

# Behaviour of RC beams with a fibre-reinforced polymer (FRP)-strengthened web opening

X.F. Nie<sup>1</sup>, S.S. Zhang<sup>2,\*</sup> and T. Yu<sup>3</sup>

<sup>1</sup> Post-doctoral Fellow, School of Civil Engineering and Mechanics, Huazhong University of Science and Technology, Wuhan 430074, China.

<sup>2</sup> Professor, School of Civil Engineering and Mechanics, Huazhong University of Science and Technology, Wuhan 430074, China. (Corresponding author), E-mail address: [shishun@hust.edu.cn](mailto:shishun@hust.edu.cn)

<sup>3</sup> Professor, Department of Civil and Environmental Engineering, The Hong Kong Polytechnic University, Hong Kong, China.

## Abstract:

The beam opening (BO) technique, which involves (1) the creation of a web opening in the beam to weaken its flexural capacity and (2) the fibre-reinforced polymer (FRP) shear strengthening around the opening to avoid shear failure of the beam, was proposed to realize the strong column-weak beam hierarchy in existing reinforced concrete (RC) frames, which were designed using previous codes and thus violated such hierarchy. In the present study, six large-scale T-section beams with a web opening of different sizes and made by different methods (pre-formed and post-cut) were tested to assess the effectiveness of BO technique and the test results are presented. The experimental study show that the post-cutting method is feasible for making web openings in existing RC beams, the BO technique can effectively reduce the flexural capacity of the beam to the desired value if the size of web opening is appropriate, and the FRP strengthening can well compensate the loss of shear capacity and ductility of the beam caused by the creation of web opening. The present study provides a basis for the safe use of BO technique to achieve the strong column-weak beam hierarchy in existing RC frames.

**Keywords:** reinforced concrete (RC); beam opening; fibre-reinforced polymer (FRP) strengthening; strong column-weak beam; seismic performance

## 34 1. INTRODUCTION

35 For reinforced concrete (RC) frames subjected to seismic effects, there are mainly two  
36 possible failure modes: beam-sway mechanism (i.e., plastic hinges first form at the ends of  
37 beams) and story-sway mechanism (i.e., plastic hinges first form at the ends of columns).  
38 Beam failure usually affects only a limited part of the structure, while column failure may  
39 lead to progressive collapse of the whole structure. Therefore, beam-sway mechanism is  
40 preferred to story-sway mechanism if the failure of RC frames cannot be avoided. The strong  
41 column-weak beam design philosophy which can realize the beam-sway mechanism has been  
42 widely adopted in the seismic design of RC frames, according to a comprehensive literature  
43 review conducted by the authors [1]. To achieve the strong column-weak beam hierarchy in  
44 RC frames, a flexural strength ratio (i.e., ratio of the sum of flexural capacities of the columns  
45 at a joint to that of the beams framing into the joint) greater than 1 has been stipulated in the  
46 relevant design codes from different countries [1]. For instance, the current ACI code [2] and  
47 Eurocode [3] specify a flexural strength ratio of 1.2 and 1.3 respectively, and the current  
48 Chinese code [4] specifies a range of flexural strength ratio from 1.1 to 1.7.

49

50 However, studies have shown that the beam-sway mechanism rarely formed in failed RC  
51 frames after large earthquakes [e.g. 5-7], although these frames were designed to achieve the  
52 strong column-weak beam hierarchy. For example, after the magnitude ( $M_s$ ) 8.0 Wenchuan  
53 earthquake in 2008, only RC frames without floor slabs or with precast floor slabs exhibited  
54 the beam-sway mechanism, while the cast-in-place RC frames commonly failed at the ends of  
55 columns [6]. This is mainly because that the contribution of cast-in-place slab to the flexural  
56 capacity of the beam was not properly considered in design codes of previous versions,  
57 leading to an underestimation of the flexural capacity of beam and thus the violation of the  
58 strong column-weak beam hierarchy. For instance, the Chinese seismic design code of  
59 previous versions [e.g. 8] ignored the contribution of cast-in-place floor slab to both the  
60 negative flexural capacity (i.e., the flange of the beam is in tension) and the positive flexural  
61 capacity (i.e., the flange of the beam is in compression) of the supporting beam [9]. Existing  
62 experimental studies on RC exterior/interior joints with a cast-in-place floor slab have

63 confirmed that the floor slab can significantly enhance the flexural capacity of the beam,  
64 especially when the beam is in negative bending [e.g. 10-20]. Therefore, it is not  
65 unreasonable to believe that many existing RC frames in China and other countries/regions  
66 are likely to violate the strong column-weak beam requirement. The current design codes [e.g.  
67 2-4] require the consideration of the contribution of the cast-in-place slabs to the flexural  
68 capacity of the beams. A larger number of existing RC frames, however, cannot meet this  
69 requirement and need to be retrofitted.

70

71 In order to achieve the strong column-weak beam hierarchy of an existing cast-in-place RC  
72 frame which violates such hierarchy, the strengthening of column is a straightforward option  
73 [e.g. 21-27]. There are mainly three common column strengthening techniques: (1) concrete  
74 jacketing [e.g. 21, 22]; (2) steel jacketing [e.g. 23, 24]; and (3) fibre-reinforced polymer (FRP)  
75 jacketing [e.g. 25-27]. However, concrete jacketing or steel jacketing results in the increase in  
76 seismic forces by increasing the mass and/or stiffness of the columns, while the FRP  
77 jacketing is not effective enough for non-circular columns, compared with that for circular  
78 columns [28]. Furthermore, the successful strengthening of column may simply shift the  
79 failure location from the column ends to the beam-column joint, which is more difficult to  
80 retrofit. Against the above background, a novel seismic retrofit method was proposed to  
81 achieve good seismic performance of cast-in-place RC frames which violate the strong  
82 column-weak beam requirement, based on the concept of Beam-end Weakening in  
83 combination with FRP Strengthening (referred to as BWFS method hereinafter for simplicity)  
84 [29]. Three specific techniques were proposed to implement the BWFS method [29]: (1) the  
85 beam opening (BO) technique; (2) the slab slit (SS) technique; and (3) the beam section  
86 reduction (SR) technique. More details of the above three techniques can be found in Ref.  
87 [29], and the present study is focused on the BO technique. The BO technique involves the  
88 creation of a web opening in the T-section beam adjacent to the beam-column joint and the  
89 installation of local shear strengthening system (e.g., using FRP wraps and FRP U-jackets)  
90 around the opening (as shown in Fig. 1). It should be noted that the strong column-weak  
91 beam design philosophy requires that the Sum of Flexural Capacities (referred to as SFC  
92 hereafter for simplicity) of the beam at a joint (i.e., the sum of positive and negative flexural

93 capacities of the beam) are smaller than that of the column at the same joint. If the size of the  
94 web opening is suitable, the SFC of the T-section beam can be ideally reduced to a desired  
95 value (i.e., the SFC of the corresponding rectangular beam). Compared with other shapes of  
96 web openings such as circular and elliptical web openings, rectangular web opening can be  
97 more flexibly designed to achieve a required reduction of the flexural capacity of the  
98 T-section beam, and at the same time, rectangular web opening leads to regular shapes of the  
99 chords which can facilitate the development of design methods. Therefore, rectangular web  
100 opening is adopted in the BO technique. Meanwhile, to prevent the brittle shear failure of the  
101 beam with a web opening, the shear strengthening using FRP is applied around the opening.  
102 Actually, creating web openings in existing RC beams is not a new thing. It has been widely  
103 adopted in practice for the passages of utility pipes [e.g. 30-32].

104  
105 A preliminary study has been conducted by the authors [33] to experimentally assess the  
106 concept of the BO technique in reducing the flexural capacity of the T-section beam. In the  
107 preliminary study [33], a total of eight RC beams, including one rectangular beam and seven  
108 T-section beams were tested. The rectangular beam (CB-Rec) and one T-section beam (CB-T)  
109 did not contain web openings and served as control specimens, while the remaining six  
110 T-section beams had a web opening. Two different web opening sizes (length  $\times$  height being  
111 700 mm  $\times$  300 mm and 800 mm  $\times$  280 mm respectively, referred to as web openings of large  
112 size) were examined. For each large web opening size, three beams were tested: one with an  
113 un-strengthened web opening (tested under negative bending) and two with an  
114 FRP-strengthened web opening (one tested under negative bending and the other one tested  
115 under positive bending).

116  
117 In the preliminary study [33], the adopted web opening sizes were found to be too large so  
118 that the flexural capacity of the T-section beam was largely over-weakened. In addition, the  
119 web openings in the preliminary study [33] were pre-formed through manipulating the  
120 formwork for casting concrete, which is a simplification for test and not feasible for  
121 retrofitting of existing structures. The post-cut web opening, which is more practical for  
122 existing structures, needs to be investigated. To more comprehensively verify the

123 effectiveness of the BO technique and to gain an improved and in-depth understanding on the  
124 behaviour of RC beams with a web opening, large-scale tests on RC beams with a  
125 pre-formed/post-cut web opening of more reasonable sizes were conducted and the test  
126 results are presented and analysed in the present study. In this paper, unless otherwise  
127 specified: (1) when presenting the test results, it is assumed that the web opening is located in  
128 the right shear span of the beam (i.e., the left opening edge refers to the edge closer to the  
129 loading point while the right opening edge refers to the edge closer to the right support); and  
130 (2) for the sake of brevity, the concrete chords in the beam flange and beam web are  
131 respectively referred to as flange chord and web chord.

## 132 **2. EXPERIMENTAL PROGRAM**

### 133 **2.1 Specimen details**

134 A total of six large-scale RC T-section beams were tested under three-point bending in the  
135 present study. The studied parameters included the web opening size (i.e., length  $\times$  height)  
136 and the effect of FRP strengthening. Four different web opening sizes (length  $\times$  height being  
137 600 mm  $\times$  220 mm, 700 mm  $\times$  200 mm, 600 mm  $\times$  280 mm and 700 mm  $\times$  260 mm  
138 respectively) were investigated. For web openings of 600 mm  $\times$  220 mm and 700 mm  $\times$  200  
139 mm (referred to as web openings of small size for simplicity), each web opening size  
140 contained two specimens with one having an un-strengthened web opening and the other one  
141 having an FRP-strengthened web opening. For web openings of 600 mm  $\times$  280 mm and 700  
142 mm  $\times$  260 mm (referred to as web openings of medium size for simplicity), only specimens  
143 with an FRP-strengthened web opening were tested. The test specimens had the same  
144 dimensions: a total length of 3500 mm, a clear span of 3300 mm, a web thickness of 250 mm,  
145 an overall depth of 500 mm, a flange thickness of 100 mm and a flange width of 1450 mm.  
146 Details of the test specimens are listed in Table 1. Each specimen is given a name which  
147 consists of a letter to indicate whether FRP strengthening is applied (i.e., “O” for  
148 un-strengthened beam, and “F” for FRP-strengthened beam) and two three-digit numbers to  
149 show the length and height of the web opening respectively. It has been found from the  
150 preliminary study [33] that the behaviour of RC T-section beams with a web opening in

151 positive bending is quite similar to that in negative bending. Moreover, the contribution of a  
152 cast-in-place floor slab to the flexural capacity of an RC beam in negative bending is much  
153 more significant than that in positive bending. Therefore, all specimens were tested in  
154 negative bending (i.e., the flange of the beam was in tension) in the present study.

155

156 The details of Specimen O-700×200 are plotted in Fig. 2 as an example to show the layout of  
157 the test specimens. As shown in Fig. 2, all specimens were such placed that they were all  
158 tested in negative bending. All six specimens had the same layout of longitudinal/shear steel  
159 reinforcement: three deformed steel bars of 20 mm in diameter were adopted as the primary  
160 compression reinforcement, four deformed steel bars of 20 mm in diameter were adopted as  
161 the primary tension reinforcement, and smooth steel bars of 8 mm in diameter with a spacing  
162 of 100 mm were adopted as the shear reinforcement; in addition, six smooth steel bars of 8  
163 mm in diameter were adopted as the longitudinal reinforcement on each side of the beam  
164 flange (with three bars placed near the bottom surface while the other three bars near the top  
165 surface), and smooth steel bars of 8 mm in diameter with a spacing of 200 mm were adopted  
166 as the transverse reinforcement in the flange. The concrete cover was 30 mm within the beam  
167 web and 15 mm within the beam flange. The web opening was only created in the right shear  
168 span of the beam, and its location was determined as follows (Fig. 2): (1) the bottom edge of  
169 the web opening coincided with the web-flange intersection for ease of making the opening  
170 and subsequent theoretical studies; and (2) the horizontal distance between the left vertical  
171 edge of the web opening and the loading point was 250 mm, considering that the distance  
172 between the edge of the column and the nearer edge of the opening was assumed to be 250  
173 mm, in order for the installation of the CFRP-U-jacket on the left side of the web opening  
174 (i.e., closer to the loading point).

## 175 2.2 Preparation of specimens

### 176 2.2.1 Formation of web opening

177 Two different approaches were adopted in the present study to make the web openings. In the  
178 first approach, through manipulating the formwork for casting the concrete, the web openings  
179 were pre-formed (i.e., the approach used in the preliminary study [33]). According to the size  
180 and location of the web opening, the stirrups intersected with the web opening were cut

181 carefully. A typical pre-formed web opening is shown in Fig. 3. This approach is suitable for  
182 the new construction of RC beams with web openings but does not suit the scenario of web  
183 weakening of existing RC beams. Therefore, another approach was also examined in the  
184 present study to verify the feasibility of post-cutting web openings in the existing RC beams.  
185 In the second approach, the web openings were post-cut after 28 days' curing of the concrete  
186 by adopting the following four steps (as shown in Fig. 4): (1) drill small round holes along  
187 the boundary of the opening and cut the stirrups passing through the opening (Fig. 4a); (2)  
188 remove the concrete chunk to form a rough opening (Fig. 4b); (3) chip away the extrusive  
189 concrete by using an electric chisel along the boundary of the opening (Fig. 4c); and (4)  
190 polish the boundary of the opening by using a grinding machine (Fig. 4d). In the present  
191 study, the web openings in the three specimens with an opening length of 700 mm were  
192 prepared using the first approach and the rest three specimens with an opening length of 600  
193 mm were prepared using the second approach, as shown in Table 1. Both approaches were  
194 proved to be feasible in fabricating the web opening.

195

#### 196 2.2.2 *Installation of FRP jackets*

197 Carbon fibre-reinforced polymer (CFRP) was used for all four specimens with an  
198 FRP-strengthened web opening. The strengthening region is shown in Fig. 5a. After rounding  
199 the four corners of the web chord with a radius of 25 mm, one layer of CFRP sheet with a  
200 thickness of 0.334 mm was used to wrap the web chord. In addition, one layer of vertical  
201 CFRP U-jacket with a thickness of 0.334 mm and a width of 200 mm was adopted to  
202 strengthen the beam web at the two sides of the web opening (as shown in Fig. 5a), in order  
203 to prevent the development of possible diagonal cracks at the opening corners. The CFRP  
204 strengthening system was installed through wet-layup process and the detailed procedures  
205 were as follows: (1) use a needle gun to roughen the concrete surface (Fig. 6a); (2) use a  
206 clean brush to apply well-mixed primer (Sikadur 330) onto the concrete surface (Fig. 6b); (3)  
207 impregnate the carbon fibre sheets with well-mixed epoxy (Sikadur 300) and lay onto the  
208 concrete surface (Fig. 6c); and (4) evenly distribute the resin and release air bubbles through  
209 slowly rolling the FRP sheet (Fig. 6d).

210

#### 211 2.2.3 *Fabrication and installation of CFRP spike anchors*

212 CFRP spike anchors which were made from the same type of carbon fibres used in the CFRP  
213 wraps and U-jackets were adopted to anchor the ends of the CFRP U-jackets to the beam  
214 flange (as shown in Fig. 5), in order to prevent the CFRP U-jackets from premature  
215 debonding. As can be seen from Figs. 5b and c, the CFRP spike anchors consist of two parts:  
216 anchor dowel and anchor fan. The anchor dowel is a hardened bundle of carbon fibres with a  
217 length of 90 mm and a diameter of around 11 mm. The anchor fan is a loose fibre tail with a  
218 length of 80 mm. The installation of CFRP spike anchors included two steps: (1) insert the  
219 anchor dowel into the predrilled holes filled with epoxy in the beam flange (the holes were  
220 evenly distributed along the web-flange intersection at a distance of 50 mm and drilled  
221 towards the direction of the mid-width of the cross section, and the inclination angle between  
222 the holes and the side surface of the beam web was 20 degrees, as shown in Figs. 5a and b);  
223 and (2) bond the anchor fan onto the ends of the CFRP U-jackets during the wet-layup  
224 process. As shown in Fig. 5a, four CFRP spike anchors which were evenly distributed with a  
225 spacing of 50 mm were used for each end of the CFRP U-jackets.

### 226 **2.3 Material properties**

227 In the present study, commercial concrete of normal strength was used. On the same day of  
228 beam test, three concrete cylinders (150 mm × 300 mm) were tested for each beam specimen  
229 to obtain the cylinder compressive strength of concrete. The average concrete strength of  
230 each beam specimen is shown in Table 1.

231

232 The material properties of steel bars used in this study were determined through standard  
233 tensile tests according to BS-18 [34]. The yield stress and ultimate stress of the deformed  
234 steel bars of 20 mm in diameter were 434 MPa and 559 MPa respectively, and the yield stress  
235 and ultimate stress of the smooth steel bars of 8 mm in diameter were 349 MPa and 526 MPa  
236 respectively. The elastic moduli of the steel bars of 20 mm in diameter and 8 mm in diameter  
237 were measured to be 203 GPa and 196 GPa, respectively.

238

239 Following ASTM D3039 [35], the material properties of CFRP sheet were determined  
240 through tensile tests on 7 coupons. The length and width of the test region of the CFRP

241 coupons were 250 mm and 25 mm respectively. According to the nominal thickness of the  
242 CFRP sheet (0.334 mm per ply), its tensile strength and elastic modulus were measured to be  
243 2820 MPa and 227 GPa respectively.

## 244 **2.4 Test set-up and instrumentation**

245 In the present study, a total of 13 linear variable displacement transducers (LVDTs) were  
246 used to measure the deflections of each beam specimen, with the layout of the LVDTs shown  
247 in Fig. 7. Six LVDTs were installed on the bottom surface of the beam flange, with three  
248 LVDTs (one was installed at the mid-width of the beam flange and the other two were  
249 respectively installed 300 mm away from the nearer edge of the beam flange) installed at the  
250 mid-span of the beam (i.e., 01, 02 and 03 shown in Fig. 7) and the mid-span of the web  
251 opening (i.e., 04, 05 and 06 shown in Fig. 7), respectively. Two LVDTs were installed on the  
252 top surface of the beam web at the two supports (i.e., 07 and 08 shown in Fig. 7). The rest  
253 five LVDTs were evenly distributed on the top surface of the web chord (i.e., 09 to 13 shown  
254 in Fig. 7).

255

256 In addition, a large number of strain gauges were used to measure the strain development of  
257 the steel bars and FRP. The strain gauge arrangement of the steel bars in all test specimens  
258 was all the same. Taking Specimen F-700×200 as an example, the layout of strain gauges on  
259 the steel bars is shown in Fig. 8. As can be seen from Fig. 8a, the whole longitudinal steel  
260 bars were divided into three groups: top steel bars, middle steel bars and bottom steel bars.  
261 The top steel bars included the three bars in the compression zone; the middle steel bars  
262 included the six bars in the beam flange nearer the top surface of the flange; and the bottom  
263 steel bars included the ten bars nearer the bottom surface of the beam flange (i.e., four bars in  
264 the web and six in the flange). For the top steel bars, strain gauges were installed onto two  
265 bars including the middle one (Fig. 8b); for each selected bar, the strains of the following four  
266 critical positions were monitored using strain gauges: positions corresponding to the  
267 mid-span of the beam, the mid-span and the two vertical edges of the web opening,  
268 respectively. For the bottom steel bars, strain gauges were installed onto a half of the bars in  
269 the same side of the beam (i.e., two bars in the web and three in the flange, taking advantage

270 of symmetry) and the outmost bar in the other side of the beam (Fig. 8c); the arrangement of  
271 the strain gauges for all selected bottom steel bars were the same as that for the top steel bars.  
272 For the middle steel bars, strain gauges was installed onto the two middle bars in each side of  
273 the flange (Fig. 8d); for each selected bar, only the strain of the position corresponding to the  
274 mid-span of the beam was monitored using one strain gauge.

275

276 Fig. 9 shows the layout of strain gauges on the CFRP strengthening system for specimens  
277 with an FRP-strengthened web opening. For the two CFRP U-jackets, only the strains of one  
278 arm of the jackets were monitored using strain gauges by taking advantage of symmetry; a  
279 total of eight strain gauges were used, with four evenly distributed strain gauges vertically  
280 attached on each CFRP U-jacket (i.e., along the fibre direction of the CFRP). For the CFRP  
281 wrap on the web chord, the strains of three critical positions (i.e., the mid-span and the two  
282 ends of the web chord) were monitored using a total of 15 strain gauges, with five strain  
283 gauges on each critical position (two on the bottom surface of the chord, one on the side  
284 surface of the chord and two on the top surface of the chord), as shown in Fig. 9. The strain  
285 gauge on the side surface of the chord was applied at the mid-height of the chord and in the  
286 hoop direction of the CFRP wrap; one of the two strain gauges on the top/bottom surface of  
287 the chord was applied at the mid-width of the chord and in the hoop direction of the CFRP  
288 wrap, and the other one was also applied at the mid-width of the chord but in the longitudinal  
289 direction of the web chord.

290

291 All six beam specimens were tested under three-point negative bending with the test set-up  
292 shown in Fig. 10. The load was applied at the mid-span of the beam through a hydraulic jack.

### 293 **3. TEST RESULTS**

#### 294 **3.1 Failure mode**

295 The failure modes of all test specimens are shown in Fig. 11. For the two specimens with an  
296 un-strengthened web opening of small size (i.e., O-600×220 and O-700×200), the first crack  
297 appeared at the top-left corner of the web opening (i.e., the opening corner nearest to the

298 loading point) and extended diagonally towards the loading point (around 45 degrees with  
299 respect to the horizontal direction). Then a horizontal crack between the flange and the web  
300 appeared at the bottom-right corner of the web opening (i.e., the opening corner nearest to the  
301 right support). Afterwards, diagonal cracks (around 30 to 45 degrees with respect to the  
302 horizontal direction) occurred and further developed in the web chord, which finally  
303 dominated the failure of the specimens (Figs. 11a and b). It should be noted that the failure  
304 modes of specimens with an un-strengthened web opening of small size tested in the present  
305 study are quite different from the failure modes of specimens with an un-strengthened web  
306 opening of large size tested in the preliminary study (i.e., O-700×300 and O-800×280) [33],  
307 which were controlled by the combined local mixed flexural and shear actions at the right end  
308 of the flange chord as well as the left end of the web chord, and the local flexural failure (i.e.,  
309 crushing of concrete in compression) at the left end of the flange end as well as the right end  
310 of the web chord.

311

312 For the four specimens with an CFRP-strengthened web opening (two with a web opening of  
313 small size and two with a web opening of medium size), the existence of the CFRP wraps and  
314 CFRP U-jackets well prevented/mitigated the initiation/development of shear cracks in the  
315 web chord and the corners of the web opening. As can be seen from Figs. 11c-f, due to the  
316 presence of the web opening, the left ends of the flange and web chords were under a sagging  
317 moment while the right ends of the flange and web chords were under a hogging moment,  
318 which is quite different from the behaviour of RC T-section beams without a web opening.  
319 The final failure of all these four specimens was dominated by the flexural failure at the two  
320 ends of the flange chord as well as the web chord, with plastic hinges formed clearly at the  
321 two ends of the flange and web chords (Figs. 11c-f), which was similar to the failure modes  
322 of specimens with an FRP-strengthened web opening tested in the preliminary study [33].

### 323 **3.2 Load-deflection response of the beam**

324 Load-deflection curves of the test specimens are shown in Fig. 12, in which the horizontal  
325 axis shows the mid-span deflection, averaged from the readings of the three LVDTs 01, 02  
326 and 03 shown in Fig. 7. The key results (including cracking load, yield load and ultimate load

327 which is the maximum recorded load) are listed in Table 2. In the present study, numerical  
328 results of the control beams (i.e., rectangular and T-section beams without a web opening)  
329 obtained from finite element (FE) modelling were used for the comparisons of the test results.  
330 In the FE modelling, the concrete was modelled using the concrete damaged plasticity model  
331 available in ABAQUS [36], and the bond behaviour between concrete and internal steel  
332 reinforcements was properly considered. The accuracy of this FE model has been verified  
333 with the test results in the preliminary study [33]. The predicted load-deflection curves and  
334 key results (cracking load and yield load) of the two control beams (referred to as CB-Rec-2  
335 for rectangular control beam and CB-T-2 for T-section control beam respectively) obtained  
336 from the FE modelling are respectively shown in Fig. 12 and Table 2 for references. As can  
337 be seen from Fig. 12, due to the existence of a flange (i.e., cast-in-place floor slab in a real  
338 structure), Specimen CB-T-2 has much larger flexural capacity and stiffness than Specimen  
339 CB-Rec-2, indicating that the flange can significantly enhance the flexural capacity and  
340 stiffness of the beam in negative bending. Moreover, it should be noted that for all test  
341 specimens in this study, the yield strain of the bottom steel bars at the mid-span of the beam  
342 was not reached during the loading process. As a result, the yield load  $F_y$  for the control  
343 specimens (as listed in Table 2) cannot be obtained for RC beams with a web opening.  
344 Instead, the load corresponding to yielding of the bottom steel bars at the left end of the  
345 flange chord ( $F_{y1}$ ) and the load corresponding to yielding of the steel bars at the right end of  
346 the web chord ( $F_{y2}$ ) were obtained and listed in Table 2.

347

### 348 3.2.1 Specimens with a web opening of small size

349 The load-deflection curves of Specimens O-600×220 and O-700×200 having an  
350 un-strengthened web opening of small size are shown in Fig. 12a. The initial stiffness of  
351 Specimens O-600×220 and O-700×200 was similar to that of Specimen CB-Rec-2. After  
352 cracking of concrete, their stiffness decreased and was a little lower than that of CB-Rec-2.  
353 Shortly after yielding of the specimen, the load experienced an abrupt drop (around 30%-35%  
354 of the yield load) due to the brittle shear failure in the web chord and then gradually dropped  
355 to around half of the yield load. As shown in Table 2, the cracking loads of Specimens  
356 O-600×220 and O-700×200 were respectively around 160 % and 120% of that of Specimen

357 CB-Rec-2, the yield loads were respectively around 74% and 79% of that of Specimen  
358 CB-Rec-2, and the ultimate loads were respectively around 99% and 94% of that of  
359 Specimen CB-Rec-2.

360

361 With FRP strengthening (i.e., Specimens F-600×220 and F-700×200), the load did not  
362 experience a sudden drop after yielding of the specimens, revealing a significantly improved  
363 ductility of the specimens, as shown in Fig. 12a. As can be seen from Table 2, the cracking  
364 loads of Specimens F-600×220 and F-700×200 were both around 202% of the Specimen  
365 CB-Rec-2, the yielding loads were both around 89% of that of Specimen CB-Rec-2, and the  
366 ultimate loads were respectively around 121% and 128% of that of Specimen CB-Rec-2.

367

### 368 *3.2.2 Specimens with a web opening of medium size*

369 To further investigate the effect of web opening size on the behaviour of RC T-section beams,  
370 two specimens with an FRP-strengthened web opening of medium size (i.e., Specimens  
371 F-600×280 and F-700×260) were tested. It can be seen from Fig. 12b that the shapes of the  
372 load-deflection curves of Specimens F-600×280 and F-700×260 are quite similar to those of  
373 the two control specimens (i.e., CB-Rec-2 and CB-T-2). As shown in Table 2, the cracking  
374 loads of the two specimens were both 76 kN which were around 152% of that of Specimen  
375 CB-Rec-2, and the ultimate loads were respectively around 81% and 84% of that of  
376 Specimen CB-Rec-2.

## 377 **3.3 Deflection response of the web chord**

378 The vertical deflections of the web chord were measured using five evenly distributed  
379 LVDTs along the span of the web chord (i.e., LVDTs 09-13 in Fig. 7). The deflections of the  
380 web chords of the test specimens are plotted in Fig. 13. As can be seen from Fig. 13, for all  
381 the selected load levels, the distributions of deflections along the span of the web chord are  
382 nearly linear. As the failure was postponed by the FRP strengthening system, specimens with  
383 an FRP-strengthened web opening have a larger ultimate deflection than the corresponding  
384 specimens with an un-strengthened web opening. Moreover, it is interesting to notice that the  
385 specimens with a web opening of small size (i.e., Specimens O-700×200, F-700×200,

386 O-600×220 and F-600×220) only have downward deflections (i.e., negative values in the  
387 figures) of the web chord over its span, while in the deflected shapes of the web chord of the  
388 specimens with a web opening of medium size (i.e., Specimens F-700×260 and F-600×280),  
389 a zero-deflection point (where the deflection is equal to zero) can be found, with the  
390 deflections being upward (i.e., positive values in the figures) on the right part of the web  
391 chord (i.e., closer to the right support) while downward on the left part (i.e., closer to the  
392 loading point). Combining the test results of the preliminary study [33], a further  
393 investigation of these deflected shapes indicates that a larger length-to-height ratio of the web  
394 chord gives a higher possibility of the formation of zero-deflection point in the span of the  
395 web chord. Furthermore, the relative position of the zero-deflection point is also dependent  
396 on the length-to-height ratio of the web chord: a larger ratio gives a larger relative distance  
397 from the zero-deflection point to the right end of the web chord (defined as the distance from  
398 the zero-deflection point to the right end of the web chord divided by the total length of the  
399 web chord). This is because a larger length-to-height ratio of the web chord leads to a smaller  
400 stiffness of the web chord and thus a larger upward deflection of the right end of the web  
401 chord under hogging bending. For example, the relative distance from the zero-deflection  
402 point to the right end of the web chord of Specimen F-800×280 is 0.25 (i.e., 200 mm/800 mm)  
403 [33], which is larger than that of Specimen F-600×280 (i.e., 0.17 = 100 mm/600 mm). This is  
404 because the former specimen has a length-to-height ratio of the web chord of 6.7 (i.e., 800  
405 mm/120 mm), which is larger than that of the latter specimen (i.e., 5.0 = 600 mm/120 mm).

### 406 **3.4 Strains in the steel bars and FRP**

407 An examination of the readings of strain gauges on steel bars and FRP showed that the  
408 general feature of strain distribution and development is similar for all specimens tested in the  
409 present study. The strain distributions in the steel bars revealed that the left ends of the flange  
410 and web chords were under a sagging moment (i.e., the bottom surface of the chord was in  
411 tension and the top surface of the chord was in compression), while the right ends of the  
412 flange and web chords were under a hogging moment (i.e., the bottom surface of the chord  
413 was in compression and the top surface of the chord was in tension). For all test specimens in  
414 the present study, the bottom steel bars at the left end of the flange chord (i.e., the positions

415 where strain gauges B21-B26 in Fig. 8c installed) and the top steel bars at the right end of the  
416 web chord (i.e., the positions where strain gauges T41 and T42 in Fig. 8b installed) were all  
417 in tension and yielded during the loading process, while the steel bars at the other monitored  
418 positions (including the bottom steel bars at mid-span of the beam) did not yield, indicating  
419 that the failure of the beam was controlled by the failure of the chords.

420

421 The readings of the six longitudinal strain gauges on the FRP wrap (strain gauges WL1, WL2,  
422 WM1, WM2, WR1 and WR2 in Fig. 9) also showed that the bottom surface of the web chord  
423 at its left end (i.e., the position where strain gauge WL1 installed) and the top surface of the  
424 web chord at its right end (i.e., the position where strain gauge WR2 installed) were in  
425 tension, while the top surface of the web chord at its left end (i.e., the position where strain  
426 gauge WL2 installed) and the bottom surface of the web chord at its right end (i.e., the  
427 position where strain gauge WR1 installed) were in compression. Consequently, the hoop  
428 strains of the FRP wrap on top-left end of the web chord (i.e., the position where strain gauge  
429 WL5 in Fig. 9 installed) and the FRP wrap on bottom-right end of the web chord (i.e., the  
430 position where strain gauge WR3 in Fig. 9 installed) were both positive (i.e., the FRP was in  
431 tension), which was caused by the expansion of concrete due to the large compressive strain  
432 at these two positions. The readings of strain gauges WR3 and WL5 were both large  
433 [especially WR3, whose reading reached around  $8000 \mu\epsilon$ , exceeding half of the ultimate  
434 strain of the used CFRP (around  $12800\mu\epsilon$ )], indicating that the compressive concrete at the  
435 two ends of the web chord where plastic hinges formed was effectively confined by the FRP  
436 wrap.

#### 437 **4. EFFECT OF WEB OPENING SIZE**

438 From the above comparisons, it can be seen that a larger web opening unsurprisingly gives a  
439 lower load-carrying capacity and stiffness of the RC T-section beam. It can be found from Fig.  
440 12 and Table 2 that the reduction in the load-carrying capacity of the RC T-section beam  
441 caused by an increase of 100 mm in the web opening length is comparable to that caused by  
442 an increase of 20 mm in the web opening height (e.g., O-600×220 and O-700×200;

443 F-600×280 and F-700×260), which indicates that increasing the web opening height is more  
444 efficient than increasing the web opening length in reducing the load-carrying capacity of the  
445 RC T-section beam. Considering that the web opening height directly affects the height of the  
446 web chord, it can be reasonably deduced that the reduction in the load-carrying capacity of  
447 the RC T-section beam highly depends on the height of the web chord.

448

449 Moreover, the web opening size also affects the failure mode of the RC T-section beam. The  
450 RC T-section beams with an un-strengthened web opening of small size tested in the present  
451 study (i.e., O-600×220 and O-700×200) failed in a shear mode due to the formation of  
452 diagonal cracks in the web chord, while the failure of the RC T-section beams with an  
453 un-strengthened web opening of large size tested in the preliminary study (i.e., O-700×300  
454 and O-800×280) [33] were controlled by the local flexural failure or the local mixed failure  
455 (flexural and shear) at the two ends of the web and flange chords. The web opening size  
456 directly influences the size of the web chord, and therefore influences the flexural and shear  
457 capacities of the web chord. It can be reasonably inferred that if the shear capacity of the web  
458 chord is smaller than its flexural capacity, shear failure will occur in the web chord (e.g.,  
459 Specimens O-600×220 and O-700×200); while if the shear capacity of the web chord is  
460 larger than its flexural capacity, flexural failure will occur at the two ends of the web chord  
461 (e.g., Specimens F-600×220 and F-700×200). More studies, however, are needed to justify  
462 the above hypothesis.

## 463 5. EFFECT OF FRP STRENGTHENING

464 As can be seen from Figs. 11a-d, the existence of the FRP strengthening system which  
465 included CFRP U-jackets on the beam web with their ends anchored with the beam flange  
466 using spike anchors and CFRP wrap on the web chord contributed to changing the failure  
467 mode of the web opening-weakened RC T-section beam from shear failure in the web chord  
468 to flexural failure at the two ends of the web and flange chords. Moreover, it can be found  
469 from Fig. 12 that the adopted FRP strengthening system not only increased the stiffness and  
470 load-carrying capacity of the beam, but also enhanced the ductility of the beam significantly.

471 The performance enhancement of the RC T-section beam with a web opening due to the  
472 existence of the FRP strengthening system can be attributed to the following three reasons: (1)  
473 the CFRP wrap on the web chord can provide shear contribution to the web chord and thus  
474 enhance the load-carrying capacity of the beam; (2) the FRP U-jackets with spike anchors can  
475 restrict/mitigate the initiation/development of diagonal cracks at the opening corners and the  
476 horizontal cracks between the flange and the web, and therefore avoid the brittle behaviour of  
477 the beam caused by such cracks; and (3) the concrete in the web chord is effectively confined  
478 by the CFRP wrap and thus the compressive strength and ductility of the web chord can be  
479 enhanced significantly.

## 480 **6. ASSESSMENT OF THE EFFECTIVENESS OF BO TECHNIQUE**

481 As has been mentioned earlier, the proposed BO technique aims to reduce the SFC of the  
482 T-section beam to the desired value (i.e., the SFC of the corresponding rectangular beam). A  
483 strength model for RC beams with an FRP-strengthened web opening has been proposed by  
484 the author [37] based on the test results of the preliminary study [33]. In this section, the  
485 comparison of the strength of RC beams with an FRP-strengthened web opening between the  
486 prediction of the proposed model and the test results of present study will be made first to  
487 examine the accuracy of the proposed model. After further verification with the test results,  
488 the proposed model will be adopted to predict the positive flexural capacities of the  
489 specimens tested in this study and the effectiveness of the BO technique will be assessed  
490 through the comparison of SFCs of the beams.

### 491 **6.1 Comparison of beam strength between prediction and test**

492 In proposing the strength model [37], the top and the bottom chords which dominate the  
493 strength of RC beam with a web opening were isolated to form a free-body diagram (as  
494 shown in Fig. 14), based on which a series of force equilibrium equations can be set up.  
495 Through cross-sectional analyses, the simplified interaction diagrams between axial force ( $N$ )  
496 and bending moment ( $M$ ) (referred to as  $N$ - $M$  curves for simplicity) of the cross-sections at  
497 the two ends of the top and the bottom chords can be obtained, as shown in Fig. 15, in which

498 the equations of the four  $N-M$  curves are given. It should be noted that, if the top/bottom  
 499 chord is wrapped using FRP, the confinement effect from FRP to concrete should be properly  
 500 considered when calculating the  $N-M$  curves. The reader can refer to Ref. [37] for more  
 501 details. Combining the equations of the  $N-M$  curves with the force equilibrium equations, the  
 502 ultimate of the beam can be figured out, as expressed in Eq. (1).

$$503 \quad F = \frac{L}{L_{LS}} \frac{(b_{tL} + b_{bL})(z - a_{tR} - a_{bR}) + (b_{tR} + b_{bR})(z + a_{tL} + a_{bL})}{(z - a_{tR} - a_{bR})(L_R + l) - (z + a_{tL} + a_{bL})L_R} \quad (1)$$

504 where  $L$  is the clear span of the whole beam;  $L_{LS}$  is the left shear span of the beam;  $z$  is the  
 505 distance between the midlines of the top and the bottom chords;  $L_R$  is the distance between  
 506 the right end of the opening and the right support;  $l$  is the opening length;  $a_{tR}$ ,  $b_{tR}$ ,  $a_{tL}$ ,  $b_{tL}$ ,  
 507  $a_{bR}$ ,  $b_{bR}$ ,  $a_{bL}$  and  $b_{bL}$  are the coefficients of equations of the four  $N-M$  curves as shown in  
 508 Fig. 15. For more details, the reader can refer to Ref. [37].

509

510 The predicted ultimate loads of the four RC T-section beams with an FRP-strengthened web  
 511 opening are compared with test results in Table 3. It can be seen from Table 3 that the  
 512 strength model gives very close predictions to the test results, with an average  
 513 prediction-to-test ratio of 0.952, a standard deviation (STD) of 0.00778, and a coefficient of  
 514 variation (CoV) of 0.00817.

## 515 6.2 Comparison of SFCs

516 The SFCs of the two control specimens (i.e., CB-Rec-2 and CB-T-2) as well as the four  
 517 T-section beams with an FRP-strengthened web opening of small/medium size (600 mm ×  
 518 220 mm, 700 mm × 200 mm, 600 mm × 280 mm and 700 mm × 260 mm) are listed in Table  
 519 4. It should be noted that the negative and positive flexural capacities of the two control  
 520 specimens were obtained from the FE analyses, as has been explained earlier; the negative  
 521 flexural capacities of the four T-section beams with an FRP-strengthened web opening were  
 522 obtained from the tests; and the positive flexural capacities of the four T-section beams with  
 523 an FRP-strengthened web opening were obtained from the strength model.

524

525 As can be seen from Table 4, the SFC of Specimen CB-T-2 is 146% of that of the rectangular  
526 control beam CB-Rec-2, which indicates that the flange (i.e., the existence of a floor slab in a  
527 real structure) has a substantial effect on the SFC of the beam. With the presence of an  
528 FRP-strengthened web opening of medium size (600 mm × 280 mm or 700 mm × 260 mm),  
529 the SFC of the T-section beam can be reduced to around 86% of that of the control beam  
530 CB-Rec-2; while with the presence of an FRP-strengthened web opening of small size (600  
531 mm × 220 mm or 700 mm × 200 mm), the SFC of the T-section beam can be reduced to  
532 around 112% of that of the control beam CB-Rec-2. All these results indicate that the  
533 proposed BO technique is very effective in reducing the SFC of the T-section beam, and a  
534 web opening between the medium size and small size examined in this experimental study  
535 will be able to reduce the SFC of the T-section beam to the ideally desired value (i.e., the SFC  
536 of the corresponding rectangular beam). Moreover, the adopted FRP strengthening system in  
537 the present study including CFRP complete wrap on the web chord and CFRP U-jackets with  
538 spike anchors on the beam web can effectively prevent the web opening-weakened beam  
539 from failing in a brittle shear model, and significantly enhance the ductility of the beam.  
540 Therefore, this FRP strengthening system is necessary for the strengthening of web  
541 opening-weakened beams in practice.

## 542 **7. CONCLUDING REMARKS**

543 As the contribution of cast-in-place floor slabs to the flexural capacities of RC beams was not  
544 properly considered in the design based on previous codes, a large number of existing RC  
545 frames may violate the strong column-weak beam hierarchy. Based on the concept of  
546 Beam-end Weakening in combination with FRP Strengthening (BWFS) method, a novel  
547 seismic retrofit technique (BO technique) which involves the creation of a web opening in the  
548 T-section beam and the installation of FRP strengthening system around the opening was  
549 proposed. This paper first presents an experimental study on six large-scale RC T-section  
550 beams with a web opening of small/medium size to access the effectiveness of the BO  
551 technique in reducing the flexural capacity of the beam, then verifies the accuracy of the  
552 existing strength model for such FRP-strengthened RC beams with the test results, and finally

553 compares the SFCs between T-section beams and rectangular beams. Based on the  
554 experimental and theoretical studies, the following conclusions can be drawn:

555

556 1) The proposed BO technique can effectively reduce the SFC of the RC T-section beam  
557 and making a web opening in an existing RC beam (i.e., post-cut opening) was proved to  
558 be feasible. Therefore, the BO technique can be an effective approach to achieve the  
559 strong column-weak beam hierarchy in existing RC frames which originally violate such  
560 hierarchy;

561 2) A larger web opening usually leads to a larger reduction of SFC of the beam, and  
562 increasing the height of web opening was found to be more efficient in reducing the SFC  
563 of the beam than increasing the length of web opening. The comparison of SFCs of the  
564 test beams revealed that for beams in the present study, a web opening between the  
565 medium size and small size will be able to reduce the SFC of the T-section beam to the  
566 desired value (i.e., the SFC of the corresponding rectangular beam). The size of the web  
567 opening, which is required to perfectly reduce the SFC of the T-section beam to the  
568 desired value, can be designed using the proposed strength model through a trial and  
569 error progress;

570 3) The proposed FRP strengthening system, including CFRP U-jackets with spike anchors  
571 on the beam web and CFRP wrap on the web chord, is necessary for the BO technique,  
572 as it can not only increase the shear capacity and stiffness of the beam but also  
573 significantly enhance the ductility of the beam; and

574 4) The accuracy of the strength model proposed by the authors was further verified with the  
575 test results of RC beams with an FRP-strengthened web opening of medium/small sizes  
576 in the present study, indicating that the strength model can be used for the prediction of  
577 flexural capacity of such FRP-strengthened beams.

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## 585 **DATA AVAILABILITY**

586 The raw/processed data required to reproduce these findings cannot be shared at this time as  
587 the data also forms part of an ongoing study.

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Table 1. Specimen details

Specimen	Opening size		Web/flange chord height (mm)	FRP strengthening	Bending direction	Fabrication of web opening	Cylinder compressive strength of concrete $f_c$ (MPa)
	Length (mm)	Height (mm)					
O-600×220	600	220	180/100	No	Negative bending <sup>(a)</sup>	Post-cut	40.3
F-600×220				Yes	Negative bending	Post-cut	40.3
O-700×200	700	200	200/100	No	Negative bending	Pre-formed	36.2
F-700×200				Yes	Negative bending	Pre-formed	39.6
F-600×280	600	280	120/100	Yes	Negative bending	Post-cut	42.0
F-700×260	700	260	140/100	Yes	Negative bending	Pre-formed	42.0

Note: (a) The beam flange was in tension.

Table 2. Key results

Specimen	Cracking load $F_{cr}$ (kN)	Yield load $F_y$ (kN)	Yield load $F_{y1}^{(a)}$ (kN)	Yield load $F_{y2}^{(b)}$ (kN)	Ultimate load $F_u$ (kN)	Cracking load ratio <sup>(c)</sup> (%)	Ratio of yield load $F_{y1}^{(c)}$ (%)	Ultimate load ratio <sup>(c)</sup> (%)	Gain in flexural capacity due to CFRP (%)
CB-Rec-2 (FE)	50	320	/	/	320	/	/	/	/
CB-T-2 (FE)	146	500	/	/	500	/	/	/	/
O-600×220	80	/	238	316	316	160.0	74.4	98.8	/
F-600×220	101	/	284	NA <sup>(d)</sup>	388	202.0	88.8	121.3	24.0
O-700×200	60	/	253	291	300	120.0	79.1	93.8	/
F-700×200	101	/	284	NA <sup>(d)</sup>	410	202.0	88.8	128.1	31.3
F-600×280	76	/	NA <sup>(d)</sup>	211	260	152.0	NA <sup>(d)</sup>	81.3	/
F-700×260	76	/	196	199	270	152.0	61.3	84.4	/

Note:

- (a)  $F_{y1}$ = load at yielding of the bottom steel bars at the left end of flange chord;  
(b)  $F_{y2}$ = load at yielding of the top steel bars at the right end of web chord;  
(c) Ratio between web opening-weakened T-section beam and rectangular control beam;  
(d) The relevant strain gauge was damaged during loading.

Table 3. Verification of the proposed strength model [35]

Specimen	Test (kN)	Prediction (kN)	Prediction / Test
F-600×280	256	246	0.961
F-700×260	265	252	0.951
F-600×220	380	358	0.942
F-700×200	388	370	0.954
<b>Statistical characteristics</b>	<b>Average =</b>		0.952
	<b>STD =</b>		0.00778
	<b>CoV =</b>		0.00817

Table 4. Sum of negative and positive flexural capacities of test specimens

Specimen	Negative flexural capacity (kN)	Positive flexural capacity (kN)	Sum of flexural capacities (kN)	Ratio of sum between T-section beam and CB-Rec/ CB-Rec-2
CB-Rec-2	320 <sup>(a)</sup>	240 <sup>(a)</sup>	560	100%
CB-T-2	500 <sup>(a)</sup>	320 <sup>(a)</sup>	820	146%
T-section beam with an FRP-strengthened web opening of 600 mm × 280 mm	256 <sup>(b)</sup>	231 <sup>(c)</sup>	487	87.0%
T-section beam with an FRP-strengthened web opening of 700 mm × 260 mm	265 <sup>(b)</sup>	215 <sup>(c)</sup>	480	85.7%
T-section beam with an FRP-strengthened web opening of 600 mm × 220 mm	380 <sup>(b)</sup>	251 <sup>(c)</sup>	631	113%
T-section beam with an FRP-strengthened web opening of 700 mm × 200 mm	388 <sup>(b)</sup>	233 <sup>(c)</sup>	621	111%

Note:

- (a) Obtained from the FE analyses;
- (b) Obtained from the tests;
- (c) Obtained from the proposed strength model [35].

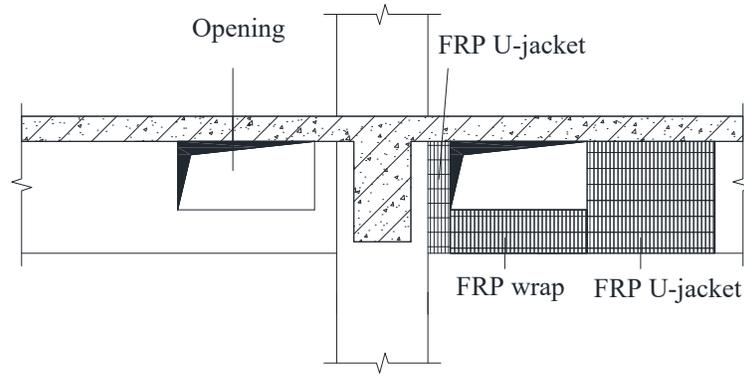
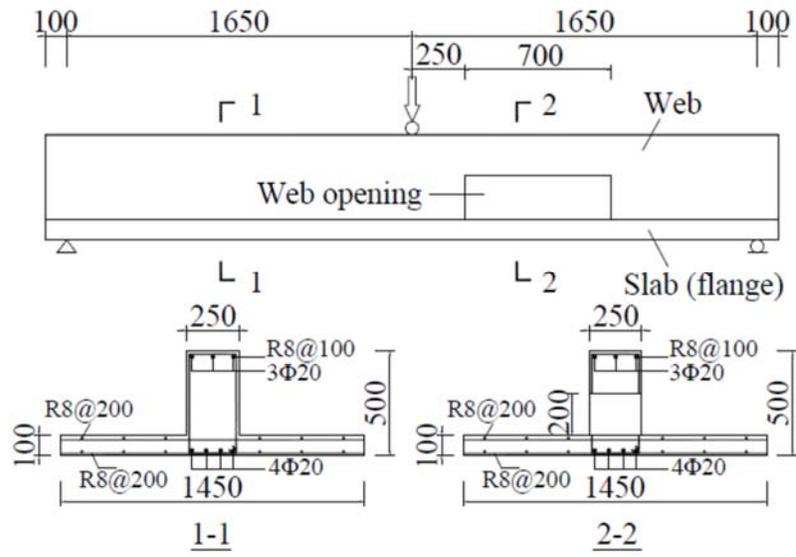


Figure 1. Beam opening (BO) technique



Note: R8-smooth steel bars of 8 mm in diameter; Φ20-deformed steel bars of 20 mm in diameter.

Figure 2. Details of test specimen (O-700x200) (dimensions in mm)



Figure 3. Making a pre-formed opening in an RC T-section beam



(a)



(b)

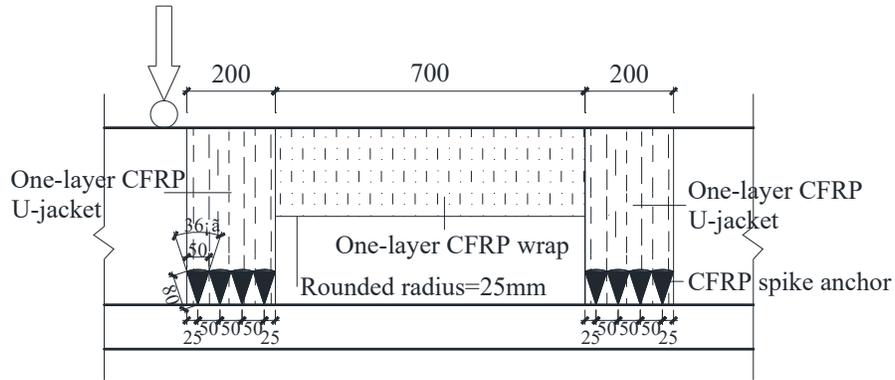


(c)

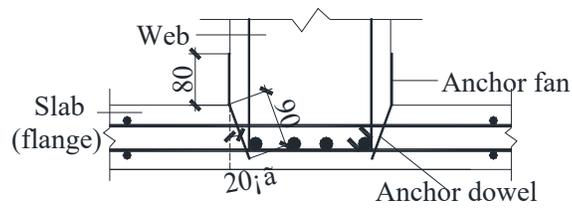


(d)

Figure 4. Making a post-cut opening in an RC T-section beam



(a) CFRP strengthening region



(b) CFRP spike anchors shown on the beam cross-section



(c) CFRP spike anchor

Figure 5. CFRP strengthening system (F-700×200) (dimensions in mm)



(a)



(b)



(c)



(d)

Figure 6. Installation of CFRP strengthening system

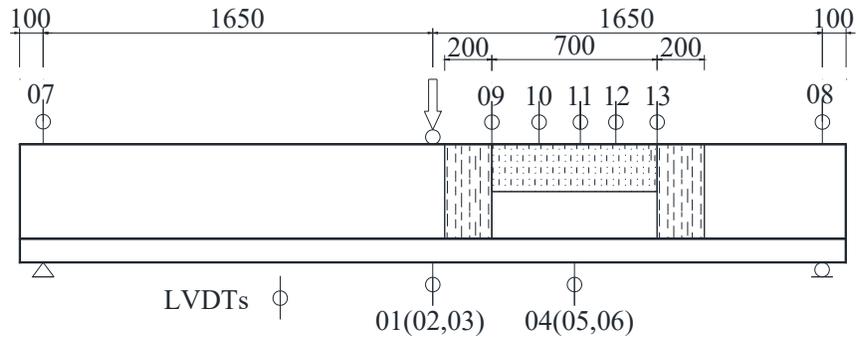
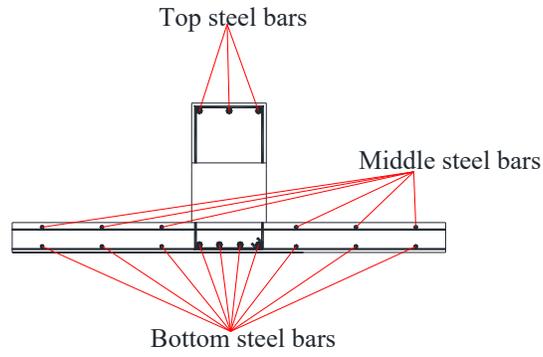
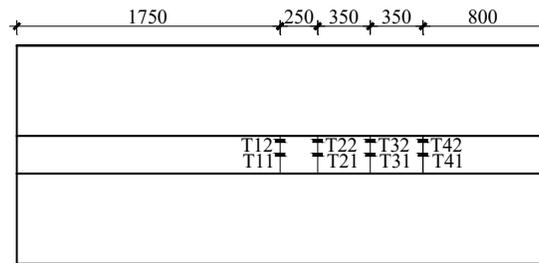


Figure 7. Layout of LVDTs (F-700×200) (dimensions in mm)



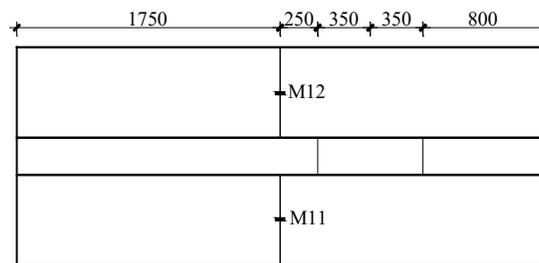
(a) Grouping of steel bars



(b) Strain gauges on top steel bars

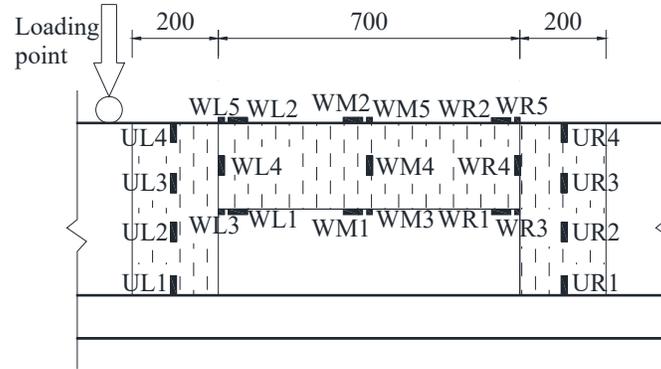


(c) Strain gauges on bottom steel bars



(d) Strain gauges on middle steel bars

Figure 8. Layout of strain gauges on steel bars (F-700×200) (dimensions in mm)



Note: L-left; M-middle; R-right; U-U-jacket; W-wrap; W\*1/2 (\*=L/M/R)-strain gauges in the longitudinal direction of the web chord, with 1 representing the strain gauge on the bottom surface of the web chord, and 2 representing the strain gauge on the top surface of the web chord; W\*3/4 (\*=L/M/R)-strain gauges in the hoop direction of the FRP wrap, with 3 representing the strain gauge on the bottom surface of the web chord, 4 representing the strain gauge on the side surface of the web chord, and 5 representing the strain gauge on the top surface of the web chord.

Figure 9. Layout of strain gauges on FRP (F-700×200) (dimensions in mm)



Figure 10. Test set-up



(a) O-600×220



(b) O-700×200



(c) F-600×220



(d) F-700×200

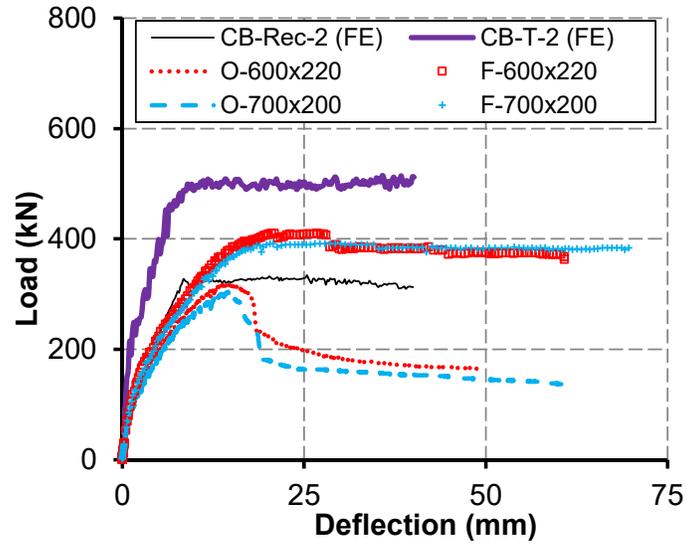


(e) F-600×280

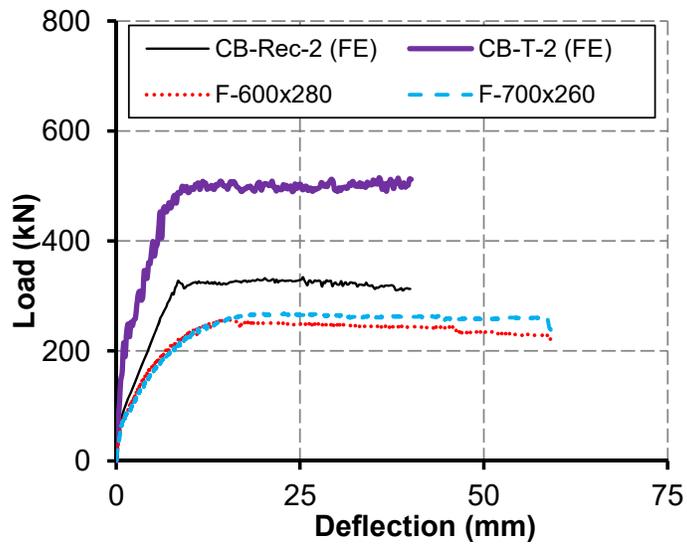


(f) F-700×260

Figure 11. Failure modes of test specimens

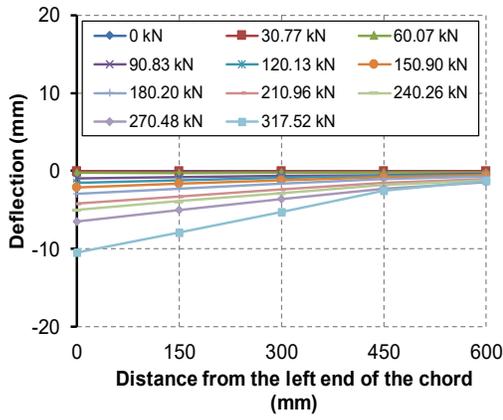


(a) Specimens with a small web opening

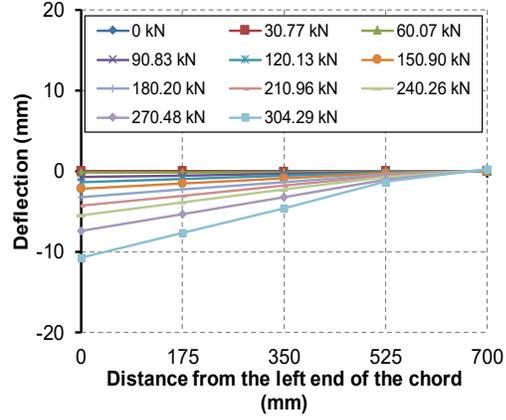


(b) Specimens with a medium web opening

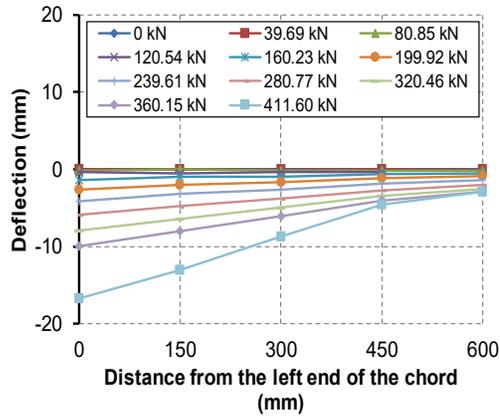
Figure 12. Load-deflection curves of test specimens



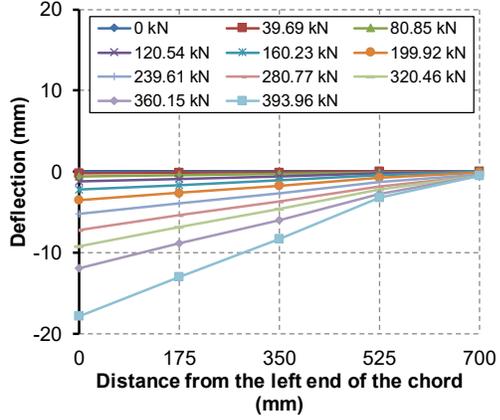
(a) O-600×220



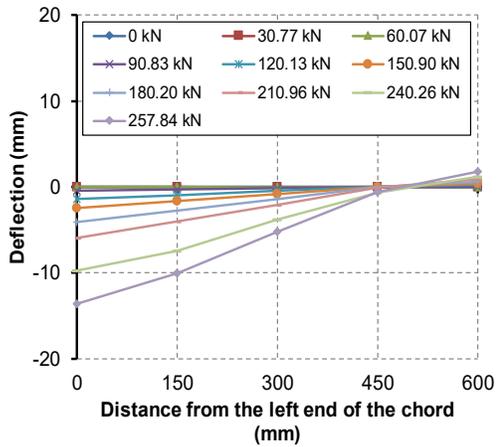
(b) O-700×200



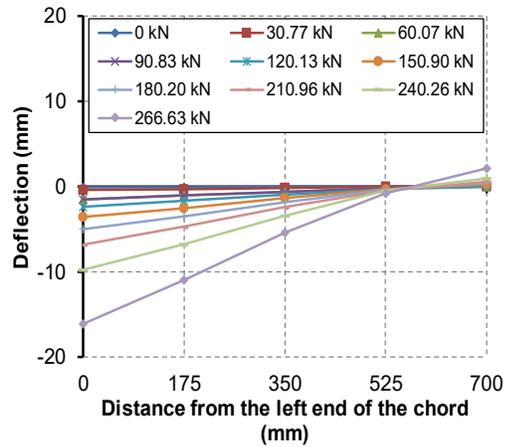
(c) F-600×220



(d) F-700×200



(e) F-600×280



(f) F-700×260

Figure 13. Deflection of the web chord

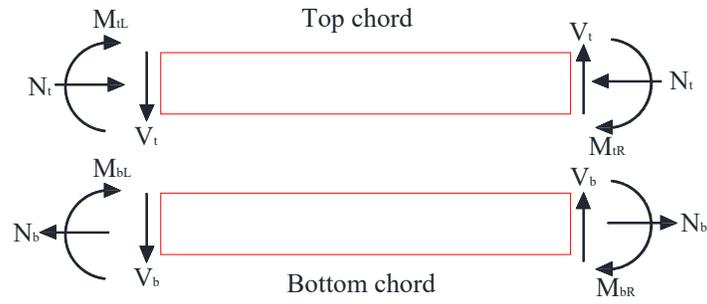


Figure 14. Free-body diagram of the chords

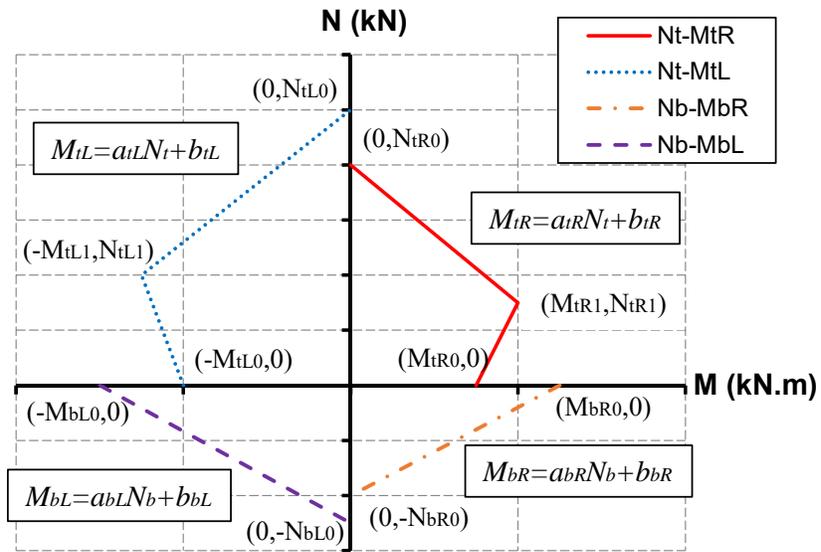


Figure 15. Simplified  $N$ - $M$  curves of the chords