

Adaptive Feedforward and Feedback Control Schemes for Sliding Mode Controlled Power Converters

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Abstract—A major disadvantage of applying sliding mode control to dc/dc converters is that the steady-state switching frequency is affected by line and load variations. This is undesirable as it complicates the design of the input and output filters. To reduce switching frequency deviation in the events of line and load variations, an adaptive feedforward control scheme that varies the hysteresis band according to the change of line input voltage and an adaptive feedback control scheme that varies the control parameter (i.e., sliding coefficient) according to the change of the output load are proposed. This paper presents a thorough investigation into the problem and the effectiveness of the proposed solutions. In addition, methods of implementing the proposed adaptive control strategies are discussed. Experimental results confirm that the adaptive control schemes are capable of reducing the switching frequency variations caused by both line and load variations.

Index Terms—Adaptive feedback control, adaptive feedforward control, buck converter, hysteresis modulation, pulse-width-modulation (PWM), sliding mode (SM) control.

I. INTRODUCTION

SLIDING MODE (SM) controllers are well known for their stability and robustness against parameter, line, and load variations (i.e., their ability to handle large transient disturbances) [1]. The feasible application of SM controllers for controlling power converters has recently been reported [2], [3]. However, it has been shown that SM controlled converters generally suffer from significant switching frequency variation when the input voltage and output load are varied [3], [4]. This complicates the design of the input and output filters. Obviously, designing the filters under a worst-case (lowest) frequency condition will result in oversized filters. Hence, it is more desirable to operate the converters at a constant switching frequency that does not deviate too far from its nominal value.

Basically, there are three possible approaches in keeping the switching frequency of the SM controller constant. One approach is to incorporate a constant ramp or timing function directly into the controller [3], [5], [6]. The main advantage of this approach is that the switching frequency is constant under all operating conditions, and can be easily controlled through varying the ramp/timing signal. However, due to the imposition of the ramp or timing function onto the SM switching function, the resulting converter system suffers from deteriorated transient response.

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The other approach is to employ pulse-width modulation (PWM) instead of hysteresis modulation (HM) [7], [8]. In practice, this is similar to classical PWM control schemes in which the control signal is compared to the ramp waveform to generate a discrete gate pulse signal [9]. The advantages are that it does not need additional hardware circuitries since the switching function is performed by the PWM modulator, and that its transient response is not deteriorated. However, implementation is nontrivial in order to preserve the original SM control law, especially when both current and voltage state variables are involved.

In this paper, we consider the third approach for alleviating the problem of switching frequency variation in the HM based controller. Specifically, we consider the use of some form of adaptive control to contain the switching frequency variation [10]. For line variation, we propose an adaptive feedforward control that varies the hysteresis band in the hysteresis modulator of the SM controller in the event of any change of the line input voltage [11]. For load variation, we propose an adaptive feedback controller that varies the control parameter (i.e., sliding coefficient) with the change of the output load.

In this paper, we will present a thorough investigation into the problem of switching frequency variation due to the deviation of operating conditions, and the effectiveness of the proposed solutions in alleviating the problem. In addition, methods of implementing the proposed adaptive control strategies are discussed in detail. Finally, experimental results will be presented for verification.

II. REVIEW OF CONVENTIONAL SM CONTROLLED CONVERTERS

The system studied here is a buck converter controlled by a SM voltage mode controller, in which the state variables to be controlled are the output voltage error and the voltage error derivative (in phase canonic form). The theoretical model and analysis are summarized below. Details can be found in [4].

A. Converter's Model

Fig. 1 shows the schematic diagram of a sliding mode voltage controlled (SMVC) buck converter. Here, the voltage error x_1 and the voltage error dynamics (or the rate of change of voltage error) x_2 under continuous conduction mode (CCM) of operation can be expressed as

$$\begin{aligned} x_1 &= V_{\text{ref}} - \beta V_o \\ x_2 &= \dot{x}_1 = -\beta \frac{dV_o}{dt} = \frac{\beta}{C} \left(\frac{V_o}{R_L} - \int \frac{uV_i - V_o}{L} dt \right) \end{aligned} \quad (1)$$

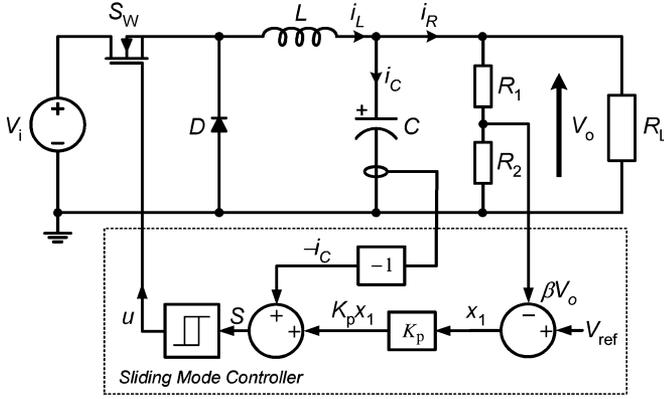


Fig. 1. Basic structure of an SMVC buck converter.

where C , L , R_L are the capacitance, inductance, and load resistance, respectively; V_{ref} , V_i , and βV_o are the reference, input, and sensed output voltage respectively; $u = 1$ or 0 is the switching state of power switch S_W . Then, by differentiating (1) with respect to time, the state space model can be obtained as

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\frac{1}{LC} & -\frac{1}{R_L C} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{\beta V_i}{LC} \end{bmatrix} u + \begin{bmatrix} 0 \\ \frac{V_{\text{ref}}}{LC} \end{bmatrix}. \quad (2)$$

B. Controller's Model

The SM voltage controller adopted in this study controls the state variables x_1 and x_2 . Hence, the switching state u can be determined from the control parameters x_1 and x_2 using the switching function

$$u = \begin{cases} 1 = \text{'ON'} & \text{when } S > \kappa \\ 0 = \text{'OFF'} & \text{when } S < -\kappa \\ \text{unchanged} & \text{otherwise} \end{cases} \quad (3)$$

where control signal $S = \alpha x_1 + x_2$, and the hysteresis bandwidth κ , is a fixed parameter that can be determined using the equation

$$\kappa = \frac{V_{\text{od}} \left(1 - \frac{V_{\text{od}}}{V_{i(\text{nom})}}\right)}{2f_{\text{sd}}L} \quad (4)$$

with f_{sd} , V_{od} , and $V_{i(\text{nom})}$ representing the desired steady-state switching frequency, the desired output voltage, and the nominal input voltage, respectively. It should be noted that the above equation is valid only if the sliding coefficient is set as $\alpha = 1/R_{L(\text{nom})}C$, and the converter is operating under the nominal load resistance $R_{L(\text{nom})}$. Otherwise, if $\alpha \neq 1/R_{L(\text{nom})}C$ or that the load resistance differs from $R_{L(\text{nom})}$, the actual switching frequency will differ slightly from the desired frequency f_{sd} .

Furthermore, as previously discussed in [4], in terms of implementation, it is more practical to reconfigure the SM controller equation (by gain scaling S by a factor of C/β) to the following form:

$$S = K_p(V_{\text{ref}} - \beta V_o) - i_C \quad (5)$$

where $K_p = 1/\beta R_{L(\text{nom})}$ is a fixed gain parameter of the voltage error. It has also been shown in [4] that under this configuration, the conditions for SM control to exist are

$$\begin{cases} \lambda_1 = \left(\frac{C}{\beta}\alpha - \frac{1}{\beta R_L}\right)x_2 - \frac{1}{\beta L}x_1 + \frac{V_{\text{ref}} - \beta V_i}{\beta L} < 0 \\ \lambda_2 = \left(\frac{C}{\beta}\alpha - \frac{1}{\beta R_L}\right)x_2 - \frac{1}{\beta L}x_1 + \frac{V_{\text{ref}}}{\beta L} > 0 \end{cases}. \quad (6)$$

Now, considering that the converter is to operate at an input voltage range $V_{i(\text{min})} \leq V_i \leq V_{i(\text{max})}$ and an output load resistance range $R_{L(\text{min})} \leq R_L \leq R_{L(\text{max})}$, (6) can be rewritten as

$$\begin{cases} \frac{V_{\text{od}} - V_{i(\text{min})}}{L} < -\left(\alpha - \frac{1}{R_{L(\text{max})}C}\right)|\hat{i}_C| \\ \frac{V_{\text{od}}}{L} > \left(\alpha - \frac{1}{R_{L(\text{max})}C}\right)|\hat{i}_C| \end{cases} \quad (7)$$

or more explicitly as

$$\alpha < \begin{cases} \frac{V_{i(\text{min})} - V_{\text{od}}}{L|\hat{i}_C|} + \frac{1}{R_{L(\text{max})}C} & \text{when } V_{i(\text{min})} < 2V_{\text{od}} \\ \frac{V_{\text{od}}}{L|\hat{i}_C|} + \frac{1}{R_{L(\text{max})}C} & \text{otherwise} \end{cases} \quad (8)$$

where \hat{i}_C is the peak magnitude of the bidirectional capacitor current flow. Also, it should be noted that α must be positive to achieve system's stability. The proof is illustrated in [4].

C. Problems Identification

It is generally known that SM controllers using a hysteresis type of modulation suffer from frequency variation when operating conditions differ from their nominal conditions. Experimental evidence can be found in [4].

1) *Experimental Observation*: Fig. 2 shows the experimental data for the described converter system, with specifications as shown in Table I, operating under different input voltages V_i (left) and different load resistances R_L (right). It is observed that both the output voltage and switching frequency increase with increasing input voltage. These behaviors can be explained in terms of a general form of design (4), i.e.,

$$f_S = \frac{V_o \left(1 - \frac{V_o}{V_i}\right)}{2\kappa L} \quad (9)$$

which suggests that with preset design parameters, inductor L and hysteresis band κ , and the assumption that output voltage is held at some constant value V_o , a deviation in the actual input supply V_i will result in a change in the actual switching frequency f_S . This in turn affects the regulation of the output voltage.

As for load variation, it is observed that switching frequency decreases while output voltage increases with increasing load resistance. This is because the change in switching frequency is caused by two components. First, the imperfect feedback loop causes a small steady-state error in the output voltage, i.e., $V_o \neq V_{\text{od}}$, which in turn causes small deviation of the switching frequency from its nominal value, i.e., $f_S \neq f_{\text{sd}}$ [see (9)]. Hence, a change in load will lead to a small change in output voltage and consequently a small change in frequency. Second, in practice, the nominal load almost always differs from the operating load. As previously discussed, (4) and therefore (9), will not be strictly true if $\alpha \neq 1/R_{L(\text{nom})}C$ or the load resistance differs from $R_{L(\text{nom})}$.

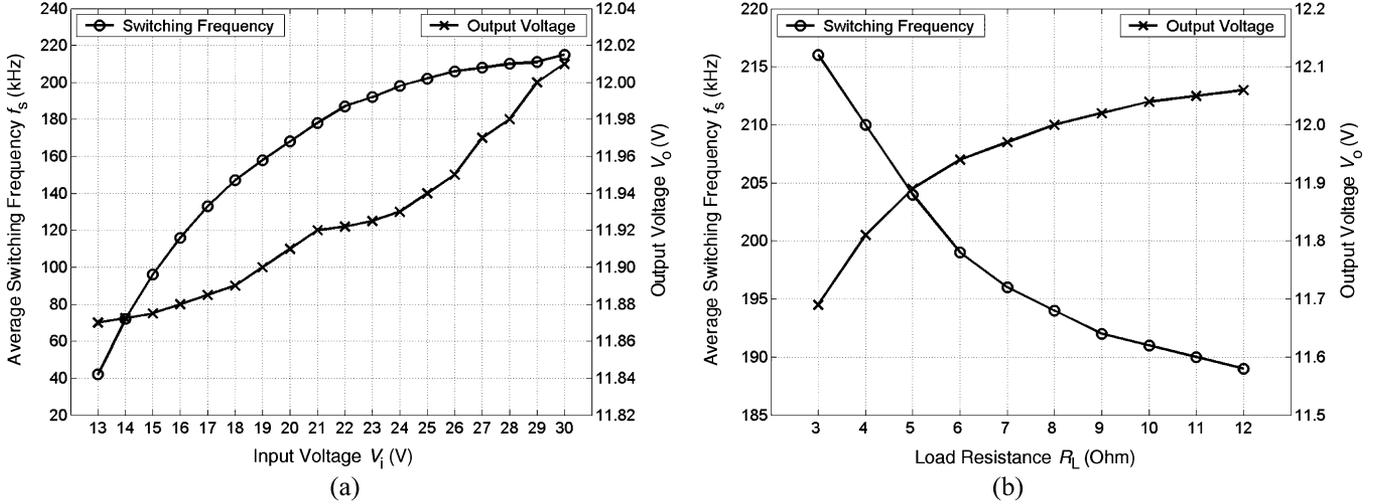


Fig. 2. Experimentally measured values of average switching frequency \bar{f}_s and average output voltage \bar{V}_o for (a) different input voltage V_i and (b) different load resistance R_L .

TABLE I
SPECIFICATIONS OF BUCK CONVERTER

| Description | Parameter | Nominal Value |
|-----------------------------|--------------|----------------|
| Input voltage | $V_{i(nom)}$ | 24 V |
| Capacitance | C | 100 μ F |
| Capacitor ESR | r_C | 25 m Ω |
| Inductance | L | 110.23 μ H |
| Inductor resistance | r_L | 144 m Ω |
| Desired switching frequency | f_{sd} | 200 kHz |
| Load resistance | R_L | 6 Ω |
| Desired output voltage | V_{od} | 12 V |

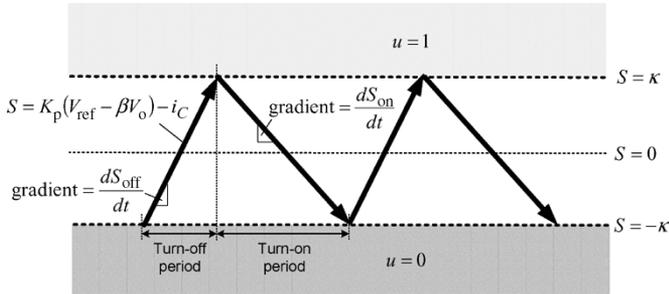


Fig. 3. Switching mechanism of the HM based SMVC buck converter.

2) *Analytical Explanation:* The controller operates according to (3) and (5), which may be graphically represented as shown in Fig. 3.

Here, the controller generates a turn-on signal $u = 1$ if $S > \kappa$, and a turn-off signal $u = 0$ if $S < -\kappa$. The parameter S is a continuous signal computed using (5). By substituting $i_C = i_L - i_R$, where i_L and i_R are, respectively, the inductor and load currents, S can be expressed as

$$S = K_p(V_{ref} - \beta V_o) + \frac{V_o}{R_L} - \int \frac{uV_i - V_o}{L} dt. \quad (10)$$

Close examination of this equation and the switching mechanism reveals that in the steady state, the terms $K_p(V_{ref} - \beta V_o)$ and V_o/R_L , which contain only dc information, will cancel out

the dc component of the term $\int ((uV_i - V_o)/L) dt$, leaving its ac component. This means that during steady-state operation, it is effectively the ac component of the term $\int ((uV_i - V_o)/L) dt$ that controls the behavior of the trajectory of S . Thus, only a change in V_o or V_i can affect the steady-state switching frequency.

Now, assume that V_o is constant. With $u = 1$ (i.e., switch is turned on), if V_i is high, the gradient dS_{on}/dt will be high, and the turn-on period of the switch will be short. Conversely, if V_i is low, dS_{on}/dt will be low, and the turn-on period will be long. However, with $u = 0$, the term V_i is nulled from the expression $\int ((uV_i - V_o)/L) dt$. Therefore, gradient dS_{off}/dt , i.e., the turn-off period is not affected by V_i . Hence, it can be concluded that with increasing V_i , turn-on period will be shorter, and considering that there is no change in the turn-off period, the switching frequency will be higher. Conversely, the switching frequency will be lower for smaller V_i . Also, since the switching frequency does influence the magnitude of the steady-state output voltage error caused by the imperfect feedback loop, the output voltage is affected by line variation.

However, unlike V_i which has a direct control over the gradient of the trajectory of S , load R_L has an indirect and small influence over it. Although R_L appears in (10), it is important to recall that in steady state, the effective ac term in the expression $\int ((uV_i - V_o)/L) dt$ does not include R_L . Hence, variation of R_L does not directly affect the trajectory of S . Instead, it is the steady-state error in the output voltage caused by the imperfect feedback loop, which depends on R_L , that leads to the change in the gradient. It should be noted that in this case, both the turn-on and turn-off periods are influenced by R_L . However, since the output voltage is well regulated, the change in its steady-state error will be small. This explains why load changes has only a small effect on the switching frequency. Specifically, as R_L increases, V_o will increase, the gradient of trajectory of S will decrease, and the frequency will decrease [see (4)].

D. Possible Solutions

As mentioned earlier, there are three possible approaches to alleviating the problem of frequency variation caused by line and load variations. The simplest approach is to fix the switching

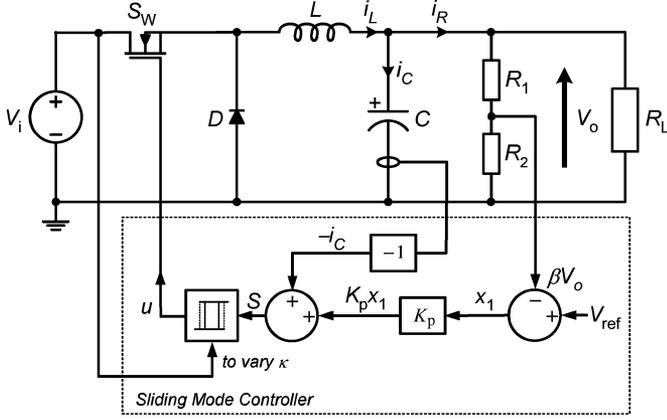


Fig. 4. Basic structure of an adaptive feedforward SMVC buck converter.

frequency by incorporating a constant ramp or timing function directly into the controller [3], [5], [7], [8], for example, by superimposing a constant ramp signal into switching function [3]; or by including a constant switching frequency circuit in the switching function [5]. Despite their simplicity, realization methods in this approach suffers from deteriorated transient response. The second approach is by replacing the HM with PWM [7], [8]. However, this approach is not always implementable for some SM controller types.

Hence, it may be better to consider an alternative approach to solving this problem. Our proposed approach is to incorporate some form of adaptive control into the HM based SM controller. Although the idea has been previously mentioned in [4], [10], it has not been seriously investigated. The remaining sections of this paper will describe the adaptive control strategies, their means of implementation, and the major results and conclusions.

III. ADAPTIVE FEEDFORWARD CONTROL SCHEME

A. Theory

To keep the switching frequency fixed against line variation, we introduce an adaptive feedforward control scheme that varies the hysteresis band in the hysteresis modulator of the SM controller in the event of any change of the line input voltage. Fig. 4 shows the basic structure of the adaptive feedforward SMVC buck converter.

The operation of the adaptive feedforward variable hysteresis band is illustrated in Fig. 5, which shows the trajectory of S for one switching cycle of the steady-state operation. Here, the terms $S_{off(min)}$ and $S_{on(min)}$ represent the trajectory of S when the input voltage is minimum, for, respectively, the turn-off period $T_{off(min)}$ and turn-on period $T_{on(min)}$. Similarly, $S_{off(max)}$ and $S_{on(max)}$ represent the trajectory of S when the input voltage is maximum, for, respectively, the turn-off period $T_{off(max)}$ and turn-on period $T_{on(max)}$. Also, κ_{min} and κ_{max} represent the required hysteresis bandwidth for maintaining the same switching frequency at minimum and maximum input voltage. Recall that when $u = 0$, V_i does not affect the gradient of trajectory S . Hence, the gradient of trajectory $S_{off(min)}$ and that of trajectory $S_{off(max)}$ are equivalent. But when $u = 1$, the gradient of trajectory $S_{off(min)}$ will be smaller than that

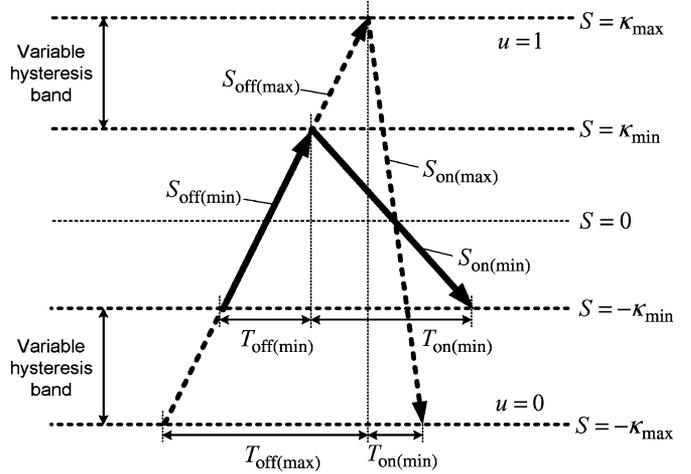


Fig. 5. Operating mechanism of the adaptive feedforward variable hysteresis band.

of trajectory $S_{off(max)}$. Therefore, it is possible to obtain a hysteresis bandwidth κ_{max} that produces a switching time period $T_{max} = T_{off(max)} + T_{on(max)}$ when the input voltage is maximum, and is equivalent to the switching time period $T_{min} = T_{off(min)} + T_{on(min)}$ that employs the hysteresis bandwidth κ_{min} when the input voltage is minimum. Finally, the input voltage is sensed and the hysteresis bandwidth is adjusted accordingly to maintain a certain desired switching frequency.

The real-time computation of the hysteresis bandwidth for different input voltages can be performed using a general form of (4), where the input voltage term is now V_i , instead of $V_{i(nom)}$, i.e.,

$$\kappa = \frac{V_{od} \left(1 - \frac{V_{od}}{V_i}\right)}{2f_{sd}L}. \quad (11)$$

Simulation¹ has been performed to verify the idea. Fig. 6 shows the simulated data for the SMVC buck converter, with and without incorporating the adaptive feedforward control scheme. It can be seen that the adoption of the adaptive feedforward control scheme reduces the variation of f_s for the input voltage range $18 \text{ V} \leq V_i \leq 30 \text{ V}$ from $\pm 35\%$ to within $\pm 5\%$ of f_{sd} (200 kHz).

B. Implementation Method

Several methods of varying the hysteresis band of the hysteresis modulator are possible. In the case of employing the Schmitt trigger as the hysteresis modulator, the hysteresis band can be adjusted by changing the resistor gain ratio R_{ST2}/R_{ST1} , or by adjusting the power supply V_{CC}^+/V_{CC}^- . In this work, the latter option is chosen.

Fig. 7 shows the schematic of the noninverting Schmitt Trigger used in our implementation. The hysteresis bandwidth of this circuit is

$$2\kappa = \frac{R_{ST1}}{R_{ST2}} (V_{CC}^+ - V_{CC}^-). \quad (12)$$

¹The simulation is performed using Matlab/Simulink. The step size taken for all simulations is 10 ns.

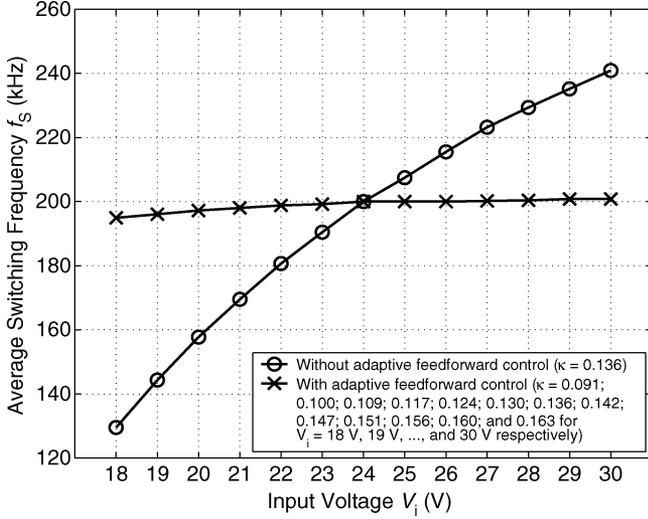


Fig. 6. Simulated data of average switching frequency \bar{f}_s of the SMVC buck converter, with and without the incorporation of the adaptive feedforward control scheme, operating under line variation with input voltages $18 \text{ V} \leq V_i \leq 30 \text{ V}$ and at $R_L = 6 \Omega$.

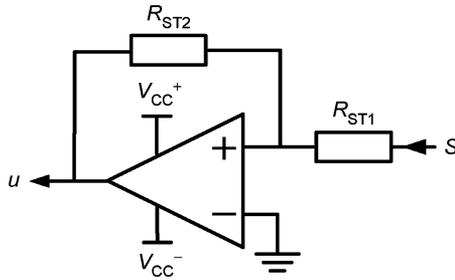


Fig. 7. Schematic of a standard noninverting Schmitt trigger circuit.

Equating with (11) gives

$$V_{CC}^+ - V_{CC}^- = \frac{R_{ST2}}{R_{ST1}} \frac{V_{od}}{f_{sd}L} \left[1 - \frac{V_{od}}{V_i} \right]. \quad (13)$$

Also, V_{CC}^+ and V_{CC}^- should be

$$\begin{aligned} V_{CC}^+ &= \frac{1}{2} G_S \left[1 - \frac{V_{od}}{V_i} \right] \\ V_{CC}^- &= -\frac{1}{2} G_S \left[1 - \frac{V_{od}}{V_i} \right] \end{aligned} \quad (14)$$

where $G_S = (R_{ST2}/R_{ST1})(V_{od}/f_{sd}L)$. In practice, this variable power supply, V_{CC}^+/V_{CC}^- , can be obtained through simple analog computation (see Fig. 8).

IV. ADAPTIVE FEEDBACK CONTROL SCHEME

A. Theory

The problem of variable switching frequency as load varies is caused by the difference between the operating load resistance and the nominal load resistance used in the controller design, i.e., $R_L \neq R_{L(\text{nom})}$. When this occurs, (4), which assumes that the sliding coefficient is chosen as $\alpha = 1/R_{L(\text{nom})}C$ and that the converter is operating with the nominal load resistance $R_{L(\text{nom})}$, becomes invalid [4]. This results in the deviation of

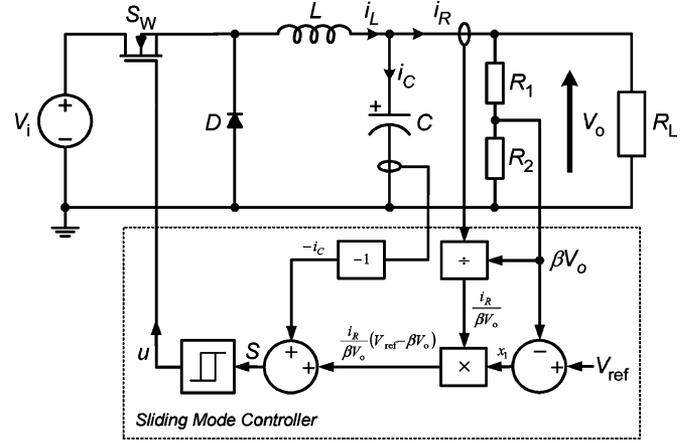


Fig. 8. Basic structure of an adaptive feedback SMVC buck converter.

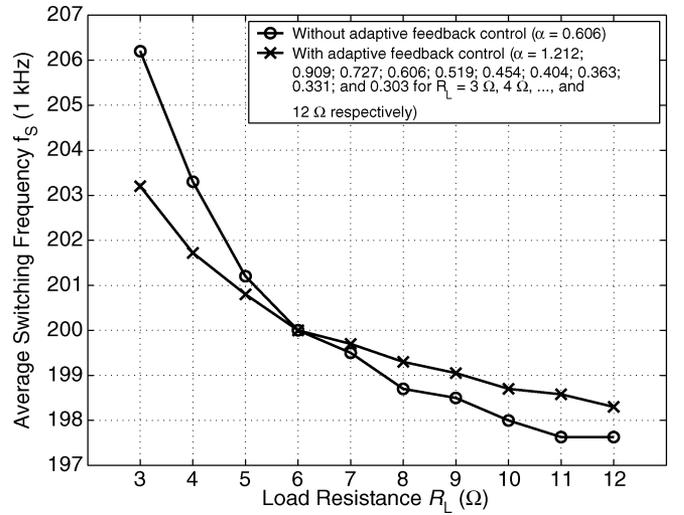


Fig. 9. Simulated data of average switching frequency \bar{f}_s of the SMVC buck converter, with and without the incorporation of the adaptive feedback control scheme, operating under load variation with load resistances $3 \Omega \leq R_L \leq 12 \Omega$ and at $V_i = 24 \text{ V}$.

the switching frequency from the nominal value. Thus, a logical solution is to ensure that (4) is valid for all operating conditions. This can be accomplished by making the sliding coefficient adaptive. Instead of simply fixing it at $\alpha = 1/R_{L(\text{nom})}C$, the sliding coefficient is designed to be load dependent: $\alpha = 1/R_L C$, i.e., a change in the operating load resistance R_L will immediately change α . Such a system has been proposed in [12] to improve system's performances. Here, it is suggested as a means to also maintain the validity of (9) so that f_s becomes independent of R_L . Hence, the effect of frequency variation caused by the mismatch between the nominal and the operating load is alleviated. Note that although the convergency rate of the system is affected by the adaptive feedback control, its stability is preserved since $\alpha > 0$.

Fig. 9 shows the simulated data for the SMVC buck converter, with and without the incorporation of the adaptive feedback control scheme. It can be seen that the adoption of the adaptive feedback control scheme reduces the variation of \bar{f}_s for the load resistance range $3 \Omega \leq R_L \leq 12 \Omega$ from ± 3.1 to within $\pm 1.6\%$ of f_{sd} (200 kHz).

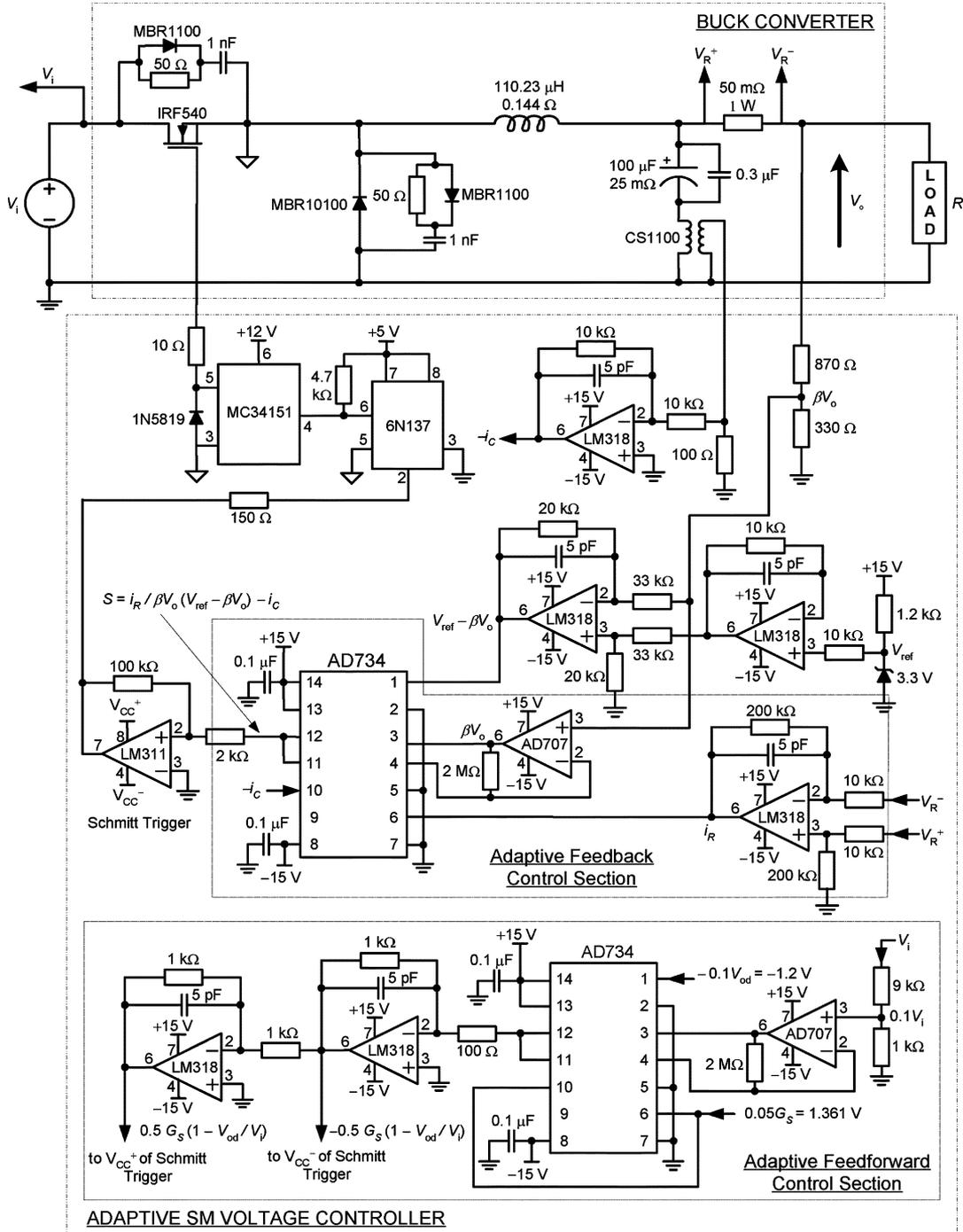


Fig. 10. Full schematic diagram of the adaptive SMVC buck converter prototype.

B. Implementation Method

By making the sliding coefficient adaptive, i.e., $\alpha = 1/R_L C$, SM control equation (10) becomes

$$S = \frac{1}{\beta R_L} (V_{ref} - \beta V_o) - i_C \tag{15}$$

Clearly, the computation of the control signal S requires the measurement of all involving variables in the equation. How-

ever, since it is not possible to measure resistance directly, the relationship

$$R_L = \frac{V_o}{i_R} \tag{16}$$

is exploited to obtain the instantaneous loading resistance. Hence, the adaptive feedback control scheme is practically implemented using

$$S = \frac{i_R}{\beta V_o} (V_{ref} - \beta V_o) - i_C \quad \text{where } V_o \neq 0. \tag{17}$$

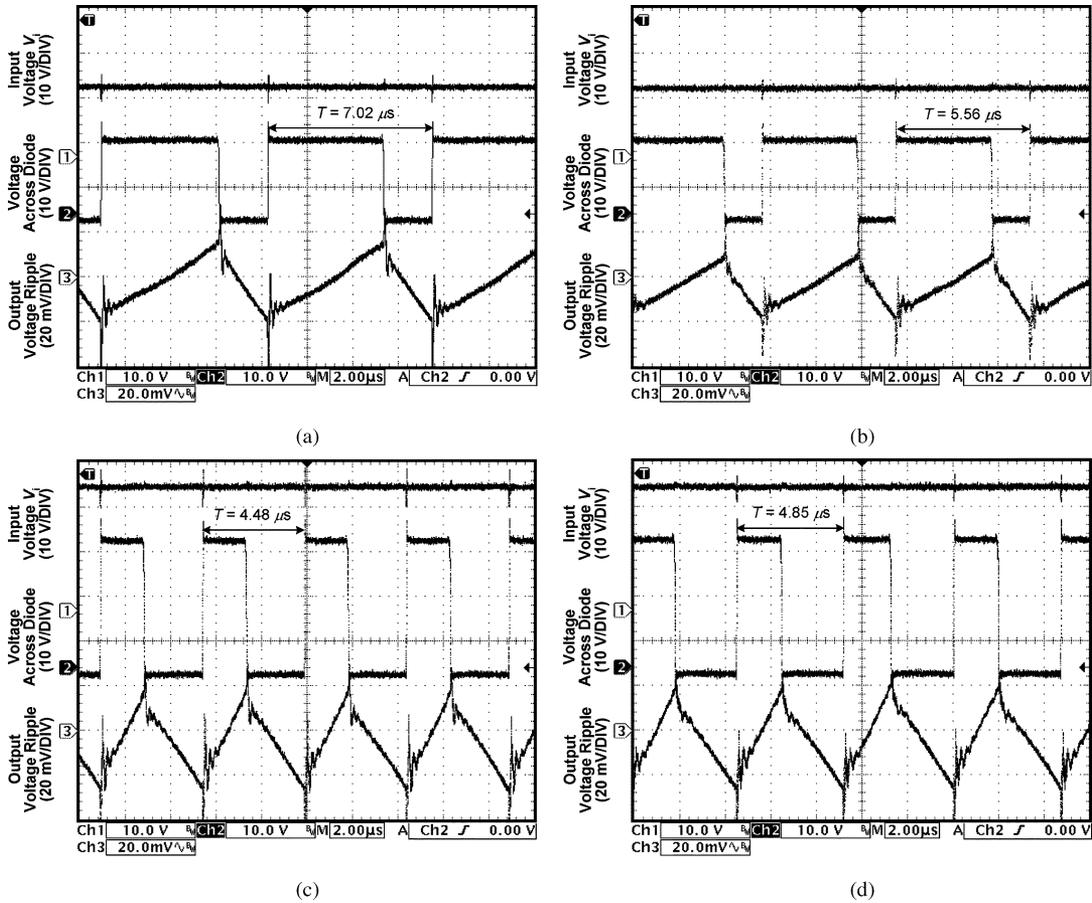


Fig. 11. Experimental waveforms of input voltage V_i , voltage across freewheeling diode D , and output voltage ripple \tilde{V}_o of the SMVC converter that is operating at input voltage (a) $V_i = 18$ V (without adaptive feedforward control), (b) $V_i = 18$ V (with adaptive feedforward control), (c) $V_i = 30$ V (without adaptive feedforward control), and (d) $V_i = 30$ V (with adaptive feedforward control), under nominal load resistance $R_L = 6 \Omega$.

With this arrangement, the monitoring of instantaneous i_R and V_o allows information of the instantaneous R_L to be known. By absorbing this information into the control scheme, an adaptive feedback SM voltage controller, which basically varies α according to R_L , is obtained. Note also that $V_o \neq 0$, which otherwise causes a division by zero problem. In case of an analog implementation of this equation, a divider that saturates the computation signal at zero division may be used.

V. EXPERIMENTAL RESULTS AND DISCUSSIONS

To verify the proposed adaptive feedforward and adaptive feedback control strategies, an experimental prototype has been constructed with specifications as shown in Table I. Fig. 10 shows the full schematic diagram of the proposed converter and controller. Separate tests are performed to evaluate the performance of the adaptive controllers with respect to line regulation and load regulation.

A. Line Variation

Fig. 11(a)–(d) shows the experimental waveforms of the converter system at minimum and maximum input voltages, for the SM controller with and without using the adaptive feedforward control scheme. It can be easily observed that for both the cases $V_i = 18$ V and $V_i = 30$ V, with the same input voltage, the

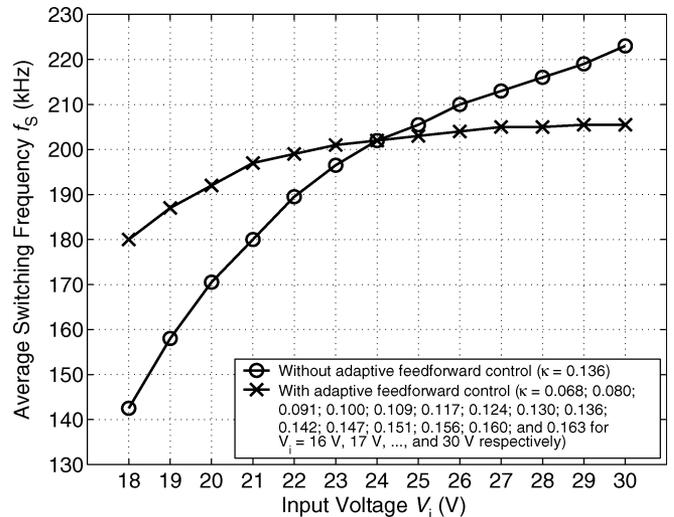


Fig. 12. Experimentally measured average switching frequency \bar{f}_s of the SMVC buck converter, with and without the incorporation of the adaptive feedforward control scheme, operating under line variation with input voltages $18 \text{ V} \leq V_i \leq 30 \text{ V}$ and at $R_L = 6 \Omega$.

system with the adaptive feedforward control has switching period much closer to the desired switching period $T = 5 \mu\text{s}$. A plot of the measured average switching frequency versus different input voltages is shown in Fig. 12. The experimental data

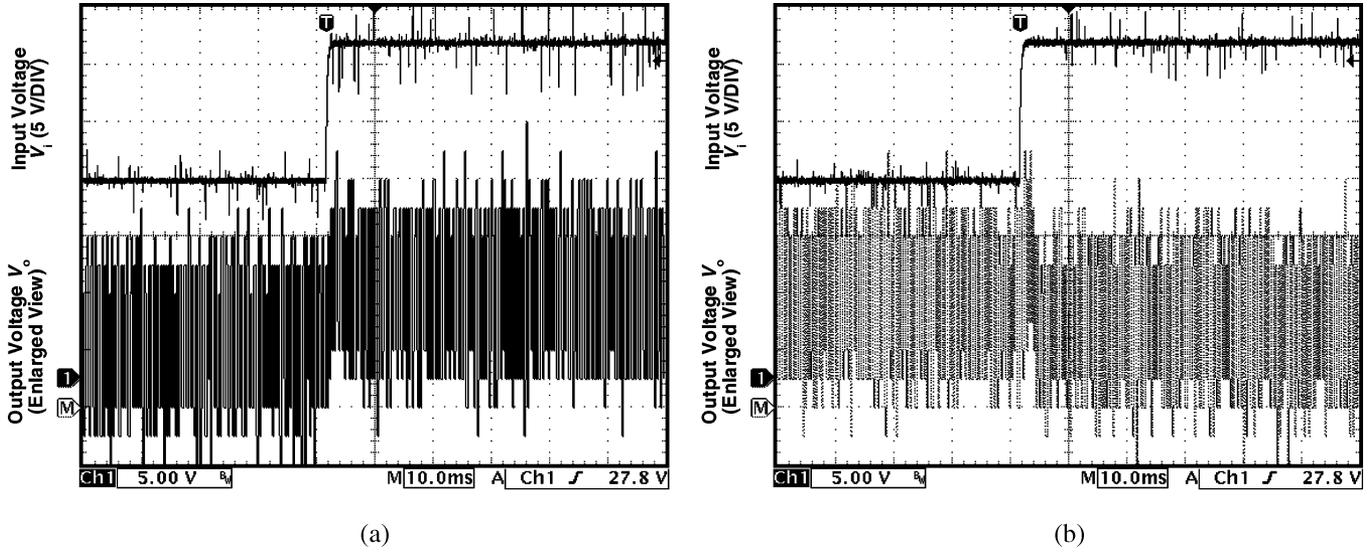


Fig. 13. Experimental waveforms of input voltage V_i and enlarged view of output voltage V_o of the SMVC buck converter (a) without adaptive feedforward control and (b) with adaptive feedforward control, operating at step input voltage change from $V_i = 18$ V to $V_i = 30$ V, and at $R_L = 6 \Omega$.

confirms more conclusively the capability of the adaptive feedforward control scheme in reducing the variation of f_s . For the input voltage range $18 \text{ V} \leq V_i \leq 30 \text{ V}$, the frequency variation is reduced from $\pm 28.8\%$ to within $\pm 10.0\%$ of f_{sd} . The improvement is less than the one obtained from simulation as shown in Fig. 6, which reduces the variation for the same input voltage range from $\pm 35\%$ to within $\pm 5\%$ of f_{sd} . The deterioration is caused by practical components' variations and delay times. These factors are not modeled in the simulation program.

Fig. 13(a) and (b) shows the experimental waveforms of the converter system to which a step change of input voltage from minimum to maximum is applied. For the converter without the adaptive feedforward control, the enlarged view of the output voltage indicates that there is an upward dc shift when the input voltage steps up to a higher value. As explained earlier, this is due to the change in switching frequency, which increases or decreases the magnitude of the steady-state output voltage error caused by the imperfect feedback loop. Hence, for the converter with the adaptive feedforward control where the switching frequency variation is much reduced, there is less dc shift in the output voltage associated with the step change. This situation is experimentally captured and illustrated in Fig. 14. For the input voltage range $18 \text{ V} \leq V_i \leq 30 \text{ V}$, the line regulation is improved from 1.59% of $V_o(V_i=24 \text{ V})$ to 0.17% of $V_o(V_i=24 \text{ V})$ through the adaptive feedforward control scheme.

Fig. 15(a) and (b) show the output voltage ripple waveforms of the converter operating at nominal load when V_i is sinusoidally varied from 20.9 V to 27.1 V at a frequency of 100 Hz. The aim is to test the robustness of the converter against a slowly varying input voltage. Without the adaptive feedforward control, the maximum peak-to-peak output voltage is around 80 mV, i.e., the input voltage ripple rejection is -37.81 dB at 100 Hz. With the adaptive feedforward control, the maximum peak-to-peak output voltage is around 200 mV, i.e., the input voltage ripple rejection is -29.85 dB at 100 Hz. The slight deterioration in the audio susceptibility performance illustrates the main tradeoff in using the adaptive feedforward control scheme. Yet, in both

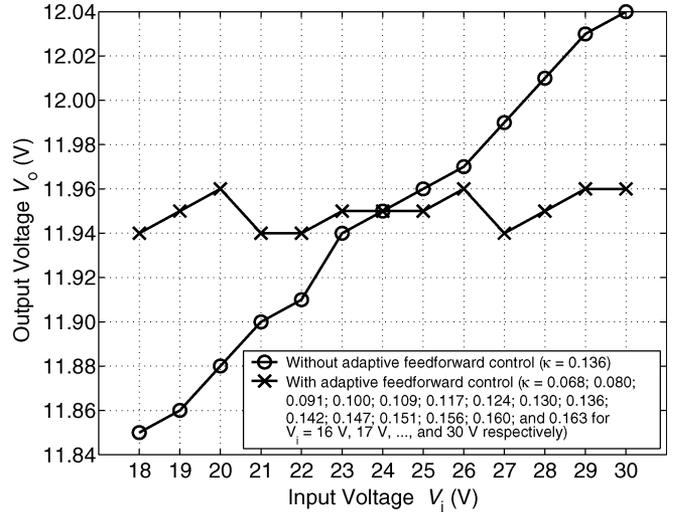


Fig. 14. Experimentally measured output voltage V_o of the SMVC buck converter, with and without the incorporation of the adaptive feedforward control scheme, operating under line variation with input voltages $18 \text{ V} \leq V_i \leq 30 \text{ V}$ and at $R_L = 6 \Omega$.

cases, the converter still has an adequate audio susceptibility performance.

It is worth noting that the output voltage varies twice as fast as the line variation. Without the adaptive feedforward control, the output voltage varies at the same frequency as the input voltage, i.e., 100 Hz. However, with the adaptive feedforward control, the output voltage varies at twice the frequency of the input voltage, i.e., 200 Hz. This can be explained by inspecting (9): $f_s = V_o(1 - (V_o/V_i))/2\kappa L$. Without adaptive control, since κ is kept constant and f_s is varying with the change of input voltage V_i , both f_s and V_o vary at the same frequency as V_i . With the adaptive control, κ varies sinusoidally at 100 Hz. Since the adaptive control cannot fully eliminate the frequency variation due to line variation, f_s will also vary sinusoidally at 100 Hz. Hence, V_o will vary according to the product of κ and f_s , i.e., $\sin^2 2\pi 100t \Rightarrow \cos 2\pi 200t$.

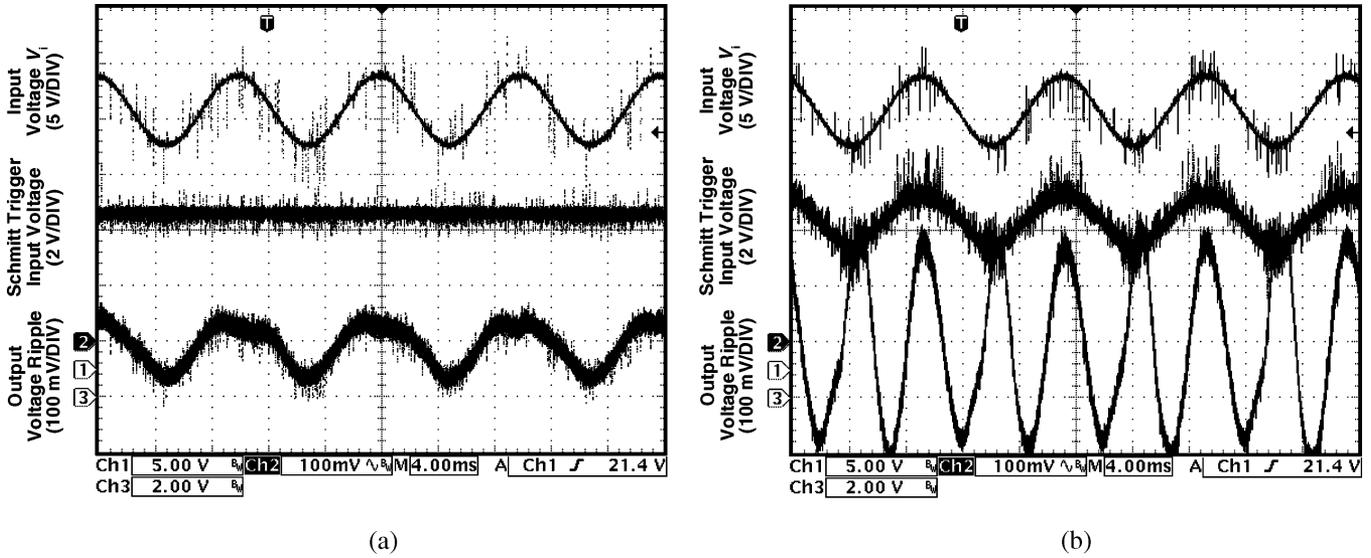


Fig. 15. Experimental waveforms of input voltage V_i , positive input voltage to the Schmitt trigger V_{CC}^+ , and output voltage ripple \tilde{V}_o of the SMVC buck converter (a) without adaptive feedforward control and (b) with adaptive feedforward control, operating at sinusoidally varying input voltage from $V_i = 20.9$ V to $V_i = 27.1$ V, and at $R_L = 6 \Omega$.

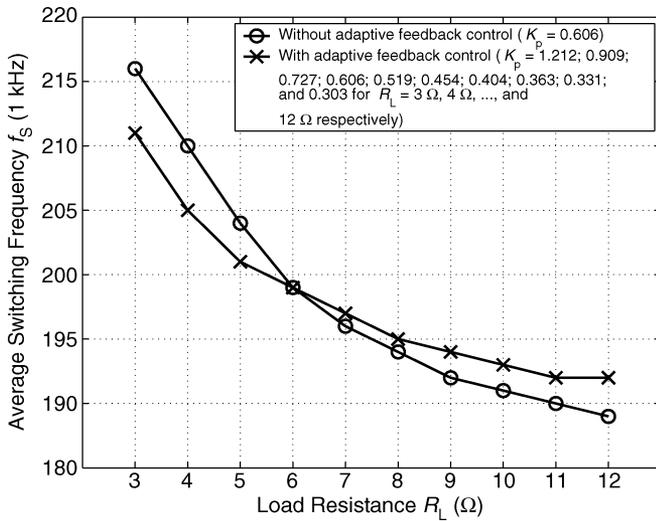


Fig. 16. Experimentally measured average switching frequency \bar{f}_S of the SMVC buck converter, with and without the incorporation of the adaptive feedback control scheme, operating under load variation with load resistances $3 \Omega \leq R_L \leq 12 \Omega$ and at $V_i = 24$ V.

B. Load Variation

Figs. 16 and 17 show the experimental data of the converter system at different load resistances for the SM controller with and without the adaptive feedback control scheme. From Fig. 16, it can be seen that with the adaptive feedback control, the variation of switching frequency with respect to load resistance improves from an average of $d\bar{f}_S/dR_L = -3.0$ kHz/ Ω (without adaptive feedback control) to an average of $d\bar{f}_S/dR_L = -2.1$ kHz/ Ω (with adaptive feedback control). Thus, for the load resistance range $3 \Omega \leq R_L \leq 12 \Omega$, the frequency variation has been reduced from $\pm 8.5\%$ to within $\pm 6.0\%$ of f_{sd} . This verifies the capability of the adaptive feedback control scheme in suppressing the variation of switching frequency caused by load variation. Furthermore, it should be pointed out that the quantitative

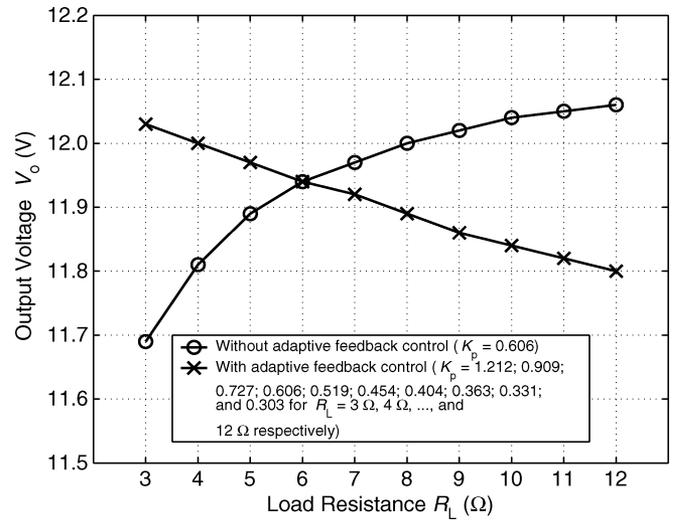


Fig. 17. Experimentally measured output voltage V_o of the SMVC buck converter, with and without the incorporation of the adaptive feedback control scheme, operating under load variation with load resistances $3 \Omega \leq R_L \leq 12 \Omega$ and at $V_i = 24$ V.

difference between the results obtained from the experiment and the simulation in Fig. 9 is due to practical components' variations and delay times that are not modeled in the simulation program.

The reduction in the switching frequency variation with the adaptive feedback control is predictably the outcome of better performance in the load regulation. This has been explained earlier and can be observed from Fig. 17. Without the adaptive feedback control, there is a 0.37-V deviation (i.e., 3.1% of $V_{o(\text{nominal load})}$) in V_o for the entire load range, i.e., load regulation dV_o/dR_L averages at 0.040 V/ Ω . With the adaptive feedback control, there is a -0.23 V deviation (i.e., -1.9% of $V_{o(\text{nominal load})}$) in V_o for the entire load range, i.e., load regulation dV_o/dR_L averages at -0.026 V/ Ω . Noticeably, the incorporation of the adaptive feedback control scheme has

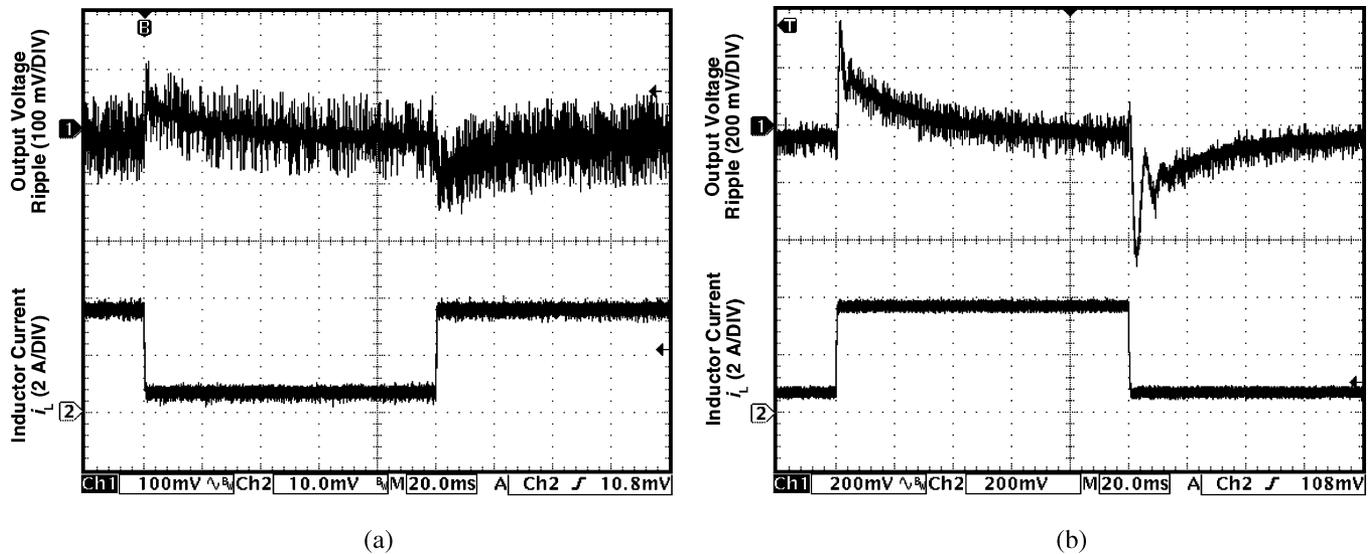


Fig. 18. Experimental waveforms of output voltage ripple \tilde{V}_o and inductor current i_L of the SMVC buck converter (a) without adaptive feedback control and (b) with adaptive feedback control, operating at $V_i = 24$ V and step load changes that alternates between $R_L = 12 \Omega$ and $R_L = 3 \Omega$.

changed the way in which the output voltage is regulated. This is evident from the fact that the output voltage without the adaptive feedback control increases with increasing resistance whereas output voltage with the adaptive feedback control decreases with increasing resistance. Note that we are varying α as the load changes. Since α is effectively the dc gain parameter in the controller, it is actually controlling the steady-state output voltage. Thus, when the load resistance increases, the output voltage of the converter (without adaptive feedback control) should supposedly increase, and its switching frequency should drop below the nominal value. However, when α is adaptive (with the adaptive feedback control) and could react to the increment in the load resistance, it actually decreases, causing the output voltage to decrease. The switching frequency thus increases accordingly.

Fig. 18(a) and (b) show the output waveforms of the operation with load resistance that alternates between $R_L = 12 \Omega$ and $R_L = 3 \Omega$. The comparison shows that the incorporation of the adaptive feedback control scheme will have little effect on the transient performance. Specifically, the overshoot voltage ripple is increased from 120 mV (without adaptive feedback) to 180 mV (with adaptive feedback), and the settling time from 60 to 70 ms.

Remarks: In our case studies, the ability of the adaptive feedback control scheme to reduce the switching frequency variation is seemingly insignificant as compared to the adaptive feedforward control scheme. However, recalling that the switching frequency variations are much larger for larger load variations, the ability of the adaptive feedback control scheme to suppress variations in such circumstance, will be better appreciated. Moreover, the inclusion of the adaptive feedback control scheme also constitutes a significant improvement in the load regulation of the converter, which is also an important aspect of its application. Yet, considering that the employment of the scheme requires additional circuitries and a current sensor, which adds more complexity to the SM controller, the decision for its adoption in converter control is therefore application specific.

VI. CONCLUSION

We have investigated to some depth the problem of switching frequency variation in the SM controlled dc/dc converter. Our discussion has focused on the circuit operation. We have also proposed practical solutions to the problem of switching frequency variation and discussed in detail the implementation methods. The effectiveness of our proposed solutions have been verified by experiments. In conclusion, we have found that simple adaptive schemes can be applied to SM controllers for eliminating frequency variation and hence provide more practical means of implementing SM controller for dc/dc converters.

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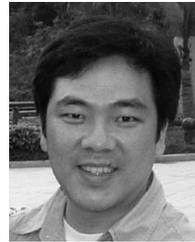
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