 348 satisfaction on each perceptual indicator.

349



350

351

Figure 4. An aspect model of user perception

352

353 Initially, a user comment dataset that has been segmented into short phrases with positive or
 354 negative labels can be used for the SVM classifier training process. The classifier will learn a
 355 function to separate the positive and negative data with the maximum margin. Similar to the
 356 membership degree identification for usage scenarios, the kernel function providing the best
 357 performance will be selected.

358 The outputs of the SVM classifier are the short phrases' probabilities of belonging to positive
 359 sentiment on different aspects. Let pr_{ijt} be the probability of the positive sentiment of PSB_i on
 360 the aspect j from the PSB_i 's t -th comment. Consistent with the design ranges of $(0,1)$ where 1

361 represents the best experience, pr_{ijt} approaching 1 also represents the best experience, and
 362 pr_{ijt} approaching 0 denote the worst experience.

363 To derive the total user perception pr_{ij} of PSB_i on each aspect j , all the pr_{ijt} are averaged,
 364 following Equation (9).

365
$$pr_{ij} = \frac{\sum_{t=1}^T pr_{ijt}}{\text{card}(T|if j \text{ appears in } t)} \quad (9)$$

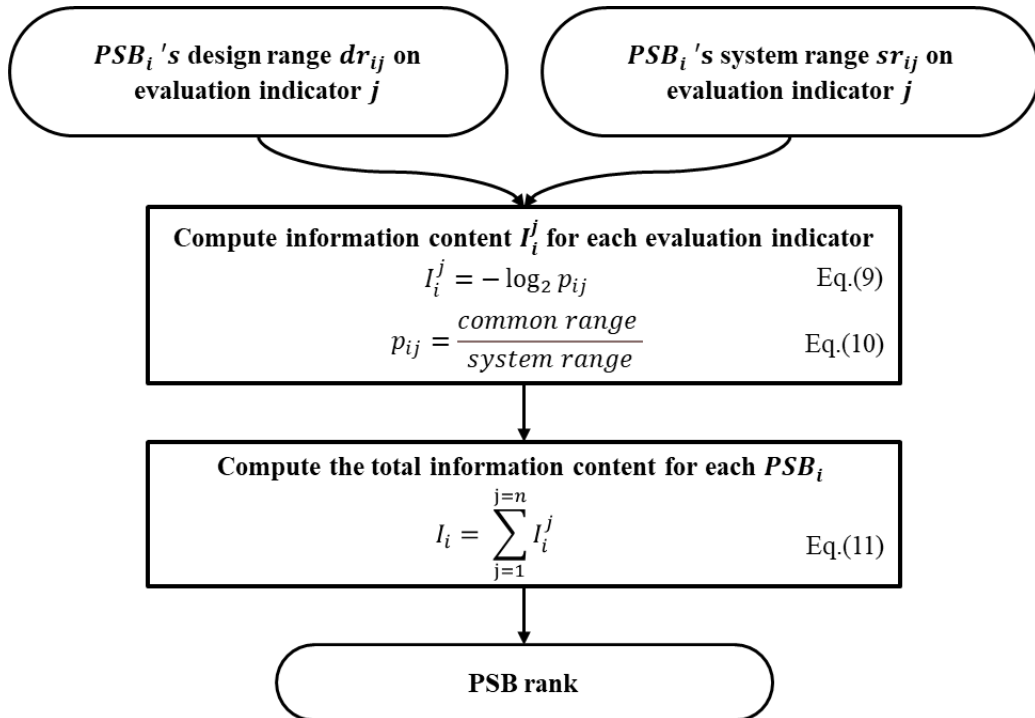
366 , where $\text{card}(T|if j \text{ appears in } t)$ is the number of comments in which the aspect j was
 367 mentioned. pr_{ij} is the final system range of PSB_i on aspect j , it will be applied for information
 368 content calculation in the later step.

369

370 3.3 Phase III: Compute information content (Context usage)

371 In the Phase III, the information content is supposed to be calculated following the
 372 information axiom's logic. As shown in Figure 5, the first step in Phase III is to compute the
 373 information content I_i^j for each evaluation indicator, followed by the step of total information
 374 content I_i calculation.

375



376

377 Figure 5. Flowchart of information content calculation

378 Specifically, the information content I_i^j of each evaluation indicator for each psb_i can be
 379 calculated following the equations in axiomatic design [73]:

380
$$I_i^j = -\log_2 p_{ij} \quad (10)$$

381 , where p_i is the probability of a design that can fulfill the users' expectations. Meanwhile, p_i is
 382 defined as

383
$$p_{ij} = \frac{\text{common range}}{\text{system range}} \quad (11)$$

384 Particularly, *common range* is the overlapping between the system range and the design range.

385 To calculate the information content for all PSBs on all evaluation indicators, let $E =$
 386 $\{e_1, e_2, \dots, e_n\} = S \cup P$ be the set of evaluation indicators, where the subset $S = \{s_1, s_2, \dots, s_t\}$ is
 387 a set of usage scenarios as the evaluation indicators, and $P = \{p_1, p_2, \dots, p_m\}$ is a set of perceptive
 388 features as the evaluation indicators. For each PSB candidate PSB_i , we can set a column vector
 389 $PSB_i \in \mathbb{R}^n$ whose elements equal to the system range on each e_j within the range (0,1). The total
 390 information content I_k of psb_k is the sum of all the information content on each e_i , expressed as

391
$$I_i = \sum_{j=1}^{j=n} I_i^j \quad (12)$$

392 Finally, the PSBs can be ranked in terms of the total information content I_i , the higher the I_i , the
 393 more robust the PSB will be.

394 **4 An illustrative example of the design upgrades of a 3D printer company**

395 To address the proposed concept evaluation framework for Smart PSS design, an illustrative
 396 example of a 3D printer company was discussed in this section.

397 3D printing has become widespread among individuals and companies as a new type of
 398 manufacturing due to its low cost and ease of customization. This case comes from a 3D printer
 399 company that currently sells 3D printers online together with essential services, including install
 400 instruction, delivery, and customer service. Now the company attends to expand its market with
 401 digital servitization by attracting more novice users. One of the value proposals is to offer 3D
 402 printer rents called "try before you buy". However, the company wonders which 3D printers can
 403 guarantee success before the design upgrade. During the upgrade, they also hope to quickly check
 404 whether the launched solutions can satisfy the user requirements. The situation faced by the 3D
 405 printer company is a typical design iteration situation for many manufacturing companies who
 406 have the goal of digital servitization.

407 This example is a typical use-oriented PSS [74] since the users pay for the usage of a 3D
 408 printer instead of owning a 3D printer. Meanwhile, this example's "smartness" is reflected in the
 409 automation evaluation process, making the design iteration a Smart PSS case in the design field.

410 **4.1 Identify evaluation indicators for Smart PSS concept evaluation**

411 Twenty-six 3D printers are identified as the candidates and 1712 pieces of user reviews on
 412 the 3D printers are accordingly collected.

413 To check the consistency between the user behavior and the assumed usage scenarios, some
 414 usage scenarios' patterns were predefined by the experts. Identifying the patterns is based on the
 415 accessible data through the daily use of 3D printers provided by the 3D printer company.

416 Four context features were predefined to constitute the usage scenarios, including *Product*
 417 *speed*, *Model Size*, *Nozzle number*, and *Print Frequency Monthly*, as listed in Table 2. Each
 418 context feature's value boundaries are decided based on the domain knowledge collected online
 419 (<http://www.3dhubs.com>). Those context features are all 3D printing-related data rather than user
 420 personal data, which cannot be applied to identify an individual user but only to evaluate the 3D
 421 printing service status.

422

423 **Table 2.**

424 The context features characterizing usage scenarios

| Contextual features | No. | Values |
|----------------------------|-----|--|
| Printing speed | C1 | [1-300] (mm/s) |
| Model size | C2 | (0x0x0, 305x305x300)(mm ³) |
| Nozzle number | C3 | {1,2} |
| Printing frequency monthly | C4 | [0, +∞) |

425

426 The scenarios of interest are represented in Table 3, including 'regular printing'(S1),
 427 'frequent printing'(S2), 'precise printing (S3), and 'fast printing'(S4). The change of usage
 428 scenarios can be reflected by the change of the patterns which are identified by different value
 429 ranges of the predefined context features.

430 Following the steps in subsection 3.1.2, the task of identifying perceptual evaluation
 431 indicators was conducted based on the trained word embeddings from the Word2Vec model, and
 432 is programmed under Python environment. Here, to ensure the word embeddings are well-trained
 433 with abundant semantic information, a larger pretraining dataset containing electronic products
 434 and 3D printers was used. We expanded the dataset by electronic products' comments since the
 435 comments on electronic products and 3D printers usually have similar features and sentiments.
 436 Totally, 23110 pieces of product comments were applied, containing 12075 pieces of positive
 437 comments and 11035 pieces of negative comments. A python package called TextRank [67] was
 438 used to extract the key phrases. Some extracted phrases with the same/similar meanings are
 439 integrated to keep the evaluation indicators concise.

440

441 **Table 3.**
 442 The usage scenarios as evaluation criterion their approximate patterns

| Scenario No. | Scenario name | Description | Approximate pattern |
|--------------|-------------------|--|---|
| S1 | regular printing | A new individual user use 3D printing service regularly | { $(10 \leq \text{printing speed} \leq 150)$ $\cap (145 \times 145 \times 145 \leq \text{model size} \leq 305 \times 305 \times 300)$ $\cap (\text{nozzle number} = 1)$ $\cap (\text{printing frequency monthly})$ } |
| S2 | frequent printing | A user who frequently use 3D printing for production | { $(10 \leq \text{printing speed} \leq 150)$ $\cap (145 \times 145 \times 145 \leq \text{model size} \leq 305 \times 305 \times 300)$ $\cap (\text{nozzle number} = 1)$ $\cap (\text{printing frequency monthly})$ } |
| S3 | precise printing | A user who use 3D printing for precise printing, e.g., jewelry | { $(10 \leq \text{printing speed} \leq 150)$ $\cap (145 \times 145 \times 145 \leq \text{model size} \leq 305 \times 305 \times 300)$ $\cap (\text{nozzle number} = 1)$ $\cap (\text{printing frequency monthly})$ } |
| S4 | fast printing | A user who want rapid prototyping | { $(10 \leq \text{printing speed} \leq 150)$ $\cap (145 \times 145 \times 145 \leq \text{model size} \leq 305 \times 305 \times 300)$ $\cap (\text{nozzle number} = 1)$ $\cap (\text{printing frequency monthly})$ } |

443

444 Table 4 shows 16 frequently-mentioned perceptions, including printing accuracy, hotbed
 445 calibration, accessories, sound and noise, and other features.

446

447

448

449

450 **Table 4.**
 451 Extracted user perceptions as evaluation indicators and their design ranges

| General user perception | Detailed user perception | No. | Value range | Design range |
|-------------------------|--------------------------|------|-------------|--------------|
| Quality | Printing accuracy | PI1 | (0,1) | (0.7721,1) |
| | Hot bed calibration | PI2 | (0,1) | (0.8133,1) |
| | Printing speed | PI3 | (0,1) | (0.5214,1) |
| | Accessory | PI4 | (0,1) | (0.7158,1) |
| | Noise | PI5 | (0,1) | (0.4250,1) |
| | Usability | PI6 | (0,1) | (0.8656,1) |
| | Stability | PI7 | (0,1) | (0.6540,1) |
| | Smell | PI8 | (0,1) | (0.3156,1) |
| Appearance | Beauty | PI9 | (0,1) | (0.5231,1) |
| | Size | PI10 | (0,1) | (0.5406,1) |
| Service | Installation instruction | PI11 | (0,1) | (0.8805,1) |
| | Customer service | PI12 | (0,1) | (0.6097,1) |
| Price | Price | PI13 | (0,1) | (0.6587,1) |
| | Cost-effective | PI14 | (0,1) | (0.5172,1) |
| Delivery | Delivery speed | PI15 | (0,1) | (0.7821,1) |
| | Damage-free package | PI16 | (0,1) | (0.8028,1) |

452

453 **4.2 Identify design ranges and system range based on context information**

454 On the one hand, the company sets its target users as the individual product designers who
 455 would like to test their product concepts; and identifies their usage scenarios as precise printing
 456 (S3) and rapid printing (S4).

457 The system range identification for the usage scenarios was trained via a SVM classifier
 458 under different kernel functions, including Linear function, Polynomial function, RBF, and
 459 Sigmoid function. The results using various kernel functions are shown in Table 5, indicating that
 460 using RBF leads to the highest F1-score (i.e., 0.974). Thus, the SVM model with RBF should be
 461 applied in this example.

462

463 **Table 5.**

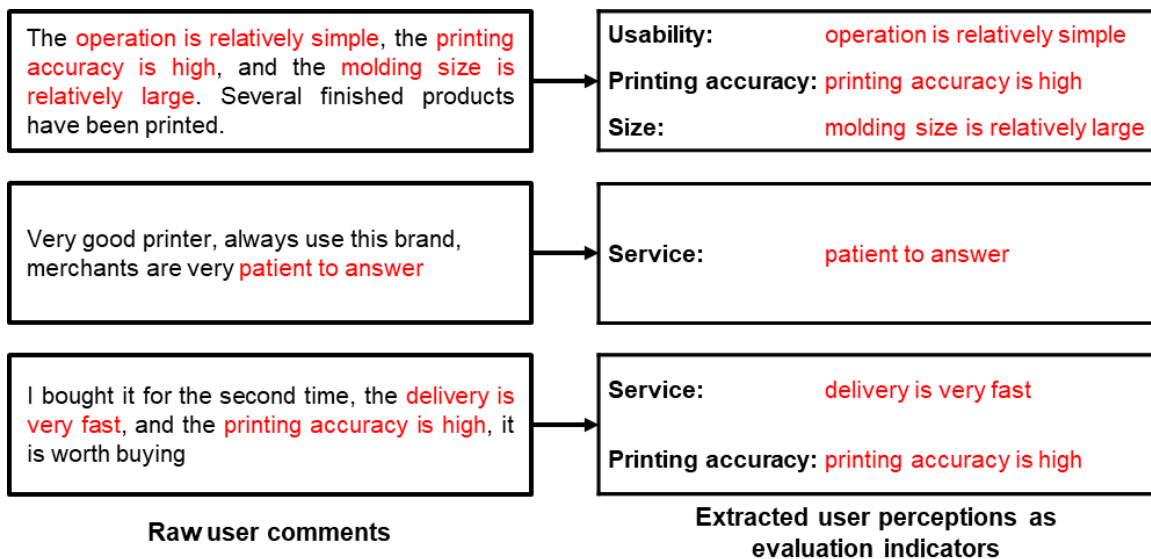
464 Comparison between different SVM models in scenario classification

| SVM model with different kernel functions | AUC | F1 | Precision | Recall |
|---|-------|-------|-----------|--------|
| Linear | 0.997 | 0.971 | 0.971 | 0.971 |
| Polynomial | 0.997 | 0.972 | 0.972 | 0.972 |
| RBF | 0.997 | 0.974 | 0.974 | 0.974 |
| Sigmoid | 0.973 | 0.895 | 0.895 | 0.896 |

465
 466 On the other hand, all the perceptual evaluation indicators are normalized into a value range
 467 of (0,1) that 0 means the worst of the indicators (e.g., expensive, hard, noise, and other features)
 468 and 1 indicates the best of the indicators (e.g., cheap, easy, quiet, and other features). The design
 469 ranges of the perceptual evaluation indicators determined by the novice users are listed in the last
 470 column of Table 4.

471 To identify the system ranges of the perceptual evaluation indicators, we followed the steps
 472 in Section 3.1.2 that first extract the key phrases from user reviews and then determine the user’s
 473 satisfaction on the user-mentioned aspects. Figure 6 displays some illustrative examples of key
 474 phrases extraction. For example, the key phrase “operation is relatively simple” can be extracted
 475 and assigned to the perceptual indicator “Usability”.

476



477

478 Figure 6. Illustrative examples of extracting user perceptions as evaluation indicators

479

480 Based on the pretraining dataset with sentiment labels, an SVM classifier model was trained

481 for sentiment classification. Totally 1176 key phrases were extracted and labelled. Part of them
 482 and the predicted sentiment label are listed in Table 6.

483 **Table 6.**

484 Examples of system range identification based on perceptual indicators

| User review No. | Psb-id | Extracted user comments | Perceptual indicators | Sentiment label | System range |
|------------------------|---------------|--|------------------------------|------------------------|---------------------|
| 1 | psb1 | complete tool accessories | accessory | 1 | 0.9548 |
| 2 | psb1 | intact packing | damage-free package | 1 | 0.9421 |
| 3 | psb2 | printing is very stable | stability | 1 | 0.7697 |
| 4 | psb4 | no smell durign printing | smell | 1 | 0.8022 |
| 5 | psb11 | machine appearance is very beautiful | beauty | 1 | 0.9800 |
| 6 | psb11 | machine is very cost-effective | cost-effective | 1 | 0.9089 |
| 7 | psb11 | customer service attitude is very good | customer service | 1 | 0.8988 |
| 8 | psb11 | logistics shipped quickly | delivery speed | 1 | 0.7617 |
| 9 | psb11 | video solves the problems of new installation | installation instruction | 1 | 0.8218 |
| 10 | psb11 | printing sound is very small | noise | 1 | 0.5972 |
| 11 | psb11 | price is cheaper than the brick-and-mortar store | price | 1 | 0.8719 |
| 12 | psb11 | price is reasonable | price | 1 | 0.6002 |
| 13 | psb11 | printing accuracy is very high | printing accuracy | 1 | 0.7651 |
| 14 | psb11 | machine stability is very good | stability | 1 | 0.9584 |
| 15 | psb11 | easy to operate | usability | 1 | 0.8820 |
| 16 | psb13 | It takes about an hour to assemble | installation instruction | 0 | 0.3581 |
| 17 | psb21 | auto-leveling is great | hot bed calibration | 1 | 0.9627 |
| 18 | psb26 | memory card only has installed software | installation instruction | 0 | 0.1472 |
| 19 | psb26 | if only the sound were smaller | noise | 0 | 0.3293 |

485

486 Table 7 proves the SVM classifier's feasibility that the precision, recall, and f1-score of the
487 sentiment classification are around 0.9. Furthermore, based on the user perception aspect model,
488 the system range on each perceptual indicator for each alternative can be derived by calculating
489 the average user perception in every user review. The results are listed in Table 8. For each PSB,
490 the system ranges on the user-mentioned perceptual indicators are calculated, the blanks in Table
491 8 indicate that the indicators are not mentioned by users.

492

493 **Table 7.**

494 Sentiment classification result

| Label | Precision | Recall | F1-score |
|---------------------|------------------|---------------|-----------------|
| Negative (label =0) | 0.90 | 0.90 | 0.90 |
| Positive (label =1) | 0.91 | 0.92 | 0.92 |

495

496 **Table 8.**

497 System ranges of each perceptual indicator for each alternative

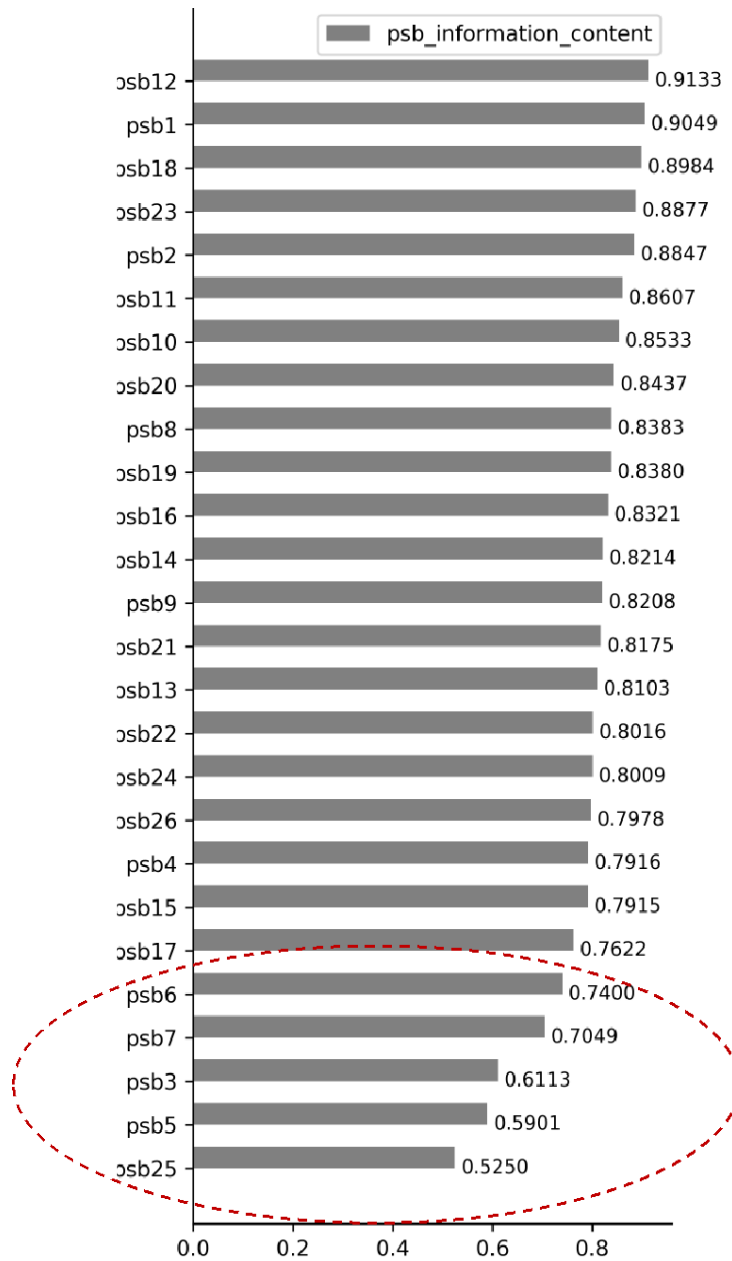
| | PI1 | PI2 | PI3 | PI4 | PI5 | PI6 | PI7 | PI8 | PI9 | PI10 | PI11 | PI12 | PI13 | PI14 | PI15 | PI16 |
|--------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| psb1 | 0.8734 | 0.4346 | 0.8277 | 0.9288 | 0.2478 | 0.8354 | 0.9081 | 0.9062 | 0.8746 | 0.9879 | 0.9091 | 0.8411 | 0.7813 | 0.9602 | 0.8972 | 0.9198 |
| psb2 | 0.9247 | | 0.6377 | | | 0.8697 | | | | | 0.5927 | 0.6489 | | | 0.8997 | |
| psb3 | 0.9124 | | | | 0.8740 | 0.9216 | 0.8918 | | | 0.8312 | 0.9972 | 0.7813 | | | 0.8683 | |
| psb4 | 0.9645 | 0.9600 | 1.0000 | | | | 0.6901 | | | | 0.8588 | 0.9467 | | 0.9243 | 0.9620 | |
| psb5 | 0.9077 | 0.7763 | | 0.9903 | 0.9463 | 0.7893 | 0.8677 | 0.7034 | 0.9623 | 0.9738 | 0.6008 | 0.7879 | | 0.9949 | 0.7920 | |
| psb6 | 0.8672 | | | | 0.5972 | 0.9144 | 0.8117 | | 0.9800 | 0.9820 | 0.8790 | 0.9023 | 0.7817 | 0.8871 | 0.8654 | |
| psb7 | 0.8605 | | | | | 0.8756 | | | | | | | 0.7974 | 0.9373 | 0.6995 | 0.8597 |
| psb8 | 0.9079 | 0.7700 | | | | 0.7969 | | | | 0.7775 | | 0.7086 | | | 0.7880 | |
| psb9 | 0.8351 | | 0.7905 | | 0.7255 | 0.7136 | | | | | 0.9669 | 0.8025 | 0.8746 | | | 0.9481 |
| psb10 | 0.8692 | | | | | 0.8918 | | | | | | | | | 0.9220 | 0.9107 |
| psb11 | 0.7837 | | | 0.7934 | 0.1002 | 0.8117 | | | | | | 0.7254 | 0.8041 | | 0.7548 | 0.8657 |
| psb12 | 0.8811 | | | 0.9079 | 0.7534 | 0.8887 | | | 0.7925 | 0.2456 | 0.1794 | 0.7658 | 0.8753 | | 0.8810 | 0.9698 |
| psb13 | 0.9180 | | | 0.7768 | 0.5972 | 0.8535 | | | 0.9441 | 0.9794 | 0.5804 | 0.8291 | 0.8965 | 0.9431 | 0.8997 | |
| psb14 | 0.8947 | 0.9912 | | 0.9584 | | 0.9878 | | | | 0.8469 | 0.9960 | 0.5937 | 0.8746 | 0.8461 | | |
| psb15 | 0.9224 | | 0.8283 | 0.6290 | 0.4536 | 0.8295 | 0.9417 | | 0.9593 | 0.9799 | 0.9449 | 0.6258 | 0.6222 | 0.9510 | 0.9087 | 0.9030 |
| psb16 | 0.8675 | 0.3896 | | 0.7336 | | 0.2991 | | | 0.4642 | 0.0488 | | 0.8626 | 0.7102 | | | 0.9348 |
| psb17 | 0.8853 | 0.9555 | | 0.8921 | | 0.9149 | 0.9832 | | | 0.2761 | 0.7013 | 0.6557 | 0.9437 | | | |
| psb18 | 0.8624 | 0.8559 | 0.8453 | 0.6741 | 0.2515 | 0.8173 | 0.8405 | | 0.9678 | 0.9516 | 0.7789 | 0.7706 | 0.8153 | 0.9231 | 0.8994 | 0.9012 |
| psb19 | 0.9059 | 0.4531 | 0.8922 | | | | 0.7683 | 0.1146 | | 0.4372 | 0.4324 | 0.6982 | 0.8943 | 0.9930 | 0.0857 | 0.6604 |
| psb20 | 0.8779 | | 0.9381 | 0.7633 | | 0.9465 | 0.7786 | | 0.8347 | | 0.7716 | 0.7869 | | | 0.7987 | 0.9402 |
| psb21 | 0.7663 | | 0.8499 | | | 0.7506 | | 0.8022 | | 0.2551 | 0.8991 | 0.9712 | 0.7802 | 0.9639 | 0.8774 | |
| psb22 | | | | | | | | | | | 0.1086 | 0.9413 | | | | |
| psb23 | 0.8153 | | 0.7869 | 0.8476 | 0.4039 | 0.9936 | 0.9817 | | | 0.9617 | | 0.4320 | 0.9919 | | | |
| psb24 | 0.8729 | | 0.9322 | 0.8764 | 0.4868 | 0.8670 | 0.9518 | | 0.9216 | 0.5639 | 0.5024 | 0.6295 | 0.8760 | 0.9358 | 0.8034 | 0.9496 |
| psb25 | 0.8630 | | | 0.9548 | | 0.8479 | | | 0.9675 | | 0.9805 | 0.9567 | 0.7666 | | 0.8650 | 0.9421 |
| psb26 | 0.7359 | 0.9400 | | 0.7453 | | 0.9311 | | | | | 0.9157 | 0.8160 | 0.4049 | 0.8928 | 0.9760 | |

498

499 **4.3 Compute information content**

500 The final information contents for each PSB were calculated by averaging the user-
501 mentioned information contents. Then we ordered the PSBs in terms of the final information
502 content from largest to smallest, as shown in Figure 7. Assume that the top 5 PSBs are selected
503 as the most robust PSBs, then $psb_{25} > psb_5 > psb_3 > psb_7 > psb_6$.

504



505

506

Figure 7. PSB ranking based on the final information content

507

508 **5 Discussion**

509 **5.1 Comparison with TOPSIS**

510 To demonstrate the rationality of the proposed approach, the case was also conducted based
 511 on a classic evaluation method, i.e., TOPSIS [75]. TOPSIS method ranks the candidates based on
 512 their closeness to the ideal solution; the selected candidate should have the shortest distance to
 513 the ideal solution and the longest distance to the worst solution. In this case, we applied the
 514 normalized Euclidean distance to measure the distances, following Equation (13), (14), and (15).

515
$$d_i^+ = \sqrt{\sum_{j=1}^n (v_{ij} - v_{bj}^+)^2} \quad (13)$$

516
$$d_i^- = \sqrt{\sum_{j=1}^n (v_{ij} - v_{wj}^-)^2} \quad (14)$$

517
$$C_i = \frac{d_i^-}{d_i^+ + d_i^-} \quad (15)$$

518 In the equations, d_i^+ refers to the distance between the PSB candidate i and the best PSB
 519 solution b . Similarly, d_i^- indicates the distance between the PSB candidate i and the worst PSB
 520 solution w . C_i is the closeness to the best solution that $0 \leq C_i \leq 1$. When the candidate
 521 approaches the worst solution, C_i approximately equals 0; in contrast, C_i will approach 1 when
 522 the candidate is the best solution. The top 5 results obtained by TOPSIS are ranked as $psb_{25} >$
 523 $psb_5 > psb_3 > psb_{13} > psb_6$, their corresponding measurements are listed in Table 9.

524 Using TOPSIS as the benchmark, 4 out of 5 candidates have the same sequences, thus
 525 proofing the proposed approach's rationality. The variance might be caused by the imputation
 526 method on the system ranges of the not-mentioned perceptual aspects. In this showcase, the
 527 average values are filled in the blanks.

528

529 **Table 9.**

530 The top 5 evaluation results based on TOPSIS

| | d_i^+ | d_i^- | C_i |
|-------|----------|----------|----------|
| psb25 | 0.5518 | 1.7145 | 0.756519 |
| psb5 | 0.55626 | 1.698 | 0.75324 |
| psb3 | 0.551748 | 1.67317 | 0.752014 |
| psb13 | 0.600942 | 1.662875 | 0.734545 |
| psb6 | 0.65812 | 1.675335 | 0.717963 |

531

532 **5.2 *The selection of the evaluation indicators***

533 Compared with the common ways, such as zigzagging and QFD [13, 76], to identify the
534 evaluation indicators in traditional axiomatic design [73], the proposed approach enriches
535 evaluation indicators from user reviews. Its strengths can be seen from the following perspectives.

536 Firstly, zigzagging and QFD require engineers to predefine the evaluation indicators, heavily
537 relying on the professional understanding of the specific domain; otherwise, it is hard to identify
538 the evaluation indicators. However, in this article, the evaluation indicators were statistically
539 defined from the key phrases, not depending on the skilled domain knowledge.

540 Simultaneously, the prerequisite of asking engineers to predefine the indicators also leads to
541 zigzagging and QFD's second limitation. The determined evaluation indicators are based on
542 designers/experts' subjective judgment, other than users' real perceptions. Nevertheless,
543 extracting the user-mentioned key phrases directly and explicitly reflects which aspects are the
544 users concerned about, thus reducing the human's prejudices.

545 Moreover, in a big and dynamic world, zigzagging and QFD will be costly and time-
546 consuming for the system maintenance/update by inviting the experts to update the evaluation
547 indicators. Unlike the traditional ones, the proposed approach used the automatic NLP techniques,
548 enabling the evaluation indicator updates at a relatively low cost.

549 **5.3 *The identification of system ranges***

550 The proposed approach can further reduce human interventions by automatically deriving
551 the system ranges for each candidate via SVM classifiers. Considering that many linguistic words,
552 such as "good" and "not bad", are involved in this paper, it is fuzzy and rough to assign them with
553 a certain label. Fuzzy set theory [77] is a conventional method to handle the fuzziness under this
554 situation. It contains the process of fuzziness based on membership functions and de-fuzziness to
555 get the final crisp probability to certain groups [77]. However, the identification of membership
556 functions is still predefined by engineers, leading to a series of system range results based on the
557 engineers' subjective judgment. In contrast, by training the SVM classifiers, no more membership
558 functions are required in our approach; hence fewer human interventions and a more automatic
559 manner are achieved.

560 **5.4 *Limitations in the proposed approach***

561 Despite the improvements, some limitations still exist. One limitation is caused by the
562 limited data that only 26 PSBs were tested in this example. The proposed approach is still
563 practicable for some small and medium enterprises that offer just dozens of PSB instead of the e-
564 commerce platforms that sell thousands of PSBs. A scalability concern in the proposed approach
565 will be further investigated, which can be considered from two perspectives. One is to enhance
566 the context-aware concept evaluation approach with a larger number of PSBs, by simulating the

567 concept evaluation situation of an integrated Smart PSS platform with different brands of PSBs.
568 The other scalability concern is that more types of user behavioral data can be tested if accessible.

569 Another limitation comes from the assumption that system ranges follow the uniform
570 distribution. In practice, users might be prone to give praise. For example, ‘good’ or ‘excellent’
571 often appear in the user reviews, making the system ranges probably follow other distributions
572 instead of uniform distribution. How the system ranges’ uneven distribution affects the concept
573 evaluation results will be further studied in the future. The pattern recognition techniques such as
574 neural networks can be considered to tackle this limitation.

575 **6 Conclusions**

576 Motivated by digital paradox, and facing the risks of (1) omitting user perceptions during
577 concept evaluation, (2) lacking a rapid evaluation indicator identification approach, and (3) the
578 lag between user requirement changes and solutions, this study proposed a comprehensive user-
579 experience-based concept evaluation framework for Smart PSS under a content-rich, user
580 experience-oriented, and context-aware environment. The main contributions of the proposed
581 approach can be concluded into three points:

582 (1) *Expand the evaluation scope from functional/technical parameters’ values to a*
583 *comprehensive scope considering both behavioral and perceptual indicators.* This expansion
584 increases the system’s capability to reflect the real user experience during the usage phase,
585 accordingly reducing the failure possibility of digital servitization caused by insufficient
586 evaluation scope.

587 (2) *Apply an automatic evaluation indicator identification approach.* It accelerates the
588 evaluation process and relieves the lag between the user requirement changes and the solutions
589 because of less human intervention.

590 (3) *Use large historical data to identify system range, rather than relying on engineers’*
591 *experience.* Hence, the prescriptive instructions in the traditional automation processes, such as
592 manually evaluation indicator identification and fuzzy membership function identification, can
593 be eliminated, therefore, realizing the intelligent automation in the concept evaluation process.

594 Based on these contributions, future research directions lie in two aspects. On the one hand,
595 a multi-sourced and multi-modal concept evaluation manner can be achieved in Smart PSS by
596 introducing more types of user behavioral data and user perception data, such as human action
597 data or emoji memes. It will enrich the quantity of raw data for the Smart PSS development,
598 making the Smart PSS development a more comprehensive digital-based ecosystem. On the other
599 hand, besides the automatic capability of identifying evaluation indicators and their system ranges,
600 advanced intelligent capabilities such as adaptability should be explored in the future. The

601 adaptability of a concept evaluation approach refers to the capability of adjusting the PSB
602 evaluation indicators or the PSBs' system ranges when the inputs change. These two research
603 directions can further enhance the Smart PSS's capability of perceiving a specific usage scenario
604 with context-awareness (i.e., offline smartness) and its capability of making proper and
605 personalized decisions (i.e., online smartness).

606 In a competitive market pursuing quick design iteration, it is hoped that this study can offer
607 practical guidance for the design practitioners in Smart PSS development to rapidly evaluate a
608 PSB family and select the most robust PSB for design iteration/upgrade. At the same time,
609 theoretically, it is also an attempt to expand the usability of information axiom into a broader
610 scope with the concern on user experience from both user behavior and user perception.

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