

1           **Analyzing freeway crash severity using a Bayesian spatial**  
2           **generalized ordered logit model with conditional autoregressive**  
3           **priors**  
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36

37 **ABSTRACT**

38 This study develops a Bayesian spatial generalized ordered logit model with conditional  
39 autoregressive priors to examine severity of freeway crashes. Our model can  
40 simultaneously account for the ordered nature in discrete crash severity levels and the  
41 spatial correlation among adjacent crashes without fixing the thresholds between crash  
42 severity levels. The crash data from Kaiyang Freeway, China in 2014 are collected for  
43 the analysis, where crash severity levels are defined considering the combination of  
44 injury severity, financial loss, and numbers of injuries and deaths. We calibrate the  
45 proposed spatial model and compare it with a traditional generalized ordered logit  
46 model via Bayesian inference. The superiority of the spatial model is indicated by its  
47 better model fit and the statistical significance of the spatial term. Estimation results  
48 show that driver type, season, traffic volume and composition, response time for  
49 emergency medical services, and crash type have significant effects on crash severity  
50 propensity. In addition, vehicle type, season, time of day, weather condition, vertical  
51 grade, bridge, traffic volume and composition, and crash type have significant impacts  
52 on the threshold between median and severe crash levels. The average marginal effects  
53 of the contributing factors on each crash severity level are also calculated. Based on the  
54 estimation results, several countermeasures regarding driver education, traffic rule  
55 enforcement, vehicle and roadway engineering, and emergency services are proposed  
56 to mitigate freeway crash severity.

57 *Keywords:* Freeway safety; Crash severity; Spatial correlation; Bayesian spatial

58 generalized ordered logit model; Conditional autoregressive prior.

59 **1. INTRODUCTION**

60 Roadway traffic crashes result in over 1.2 million fatalities and up to 50 million non-  
61 fatal injuries annually in the world, as well as an average global GDP loss of 3% ([World  
62 Health Organization, 2015](#)). To mitigate the enormous economic and emotional burden  
63 imposed on society by traffic crashes, a great number of efforts have been devoted to  
64 reducing the frequency of traffic crashes and alleviating their severity levels  
65 ([Mannering and Bhat, 2014](#)). Developing effective countermeasures for these purposes  
66 requires a comprehensive understanding of the factors contributing to the risk and  
67 severity of potential crashes. To this end, statistical models are often developed using  
68 historical crash data to establish an explicit relationship between crash frequency or  
69 severity and the factors pertaining to road users, vehicles, roadway infrastructure, traffic  
70 and weather conditions, level of emergency medical services (EMS), etc.

71 Traffic safety issues have long been a primary concern for freeway management  
72 agencies and researchers ([Ahmed et al., 2011](#); [Ma et al., 2015, 2017](#); [Wen et al., 2018](#);  
73 [Yu and Abdel-Aty, 2014](#); [Yu et al., 2013](#); [Zeng et al., 2017a](#)). Most studies in this realm  
74 have focused on analyzing freeway crash frequencies, while crash severity has not  
75 received due attention to our best knowledge. Compared with other types of roadways  
76 (such as urban roads), crash rate in freeways may be lower due to the high-standard  
77 design, construction and maintenance of freeway infrastructures, and the simpler traffic  
78 environment (for example, no junction is present in freeway systems; see [Milton and  
79 Mannering, 1998](#), and [Zeng et al., 2018a](#)). On the other hand, freeway crashes tend to

80 have more severe outcomes, probably because of the higher vehicle speeds and the  
81 greater proportion of heavy vehicles. Freeway usually ranks the first among all roadway  
82 types in terms of the fatality rate. According to the statistics from the Traffic  
83 Management Bureau of Public Security Ministry in China, freeway crashes account for  
84 only 5% of roadway crashes, while the fatalities resulting from freeway crashes account  
85 for about 10% of the total deaths in roadway crashes. In 2015, about one-third of the  
86 major roadway crashes involving ten or more fatalities in China have occurred on  
87 freeways. Therefore, a crash severity analysis is fully merited, which may suggest  
88 proper countermeasures for reducing the number of fatalities, degree of injuries, and  
89 amount of property loss in freeway crashes.

90 In previous studies on crash severity analysis, crash severity is usually measured by  
91 the most severe injury sustained by all the crash-involved road users ([Mannering and](#)  
92 [Bhat, 2014](#)). Despite its popularity, the most severe injury cannot represent all the  
93 adverse outcomes of traffic crashes. In China, police administration categorizes  
94 roadway crashes into four severity levels, namely the light crashes, medium crashes,  
95 severe crashes, and very severe crashes. These levels are defined by taking into account  
96 not only the injury severity, but also the amount of property damage and the number of  
97 people injured or killed. These levels construct a more comprehensive metric for crash  
98 severity. However, studies that use such metrics of crash severity are rare.

99 Due to the discrete nature of crash severity metric, discrete outcome models (such  
100 as logit and probit models) are usually developed to link crash severity to the observed

101 risk factors. When the number of crash severity levels is greater than two, the ordered  
102 nature between these levels is a most important inherent characteristic. Ordered  
103 outcome models have a potential advantage over unordered outcome models (e.g.,  
104 multinomial logit or probit models), because they can account for the correlation among  
105 neighboring severity levels by recognizing the ordered nature (Savolainen et al., 2011).  
106 In standard ordered logit and probit models, the latent propensity is specified as a linear  
107 function of the observed risk factors and is mapped to the observed severity levels  
108 defined by a set of fixed thresholds (Abdel-Aty, 2003). As illustrated by Eluru et al.  
109 (2008), however, the fixed thresholds may result in biased estimates for the factors'  
110 effects on the likelihood of certain severity levels. To address this issue, generalized  
111 ordered response models have been proposed, which allow the thresholds to vary with  
112 the observed explanatory variables.

113 Unobserved heterogeneity is another significant issue that is often associated with  
114 crash severity analysis (Mannering et al., 2016). This issue is often addressed using  
115 random-parameters models (Chen et al., 2018; Ma et al., 2018; Milton et al., 2008),  
116 Markov switching approaches (Malyskhina and Mannering, 2009), latent class/finite  
117 mixture methods (Yasmin et al., 2014) and combinations of the above methods (Xiong  
118 and Mannering, 2013; Xiong et al., 2014). Under the ordered response model  
119 framework, mixed (random-parameters) generalized ordered response model and its  
120 variants are developed to handle the ordered nature and unobserved heterogeneity  
121 simultaneously (Balusu et al., 2018; Eluru et al., 2008; Fountas and Anastasopoulos,

122 [2017; Fountas et al., 2018; Xin et al., 2017; Yasmin et al., 2015a](#)). To be sure,  
123 sometimes no explanatory variables were found to have significant heterogeneous  
124 effects, and thus the estimated mixed generalized ordered response model becomes a  
125 (fixed-parameters) generalized ordered response model ([Castro et al., 2013; Eluru et al.,](#)  
126 [2008](#)). Therefore, the latter has been employed in a number of recent studies under such  
127 conditions ([Abegaz et al., 2014; Eluru, 2013; Eluru and Yasmin, 2015; Kaplan and](#)  
128 [Prato, 2012; Yasmin et al., 2015b](#)). Please refer to [Savolainen et al. \(2011\)](#) and  
129 [Mannering and Bhat \(2014\)](#) for more detailed description and assessments on the  
130 methodological alternatives.

131 While the continual advances in analytical methods have enabled us to more  
132 precisely assess the impacts of observed factors on crash severity, some critical issues  
133 still remain unsolved in the present crash severity prediction models. As a result, the  
134 validity of inference results may be significantly undermined. Typically, the spatial  
135 correlation (also termed “spatial dependency” and “spatial effect”) among adjacent  
136 crashes, which has been commonly recognized in the analysis of crash frequencies and  
137 rates ([Huang et al., 2016b; Ma et al., 2017; Quddus, 2008; Zeng and Huang, 2014a;](#)  
138 [Zeng et al., 2017b; Zeng et al., 2018b](#)), is by-and-large overlooked when modeling crash  
139 severity. In the few studies that modeled spatial correlations between crash severities,  
140 some researchers have formulated the spatial correlation using the spatial lag structure  
141 or a mixed structure of spatial lags and spatial errors ([Bhat et al., 2017; Castro et al.,](#)  
142 [2013; Prato et al., 2018; Zou et al., 2017](#)), while others have employed a conditional

143 autoregressive (CAR) prior to capture the spatial correlation between the injury  
144 severities of crashes occurring at adjacent locations (Meng et al. 2017; Xu et al., 2016).  
145 Quddus (2008) compared these two methods in the context of Bayesian inference and  
146 found that the CAR prior models yielded more trustworthy estimation results than the  
147 models using spatial lag or spatial error structure. The multivariate CAR model is also  
148 a state-of-the-art method for multivariate spatial modeling in traffic safety analysis  
149 (Barua et al., 2014, 2016; Cai et al., 2018; Huang et al., 2017; Liu and Sharma, 2018;  
150 Ma et al., 2017; Osama and Sayed, 2017). The empirical analyses conducted by Meng  
151 et al. (2017) and Xu et al., (2016) have further demonstrated the strength of CAR prior  
152 method used in the spatial models of crash severity. However, the binary logistic  
153 regression models proposed in the above-cited works cannot capture the ordered nature  
154 in crash data.

155 In light of the above, this paper examines the freeway crash severity in China using  
156 a Bayesian spatial generalized ordered logit model with CAR priors, which can account  
157 for the ordered nature of crash severity levels and the spatial correlation among crashes  
158 simultaneously, without being limited by fixed thresholds. A one-year crash dataset  
159 from the Kaiyang Freeway in Guangdong Province, China is used for the empirical  
160 investigation. To demonstrate the advantage of the proposed model, we compare the  
161 estimation results against those of a traditional generalized ordered logit model.

162 The rest of the article is structured as follows. Section 2 describes the freeway crash  
163 dataset. Section 3 furnishes the formulations of the traditional generalized ordered logit



164 model and the proposed model. In Section 4, we present the Bayesian estimation  
165 processes for the two generalized ordered logit models, compare their estimation results,  
166 and examine the marginal effects of significant factors. Conclusions and directions for  
167 future research are discussed in Section 5.

168

## 169 **2. DATA PREPARATION**

170 We use the crash data from the Kaiyang Freeway in 2014, which was extracted from  
171 the Highway Maintenance and Administration Management System maintained by  
172 Guangdong Transportation Group. The four crash severity levels used in the data are  
173 defined by the Ministry of Public Security in China as follows:

174 (1) a *light crash* refers to one resulting in no more than two people slightly injured,  
175 or a property damage value of no more than 1,000 CNY;

176 (2) a *medium crash* refers to one resulting in one or two people severely injured, or  
177 more than two people slightly injured, or a property damage value between 1,000 and  
178 30,000 CNY;

179 (3) a *severe crash* refers to one resulting in one or two fatalities, or three to ten  
180 people severely injured, or a property damage value between 30,000 and 60,000 CNY;  
181 and

182 (4) a *very severe crash* refers to one resulting in three or more fatalities, or over ten  
183 people severely injured, or one fatality plus over eight people severely injured, or two  
184 fatalities plus over five people severely injured, or a property damage value of over

185 60,000 CNY.

186 Among all the 691 freeway crashes reported in 2014, there are 355 light crashes  
187 (51.4%), 307 medium crashes (44.4%), 28 severe crashes (4.1%), and only one very  
188 severe crash (0.1%). We thus combine the severe and very severe crashes into one level  
189 in this paper because the latter is rare in reality. In the rest of this paper, this combined  
190 level will be termed as “severe crash”.

191 The crash data recorded in the system also include: whether the involved driver(s)  
192 are professional or not, the involved vehicles’ types and license numbers, weather  
193 condition, the EMS response time, and the crash type, time and location. Some of these  
194 variables are explained next. The binary driver type variable, *Professional driver*, is  
195 equal to 1 if at least one driver involved is professional, and 0 otherwise. Four additional  
196 binary variables are used to represent vehicle types: (1) *Passenger car* indicates  
197 whether all the vehicle(s) involved in a crash are passenger car(s); (2) *Coach* indicates  
198 whether at least one coach was involved; (3) *Truck* indicates whether at least one truck  
199 was involved; and (4) *Other vehicle* indicates whether at least a vehicle of other types  
200 (e.g., a vehicle with trailer) was involved. The binary variable *Non-local vehicle*  
201 indicates whether there is a non-local vehicle (i.e. not registered in Guangdong Province)  
202 involved in a crash. The EMS response time is defined as the duration between the crash  
203 reporting and the arrival of EMS at the crash site.

204 More details on the freeway design features at crash locations are extracted from  
205 the freeway’s geometric profile. These include: horizontal curvature, vertical grade, and

206 whether the crash location is on a bridge or near a ramp. To examine the spatial  
 207 correlation in the crashes, we further divide the Kaiyang Freeway into 154 segments in  
 208 a way such that each segment is approximately linear both horizontally and vertically.  
 209 The same segmentation of this freeway has also been used in previous studies on crash  
 210 frequency analysis (Wen et al., 2018; Zeng et al., 2017a).

211 Regarding traffic data, we use the five vehicle classes defined by the Guangdong  
 212 Freeway Network Toll System with respect to vehicles' head height, axis number, wheel  
 213 number, and wheelbase; see Table 1 for the details. We calculate the normalized daily  
 214 traffic volumes of each vehicle class as its daily traffic volumes (which are collected  
 215 from the system) multiplied by a specific weight. The weights for classes 1 to 5 are set  
 216 to 1, 1.5, 2, 3 and 3.5, respectively, as recommended by the Guangdong Transportation  
 217 Department. The percentage of each vehicle class is then calculated using the  
 218 normalized traffic volumes. Note that traffic data in finer scales (e.g., hourly volumes)  
 219 are unavailable. However, we believe the daily volume data serve as a fairly good proxy  
 220 for the real-time traffic characteristics when and where crashes occurred.

221

222 **Table 1** Vehicle classification

Class	Criteria				Representative vehicle types
	Head height	Axis number	Wheel number	Wheelbase	
1	<1.3m	2	2-4	<3.2m	Passenger car, jeep, pickup truck
2	≥1.3m	2	4	≥3.2m	Minibus, minivan, light truck
3	≥1.3m	2	6	≥3.2m	Medium-sized bus, large ordinary

					bus, medium-sized truck
4	$\geq 1.3\text{m}$	3	6-10	$\geq 3.2\text{m}$	Large luxury bus, large truck, large trailer, 20-foot container truck
5	$\geq 1.3\text{m}$	$>3$	$>10$	$\geq 3.2\text{m}$	Heavy truck, heavy trailer, 40-foot container truck

223

224 **Table 2** presents the definitions of the covariates used for analyzing freeway crash  
225 severity and their descriptive statistics. The Pearson correlation test results calculated  
226 by Statistical Package for the Social Sciences (SPSS) (IBM, 2017) suggest that *Veh\_4*  
227 and *Veh\_5*, i.e., the proportions of vehicles in classes 4 and 5 as defined in **Table 1**, are  
228 significantly correlated with a correlation coefficient greater than 0.6. With two highly-  
229 correlated risk factors, estimates of their effects may be biased. Hence, we remove  
230 *Veh\_5* from the set of risk factors to eliminate the significant correlation between factors.

231

232 **Table 2** Descriptive statistics of covariates for analyzing freeway crash severity

Covariates	Description	Mean	S.D.
<i>Professional driver</i>	All drivers involved are non-professional = 0; otherwise = 1	0.025	0.155
<i>Traffic volume</i>	The normalized daily traffic volume in the day of crash ( $10^3 \text{pcu}^\dagger$ )	5.655	1.071
<i>EMS response time</i>	Duration between crash reporting and the arrival of EMS (min)	20.7	18.0
TRAFFIC COMPOSITION			
<i>Veh_1*</i>	The percentage of vehicles in class 1	42.2	12.2
<i>Veh_2</i>	The percentage of vehicles in class 2	2.5	0.7
<i>Veh_3</i>	The percentage of vehicles in class 3	21.3	3.3
<i>Veh_4</i>	The percentage of vehicles in class 4	6.1	2.1
<i>Veh_5</i>	The percentage of vehicles in class 5	27.9	9.7
VEHICLE TYPE			
<i>Passenger car*</i>	All vehicles involved are passenger cars = 1; otherwise = 0	0.571	0.495
<i>Coach</i>	At least one coach was involved = 1; otherwise = 0	0.072	0.259
<i>Truck</i>	At least one truck was involved = 1; otherwise = 0	0.324	0.468
<i>Other vehicle</i>	At least one other vehicle (e.g., a vehicle with trailer) was involved = 1; otherwise = 0	0.077	0.266

<i>Non-local vehicle</i>	All vehicles involved were registered in Guangdong Province (local vehicles) = 0; otherwise (at least one non-local vehicle was involved) = 1	0.27	0.443
<b>WEATHER CONDITION</b>			
<i>Sunny*</i>	Crash occurred in a sunny day = 1; otherwise = 0	0.707	0.456
<i>Overcast</i>	Crash occurred in an overcast day = 1; otherwise = 0	0.111	0.315
<i>Rainy/Foggy</i>	Crash occurred in a rainy or foggy day = 1; otherwise = 0	0.182	0.386
<b>CRASH TYPE</b>			
<i>Single-vehicle crash*</i>	The crash involved only one vehicle = 1; otherwise = 0	0.444	0.497
<i>Rear-end crash</i>	The crash is a rear-end one = 1; otherwise = 0	0.259	0.438
<i>Angle crash</i>	The crash is an angle one = 1; otherwise = 0	0.298	0.458
<b>SEASON</b>			
<i>Spring</i>	Crash occurred in February to April = 1; otherwise = 0	0.250	0.434
<i>Summer</i>	Crash occurred in May to July = 1; otherwise = 0	0.263	0.441
<i>Autumn</i>	Crash occurred in August to October = 1; otherwise = 0	0.284	0.451
<i>Winter*</i>	Crash occurred in November, December or January = 1; otherwise = 0	0.203	0.402
<i>Day of week</i>	Crash occurred on a weekend = 1; otherwise = 0	0.331	0.471
<b>TIME OF DAY</b>			
<i>Before dawn*</i>	Crash occurred during 0 to 6 a.m. = 1; otherwise = 0	0.224	0.417
<i>Morning</i>	Crash occurred during 6 a.m. to 12 p.m. = 1; otherwise = 0	0.392	0.489
<i>Afternoon</i>	Crash occurred during 12 to 6 p.m. = 1; otherwise = 0	0.207	0.405
<i>Evening</i>	Crash occurred during 6 p.m. to 12 a.m. = 1; otherwise = 0	0.178	0.383
<b>ROADWAY GEOMETRY</b>			
<i>Horizontal curvature</i>	The horizontal curvature of the freeway segment where the crash occurred ( $0.1 \text{ km}^{-1}$ )	1.888	1.222
<i>Vertical grade</i>	The grade of the freeway segment where the crash occurred (%)	0.768	0.664
<i>Bridge</i>	Crash occurred on a bridge = 1; otherwise = 0	0.570	0.495
<i>Ramp</i>	Crash occurred in the proximity of a ramp = 1; otherwise = 0	0.236	0.425

233 <sup>‡</sup> pcu: passenger car unit.

234 \* The reference category.

235

### 236 3. MODEL FORMULATION

237 The crash severity levels are ordered by nature. For discrete outcome models with more  
238 than two outcomes, the ordered nature of the outcomes is often incorporated in the  
239 model to identify the correlation between adjacent outcomes (Savolainen et al., 2011).

240 In this section, we present the traditional generalized ordered logit model and a new

241 statistical model, termed “the spatial generalized ordered logit model”, that can capture  
 242 the spatial correlation among the crashes (Section 3.1). We then describe the method  
 243 for calculating the effects of contributing factors on the probability of each crash  
 244 severity level (Section 3.2).

245

### 246 **3.1. Model Specification**

#### 247 *3.1.1. The traditional generalized ordered logit model*

248 Generalized ordered logit models are often used for capturing the ordered nature in  
 249 crash severity without suffering from the biases resulting from fixed thresholds (Eluru,  
 250 2013). Specifically, a latent propensity variable  $z_i$  is used as a basis for modeling the  
 251 ordered ranking of severity levels for crash  $i$ , and is assumed to be a linear function of  
 252 the covariates  $\mathbf{X}_i$ :

$$253 \quad z_i = \boldsymbol{\beta}\mathbf{X}_i + \varepsilon_i. \quad (1)$$

254 where  $\boldsymbol{\beta}$  is a vector of estimable parameters associated with the covariate vector  
 255 (including a constant element),  $\mathbf{X}_i$ ; and  $\varepsilon_i$  is a residual term following a logistic  
 256 distribution.

257 The severity level  $y_i$  of crash  $i$  is defined as follows:

$$258 \quad y_i = \begin{cases} 1, & z_i \leq \mu_{i,0} \\ 2, & \mu_{i,0} < z_i \leq \mu_{i,1} \\ \vdots & \\ j, & \mu_{i,j-2} < z_i \leq \mu_{i,j-1} \\ \vdots & \\ J, & z_i > \mu_{i,J-2} \end{cases} \quad (2)$$

259 where  $j \in \{1, 2, \dots, J\}$  represents an ordered severity level, numbered from the lowest

260 (i.e., light crashes in the present paper) to the highest (i.e., severe crashes). The  
 261 thresholds  $\mu_{i,0}, \mu_{i,1}, \dots, \mu_{i,J-2}$  denote the boundaries between these severity levels for  
 262 crash  $i$ . To increase flexibility in assessing the covariates' effects, these thresholds are  
 263 written in the following parametric form as proposed by [Eluru et al. \(2008\)](#):

$$264 \quad \mu_{i,k} = \mu_{i,k-1} + \exp(\alpha_k \mathbf{Z}_{i,k}), \forall k \in \{1, \dots, J-2\}, \quad (3)$$

265 where  $\mathbf{Z}_{i,k}$  is a vector of explanatory variables associated with the  $k$ th threshold (also  
 266 including a constant element) and  $\alpha_k$  is a parameter vector to be estimated. For the  
 267 uniqueness of identification, either the constant term in the latent propensity function  
 268 or the first threshold  $\mu_{i,0}$  must be fixed to zero. Here we specify  $\mu_{i,0}$  (i.e. the  
 269 threshold between light and medium crash levels) as 0 for all crashes and keep the  
 270 constant term in the latent propensity function. Hence, in this paper only one threshold  
 271 parameter vector  $\alpha_1$  (for the threshold between medium and severe crash levels,  $\mu_{i,1}$ )  
 272 needs to be estimated.

273 Since the residual term  $\varepsilon_i$  is logistically distributed, the cumulative probability for  
 274 crash  $i$  to exhibit a severity level up to  $j$ ,  $P_{i,j}$ , can be calculated as:

$$275 \quad P_{i,1} = \frac{\exp(\mu_0 - \beta \mathbf{X}_i)}{1 + \exp(\mu_0 - \beta \mathbf{X}_i)} = \frac{\exp(-\beta \mathbf{X}_i)}{1 + \exp(-\beta \mathbf{X}_i)}, \quad (4)$$

$$276 \quad P_{i,j} = \frac{\exp(\mu_{j-1} - \beta \mathbf{X}_i)}{1 + \exp(\mu_{j-1} - \beta \mathbf{X}_i)} = \frac{\exp[\sum_{k=1}^{j-1} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i]}{1 + \exp[\sum_{k=1}^{j-1} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i]}, \forall j \in \{2, \dots, J-1\}, \quad (5)$$

$$277 \quad P_{i,J} = 1. \quad (6)$$

278 Thus, the probability for crash  $i$  to exhibit a severity level  $j$ ,  $p_{i,j}$ , is calculated as:

$$279 \quad p_{i,1} = P_{i,1} = \frac{\exp(\mu_0 - \beta \mathbf{X}_i)}{1 + \exp(\mu_0 - \beta \mathbf{X}_i)} = \frac{\exp(-\beta \mathbf{X}_i)}{1 + \exp(-\beta \mathbf{X}_i)}, \quad (7)$$

$$280 \quad p_{i,j} = P_{i,j} - P_{i,j-1} = \frac{\exp(-\beta \mathbf{X}_i) [\exp(\mu_{j-1}) - \exp(\mu_{j-2})]}{[1 + \exp(\mu_{j-1} - \beta \mathbf{X}_i)] [1 + \exp(\mu_{j-2} - \beta \mathbf{X}_i)]} =$$

281 
$$\frac{\exp(-\beta \mathbf{X}_i) \exp\left[\sum_{k=1}^{j-2} \exp(\alpha_k \mathbf{Z}_{i,k})\right] \{\exp[\exp(\alpha_{j-1} \mathbf{Z}_{i,j-1})] - 1\}}{\{1 + \exp\left[\sum_{k=1}^{j-1} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i\right]\} \{1 + \exp\left[\sum_{k=1}^{j-2} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i\right]\}}, \forall j \in \{2, \dots, J-1\}, \quad (8)$$

282 
$$p_{i,J} = 1 - P_{i,J-1} = \frac{1}{1 + \exp\left[\sum_{k=1}^{J-2} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i\right]}. \quad (9)$$

283

### 284 3.1.2. The spatial generalized ordered logit model

285 As shown by Meng et al. (2017) and Xu et al. (2016), the spatial correlation among the  
 286 severity levels of adjacent crashes can be captured by residual terms with Gaussian  
 287 CAR prior. Specifically, for crash  $i$  occurring on freeway segment  $m$ , the latent  
 288 variable  $z_i$  in Eq. (1) is modified to:

289 
$$z_i = \beta \mathbf{X}_i + \phi_m + \varepsilon_i, \quad (10)$$

290 where the residual term  $\phi_m$  denotes the spatial correlation of each crash on freeway  
 291 segment  $m$ , and is assumed to follow a CAR Gaussian distribution:

292 
$$\phi_m \sim N\left(\frac{\sum_{n \neq m} \phi_n \omega_{mn}}{\sum_{n \neq m} \omega_{mn}}, \frac{\sigma_\phi}{\sum_{n \neq m} \omega_{mn}}\right), \quad (11)$$

293 where  $\omega_{mn}$  is the proximity weight between freeway segments  $m$  and  $n$ . The binary  
 294 first-order proximity structure, which has been extensively used in previous studies  
 295 (Meng et al. 2017; Xu et al., 2016; Zeng and Huang, 2014a), is employed to define  
 296 these proximity weights. Specifically, if segments  $m$  and  $n$  are connected,  $\omega_{mn} =$   
 297 1; otherwise,  $\omega_{mn} = 0$ . The  $\sigma_\phi (> 0)$  is the variance parameter of the spatial  
 298 correlation term.

299 Consequently, the probability for crash  $i$  to exhibit a severity level  $j$  is calculated  
 300 as:

301 
$$p_{i,1} = P_{i,1} = \frac{\exp(\mu_0 - \beta \mathbf{X}_i)}{1 + \exp(\mu_0 - \beta \mathbf{X}_i)} = \frac{\exp(-\beta \mathbf{X}_i - \phi_m)}{1 + \exp(-\beta \mathbf{X}_i - \phi_m)}, \quad (12)$$



$$\begin{aligned}
302 \quad p_{i,j} &= P_{i,j} - P_{i,j-1} = \frac{\exp(-\beta \mathbf{X}_i - \phi_m) [\exp(\mu_{j-1}) - \exp(\mu_{j-2})]}{[1 + \exp(\mu_{j-1} - \beta \mathbf{X}_i - \phi_m)] [1 + \exp(\mu_{j-2} - \beta \mathbf{X}_i - \phi_m)]} = \\
303 \quad &\frac{\exp(-\beta \mathbf{X}_i - \phi_m) \exp\left[\sum_{k=1}^{j-2} \exp(\alpha_k \mathbf{Z}_{i,k})\right] \{\exp[\exp(\alpha_{j-1} \mathbf{Z}_{i,j-1})] - 1\}}{\{1 + \exp\left[\sum_{k=1}^{j-1} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i - \phi_m\right]\} \{1 + \exp\left[\sum_{k=1}^{j-2} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i - \phi_m\right]\}}, \forall j \in \{2, \dots, J-1\}, (13)
\end{aligned}$$

$$304 \quad p_{i,j} = 1 - P_{i,j-1} = \frac{1}{1 + \exp\left[\sum_{k=1}^{j-2} \exp(\alpha_k \mathbf{Z}_{i,k}) - \beta \mathbf{X}_i - \phi_m\right]}. \quad (14)$$

### 305 3.2. Marginal Effects of the Contributing Factors

306 Practitioners often express great interest in understanding the marginal effects of a  
307 certain contributing factor on the probabilities of various crash severity levels.  
308 Unfortunately, these effects cannot be directly seen from the model coefficients  $\beta$  and  
309  $\alpha_k$ , because the probabilities  $p_{i,j}$  are not linear functions of the factors. Hence, we  
310 derive the marginal effects of contributing factors analytically. Specifically, for the case  
311 discussed in this paper (i.e.  $J = 3$ ), the marginal effect of a continuous contributing  
312 factor  $x$  on  $p_{i,j}$  is calculated by taking its first-order derivative with respect to  $x$   
313 (Jalayer et al., 2018):

$$314 \quad \frac{\partial p_{i,1}}{\partial x} = \beta^x p_{i,1} (p_{i,1} - 1), \quad (15)$$

$$315 \quad \frac{\partial p_{i,2}}{\partial x} = \alpha^x \mu_{i,1} p_{i,3} (1 - p_{i,3}) + \beta^x p_{i,2} (p_{i,1} - p_{i,3}), \quad (16)$$

$$316 \quad \frac{\partial p_{i,3}}{\partial x} = (\beta^x - \alpha^x \mu_{i,1}) p_{i,3} (1 - p_{i,3}), \quad (17)$$

317 where  $\beta^x$  and  $\alpha^x$  are the coefficient estimates associated with variable  $x$  in the  
318 expressions of latent propensity  $z_i$  and threshold  $\mu_{i,1}$ , respectively.

319 In addition, the marginal effect of an indicator (binary) contributing factor  $x$  on  
320  $p_{i,j}$  is calculated by taking its first-order difference with respect to  $x$  and with  $\Delta x =$   
321 1. They are respectively:

$$322 \quad \frac{\Delta p_{i,1}}{\Delta x} = \frac{\exp(-\tilde{\beta} \tilde{\mathbf{X}}_i - \phi_m) [\exp(-\beta^x) - 1]}{[1 + \exp(-\tilde{\beta} \tilde{\mathbf{X}}_i - \phi_m)] [1 + \exp(-\tilde{\beta} \tilde{\mathbf{X}}_i - \beta^x - \phi_m)]}, \quad (18)$$

$$\frac{\Delta p_{i,j}}{\Delta x} = \frac{\exp(-\tilde{\beta}\tilde{\mathbf{X}}_i - \beta^x - \phi_m) \{ \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1} + \alpha^x)] - 1 \}}{\{1 + \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1} + \alpha^x) - \tilde{\beta}\tilde{\mathbf{X}}_i - \beta^x - \phi_m]\} \{1 + \exp[-\tilde{\beta}\tilde{\mathbf{X}}_i - \beta^x - \phi_m]\}} -$$

$$\frac{\exp(-\tilde{\beta}\tilde{\mathbf{X}}_i - \phi_m) \{ \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1})] - 1 \}}{\{1 + \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1}) - \tilde{\beta}\tilde{\mathbf{X}}_i - \phi_m]\} \{1 + \exp[-\tilde{\beta}\tilde{\mathbf{X}}_i - \phi_m]\}}, \quad (19)$$

$$\frac{\Delta p_{i,3}}{\Delta x} = \frac{\exp(-\tilde{\beta}\tilde{\mathbf{X}}_i - \phi_m) \{ \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1})] - \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1} + \alpha^x) - \beta^x] \}}{\{1 + \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1}) - \tilde{\beta}\tilde{\mathbf{X}}_i - \phi_m]\} \{1 + \exp[\exp(\tilde{\alpha}_1 \tilde{\mathbf{Z}}_{i,1} + \alpha^x) - \tilde{\beta}\tilde{\mathbf{X}}_i - \beta^x - \phi_m]\}}, \quad (20)$$

where  $\tilde{\mathbf{X}}_i$  and  $\tilde{\mathbf{Z}}_{i,1}$  denote the vectors  $\mathbf{X}_i$  and  $\mathbf{Z}_{i,1}$  less element  $x$ , respectively, and  $\tilde{\beta}$  and  $\tilde{\alpha}_1$  denote the corresponding coefficient vectors (i.e.,  $\beta$  less  $\beta^x$  and  $\alpha_1$  less  $\alpha^x$ , respectively). Note that (18-20) are applicable to the spatial generalized ordered logit model only. For the traditional generalized ordered logit model, the CAR prior term  $\phi_m$  should be removed from these equations.

The marginal effects are calculated for each individual crash. The average marginal effects of all the observations in the dataset are then reported in the following section.

333

#### 334 4. MODEL ESTIMATION, COMPARISON, AND DISCUSSIONS

335 In Section 4.1, we describe the Bayesian estimation processes of the two models and  
 336 two comparison methods built upon two metrics, respectively: the “deviance  
 337 information criterion” (DIC) and the classification accuracy. The comparison results  
 338 are presented and discussed in Section 4.2. The marginal effects of some significant  
 339 contributing factors are examined in Section 4.3.

340

##### 341 4.1 Model Estimation and Comparison Method

342 Since the traditional maximum likelihood estimation cannot be applied to models with  
 343 CAR Gaussian priors (Meng et al., 2017), in this paper we use the Bayesian method to

344 estimate the model parameters. The method is built upon Markov chain Monte Carlo  
345 (MCMC) simulation with Gibbs sampling algorithm, which can be easily implemented  
346 via the freeware WinBUGS (Lunn et al., 2000). To apply the Bayesian method, we first  
347 specify the prior distribution of each (hyper-)parameter in the models. Without  
348 additional knowledge, noninformative (vague) prior distributions are used for these  
349 (hyper-)parameters. Specifically, we use a diffused normal distribution denoted by  
350  $N(0, 10^4)$  as the priors of the coefficients in  $\beta$  and  $\alpha_1$ . The CAR priors are specified  
351 by the function *car.normal* in WinBUGS (Zeng and Huang, 2014a). A diffused gamma  
352 distribution,  $\text{gamma}(0.01, 0.01)$ , is used as the prior of the precision parameter (i.e.,  
353 the reciprocal of the variance parameter,  $1/\sigma_\phi$ ). For each model, we run a chain of  
354 150,000 MCMC simulation iterations, where the first 100,000 iterations act as a burn-  
355 in. The MCMC trace plots for the model parameters are inspected visually to ensure the  
356 simulations converge. In addition, we monitor the ratios between the Monte Carlo  
357 simulation errors and the respective estimates' standard deviations to ensure that they  
358 are less than 0.05 (a rule-of-thumb threshold).

359 We compare the models via DIC and the classification accuracies for each severity  
360 level and for the entire dataset. DIC is deemed as a Bayesian equivalent of Akaike's  
361 information criterion (Akaike, 1974) that takes model complexity into consideration.  
362 According to Spiegelhalter et al. (2002), DIC is defined as:

$$363 \quad \text{DIC} = \bar{D} + pD, \quad (21)$$

364 where  $\bar{D}$  is the posterior mean deviance that can be used as a fitness or adequacy

365 measure of the model, and  $pD$  is the effective number of parameters used to measure  
 366 model complexity (this term is added to penalize models with more parameters).  
 367 Generally, a model with a lower DIC value is preferred. DIC can be directly obtained  
 368 from WinBUGS.

369 The classification accuracy for severity level  $j$  is defined as the proportion of  
 370 accurate prediction in the set of data instances with observed severity level  $j$  (Zeng  
 371 and Huang, 2014b), that is,

$$372 \quad CA_j = \frac{\sum_{\bar{Y}_i=Y_i=j} Y_i}{\sum_{Y_i=j} Y_i} \times 100\%, \forall j \in \{1, 2, \dots, J\}, \quad (22)$$

373 where  $\bar{Y}_i$  represents the predicted crash severity level.

374 Similarly, the classification accuracy for the entire dataset is calculated as:

$$375 \quad CA_t = \frac{\sum_{\bar{Y}_i=Y_i} Y_i/Y_i}{\sum_i Y_i/Y_i} \times 100\%. \quad (23)$$

376

## 377 4.2. Model Comparison Results

378 The results of parameter estimation and model comparison are summarized in Table 3,  
 379 where only the factors that have statistically significant (at 90% credibility level or  
 380 above) effects on crash severity are included. The tabulated values outside the  
 381 parentheses are the posterior means of parameters, and those inside the parentheses are  
 382 their posterior standard deviations.

383 First note that  $\bar{D}$  of the spatial generalized ordered logit model (873) is lower than  
 384 that of the traditional generalized ordered logit model (888), which indicates that the  
 385 spatial model fits better with the data. This finding is consistent with previous studies

386 on traffic safety analysis (Xu et al., 2016; Zeng and Huang, 2014a); i.e., explicitly  
387 accounting for the spatial correlation using CAR priors can improve the model's  
388 estimation power. Although the traditional model has fewer effective parameters (50  
389 versus 60 for the spatial model; see Table 3), the spatial model still exhibits a lower  
390 DIC value (933 versus 938 for the traditional model). The difference in DIC is  
391 considered substantial (see Spiegelhalter et al., 2005), which suggests that the spatial  
392 model is preferred to the traditional one. The former's superiority in goodness-of-fit is  
393 further confirmed by its higher classification accuracies for each crash severity levels  
394 and the entire dataset, as revealed by the last four rows of Table 3. Note in particular  
395 the large difference between  $CA_3$  of the two models (7% versus 10%), which indicates  
396 the prediction accuracy for severe crashes. Given the great loss caused by severe  
397 crashes, we reckon that the spatial model is more suitable to be used in traffic safety  
398 analysis.

399 The significance of spatial correlation is also verified by the estimated standard  
400 deviation of the spatial term  $\phi_m$  (0.17), which is moderately significant as compared  
401 to the values found in previous studies (Xu et al., 2016; Zeng and Huang, 2014a). The  
402 significant spatial correlation is as expected and can be explained by some unobserved  
403 factors shared by the crashes occurring at neighboring locations. Examples of these  
404 unobserved factors may include the terrain feature, lighting condition, and traffic sign  
405 layouts. The spatial correlation unveiled from the data can also be used to suggest High  
406 Collisions Concentration Locations (Chung and Ragland, 2018).

407

408 **Table 3** Parameter estimation and model comparison results

	Generalized ordered logit model		Spatial generalized ordered logit model	
	Latent propensity	Threshold between median and severe crash levels	Latent propensity	Threshold between median and severe crash levels
<i>Professional driver</i>	1.70 (0.77)**	—	1.68 (0.78)**	—
<i>Truck</i>	—	-0.44 (0.22)**	—	-0.45 (0.21)**
<i>Other vehicle</i>	—	-0.76 (0.30)**	—	-0.79 (0.30)**
<i>Summer</i>	0.72 (0.28)**	—	0.72 (0.30)**	—
<i>Autumn</i>	—	0.67 (0.31)**	—	0.64 (0.30)**
<i>Afternoon</i>	—	0.67 (0.27)**	—	0.64 (0.27)**
<i>Overcast</i>	—	0.60 (0.32)**	—	0.57 (0.32)*
<i>Vertical grade</i>	—	-0.47 (0.13)**	—	-0.46 (0.13)**
<i>Bridge</i>	—	0.37 (0.19)**	—	0.35 (0.20)**
<i>Traffic volume</i>	-0.24 (0.12)**	0.31 (0.11)**	-0.30 (0.11)**	0.31 (0.11)**
<i>Veh_2</i>	0.56 (0.17)**	—	0.50 (0.18)**	—
<i>Veh_4</i>	—	0.12 (0.06)**	0.08 (0.05)*	0.12 (0.06)**
<i>EMS response time</i>	0.02 (0.01)**	—	0.03 (0.01)**	—
<i>Rear-end crash</i>	-2.12 (0.25)**	-0.60 (0.27)**	-2.29 (0.27)**	-0.59 (0.27)**
<i>Angle crash</i>	-2.23 (0.25)**	-1.10 (0.24)**	-2.00 (0.28)**	-1.09 (0.25)**
$\phi_m$	—	—	0.48 (0.17)**	—
$\bar{D}$	888		873	
$pD$	50		60	
DIC	938		933	
CA <sub>1</sub>	78%		79%	
CA <sub>2</sub>	76%		77%	
CA <sub>3</sub>	7%		10%	
CA <sub>t</sub>	74%		75%	

409 \* Significant at the 90% credibility level.

410 \*\* Significant at the 95% credibility level.

411

412 Further comparison between the two models unveils that the significant factors

413 contributing to the latent propensity and the threshold between median and severe crash

414 levels in the traditional model are still significant in the spatial model, and that they  
415 take similar values in the two models. This partly demonstrates the consistency between  
416 the two models. Note too for most significant factors in the latent propensity function  
417 that the standard deviation increases after accounting for spatial correlation. This  
418 finding is also consistent with the conclusions of previous studies, i.e., that omitting  
419 spatial correlation would result in underestimation of the parameters' variances and  
420 potential misidentification of the contributing factors (Quddus, 2008).

421 The marginal effects of significant factors on the probability of each crash severity  
422 level are calculated for the two models via the method described in Section 3.2. The  
423 results are shown in Tables 4 and 5, respectively. Comparing the marginal effects in the  
424 two models, we find that most factors exhibit similar impacts on the likelihoods of all  
425 severity levels. Exceptions arise for two factors whose impacts on the likelihoods of  
426 certain severity levels are considerably different between the two models: *traffic volume*  
427 and *Veh\_4*. For example, the marginal effect of *traffic volume* on the probability of  
428 medium crashes is positive in Table 4, while it is negative in Table 5. These differences  
429 again show how incorporating the spatial correlation would change the model  
430 predictions. In addition, Table 5 shows that, for *Veh\_4* and *angle crash*, the marginal  
431 effects on the probabilities of light crashes and severe crashes exhibit the same sign.  
432 Note that these results cannot be obtained by standard ordered response models,  
433 because when the thresholds between ordered severity levels are fixed, changing a  
434 single factor will always cause the probabilities of the lowest and highest levels (i.e.

435 light and severe crashes) to vary in opposing directions (Eluru et al., 2008). This finding  
 436 manifests the necessity of using a generalized ordered response framework instead of a  
 437 standard one.

438

439 **Table 4** Marginal effects of significant covariates in the generalized ordered logit model

	light crashes (%)	medium crashes (%)	severe crashes (%)
<i>Professional driver</i>	-25.4	15.2	10.2
<i>Truck</i>	0	-3.7	3.7
<i>Other vehicle</i>	0	-8.2	8.2
<i>Summer</i>	-11.6	8.9	2.7
<i>Autumn</i>	0	5.0	-5.0
<i>Afternoon</i>	0	4.5	-4.5
<i>Overcast</i>	0	3.6	-3.6
<i>Vertical grade</i>	0	-5.0	5.0
<i>Bridge</i>	0	3.0	-3.0
<i>Traffic volume</i>	3.8	0.4	-4.2
<i>Veh_2</i>	-8.9	6.8	2.1
<i>Veh_4</i>	0	1.3	-1.3
<i>EMS response time</i>	-0.38	0.29	0.09
<i>Rear-end crash</i>	42.0	-39.4	-2.6
<i>Angle crash</i>	43.8	-43.8	-0.0001



440

441 **Table 5** Marginal effects of significant covariates in the spatial generalized ordered

442 logit model

	light crashes (%)	medium crashes (%)	severe crashes (%)
<i>Professional driver</i>	-24.7	14.7	10.0
<i>Truck</i>	0	-3.7	3.7
<i>Other vehicle</i>	0	-8.7	8.7
<i>Summer</i>	-11.3	8.6	2.7
<i>Autumn</i>	0	4.8	-4.8
<i>Afternoon</i>	0	4.3	-4.3
<i>Overcast</i>	0	3.4	-3.4
<i>Vertical grade</i>	0	-1.7	1.7
<i>Bridge</i>	0	2.9	-2.9
<i>Traffic volume</i>	4.6	-2.5	-2.1
<i>Veh_2</i>	-7.8	6.0	1.8
<i>Veh_4</i>	-1.3	1.4	-0.1
<i>EMS response time</i>	-0.47	0.36	0.11
<i>Rear-end crash</i>	43.1	-40.2	-2.9
<i>Angle crash</i>	38.4	-39.7	1.3

443

444 **4.3 Interpretation of the Parameter Estimates and Marginal Effects**

445 The results show that *professional drivers* have a significant positive effect on the latent  
446 severity propensity, which indicates that they are more likely to encounter severe  
447 crashes than non-professional drivers. Specifically, when at least one professional  
448 driver is involved, the likelihoods that the crash is medium and severe will increase by  
449 14.7% and 10.0%, respectively, and the likelihood of a light crash will decrease by  
450 24.7%. This result is reasonable because most professional drivers recorded in the  
451 dataset are coach drivers operating intercity bus services. They are more likely to  
452 experience driver fatigue due to the long working hours, which may increase the  
453 possibility of severe crashes (Islam and Mannering, 2006). In addition, the large number  
454 of occupants in a coach means more casualties may occur in a crash.

455 The negative signs of *truck* and *other vehicle* on the threshold between medium and  
456 severe crashes indicate that they are more likely to be involved in severe crashes: the  
457 probabilities of a severe crash will increase by 7.5% when a *truck* is involved, and by  
458 2.8% when an *other vehicle* is involved. This may be due to the stronger crash  
459 aggressivity of these vehicles (Huang et al., 2011; Zeng et al., 2016), which would  
460 impose greater hazards on the other vehicle(s) involved in the same crash.

461 Regarding the *seasonal* effect, we find that summer is associated with a higher  
462 severity propensity as compared against winter. Specifically, in summer the  
463 probabilities of medium and severe crashes increase by 6.7% and 1.7%, respectively.  
464 These results are consistent with the findings of Jalayer et al. (2018). The reason is  
465 simple: the investigated freeway is near the South China Sea, where adverse weather

466 conditions (e.g., typhoons and rainstorms) typically occurred in summers can  
467 significantly deteriorate the driving environment. On the other hand, the weather is  
468 generally good in autumns with adequate sunlight, comfortable temperature, and low  
469 rainfall. This is a reason why severe crashes are 4.8% less likely to occur in autumns  
470 than in winters.

471 The *time of day* has a significant influence on the threshold between medium and  
472 severe crashes. The results show that there are 4.3% fewer severe crashes in afternoons  
473 than before dawn (the reference category). This result is also as expected because  
474 drivers' vision is better in afternoons (Christoforou et al., 2010), and thus they have  
475 more time to perceive the potential hazards and react properly to alleviate the impact of  
476 an incoming crash. Moreover, speeding and fatigue/drowsy driving are more likely to  
477 appear before dawn, which are major causes of severe crashes (Huang et al., 2008).

478 Another interesting finding from the results is the positive coefficient for *overcast*  
479 on the threshold, resulting in a 3.4% lower odds of severe crashes on overcast days than  
480 on sunny days. This finding can be counterintuitive. Nevertheless, similar results were  
481 reported by previous studies (Abdel-Aty, 2003; Xie et al., 2009), in which the authors  
482 argued that drivers tended to drive slowly and cautiously on overcast days.

483 The results also show that for every 1% increase in the *vertical grade*, the  
484 probabilities of medium and severe crashes are expected to decrease and increase by  
485 1.7%, respectively. This is also in line with the findings of previous studies  
486 (Christoforou et al., 2010; Savolainen and Mannering, 2007; Yu and Abdel-Aty, 2014).

487 As pointed out by the above-cited works, a steeper grade renders a shorter sight distance,  
488 and thus less time for the drivers to take proper actions in response to upcoming crashes.

489 The positive effect of *bridge* on the threshold indicates that bridge segments are less  
490 prone to cause severe crashes: the likelihood of severe crashes decreases by 2.9% on  
491 bridge segments. The result may be attributed to the lower posted speed limits on  
492 bridges (Renski et al., 1999).

493 The negative and positive effects of *traffic volume* on the latent severity propensity  
494 and the threshold, respectively, suggest that the severity level increases as the traffic  
495 volume decreases. Specifically, a decrease of 1,000 passenger car units in daily traffic  
496 volume results in that the probabilities of medium and severe crashes increase by 2.5%  
497 and 2.1%, respectively. This may be due to the higher travel speeds associated with low  
498 traffic volumes (Christoforou et al., 2010; Zeng et al., 2017b). Note that a vehicle  
499 traveling at high speed will significantly increase the severity level of any crash that  
500 involves it (Zeng et al., 2016).

501 Regarding the traffic composition, we find that a higher *proportion of vehicles in*  
502 *Class 2* tends to result in more severe crashes. Specifically, the probabilities of medium  
503 and severe crashes increase by 6.0% and 1.8%, respectively, for a 1% increase of Class-  
504 2 vehicles. A potential reason is that Class-2 vehicles have larger sizes than Class-1  
505 vehicles (the reference category), and thus they are more likely to obstruct the view of  
506 the following vehicle drivers. We also find that a higher *proportion of Class-4 vehicles*  
507 results in increases in both the severity propensity and the threshold. The combined

508 effects lead to a 1.3% decrease in the likelihood of light crashes, a 1.4% increase in the  
509 likelihood of medium crashes, and a 0.1% decrease in the likelihood of severe crashes,  
510 for a 1% increase of Class-4 vehicles.

511 During the post-crash period, EMS plays a key role in reducing severe human  
512 injuries by providing first aid treatments and transportation to hospitals. As expected,  
513 the *EMS response time* is positively correlated with the crash severity level. [Table 5](#)  
514 shows that every additional minute taken by the EMS before arriving at the crash site  
515 will increase the probabilities of medium and severe crashes by 0.36% and 0.11%,  
516 respectively. Similar findings were reported by [Gonzalez et al. \(2009\)](#) and [Lee et al.](#)  
517 [\(2018\)](#).

518 Finally, regarding *crash type*, rear-end crashes and angle crashes are associated with  
519 a lower severity propensity and a smaller threshold between medium and severe crashes  
520 as compared to single-vehicle crashes (the reference category). Specifically, rear-end  
521 and angle crashes are 43.1% and 38.4% more likely to be light crashes, respectively,  
522 and are about 40% less likely to be medium crashes. On the other hand, the probability  
523 of severe crashes decreases by 2.9% for rear-end crashes but increases by 1.3% for  
524 angle crashes. This is generally consistent with the findings in many previous studies  
525 [\(e.g., Huang et al., 2011, 2016a; Zeng et al., 2016\)](#), where rear-end crashes are found to  
526 impose the least adverse impacts on the involved road users and vehicles.

527

## 528 **5. CONCLUSIONS AND FUTURE RESEARCH DIRECTIONS**

529 This paper proposes a Bayesian spatial generalized ordered logit model with CAR  
530 priors for analyzing key factors that affect the severity level of freeway crashes. Instead  
531 of the commonly used metric in the literature, i.e., the most severe injury involved in a  
532 crash, we use the four crash severity levels defined by the Ministry of Public Security  
533 in China. The new metric is more comprehensive since it accounts for not only the  
534 severity level of a single injury but also the number of injuries and deaths and the  
535 financial loss in a crash.

536 A one-year crash dataset collected from the Kaiyang Freeway in China is used to  
537 calibrate the model. The results suggest significant spatial correlations in the crash  
538 severity data. The superiority of our spatial model over a traditional generalized ordered  
539 logit model is manifested by the former's improved model fit. In brief, severe crashes  
540 are more likely to occur: i) when professional drivers, trucks or other heavy vehicles  
541 (especially those with trailers) are involved; ii) in summers and sunny days; iii) before  
542 dawn; iv) for angle crashes; v) on steeper slopes; vi) at locations other than bridges; vii)  
543 with a greater share of Class-2 vehicles (e.g. minibuses, minivans or light trucks); viii)  
544 when the EMS response is slow; and iv) under light traffic conditions.

545 The above findings have practical implications on the countermeasures for reducing  
546 severe crashes on freeways. For example, traffic management agencies and  
547 transportation companies should implement more measures (e.g., education programs)  
548 for ensuring safe driving of professional drivers. Traffic management agencies should  
549 also strengthen the enforcement against risky driving behavior (e.g., by increasing the

550 number of patrols) during 0-6 a.m. of every day. Regarding the designs of vehicles and  
551 freeway infrastructure, efforts can be made to reduce the crash aggressivity for trucks  
552 and other heavy vehicles, and to eliminate or reduce the use of steep slopes. Finally,  
553 better incident management measures are recommended to facilitate timely responses  
554 of EMS. These measures may include real-time incident detection and reporting,  
555 deployment of optimally located EMS facilities, and emergency vehicle preemption.

556 The Bayesian spatial generalized ordered logit model can be applied to other  
557 datasets using different crash severity metrics, such as the KABCO scale used in the  
558 US, which consists of five levels: fatality, incapacitating injury, non-incapacitating  
559 injury, possible injury, and no injury/property damage only. Future research efforts will  
560 be steered toward this direction to examine the causal factors of severe crashes in  
561 different regions or countries of the world, and under different criteria for crash severity.

562 While the strength of the CAR prior in capturing spatial correlation has been  
563 verified in this paper, in the future we will examine other spatial modeling methods  
564 (e.g., geographic weighted regression; see [Chiou et al., 2014](#), and [Li et al., 2013](#)) and  
565 compare their performance against the CAR prior method.

566 Lastly, although we did not identify any significant heterogeneity in the current  
567 dataset (results omitted for brevity), we plan to extend the current model to further  
568 account for the unobserved heterogeneity in crash severity pending the availability of  
569 more field data. This extension will also address the non-decreasing threshold variances  
570 problem that may arise in generalized ordered response models by carefully accounting

571 for the correlations between random parameters in the model (Balusu et al., 2018).

572

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578

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