

1 **Keywords:** Nano-textured bump; Droplet impact; Water collection; Lattice
2 Boltzmann method.

3

4 **1. Introduction**

5 Water demand is ever increasing with world's growing population. Around one third
6 of total population are facing water shortage problem [1]. In such a situation fog
7 harvesting can be a viable, sustainable and potential source of water. In nature plants
8 and animals have skilled the survival abilities to collect water from fog. For example,
9 the Namib desert beetles can live in area with very little rainfall [2]. Their back is
10 composed of bumpy hydrophilic/super-hydrophobic patterns, i.e., the hydrophilic
11 bumps are surrounded by super-hydrophobic valleys featuring microstructures of
12 flattened hemispheres, which assist in collection of passing by fog droplets [3].

13 Inspired by this kind of beetles, several surfaces have been mimicked and investigated
14 for condensation process [4–7]. However, in fog harvesting process, droplet impact is
15 another leading phenomenon for water collection [8]. Therefore, a surface with the
16 best overall water collection efficiency should perform well for both condensation and
17 droplet impact processes.

18 Droplet impact on smooth as well as textured surfaces has been widely investigated.
19 Normal impacts have been comprehensively reviewed by Yarin [9]. In addition to level
20 surfaces, several works on single and multiple droplets impact on inclined surfaces
21 have also been conducted in the past [10–14]. Recently, several studies have been
22 conducted to investigate droplet impact on smooth convex surfaces [15–17]. Liu et al.
23 [16] studied droplet impact on Echevaria leaves, which have convex/concave
24 architecture. Their results showed nearly 40% reductions in contact time owing to
25 asymmetric bounce off. Khojasteh et al. [17] studied droplet impact on hydrophobic
26 and super-hydrophobic hemispherical surfaces and focused on the effects of Weber
27 number, surface curvature and contact angle. They found higher area of liquid in
28 contact with the hemispherical surface compared to flat surfaces.

1 Apart from smooth surfaces, droplet impact on level textured surfaces has also been
2 investigated [18–26]. Wang et al. [23] investigated water droplet impacts on super-
3 hydrophobic carbon nanotube arrays with different wetting properties, and found
4 droplet rebound at contact angle 163° and no rebound at contact angle 140° . Aria and
5 Gharib [24] studied droplet impact dynamics on super-hydrophobic carbon nanotube
6 arrays by focusing on the critical Weber number, coefficient of restitution, spreading
7 factor and contact time. Their results showed excellent water repellency with no
8 droplet pinning. Kwak et al. [25] looked at the effects of droplet velocity, surface
9 wettability, Weber number and the surface free energy on droplet impact on nano-
10 textured surfaces, and developed a relationship for transitions from rebound to wetting
11 and from rebound to splashing regimes. Tsai et al. [26] experimentally investigated
12 droplet impingement on super-hydrophobic surfaces with similar contact angles but
13 different surface roughness, i.e., one surface with regular polymeric micro-patterns
14 and the other with rough carbon nanofibers. Similar outcomes, including the Cassie
15 state, complete rebound, partial rebound, trapping of an air bubble, jetting, and sticky
16 vibrating water balls, were observed at small Weber numbers for both surfaces.
17 However, at larger Weber numbers, the splashing impacts forming several satellite
18 droplets were observed to be more favorable for rough carbon nanofiber surfaces.

19 Besides, Shen et al. [27] studied millimeter-scale droplet impingement on a convex
20 super-hydrophobic surface consisting of hierarchical micro-nano structures, and found
21 quicker rebound compared to flat surfaces and a reduction of 28.5% in the contact time.
22 However, in their study effects of post dimensions such as inter-post spacing, post
23 width and height, surface curvature and impact velocity were not investigated.

24 Different from the above studies, the current work is focused on fog droplet impact
25 dynamics on micro-scale bumps with nanotextures, inspired from desert beetle super-
26 hydrophobic surface's micro-scale hemispherical bumps. The state of droplet
27 subsequent to the impact can be crucial to water collection. A droplet impacting on
28 nano-textured bumps can either rebound or deposit. The rebounding droplet jumps
29 back to atmosphere, and is hence lost, which reduces the water collection rate. On the
30 other hand, the deposited droplet can have two possible states: the Cassie–Baxter state
31 (droplet remains suspended on the nanostructures) or the Wenzel state (droplet

1 penetrates the nanostructures and touches the bottom surface). Droplet in the Cassie
2 state can be easily removed from the surface and thus more favorable for water
3 collection, while the wetting and rebounding droplets may degrade the surface's water
4 collection efficiency. The state of droplet after the impact depends on the bump
5 geometrical parameters and impact velocity. Therefore, in the present study the focus
6 is placed on the effects of Weber number, post height, inter-post spacing and bump
7 surface curvature on the droplet impact dynamics. We aim to find the relationships
8 between bump geometrical parameters and Weber number, so as to determine the
9 parameter ranges where the Cassie state is promoted. These parameter ranges are
10 helpful in the design of bumps for better water collection.

11 **2. Problem Description**

12 Fig. 1 shows a schematic diagram of the problem. A droplet of diameter D impacts on
13 a bump with a velocity v , where the bump surface is made of nano-posts. The dynamics
14 of the droplet impact is influenced by the following key parameters: the gas density ρ_g
15 and viscosity μ_g , the liquid droplet diameter D , density ρ , viscosity μ , surface tension
16 σ , intrinsic contact angle θ_o , impact velocity v , height h and width w of the nano-post
17 and the bump radius R .

18 The fog droplets vary in size ($1\sim 50\ \mu m$) [8,28], and generally, the fog droplet-size
19 distributions have a single peak with a mode in the 10 to 14 μm range [28], while the
20 larger droplets contribute only little to fog liquid water content. In this study, the
21 droplet diameter is fixed at $D = 10\ \mu m$. The post dimensions are selected according to
22 literature [29–31] as follows: height up to $h = 5000\ \text{nm}$, inter-post spacing $s = 400\sim$
23 $2000\ \text{nm}$ and post width fixed at $w = 400\ \text{nm}$. The dimensionless bump curvature is
24 varied from $w/R = 1/180$ to $1/15$. The intrinsic contact angle is taken as $\theta_o = 110^\circ$. Due
25 to the numerical stability consideration, the liquid-to-gas density and viscosity ratios
26 are set as $\rho/\rho_g = \mu/\mu_g = 114.5$, instead of the actual ratios in nature. In previous studies
27 the wind speed for fog harvesting ranges from 1 to 9 m/s [28,32], which can be even
28 higher depending on the location. In this study, the droplet impact velocity v varies
29 from 1 to 15 m/s. Its effects are studied through varying the Weber number (We), the
30 ratio of the droplet inertia to its surface tension

1 $We = \rho U^2 D / \sigma$ (1)

2 The effect of gravity is described by the Bond number as

3 $Bo = \Delta \rho g D^2 / \sigma \sim 0.12 \times 10^{-6}$ (2)

4 where g is gravitational acceleration. Since Bo is very small in the present study, the
5 effect of gravity is neglected. Moreover, the surface tension is fixed at 0.04.

6 To describe the dynamics of impacting droplets, non-dimensional spreading factors
7 along the x axis (horizontal) and y axis (vertical), respectively, are defined as

8 $S_x^* = S_x / D$ (3)

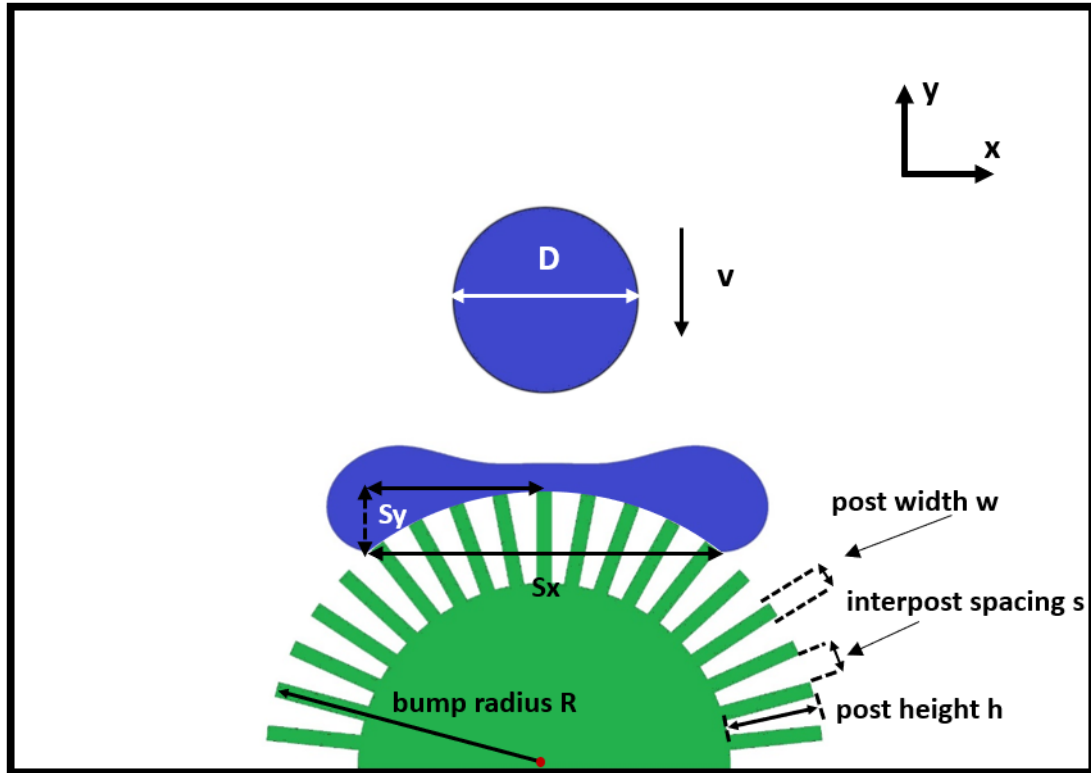
9 $S_y^* = S_y / D$ (4)

10 where S_x is the x spreading length defined as the horizontal distance between the two
11 contact lines on the surface with bump radius R , and S_y is the y spreading length
12 defined as the vertical distance from the top of the bump to either of the two contact
13 lines on the surface with bump radius R (see Fig.1).

14 Moreover, a non-dimensional time t^* is employed to describe temporal events

15 $t^* = vt / D$ (5)

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2 **Fig. 1. Droplet impact on hemispherical nano-textured bump.**

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3 **3. Methodology**

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4 In the present study, the multiple-relaxation-time lattice Boltzmann method (MRT-
 5 LBM) based on the model in Li et al. [34] is used. The fundamentals of LBM have
 6 been explained in many review articles [35,36] and monographs [37,38], and therefore
 7 are only briefly introduced here. The Shan-Chen [39] model achieves phase separation
 8 through incorporation of interparticle interaction forces. However, this model suffers
 9 from numerical instability at low viscosity. The current MRT-LBM model uses an
 10 improved forcing scheme to achieve thermodynamic consistency at relatively larger
 11 density ratios and Reynolds numbers. The wetting characteristics of the surface are
 12 achieved by computing a specific adhesion force between the gas/liquid phase and
 13 solid walls as explained in Benzi et al. [40].

14 The MRT-LBM is briefly explained for the brevity purpose and more information can
 15 be obtained from the reference [34]. The lattice Boltzmann equation with the MRT
 16 collision operator can be written as follows [41]:

$$1 \quad f_\alpha(\mathbf{x} + \mathbf{e}_\alpha \delta_t, t + \delta_t) = f_\alpha(\mathbf{x}, t) - (M^{-1} \Lambda M)_{\alpha\beta} (f_\beta - f_\beta^{eq}) + \delta_t \dot{F}_\alpha \quad (6)$$

2 where $f_\alpha(\mathbf{x}, t)$ is the density distribution function and f_β^{eq} is the equilibrium
3 distribution function, \mathbf{e}_α is the particle velocity at position \mathbf{x} , M is an orthogonal
4 transformation matrix [42], \dot{F}_α is the forcing term.

5 Using the transformation matrix M , the equation Eq. (6) can be written as

$$6 \quad m^* = m - \Lambda(m - m^{eq}) + \delta_t \left(I - \frac{\Lambda}{2} \right) S \quad (7)$$

7 where $m = Mf$ and $m^{eq} = Mf^{eq}$ represent the moment space of the distribution
8 function. I is the unit tensor the and $\left(I - \frac{\Lambda}{2} \right) S = M\dot{F}$ is the force in the moment
9 space. The collision and streaming process is expressed as

$$10 \quad f_\alpha(\mathbf{x} + \mathbf{e}_\alpha, t + \delta_t) = f_\alpha^*(\mathbf{x}, t) \quad (8)$$

11 The equilibria \mathbf{m}^{eq} is given as

$$12 \quad \mathbf{m}^{eq} = \rho(1, -2 + 3|v|^2, 1 - 3|v|^2, v_x, -v_x, v_y, -v_y, v_x^2 - v_y^2, v_x v_y)^T \quad (9)$$

13 where $|v|^2 = v_x^2 + v_y^2$

14 The macroscopic density and velocity are calculated as

$$15 \quad \rho = \sum_\alpha f_\alpha \quad (10)$$

$$16 \quad \rho \mathbf{v} = \sum_\alpha \mathbf{e}_\alpha f_\alpha + \frac{\delta_t}{2} \mathbf{F} \quad (11)$$

17 where $\mathbf{F} = (F_x, F_y)$ represent the total force, which includes the interparticle
18 interaction force F_{int} and fluid-solid interaction force F_{ads} [40].

19 The interparticle interaction force, which causes the phase segregation is given as
20 follows [39,43]

$$21 \quad F_{int} = -G\psi(\mathbf{x}) \sum_\alpha w(|\mathbf{e}_\alpha|^2) \psi(\mathbf{x} + \mathbf{e}_\alpha) \mathbf{e}_\alpha \quad (12)$$

22 where G is the interaction strength and $w(|\mathbf{e}_\alpha|^2)$ are the weights. $\psi(\mathbf{x})$ is The
23 effective mass [34]. An improved forcing scheme [34] is used to incorporate the forces

$$S = \begin{bmatrix} 6\mathbf{v} \cdot \mathbf{F} + \frac{\gamma|F_m|^2}{\psi^2 \delta_t(\tau_e - 0.5)} \\ -6\mathbf{v} \cdot \mathbf{F} - \frac{\gamma|F_m|^2}{\psi^2 \delta_t(\tau_e - 0.5)} \\ F_x \\ -F_x \\ F_y \\ -F_y \\ 2(v_y F_y - v_x F_x) \\ v_x F_y - v_y F_x \end{bmatrix} \quad (13)$$

where \mathbf{F} denotes the total force, \mathbf{v} is the fluid velocity, γ is tuning parameter for the mechanical stability and $|F_m|^2 = F_{m,x}^2 + F_{m,y}^2$.

3.1. Computational domain and boundary conditions

The computational domain is a two-dimensional rectangular box (1800 x 1800) (Fig. 1). Periodic boundary conditions are applied on the left and right sides of the domain. The half-way bounce-back method is employed on the top and bottom sides as well as on the post surfaces to realize the no-slip boundary condition.

A grid independence test has been conducted using four different sets of lattice-unit-to-physical-unit conversion factors. Changing the conversion factor affects the droplet spreading and retraction dynamics. Simulations are conducted for droplet impacts with initial diameter $D = 10 \mu\text{m}$ on bumps with post height $h = 3000 \text{ nm}$ and width $w = 400 \text{ nm}$, inter-post spacing $s = 800 \text{ nm}$, and bump radius $R = 45 \mu\text{m}$. Both the maximum horizontal and maximum vertical spreading factors are listed in Table 1. It is seen that the values produced from the conversion factor of $1 \text{ lu} = 20 \text{ nm}$ has the relative errors less than 1% compared to those from the smallest conversion factor $1 \text{ lu} = 12.5 \text{ nm}$. Hence, it is selected for the following simulations. Furthermore, to check the boundary effects on droplet dynamics a simulation case with large grid size (3600 x 3600) is conducted. The relative errors of -0.45% and -0.6% are found for the maximum spreading factors along x-axis and y-axis, respectively, for the small grid (1800 x 1800) with respect to larger grid, showing the boundary effects on maximum spreading factors are small.

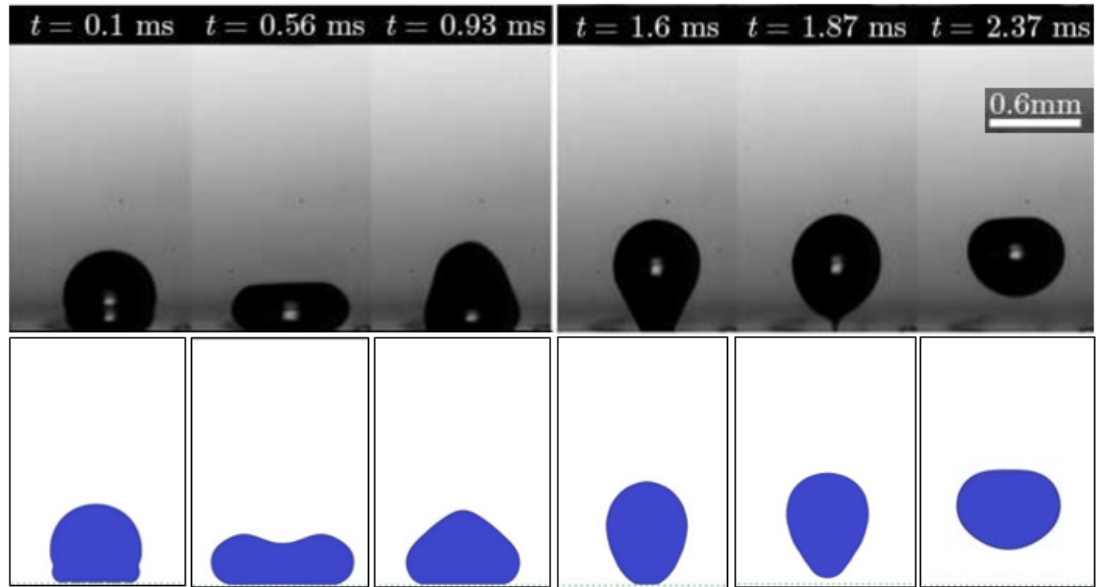
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Table 1 Results of grid independence tests

| | | | | |
|---|-----------------|-----------------|-----------------|-------------------|
| Lattice to physical unit conversion factor | 1 lu = 40 nm | 1 lu = 25 nm | 1 lu = 20 nm | 1 lu = 12.5 nm |
| Max S_x^* | 1.96 | 1.765 | 1.748 | 1.74 |
| Relative error (%) | -12.64 | -1.43 | -0.45 | - |
| Max S_y^* | -0.1 | -0.0824 | -0.082 | -0.0825 |
| Relative error (%) | -21.2 | 0.12 | 0.60 | - |

2 **3.2. Validation**

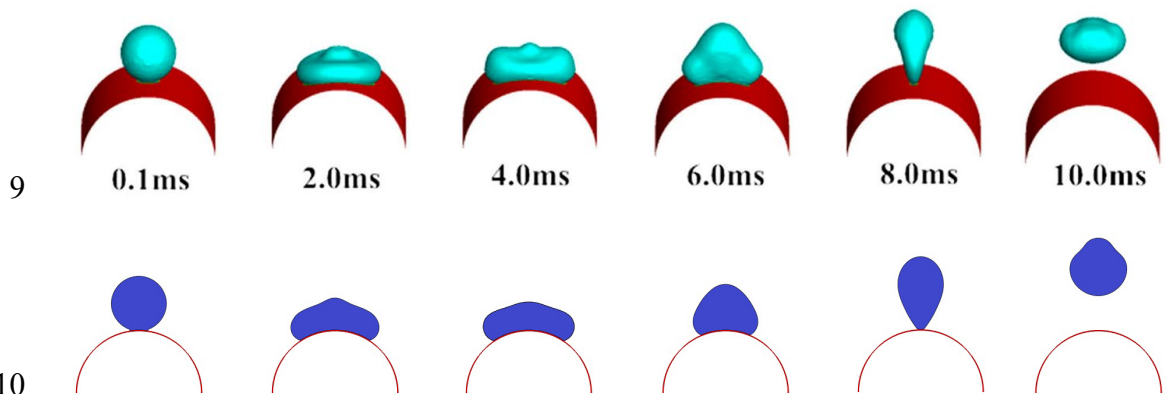
3 The simulated impact and subsequent rebound of a droplet on a micro-textured surface
4 are compared with experimental results. Bobinski et al. [44] studied a droplet of
5 diameter $D = 0.6$ mm impacting and rebounding with a Weber number 2.6 on a micro-
6 structure of post height $h = 10$ μm , post width $w = 8$ μm and inter-post spacing $s = 22$
7 μm . The impact velocity corresponding to Weber number 2.6 gives the Reynolds
8 number $\text{Re} \sim 336$ for the deionized water droplet. Due to limitations of numerical
9 method, some of the parameters are adjusted, such as the density and viscosity ratios
10 different from those between water and air are used (see section 2), to obtain the We
11 $= 2.6$ and $\text{Re} \sim 336$ in the simulations. The LBM simulations are conducted and the
12 snapshots of droplet evolution at selected instants are compared with the experimental
13 results in Fig. 2. Although slight over-prediction in spreading is observed at instants t
14 $= 0.56$ and 0.93 ms, good agreements in droplet retraction and rebound can be observed
15 at later stages.



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2 **Fig. 2. Snapshots of droplet impacting on micro-textured surface. Top row:**
 3 **experimental results [44]; Bottom row: current simulation results.**

4 In another validation case, the LBM results of droplet impact on a curved surface are
 5 compared with the Coupled Level Set and Volume of Fluid (CLSVOF) method [45].
 6 The droplet and curved surface diameters are 1.76 mm and 4 mm, respectively. The
 7 impact velocity is 0.5 m/s. It seen from Fig. 3, the current LBM is able to capture
 8 droplet rebound from the curved surface with reasonable qualitative agreement.



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11 **Fig. 3. Snapshots of droplet impacting on curved surface. Top row: CLSVOF**
 12 **results [45]; Bottom row: current simulation results.**

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1 **4 Results and discussion**

2 **4.1 Baseline case**

3 A case with the Weber number $We = 19.6$ and Reynolds number $= 120$, post height
4 $h/w = 7.5$, inter-post spacing $s/w = 2$ and bump curvature $w/R = 2/225$ is analyzed as
5 the baseline case. The evolution of the droplet's two spreading factors with several
6 selected snapshots are shown in Fig. 4. It is seen that the droplet nearly jumps off the
7 nano-structured bump after its first impact with only a small area remained in contact
8 with the central post, and then impacts again (second impact) with much lower energy
9 due to solid-liquid interactions and surface tension. As a result, the two spreading
10 factors oscillate with time.

11 During the first half of the initial impact ($t^* < 1.53$), the impacting droplet penetrates
12 to the inter-post gaps. The resulting lamella spreads both horizontally and vertically
13 on the bump till achieving the maximum spreading $S_{x,max}^* = 1.74$ and $S_{y,max}^* = -0.082$
14 at $t^* = 1.53$ (Fig. 4(d)), which is also reflected by the velocity vectors in the droplet
15 shown in Fig. 5(a). Note that the horizontal spreading evolves in a stepwise manner
16 due to the separate posts (see the insets in Fig. 4).

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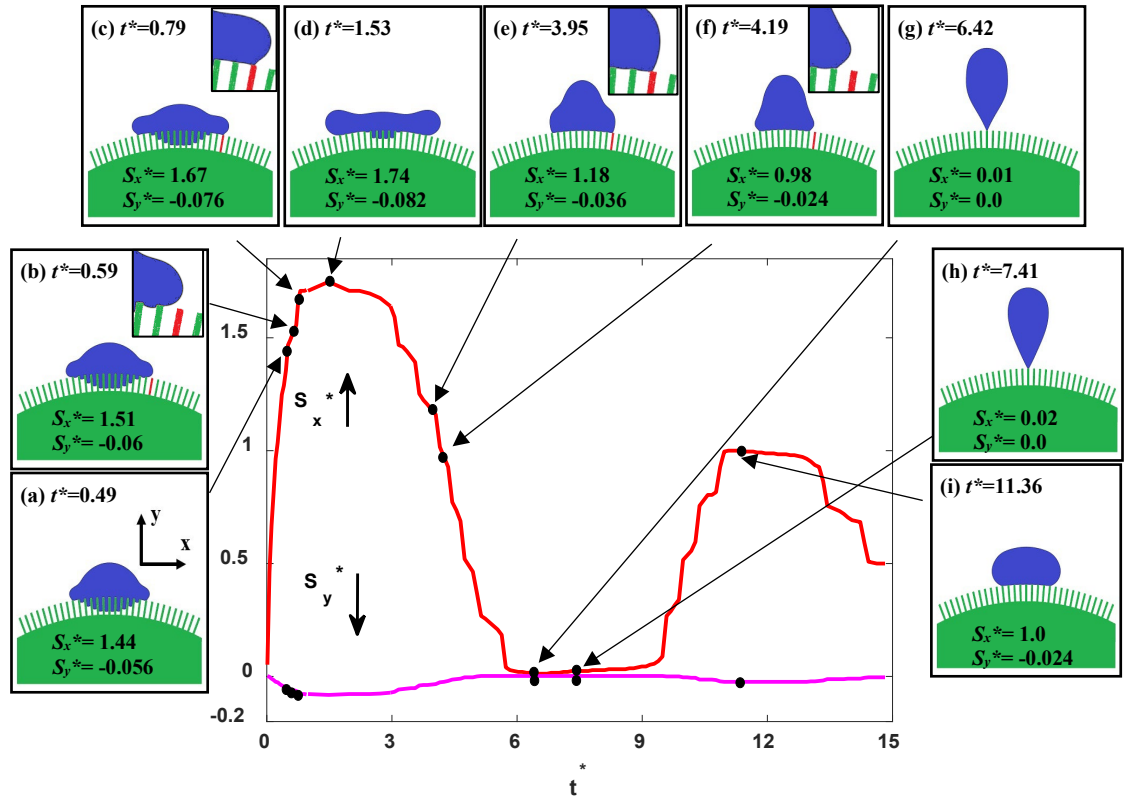
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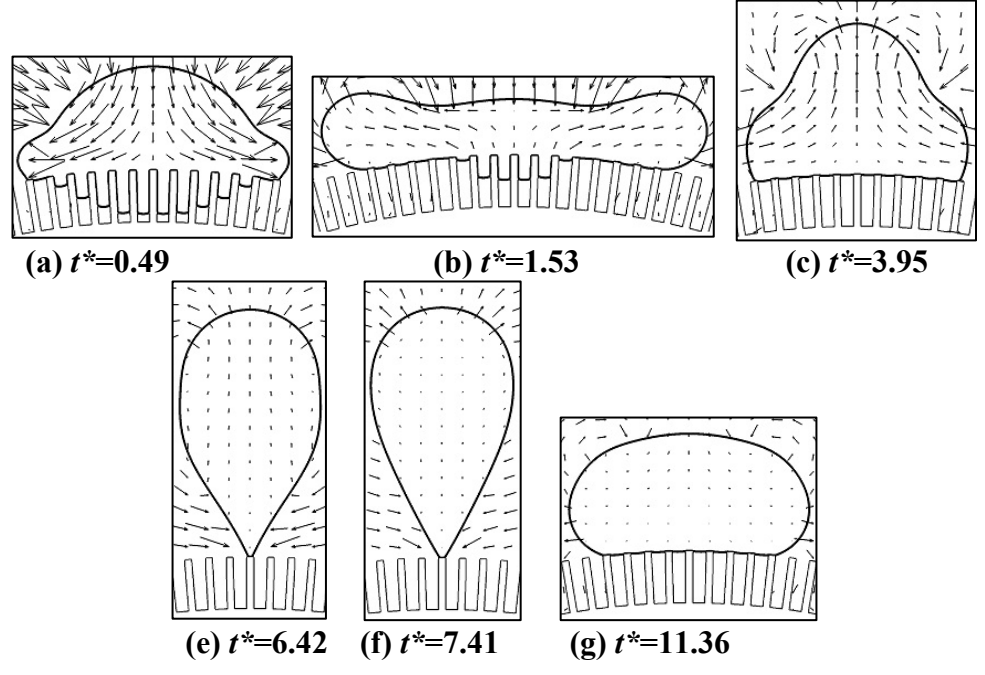
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Fig. 4. Evolution of the spreading factors in the baseline case, where the post height $h/w = 7.5$, inter-post spacing $s/w = 2.0$, bump curvature $w/R = 2/225$, and the Weber number $We = 19.6$.

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Fig. 5. Velocity vectors in the baseline case at selected instants.

1 From the energy point of view, the droplet's initial kinetic energy results in its
2 penetration to the inter-post gaps. During this penetration process the kinetic energy is
3 stored as the surface energy of the deformed droplet [46,47]. If the droplet's initial
4 kinetic energy is high enough to collapse the air-pockets contained in inter-post gaps,
5 the penetrating droop can touch the bottom surface, leading to the transition to the
6 sticky Wenzel state.

7 During the second half of the initial impact ($1.53 < t^* < 7.41$), the surface tension plays
8 a major role to retract the lamella (Figs. 4(e), 4(f) and 5(c)). Both the spreading factors
9 reduce in magnitude, resulting in the decrease of surface area. The red color posts in
10 subfigures (e and f) of Fig. 4 explain the formation of slightly vertical and horizontal
11 variations of spreading factor S_x^* during the retraction process. The lamella quickly
12 retracts back from red post at time $t^*=3.95$ in subfigure(f) to neighboring green post at
13 time $t^*=4.19$, producing a slightly vertical segment of spreading factor (Fig. 4). Then,
14 the retraction occurs on the post, producing a small roughly horizontal segment in
15 spreading factor evolution curve. During droplet retraction process, the stored surface
16 energy is transferred back into the kinetic energy. The lamella then gains an upward
17 velocity due to the constraint from the underneath bump, nearly jumping off the bump
18 (Figs. 4(g) and 4(h)).

19 After about $t^* = 7.41$, another spreading and retraction process occurs. However, due
20 to the energy dissipation, the peak magnitudes of both horizontal and vertical
21 spreading factors appearing at near $t^* = 11$ are much smaller than those in the first
22 impact. This impacting process will repeat a few times till the droplet achieves its
23 equilibrium state on the bump, which is not presented here since the present study
24 mainly focuses on the droplet's dynamics in the first spreading and retraction cycle
25 that is crucial to its final wetting state.

26 **4.2 Effect of post height**

27 Figure 6 compares the droplet impacting on bumps with three different post heights,
28 i.e., $h/w = 0$ (bump with smooth surface), 2.5 and 7.5 (the baseline case). The
29 corresponding evolutions of spreading factors are shown in Fig. 7. It is seen that both
30 the maximum horizontal and maximum vertical spreading factors reduce with the post

1 height, which is caused by increased room in the inter-post gaps and hence increased
2 stored surface energy during the droplet penetration. For the bump with $h/w = 7.5$ (i.e.,
3 the baseline case), the liquid droop in the inter-post gaps never reaches the bottom
4 surface, so that the droplet remains in the Cassie state. However, if the bump height
5 reduces to $h/w = 2.5$, the liquid droop touches the bottom surface, leading to the
6 Wenzel state.

7 From Fig. 7, it is also interesting to see that, although the spreading on different bumps
8 during the first impact completes almost at the same instant, the ensuing droplet
9 retraction on the textured bumps is generally faster than on the smooth bump. If the
10 Cassie state occurs as in the $h/w = 7.5$ case, during the retraction more kinetic energy
11 is transferred back from the stored surface energy, resulting in faster retraction. On the
12 other hand, if the Wenzel state occurs as in the $h/w = 2.5$ case, the extent of retraction
13 in the horizontal direction is significantly reduced due to the restriction from the wetted
14 bump bottom surface. For this reason, the retraction process is completed even earlier.

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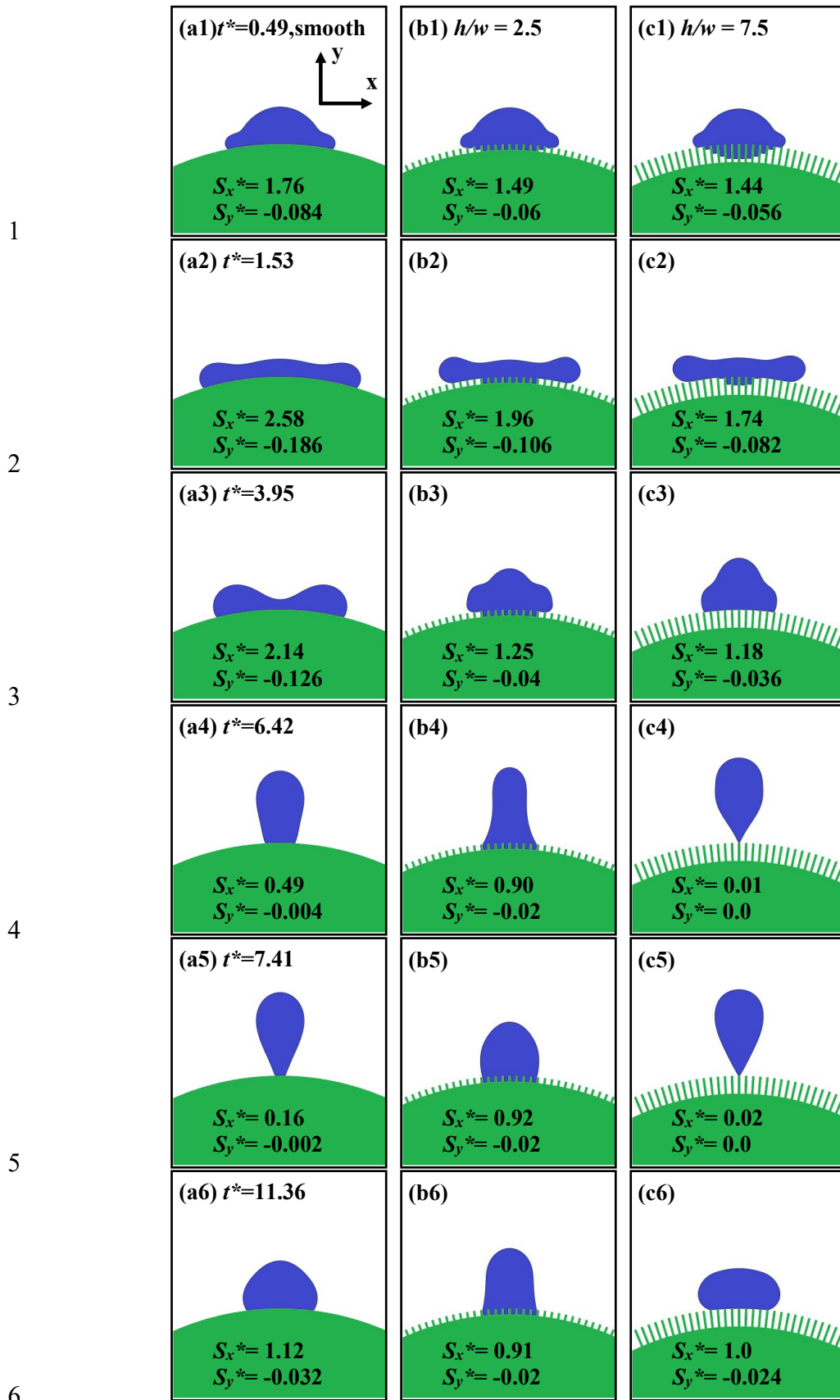
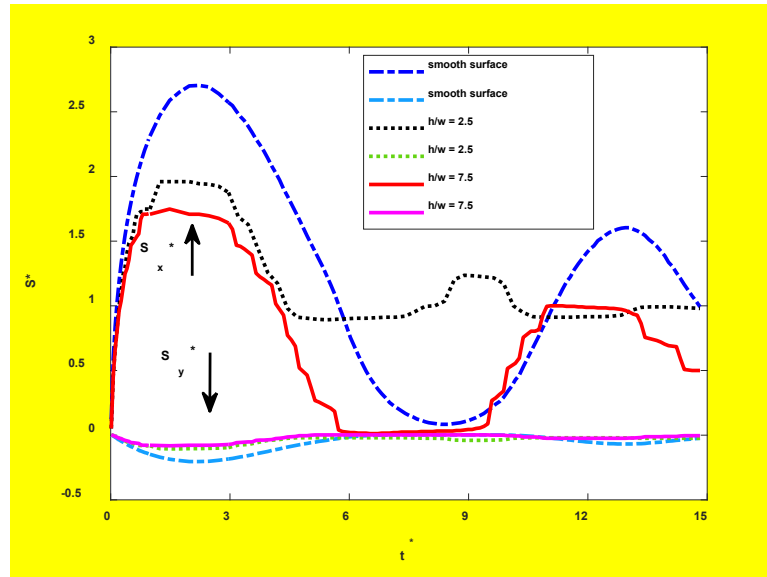


Fig. 6. Evolution of the droplet impact on bumps with different post heights.



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2 **Fig. 7. Evolution of the spreading factors of droplet impact on bumps with**
 3 **different post heights.**

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5 **4.3 Effect of inter-post spacing**

6 Figure 8 shows the evolution of droplet impact on nano-textured bumps with different
 7 inter-post spacings, i.e., $s/w = 1, 2$ (the baseline case) and 3. It is seen that, since more
 8 liquid penetrates into inter-post gaps, the droplet horizontal and vertical spreading
 9 reduces with increasing the inter-post spacing, which is also confirmed by the
 10 spreading factor curves shown in Fig. 9. Droplet rebound is observed in the case with
 11 the smallest inter-post spacing $s/w = 1$ (see Fig. 8(a6)), the Cassie state is achieved in
 12 the baseline case with moderate inter-post spacing $s/w = 2$, and the Wenzel state is
 13 obtained in the case with the largest inter-post spacing $s/w = 3$ (see Fig. 8(c6)). The
 14 rebound appearing in the $s/w = 1$ case can be understood by generation of upward
 15 velocity due to vertical retraction [27]. As witnessed from Fig. 10 a larger upward
 16 velocity is produced due to the largest vertical retraction (see Fig. 9) combined with
 17 the surface-kinetic energy conversion of the initially penetrated liquid, leading to
 18 droplet rebound. On the contrary, the occurrence of the sticky Wenzel state
 19 significantly limits the spreading and retraction of the droplet.

20 If the inter-post spacing is further reduced, it is expected that the horizontal and vertical
 21 spreading will be further increased, as reflected by the snapshots and spreading factor

1 curves in the extreme case, i.e., the smooth bump case discussed in Section 4.2.
 2 However, the reduced inter-post spacing also causes the increase of the contact area
 3 on the nano-textured bump, hence dissipates more energy through the friction between
 4 the liquid and the solid. In this case, the droplet may no longer has adequate surface-
 5 kinetic energy conversion to support rebound after the first impact [48], as reflected in
 6 the smooth bump case.

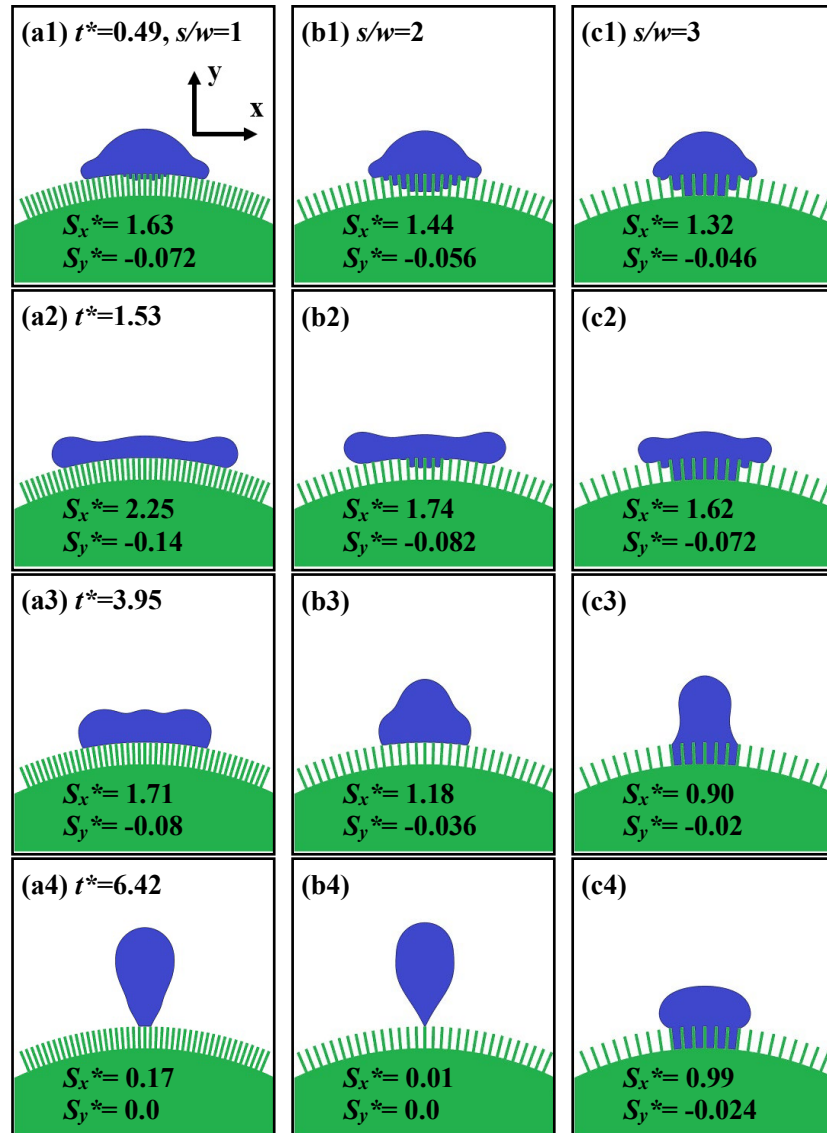
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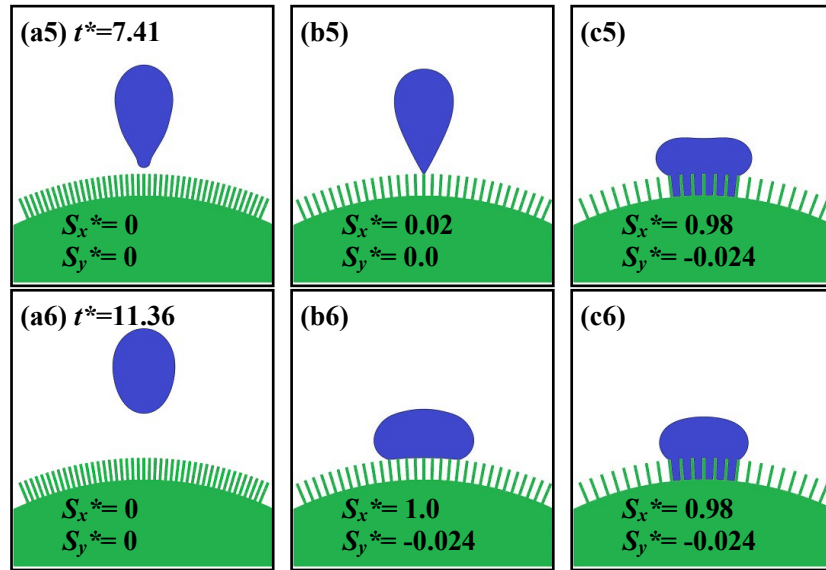
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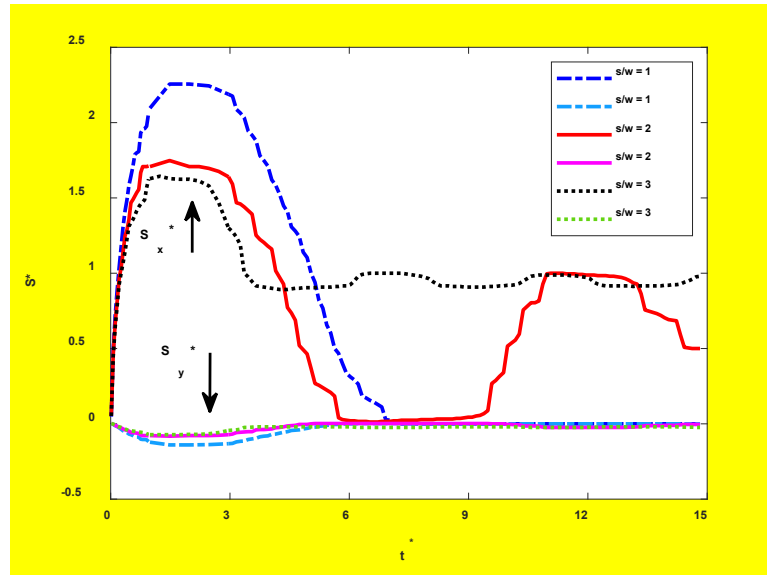
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Fig. 8. Evolution of droplet impact on nano-textured bumps with different inter-post spacing: (a) $s/w = 1.0$, (b) $s/w = 2.0$, (c) $s/w = 3.0$.

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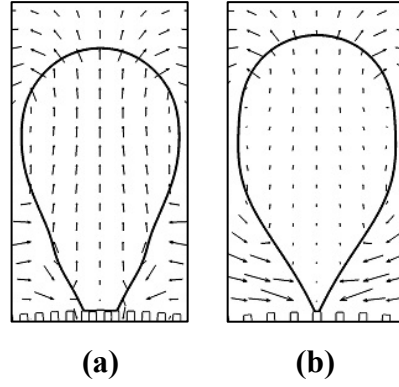


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Fig. 9. Evolution of spreading factors of droplet impact on nano-textured bumps with different inter-post spacing: $s/w = 1.0$, $s/w = 2.0$, $s/w = 3.0$.



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3 **Fig. 10. Velocity vectors during retraction phase at $t^* = 6.42$ for (a) inter-post**
4 **spacing $s/w=1.0$, (b) inter-post spacing $s/w=2.0$.**

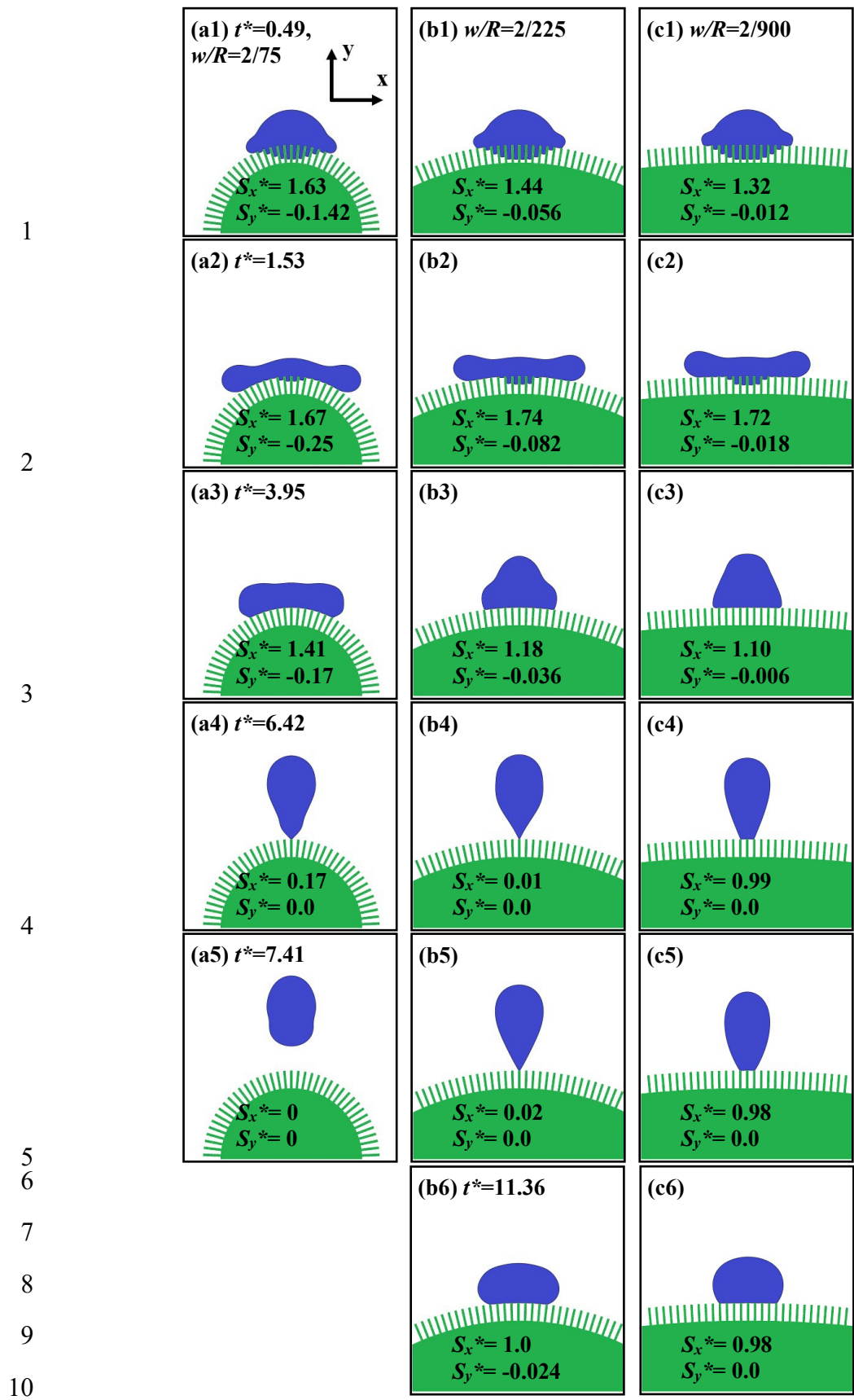
5 **4.4 Effect of bump curvature**

6 Droplet dynamics on bumps with three different surface curvature, i.e., $w/R = 2/75$,
7 $2/225$ (the baseline case) and $2/900$ are compared through selected snapshots in Fig.
8 11 and evolution of spreading factors in Fig. 12. It is seen from Fig. 11 that the droplet
9 rebounds on the bump with the largest curvature, while assumes the Cassie state on
10 the other two bumps.

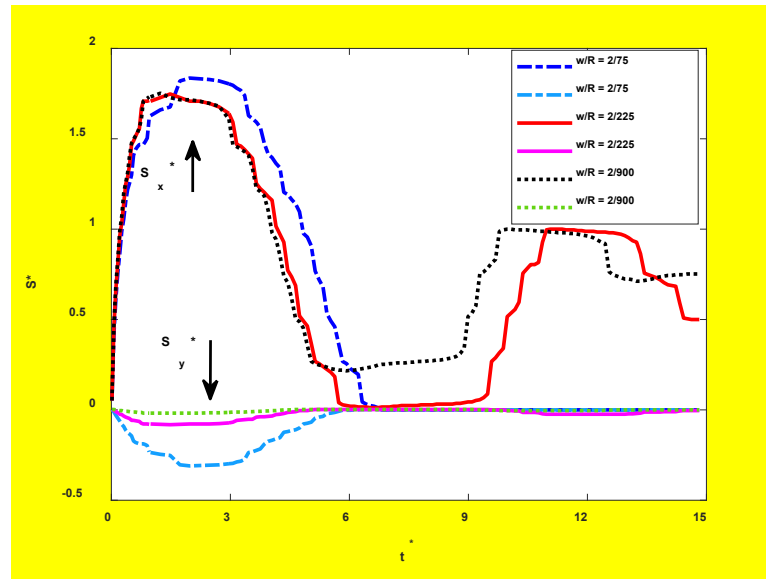
11 When the bump is nearly flat with the smallest curvature $w/R = 2/900$, the horizontal
12 spreading dominates over the negligible vertical spreading, as shown in Fig. 12. The
13 maximum horizontal and vertical spreading factors are $S_{x,\max}^* = 1.74$ and $S_{y,\max}^* = -$
14 0.0018 , respectively, both appearing at $t^* = 1.23$. The increase of bump curvature
15 allows the droplet to spread more in the vertical direction and even in the horizontal
16 direction. As revealed in Fig. 12, the $w/R = 2/225$ bump has a similar maximum
17 horizontal spreading but a much larger maximum vertical spreading $S_{y,\max}^* = -0.082$ as
18 compared with the $w/R = 2/900$ bump. As for the $w/R = 2/75$ bump, both the maximum
19 spreading factors increase significantly, i.e., $S_{x,\max}^* = 1.83$ and $S_{y,\max}^* = -0.310$.

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1 **Fig. 11. Evolution of droplet impact on nano-textured bumps with different bump**
 2 **curvature: (a) $w/R = 2/75$, (b) $w/R = 2/225$, (c) $w/R = 2/900$.**



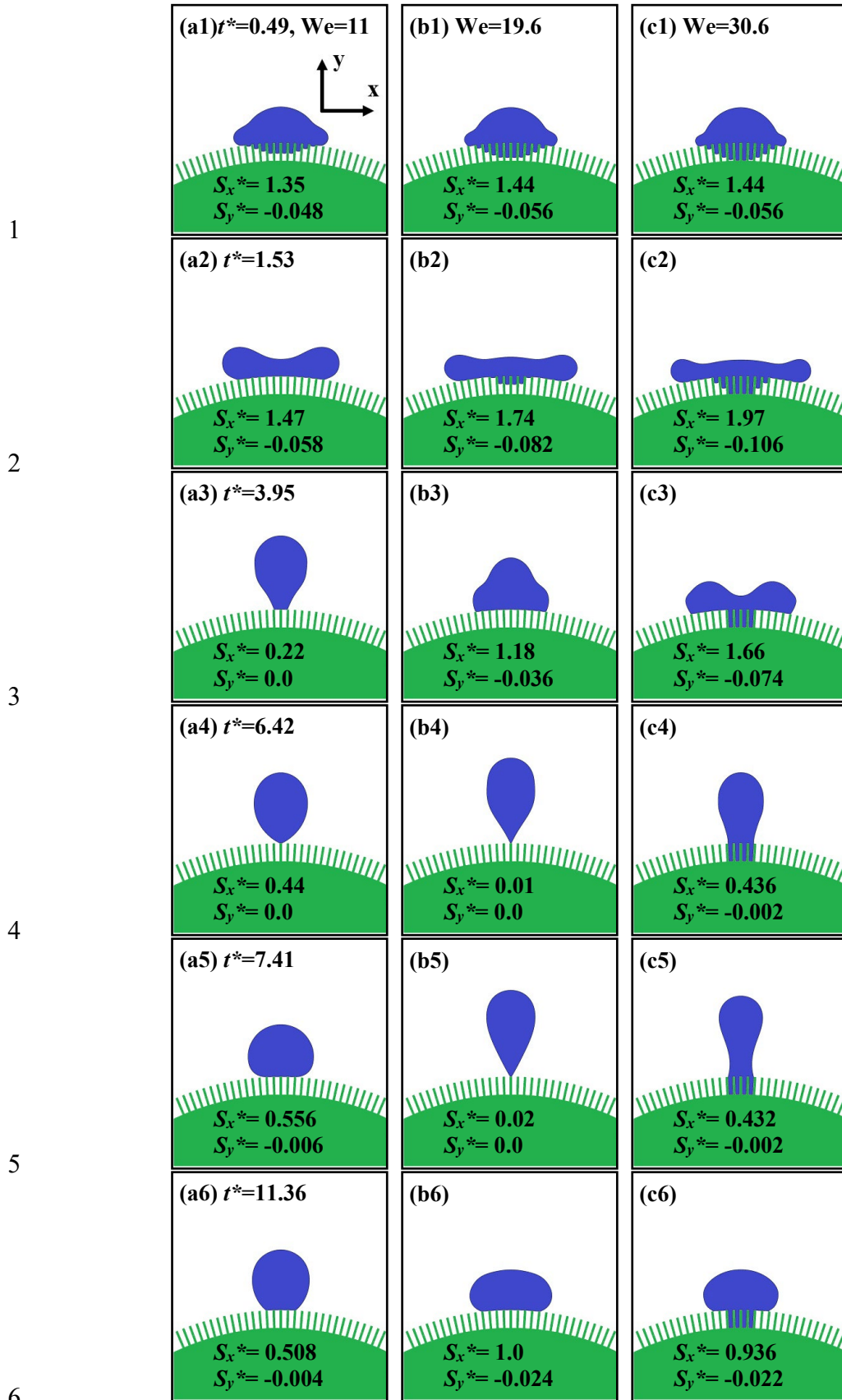
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 4 **Fig. 12. Evolution of spreading factors for nano-textured bumps with different**
 5 **bump curvature: $w/R = 2/75$, $w/R = 2/225$, $w/R = 2/900$.**

6 **4.5 Effect of impact speed**

7 Figure 13 compares the dynamics of droplet impacting on a bump with three different
 8 impact speeds, i.e., 9 m/s, 12 m/s and 15 m/s, corresponding to the Weber number We
 9 $= 11.0, 19.6$ (the baseline case) and 30.6 , respectively. Apparently increasing the
 10 Weber number increases the penetrating droop depth. With the highest impact speed
 11 as in the $We = 30.6$ case, the liquid droplet touches the bottom surface very soon leading
 12 to the Wenzel transition (Fig. 13(c1)). In the other two cases with lower Weber
 13 numbers, the Cassie state is achieved (Figs. 13(a6) and 13(b6)).

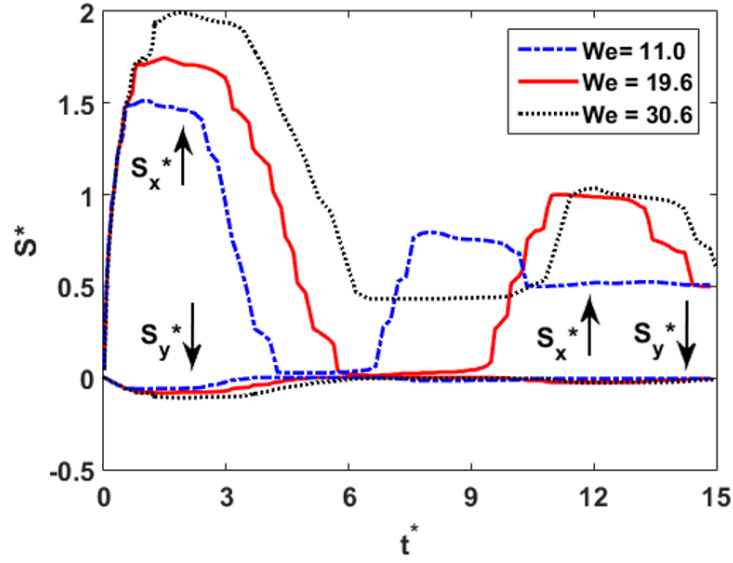
14 The spreading factor evolution curves shown in Fig. 14 reveal that the maximum
 15 horizontal and vertical spreading factors both increase with the Weber number simply
 16 due to the increase of kinetic energy carried by the impacting droplet. The time
 17 required to achieve the maximum spreading factors are $t^* = 0.91, 1.53$ and 1.7 ,
 18 respectively, also increasing with the Weber number.

19



7 Fig. 13. Evolution of droplet impact on nano-textured bumps with different
 8 Weber numbers (a) $We=11$ (b) $We=19.6$ and (c) $We=30.6$.

1



2

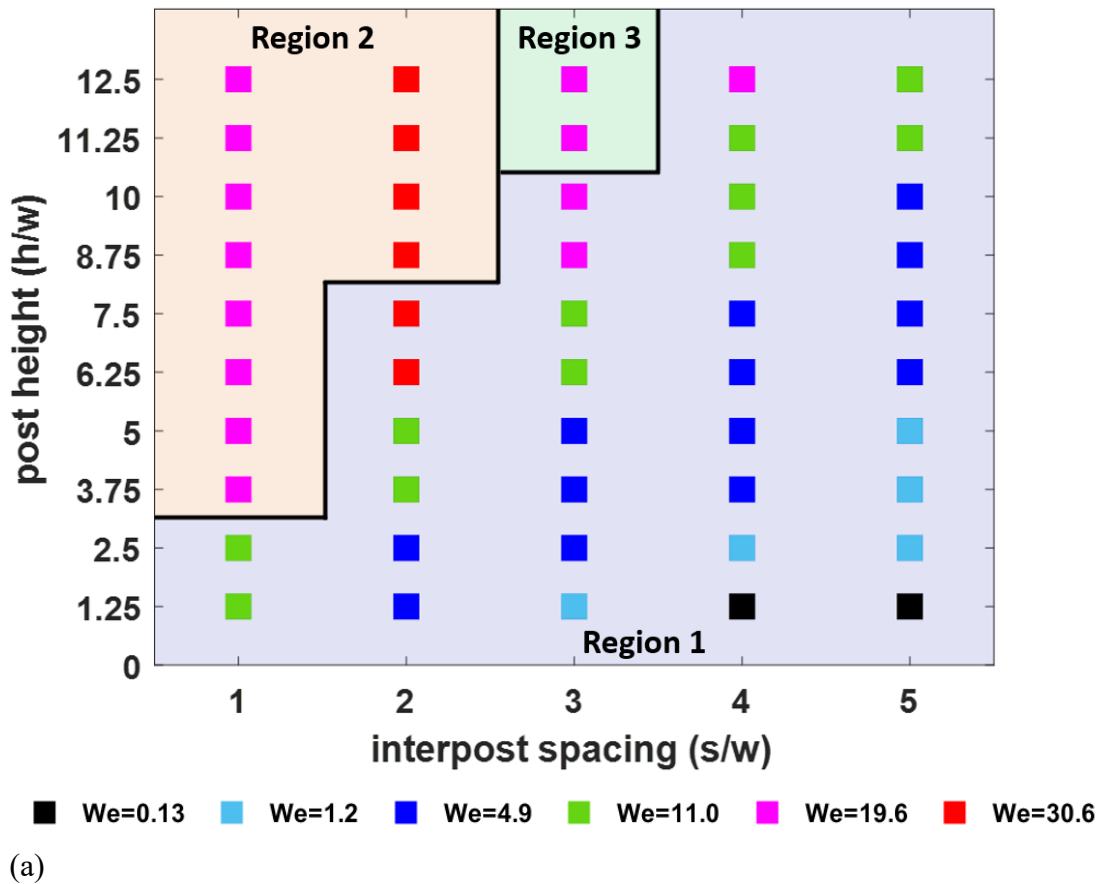
3 **Fig. 14. Evolution of spreading factors of droplet impact on nano-textured bumps**
 4 **with different Weber numbers.**

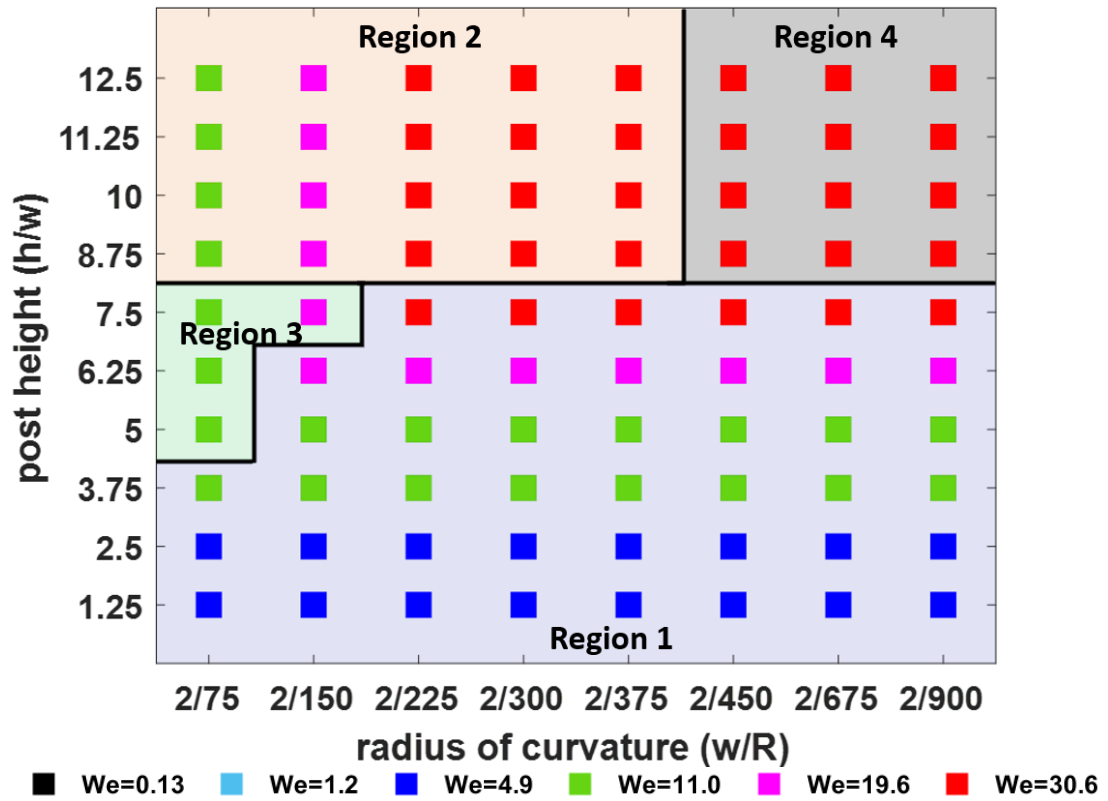
5 **4.6 Parametric maps describing the state of impacting droplet**

6 A comprehensive view of the dependence of the impacting droplet's wetting state on
 7 the bump parameters is presented in Fig. 15, where the Weber number is represented
 8 by square markers. In Fig. 15(a), the inter-post spacing varies from $s/w = 1$ to 5 and
 9 the post height varies from $h/w = 1.25$ to 12.5, while the bump curvature is fixed at
 10 $w/R = 2/225$. If the droplet's impact speed increases from 0 to 15 m/s (equivalently the
 11 Weber number increases from 0 to 30.6), three types of interfaces are captured: the
 12 blue interface (region 1) separates the Cassie state for Weber number less than the
 13 shown values from the Wenzel state for Weber number not less than the shown values,
 14 the orange interface (region 2) separates the Cassie state for Weber number less than
 15 the shown values from the rebound state for Weber number not less than the shown
 16 values, and the green interface (region 3) separates the Cassie state for Weber number
 17 less than the shown values from the rebound state for Weber number equal to the
 18 shown values and the Wenzel state for Weber number greater than the shown values.
 19 From these interfaces, one can see that, on bumps with tall posts and narrow inter-post
 20 spacing, the Cassie state is dominant at small to moderate Weber numbers, whereas
 21 the droplet rebounds at high Weber numbers. On the other hand, on bumps with short
 22 posts and wide inter-post spacing, the Wenzel state can be obtained easily even at very

1 small Weber numbers. Furthermore, the green interface indicates that on bumps with
 2 tall posts and moderate inter-post spacing, the state of the droplet depends very much
 3 on the droplet's impact speed: with the increase of speed, the droplet can experience
 4 different wetting dynamics from the Cassie state, rebound to the Wenzel state.

5 Fig. 15(b) further includes the bump curvature, which varies from $w/R = 2/75$ to $2/900$,
 6 while fixing the inter-post spacing at $s/w = 2$. In addition to the three types of interfaces
 7 (regions 1-3) presented in Fig. 15(a), Fig. 15(b) also presents a gray interface (region
 8 4), which indicates that the Cassie state holds throughout the entire range of
 9 investigated Weber numbers. From all these interfaces, one can see that, on bumps
 10 with short posts, the Wenzel state is dominant no matter how curved the bump surface
 11 is. On bumps with high posts, however, the bump curvature matters: when the bump
 12 is less curved, the droplet remains the Cassie state throughout the entire range of the
 13 investigated Weber numbers, whereas when the bump is more curved, the droplet tends
 14 to rebound if the impact speed is large enough.





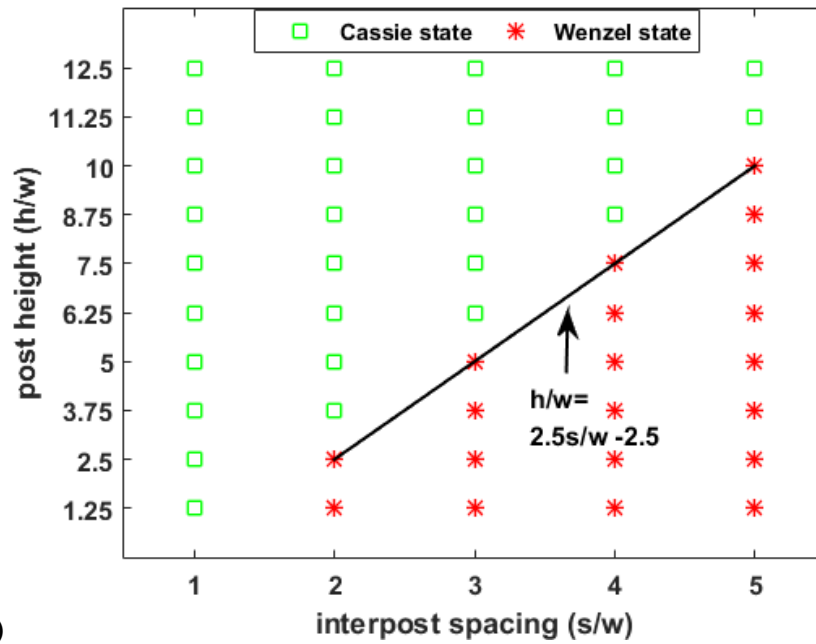
1
2
3

(b)

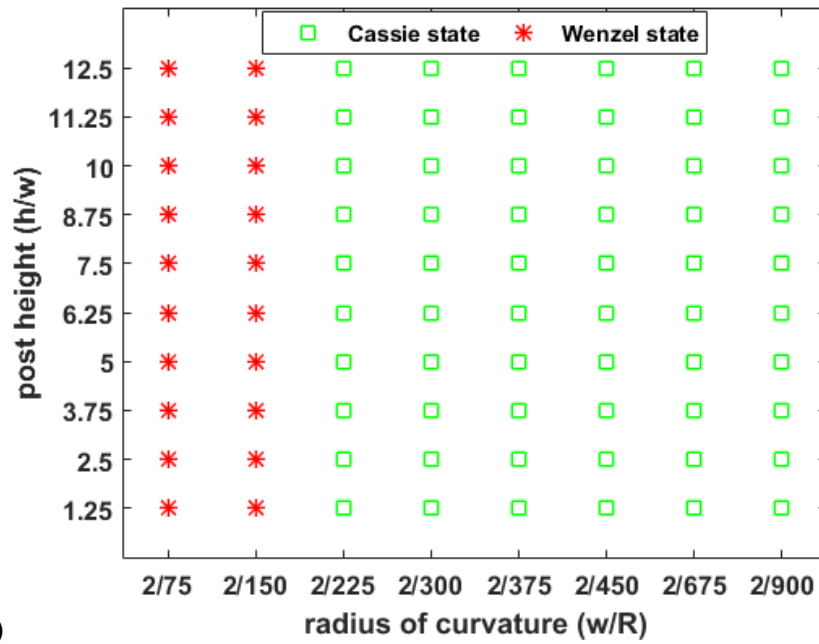
4 **Fig. 15. (a) Parametric map spanned by the post height, interpost spacing and**
5 **Weber number, where the bump curvature is fixed at $w/R = 2/225$ (b) Parametric**
6 **map spanned by the post height, bump surface curvature and Weber number,**
7 **where the inter-post spacing is fixed at $s/w = 2$. Region 1 (in blue): interface**
8 **between the Cassie state (when the Weber number is less than values shown by**
9 **square makers in the region) and the Wenzel state (when the Weber number is**
10 **equal to or greater than values shown by square makers in the region); region 2**
11 **(in orange): interface between the Cassie state (when the Weber number is less**
12 **than values in the region) and the rebound (when the Weber number is equal to**
13 **or greater than values in the region); region 3 (in green): interface between the**
14 **Cassie state (when the Weber number is less than values in the region) and the**
15 **rebound (when the Weber number is equal to values in the region) and the**
16 **Wenzel state (when the Weber number is greater than values in the region);**
17 **region 4 (in grey): no change of the Cassie state in the investigated We range. The**
18 **square markers represent the different values of Weber number by different**
19 **colors.**

20 It is particularly meaningful to examine the droplet dynamics at a moderate and
21 possibly mean impact speed, say $U = 6$ m/s (corresponding to $We = 4.9$). Since droplets
22 in the Cassie state remain suspended on the nanostructures and are much easier to
23 collect compared to those in the Wenzel or rebound state, the Cassie state is desirable

1 for fog water harvesting. Fig. 16(a) depicts a roughly straight boundary between the
 2 Cassie state and the Wenzel state. At the moderate impact speed, the Cassie state can
 3 be achieved for nearly all posts if the interpost spacing is small but only for larger posts
 4 if the interpost spacing is wide, when the bump curvature is mild, e.g., at $w/R = 2/225$.
 5 Fig. 16(b) further reveals that, when the inter-post spacing is fixed at $s/w = 2$, the
 6 droplet is in the Cassie state if the bump curvature is smaller than $w/R = 2/150$. The
 7 bump curvature seems to have very little influence on the droplet state.



8 (a)



1 (b)

2 **Fig. 16. Parametric maps showing the state of droplet dynamics when the droplet**
 3 **impact speed is moderate ($U = 6$ m/s, $We = 4.9$): (a) map spanned by the post**
 4 **height and inter-post spacing, where the bump curvature is fixed at $w/R = 2/225$**
 5 **(b) map spanned by the post height and bump surface curvature, where the inter-**
 6 **post spacing is fixed at $s/w = 2$.**

7

8 5 Conclusions

9 In this work, LBM-based simulations were conducted to study the dynamics of single
 10 fog droplet impacting on desert beetle inspired nano-textured bumps. The focus was
 11 placed on several key parameters, including post height, inter-post spacing, bump
 12 curvature and impact speed. Parametric maps describing the state of impacting droplet
 13 (i.e., the Cassie state, the Wenzel state or rebound) were obtained. The major
 14 conclusions are summarized as follows:

- 15 1. Adding nano-posts on a bump surface changes the morphology of droplet during
 16 the impact. That is, the penetration of droplet to the inter-post gaps causes the
 17 reduction of droplet spreading. If the penetration is so deep that the droplet touches
 18 the bottom surface, the undesirable Wenzel state occurs.

- 1 2. The separate posts reduce the total area on the bump top surface, which greatly
2 reduces frictional dissipation during the impact. As a result, the droplet can retract
3 with higher energy if appropriate inter-post spacing is adopted.
- 4 3. The droplet impact speed needs to be low or moderate (approximately $U < 6$ m/s
5 or $We < 4.9$ in this study) to ensure the occurrence of the desirable Cassie state.
6 On the contrary, too large impact speeds can result in either the Wenzel state or
7 rebound.
- 8 4. At moderate impact speeds, the post needs to be sufficiently high and the inter-
9 post spacing needs to be sufficiently small to achieve the desirable Cassie state. If
10 these conditions are satisfied, the bump curvature only plays a marginal role.

11 Note this study is still very limited since some parameters were fixed. However, it has
12 shed some lights on the physics and design of desert beetle inspired bumps for fog
13 water harvesting. In the near future, we will continue this study in a larger parameter
14 space and with more realistic parameter values.

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