

Edge enhancement through scattering media enabled by optical wavefront shaping

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Abstract: Edge enhancement is a fundamental and important topic in imaging and imaging processing, as perception of edge is one of the keys to identify and comprehend the contents of an image. Edge enhancement can be performed in many ways, through hardware or computation. Existing methods, however, have been limited in free space or clear media for optical applications; in scattering media such as biological tissue, light is multiply scattered and information is scrambled to a form of seemingly random speckles. Although desired, it is challenging to accomplish edge enhancement in the presence of multiple scattering. In this work, we introduce an implementation of optical wavefront shaping to achieve efficient edge enhancement through scattering media by a two-step operation. The first step is to acquire a hologram after the scattering medium, where information of the edge region is accurately encoded, while that of non-edge region is intentionally encoded with inadequate accuracy. The second step is to decode the edge information by time-reversing the scattered light. The capability is demonstrated experimentally, and furtherly the performance, as measured by the edge enhancement index (*EI*) and enhancement-to-noise ratio (*ENR*), can be controlled easily through tuning the beam ratio. *EI* and *ENR* can be reinforced by ~ 8.5 and ~ 263 folds, respectively. To the best of our knowledge, this is the first demonstration that edge information of a spatial pattern can be extracted through strong turbidity, which can potentially enrich the comprehension of actual images obtained from complex environment.

1. Introduction

Edge enhancement is uniquely important as perception of edge is a key factor for human visual system to identify or comprehend the contents of an image. It has vital roles in broad applications, such as increasing discrimination capacity in pattern recognition [1], detecting dislocation of crystal in biological cells [2], identifying lesion boundaries of cancer [3-6]. The realization of edge enhancement can be traced back to Zernike's seminal work [7], where phase or intensity gradient of an object is enhanced for conspicuity strengthening and tiny-feature detection. Nowadays, edge enhancement can be accomplished digitally through signal processing methods, such as spatial differentiation [8], wavelet transform [9], and Hilbert transform [10], or through physical settings. One well-known example is spiral phase contrast (SPC) imaging, where a spiral phase plate with a topological charge $l = 1$ is placed in the Fourier plane of a $4f$ system [11-13]. Due to the peculiar symmetry of spiral phase, gradients of phase and intensity

43 profile can be isotropically enhanced. SPC method was later extended for microscopy to make image
44 brightness and contrast be significantly better than conventional versions [14]. Another strategy is to
45 employ photorefractive effect to highlight the edge information of an intensity pattern [15-17].
46 Responding to interferogram, photorefractive materials, governed by the four-wave-mixing mechanism
47 [15], form volumetric optical grating with different local diffraction efficiencies. Manipulating such
48 grating may maximize the diffraction efficiency for edges only while minimize that for other parts;
49 consequentially boundaries of the pattern are enhanced [15]. In addition, some physical filters, such as
50 Laguerre–Gaussian spatial filter [18] and Airy spiral phase filter [19], are also developed to achieve high
51 contrast edge enhancement.

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53 Whilst promising, all filters mentioned above, no matter digital or physical, can only perform edge
54 detection in free space or process signals obtained with ballistic or quasi-ballistic light. These approaches
55 are not able or have not been verified to be compatible with strong scattering media (e.g., ~1 mm beneath
56 human skin [20]), when photons are multiply scattered and optical information is completely disordered
57 [21]. Therefore, existing edge enhancement methods encounter the same trade-off between penetration
58 depth and resolution as all other biomedical optical techniques [22]. High-resolution edge information
59 processing and retrieval at depths in scattering media has been desired in many optical applications yet
60 remains unexplored.

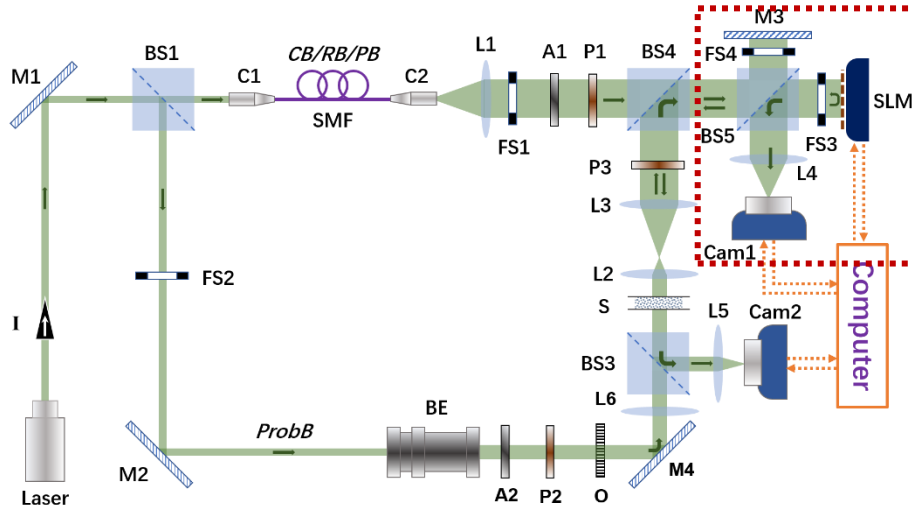
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62 This study aims to tackle this challenge from the perspective of optical wavefront shaping, a relatively
63 new field conceived to manipulate scattered light beyond the diffusion limit [23-27]. Optical phase
64 conjugation (OPC) [24, 27-29] is an example of wavefront shaping that exploits the bilateral nature of
65 light trajectory to “time-reverse” scattered light [30]. The execution of OPC requires an analog [27, 31]
66 or digital [28, 29, 32, 33] phase conjugation mirror (PCM) that firstly holographically records the phase
67 profile of scattered light and secondly projects its phase-conjugated copy back to the medium. As a result,
68 intensity profile of the original incident light field before being scattered can be reconstructed. The whole
69 procedure can be accomplished with two or three steps [33], achieving light manipulation through
70 turbidity as rapidly as a few milliseconds [34, 35]. While related, such a capability thus far has not yet
71 been extended for edge enhancement through scattering media. In this study, we take inspiration from
72 the classic photorefractive approach for edge enhancement in free space [15], and develop a digital
73 optical phase conjugation (DOPC) setup to achieve robust and tunable time-reversed speckle suppression
74 and edge enhancement through thick scattering media by a two-step procedure. First, a hologram that
75 accurately encodes the information of edge only is recorded. Secondly, the edge pattern is selectively
76 decoded by phase conjugating the scattered light. The proposed method is demonstrated experimentally
77 with scalable edge enhancement performance out of seemingly random speckle patterns. Although a lot
78 need to be furthered, this work potentially can be of instructive significance to the processing,
79 comprehension, and analysis of optical images with the presence of scattering.

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81 **2. Methods**

82 *2.1 Experimental setup*



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Fig. 1. System setup of DOPC. A_{1,2}: Neutral-density attenuator; BE: Collimated beam expander; BS_{1,5}: Beam splitter cube; C_{1,2}: Optical fiber collimator; Cam₁: Scientific complementary metal–oxide–semiconductor (sCMOS) camera; Cam₂: CMOS camera; FS_{1,4}: Fast shutter; I: Isolator; L_{1-3, 5, 6}: Best-form lens; L₄: Camera lens; Laser: CW laser, $\lambda = 532$ nm; M₁₋₄: Mirror; O: Object, a 1951 USAF resolution test chart; P_{1,3}: Linear polarizer; S: Scattering medium; SLM: Phase-only spatial light modulator; SMF: Single-mode optical fiber; CB/RB/PB: Calibration/Reference/ Playback beam; ProbB: Probe beam. Red dash line indicates the module of digital phase conjugation mirror (PCM).

The configuration of DOPC system is presented in Fig. 1. A CW laser source (EXLSR-532–200-CDRH, SPECTRA PHYSICS, coherence length = 300 m) emits a laser beam ($\lambda = 532$ nm) which is split by a beam splitter cube (BS₁) into two arms. One is probe beam, and the other is multi-functional beam (calibration/reference/playback beam). The probe beam is expanded by a collimated beam expander and its intensity profile is shaped by a 1951 USAF resolution test chart (Edmund Optics Inc.). The image of the resolution test chart is relayed onto the interior surface of a diffuser (600 grit polished, Thorlabs Inc) by L₆. On the other side, the multi-functional beam is spatially shaped by a single-mode fiber (HP-532, Thorlabs, 1 meter long) to mimic a quasi-ideal point source at the exit of the collimator (C₂). The beam is expanded by a best-form lens (L₁) before entering the digital PCM module. At the beam splitter cube (BS₄), the probe beam and the multipurpose beam merge and are relayed together to the digital PCM, which is configured by the combination of a scientific CMOS camera (sCMOS, pco.edge 5.5, PCO, pixel size: 6.5×6.5 μm) and a phase-only spatial light modulator (SLM, PLUTO-VIS-056, HOLOEYE). The SLM and the sCMOS camera are pixel-to-pixel conjugated to each other, with a misalignment error less than one pixel. The diffused light pattern right after the diffuser is imaged on the plane of SLM through a 4f system configured by L₂ and L₃, where the diffuser and the plane of SLM is spatially quasi-conjugated with each other. The digital PCM has two main purposes, hologram recording and playback, which are respectively accomplished by the sCMOS camera and the phase-only SLM. To observe the playback wavefront, another CMOS camera (Cam₂, pixel size: 2.5×2.5 μm) and L₅ are employed to image the reconstructed intensity distribution of the playback beam after transmitting through the turbid sample. Polarizations and intensities of the probe beam and the multipurpose beam are adjusted by two linear polarizers (P₁ and P₂) and neutral-density attenuators (A₁ and A₂), respectively. Four fast shutters

113 (FS₁₋₄) are equipped to control the ON or OFF state of light beams. Detailed procedures of DOPC
 114 operation can be referred to [32, 33].

115 2.2 Principles of DOPC-based edge enhancement through scattering media

116 A former study has demonstrated how edges of a binary pattern can be enhanced in free space via
 117 photorefractive effect with a piece of BaTiO₃ photorefractive crystal [15]. The method proposed in
 118 this work is actually a digital analogue of the aforementioned photorefractive edge enhancer.
 119 Functions of the photorefractive crystal are provided by a digital PCM, a spatially conjugated camera-
 120 SLM module, as enclosed by the red dash line in Fig. 1. On one hand, holographic information is
 121 recorded digitally using a digital camera (Cam₁, Fig. 1); on the other hand, a SLM is able to create
 122 variable phase profiles, mimicking the effect of grating with variable diffraction efficiency in the
 123 crystal.

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125 Starting with hologram recording, the working principles of DOPC-based edge enhancement can be
 126 explained as below. The hologram recorded by Cam₁ can be written as

$$127 \quad I_h = I_{ref} + I_{prob} + 2\cos(\varphi)\sqrt{I_{ref} * I_{prob}} \quad (1)$$

128 where I_h , I_{ref} and I_{prob} denote the intensity of hologram, the reference beam, and the probe beam,
 129 respectively; φ is the phase difference between the reference beam and the probe beam. The local
 130 modulation efficiency ($M.E.$) of PCM, determined by contrast of the hologram recorded by Cam₁,
 131 can be expressed as

$$132 \quad M.E. = \frac{I_h}{I_{ref} + I_{prob}} = 1 + MD * \cos(\varphi) \quad (2)$$

133 It can be seen that local $M.E.$ of PCM is dominated by the modulation depth ($MD = \frac{2\sqrt{I_{prob}*I_{ref}}}{I_{prob}+I_{ref}}$)
 134 [15]. This term can be expressed as a function of the intensity ratio of the probe and reference beams,
 135 i.e. $r = \frac{I_{prob}}{I_{ref}}$. So that, $MD(r) = \frac{2\sqrt{r}}{1+r}$. As a result, $M.E.$ can be written as $M.E. = 1 + MD(r) * \cos \varphi$. Considering the one-dimensional situation as following without scattering media:

$$137 \quad I_{ref}(x) = a \text{ (for all } x\text{)}; I_{prob}(x) = \begin{cases} 0 & x \leq -m/2 \\ b & -m/2 < x < m/2 \\ 0 & x \geq m/2 \end{cases} \quad (3)$$

138 where a , b and m are three finite constants. It represents a simple case of hologram written to
 139 Cam₁, where the reference beam is of uniform intensity while the probe beam is of a binary intensity
 140 profile, i.e. a box function with a width of m , symmetrical with respect to the origin. But there is an
 141 extreme condition for this situation, that is the intensity of the probe beam is considerably larger than

142 that of the reference beam i.e. $a \ll b$. For the dark region of the probe beam ($x < -\frac{m}{2}$ or $x > \frac{m}{2}$),

143 $r = 0$, which leads to $MD(r) = 0$. For the bright region of probe beam ($-\frac{m}{2} < x < \frac{m}{2}$), $r = \frac{b}{a}$, being

144 considerably large, which also yields $MD(r) \approx 0$. The situation is different, however, for the edges

145 ($x = -\frac{m}{2}$ or $x = \frac{m}{2}$). It is considered to exist a transition status where $I_{ref}(x) \sim I_{prob}(x)$, making the

146 *in situ* $MD(r)$ maximum that equals to unity [15].

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148 In the existence of the scattering media, the scattering light field recorded by Cam₁ can be expressed
149 by:

$$150 E_{out} = TE_{in} \quad (4)$$

151 where E_{in} is the light field of probe beam before the scattering medium, and T is the transmission
152 matrix of the scattering medium. Due to the scattering, the spatial pattern gets completely chaotic and,
153 as a result, edge profile cannot be seen in the disordered optical field. Specifically, the spatial pattern
154 evolves as random speckle pattern when light propagates through the scattering medium in the
155 hologram recording stage. Thus, the original spatial information is encoded in the recorded random
156 speckle pattern; the recorded speckle pattern carries information of the original incident spatial pattern
157 and the scattering medium. Therefore, signal input to the PCM is the fused information of TE_{in} . Due
158 to the phase-conjugated nature, the PCM turns the input into its phase-conjugated copy, $[TE_{in}]^*$. In
159 the hologram playback stage, the light field (E_{PB}) out of the scattering medium is recorded by Cam₂,
160 which can be written as

$$161 E_{PB} = (T)^t [TE_{in}]^* = [(T)^+ TE_{in}]^* \quad (5)$$

162 where $*$ denotes complex conjugate while t and $^+$ respectively signify transpose and conjugate
163 transpose.

164

165 A further justification why the time reversal identity of DOPC is able to overcome the scattering and
166 achieve edge enhancement simultaneously is briefed below. In the phase recording stage, Cam₁
167 records an interferogram formed by the reference beam (E_{ref}) and the scattered probe beam (TE_{in}).
168 After the scattering medium, the probe beam is scrambled. In the playback section, the output light
169 field ($(T)^+(T)E_{in}$) from the scattering medium appears even more scrambled. But, within a time-
170 invariant system, one can assume that $(T)^+(T) \approx I$, where I denotes an identity matrix. That is, the
171 output light is exactly conjugated to the probe beam. Therefore, the time-reversal playback essentially
172 decodes the original pattern from a seemingly random speckle pattern by reciprocating the
173 transmission matrix, enabling scattering suppression at the front side of the scattering medium.

174

175 For DOPC systems, a Camera-SLM module is employed to record the probe-reference interference
176 pattern and retrieve a phase profile to mimic the effect of grating in analogue OPC. Thus, the precision
177 of the retrieved phase (to be loaded on the SLM) matters. In our system, the primary phase retrieval
178 precision is determined by the smallest bit depth of the digital devices (Cam₁: 16 bits; SLM: 8 bits)
179 Through simulation (please refer to the Supplementary), it is found that the calculated phase is most
180 accurate when the two beams of interference are equally intense, and the accuracy is reduced with
181 increased imbalance in beam ratio (Fig. S1). Therefore, in our system, when the beam ratio $r = 1$,
182 the whole object can be recovered with fair fidelity due to the minimum phase error. With increased
183 beam ratio r , for non-edge regions the phase retrieval accuracy drops due to imbalance of interfering
184 beam ratio. But for edges, the precision of calculated phase remains optimum due the existence of
185 transition status where $I_{ref}(x) \sim I_{prob}(x)$. Under this condition ($I_{obj} \gg I_{ref}$), when the SLM is
186 illuminated by the reference beam in the playback stage, the generated conjugated light corresponding
187 to the non-edge regions may deviate from its ideal optical paths. As a result, the non-edge regions are
188 harder to be recovered; more and more photons contribute to the background noise when they
189 propagate through the scattering medium. In comparison, the edge areas are reinforced from the
190 background.

191

192 2.3 Quantification of edge enhancement effect

193 For a characteristic unenhanced edge (Fig. 2a) in an intensity pattern, it can be divided into three
 194 portions, ground level (G), brink (B), and upper level (U). In our experiment, the lengths of G and U
 195 are both set to be 30 pixels. For an enhanced edge (Fig. 2b), two additional parameters are defined,
 196 the summit (S) (maximum pixel intensity) and the valley (V) (minimum pixel intensity) in the regime
 197 of brink. To quantify the absolute edge enhancement effect, the concept of edge enhancement-index

198 (EI) is introduced [38, 39]: $EI = \frac{(S-V)/(S+V)}{(\mu_U - \mu_G)/(\mu_U + \mu_G)}$, where μ_U and μ_G are the mean of intensity

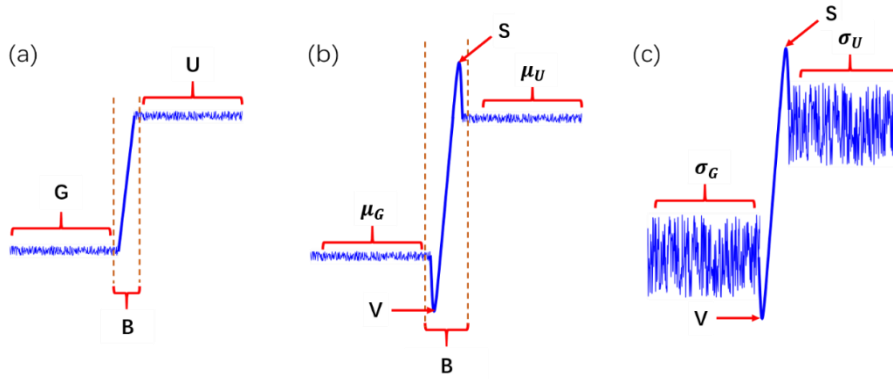
199 values of U and G, respectively. For a non-enhanced typical edge, $\mu_U \approx S$, $\mu_G \approx V$ and therefore
 200 the edge enhancement index $EI \approx 1$. Larger EI indicates greater absolute edge enhancement effect.

201 However, only EI is not sufficient for quantifying the visual conspicuity of the edge, as the noise
 202 level also influences the visual effect (Fig. 2c). Thus, the concept of edge enhancement-to-noise ratio

203 (ENR) is also defined to quantify the edge enhancement effect relative to the noise level [38]: $ENR =$

204 $\frac{(S-V)}{\sqrt{\sigma_U^2 + \sigma_G^2}}$, where σ_U and σ_G are the standard deviation of intensity values of U and G, respectively.

205 Less noise in U and G and greater difference in S and V will lead to larger value of ENR , indicating
 206 better visual edge enhancement effect relative to the noise level.



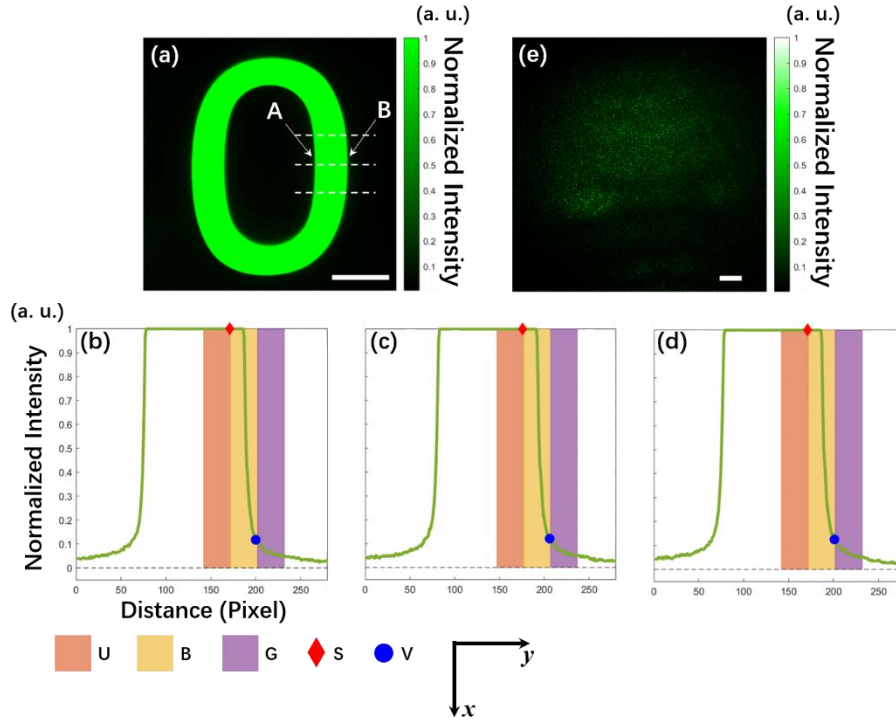
207
 208 Fig. 2. Anatomy and metrics of an edge. (a) A regular unenhanced edge can be divided into three portions, including ground
 209 level (G), brink (B), and upper level (U). The lengths of G and U occupy 30 pixels in our experiment. (b) For an enhanced edge,
 210 the maximum and minimum pixel intensity of the portion B are termed as summit (S) and valley (V). To quantify the absolute
 211 edge enhancement effect, the concept of edge enhancement-index $EI = \frac{(S-V)/(S+V)}{(\mu_U - \mu_G)/(\mu_U + \mu_G)}$ is introduced, where μ_U and μ_G are
 212 mean of intensity values of U and G, respectively. (c) The noise level of an edge influences the visual enhancement effect and
 213 thus the concept of edge enhancement-to-noise ratio $ENR = \frac{(S-V)}{\sqrt{\sigma_U^2 + \sigma_G^2}}$ is defined, where σ_U and σ_G are standard deviation of
 214 the intensity values of U and G, respectively.

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217 **3. Results and Discussion**

218 With a fine-tuned DOPC system, experiments are conducted to enhance edge of an intensity pattern
 219 through strong scattering media. Transmitting through the resolution test chart, the intensity profile of
 220 the probe beam is shaped into a pattern “0”, carrying the spatial information. This original pattern of
 221 interest is recorded by Cam₁, as shown in Fig. 3a. Three horizontal dashed primitive lines with the
 222 length of 280 pixels are created in the Fig. 3a and the line charts (b)-(d) correspondingly show the
 223 horizontal intensity distributions along these lines. A and B denote the inner and outer rim of the

224 pattern “0”, respectively. For edge B, the mean EI and ENR are calculated as 0.91 and 42.77,
 225 respectively. Then, a scattering 600-grit ground glass diffuser (S, Fig. 1) is positioned into the DOPC
 226 system. As shown in Fig. 3e, the intensity profile of the probe beam captured by Cam₁ becomes a
 227 random speckle pattern after penetrating through the ground glass and no edge profile can be found,
 228 indicating that the spatial information of the object has been completely disordered due to scattering.
 229 Despite of that, information of the object is encoded within the speckle pattern. Therefore, the next
 230 step is to selectively retrieve the edge pattern from this scrambled light field.



231
 232 Fig. 3. Intensity profile of the probe beam before and after transmitting through the scattering medium. (a): Intensity profile of
 233 the incident probe beam, a quasi-binary pattern of number “0”, shaped by the resolution test chart. Three horizontal white
 234 dashed primitive lines (1-3) with the length of 280 pixels are created. The intensity distribution along the line 1-3 are
 235 respectively shown in (b)-(d). A and B denote the inner and outer rim of the pattern “0”, respectively. For edge B, the mean EI
 236 and ENR are calculated as 0.91 and 42.77, correspondingly. U: Upper level; B: Brink; G: Ground level; S: Summit; V: Valley.
 237 (e) Intensity profile of the probe beam after penetrating a ground glass diffuser, which is a seemingly random speckle pattern
 238 with no obvious edge profile can be found. Scale bar: 500 μm

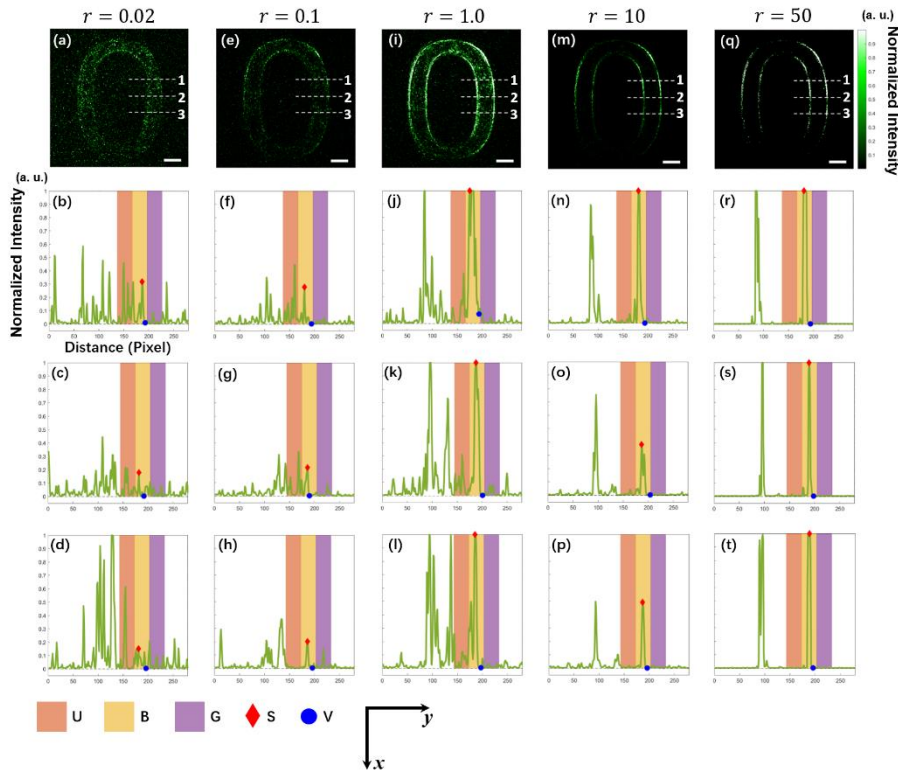
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 241 To demonstrate the progressive formation of DOPC-based edge enhancement through scattering
 242 media, the intensity ratio ($r = \overline{I_{prob}} / \overline{I_{ref}}$) between the probe and reference beams is carefully adjusted
 243 to be 0.02, 0.10, 1.0, 10, and 50, respectively, during the hologram writing. Note that the intensity of
 244 the probe beam/speckle pattern ($\overline{I_{prob}}$) is represented by the mean value of all pixels within the region
 245 of interest (ROI), e.g. Fig. 3(e), while the intensity of the reference beam ($\overline{I_{ref}}$) is characterized within
 246 the same ROI in the same manner.

247
 248 The intensity patterns of the conjugated light field recorded by Cam₂ in the playback stage are shown
 249 in Fig. 4 (the first row). As seen, the edge information can be retrieved well from random speckle
 250 patterns through DOPC. That said, there are still quite some residual speckle grains even with the

251 DOPC compensation. Especially in Fig. 4a and e, speckle grains are not sufficiently suppressed
 252 because of inefficient hologram writing due to the small value of r . With increased r value, intensities
 253 of the retrieved non-edge regions are suppressed, but the edges are now selectively highlighted (Fig.
 254 4i, m, and q). To quantify the transition, similar to Fig. 3a, three 280-pixel horizontal dashed lines (1-
 255 3) are created for the first row of Fig. 4. The intensity distributions along these lines are respectively
 256 plotted in the subfigures in the second, third and fourth rows of Fig. 4, as indicated by the green lines.
 257 For example, (b)-(d) are the intensity profiles corresponding to Lines 1-3 in (a), while (f)-(h)
 258 correspond to Lines 1-3 in (e). As seen, when r is increased, the degree of edge enhancement is
 259 boosted due to the robust speckle elimination. When $r = 50$, as shown in Fig. 4r, s and t, the ratio of
 260 the noise (speckle grains) to the signal (edges) is strongly suppressed yet the image boundaries are
 261 greatly highlighted.

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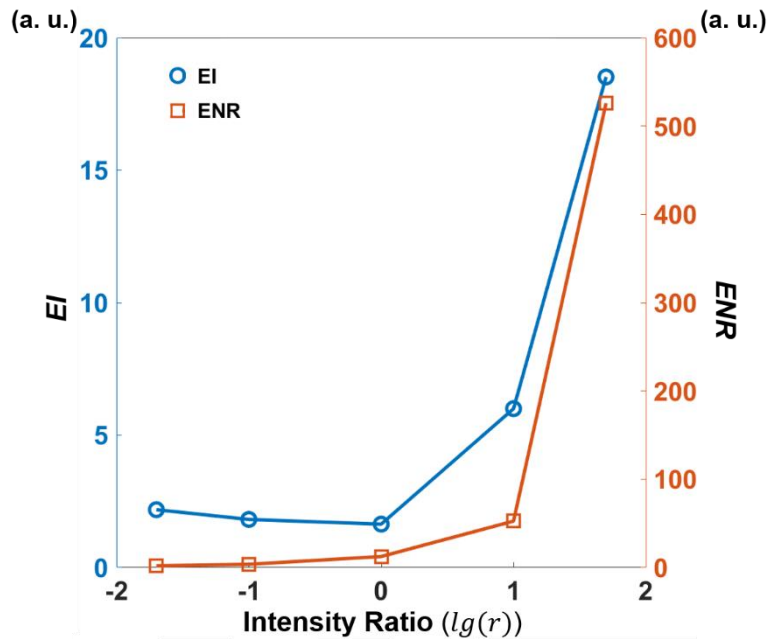
263 It is also very important to note that whist related, DOPC-based image and edge enhancement through
 264 scattering media are essentially two different directions: for regular imaging through scattering media
 265 (not aimed for edge enhancement), the optimal performance is usually acquired around $r = 1$, when
 266 the *M.E.* of the PCM achieves maximum at both bright region and edges (but is still zero in the dark
 267 region), as confirmed in Fig 4i. It should be clarified that the mean intensity of speckle in the ROI
 268 equal to that of reference beam is not necessary to be the optimal intensity ratio for recovering the full
 269 image. As seen in Fig. 4i, edges start to protrude when $r = 1$. However, situation of $r = 1$ is the one
 270 closest to the optimal image recovery, compared to other four intensity ratios in Fig. 4. If the purpose
 271 is to enhance the edge profile only while the other parts of the image are suppressed, a large value of
 272 r is preferred, i.e., the probe beam should be sufficiently stronger than the reference beam (as in Fig.
 273 4q). Such difference also highlights the motivation of the study as existing knowledges or experiences
 274 on optical focusing and imaging through scattering media cannot be directly applied for edge
 275 enhancement.



276

277 Fig. 4. DOPC-based edge enhancement through scattering media. Five images, (a), (e), (i), (m), (q) are recorded by the CMOS
 278 camera (Cam₂ in Fig. 1) in the playback stage. The intensity ratio (r) between the probe and the reference beams is tuned to
 279 different values (0.02, 0.10, 1.0, 10, 50) during the hologram writing. Three 280-pixel horizontal dashed lines (1-3) are created
 280 for the figures in the first row. The intensity distributions along Lines 1-3 are respectively shown in the figures in the second,
 281 third and fourth row, as indicated by the green lines. For example, (b)-(d) are the intensity profiles corresponding to Lines 1-3
 282 in (a), while (f)-(h) correspond to the lines in (e). U: Upper level; B: Brink; G: Ground level; S: Summit; V: Valley. Scale bar:
 283 250 μm .

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 286 To further quantify the performance of DOPC-based edge enhancement through turbidity, in Fig. 5
 287 we plot EI and ENR versus different beam intensity ratios. Each data point represents the mean value
 288 of EI or ENR from calculations of Lines 1-3. The x -axis represents the common logarithmic scale of
 289 the intensity ratio of between the probe and reference beams, i.e. $\lg(r)$. As seen, the mean EI (to the
 290 left axis) increases from 2.18 ($r=0.02$) to 18.52 ($r=50$), and the mean ENR (to the right axis) increases
 291 from 2.00 ($r=0.02$) to 525.94 ($r=50$). Even compared to the direct image of the object in free space
 292 (Fig. 3a), whose mean EI and mean ENR are respectively 0.91 and 42.77, the effect of edge
 293 enhancement as measured by these two parameters are quite significant, even though a strong
 294 scattering medium is penetrated.



295
 296 Fig. 5. Edge enhancement-index (EI) and edge enhancement-to-noise ratio (ENR) of edge B for different values of r (0.02,
 297 0.10, 1.0, 10, 50). The x -axis represents the common logarithmic scale of the intensity ratio of between the probe and
 298 reference beams, i.e. $\lg(r)$. EI increases from 2.18 to 18.52, and ENR increases from 2.00 to 525.94.

299
 300
 301 The aforementioned results once again confirm the rationality of the proposed method to enhance
 302 object boundary through scattering media. Without wavefront manipulation, optical signals, which is
 303 an intensity spatial pattern in this study, are thoroughly disordered when transmitting through
 304 scattering media and become seemingly random speckle patterns. In this work, DOPC serves as an
 305 effective turbidity suppressor and is able to manipulate the optical wavefronts even through complex

306 media. By tuning the probe-reference beam intensity ratio and hence the local modulation efficiency
307 of the PCM as well as calculated phase precision, DOPC is capable to generate modulated wavefronts
308 so that edge profile can be significantly reinforced from massive speckle noise. That said, we should
309 note the limitation of the performance. Even with a perfect DOPC system, the recovery efficiency is
310 still limited due to the finite control elements of the SLM and other factors such as the uneven spatial
311 distribution of the optical beams and the system calibration imperfection. As a result, only a fraction
312 of speckles is collected and only a fraction of the transmission matrix of the scattering medium is
313 utilized to time reverse the scattered probe beam. Therefore, in practice DOPC is not able to totally
314 overcome scattering, and the recovered edges are still influenced by scattering, as can be observed in
315 Fig. 4.

316

317 **4. Conclusion**

318 Edge enhancement plays an important role in many aspects of optical imaging and imaging processing.
319 Recent developments in optical wavefront shaping have paved the way to achieve high quality optical
320 focusing and imaging within or through scattering media; edge enhancement through strong turbidity,
321 however, remains unexplored. While related, existing knowledges or experiences cannot be directly
322 applied for edge enhancement through scattering media. In this study, we propose an effective two-
323 step digital optical phase conjugation (DOPC) approach. First, a digital hologram is obtained, where
324 information of the object and the edge is encoded with distinct accuracy (high for edges but low for
325 non-edge regions); second, the edge profile is reinforced by phase conjugating the scattered light while
326 the non-edge regions are significantly suppressed. In experiment, with a 600-grit ground glass diffuser
327 as the scattering medium, our method allows for significant visual enhancement of the edges from
328 noisy speckle patterns. As measured by the enhancement index (EI) and enhancement to noise ratio
329 (ENR), the edges can be reinforced by ~ 8.5 and ~ 263 times, respectively, benefiting from the robust
330 speckle suppression capability. To the best of our knowledge, this is the first time that edge
331 information of a spatial pattern can be extracted clearly through strong turbidity. Moreover, the
332 performance of the edge extraction and enhancement is controllable through tuning the efficiency of
333 the phase conjugation mirror. With further development, this approach may potentially find broad
334 applications or inspire new methods to enrich the comprehension of optical images in the scenario of
335 scattering, such as at depths in biological tissue.

336

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346 **Disclosures**

347 The authors declare no conflicts of interest.

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