## Revisit of the Vögel–Fulcher freezing in lead magnesium niobate relaxors

Shanming Ke,<sup>1</sup> Huiqing Fan,<sup>2,a)</sup> and Haitao Huang<sup>1,b)</sup>

<sup>1</sup>Department of Applied Physics and Materials Research Center, The Hong Kong Polytechnic University, Hung Hom, Kowloon, Hong Kong

<sup>2</sup>State Key Laboratory of Solidification Processing, School of Materials Science and Engineering, Northwestern Polytechnical University, Xi'an 710072, People's Republic of China

(Received 26 August 2010; accepted 8 September 2010; published online 28 September 2010)

The Vögel–Fulcher (VF) equation  $\omega = \omega_0 \exp[-E_a/k_B(T_m - T_f)]$  was frequently used to describe the dielectric relaxation of relaxor ferroelectrics where  $\omega$  is the probe frequency at the peak temperature  $T_m$  of either the real or imaginary parts of the dielectric constant. We revisited this relation in a typical relaxor lead magnesium niobate and found that the parameters obtained were not physically meaningful. Meaningful results can only be obtained by fitting the VF relation on the characteristic relaxation time  $\tau_c$ , whose temperature dependence can be obtained from the Cole–Cole model. The freezing temperature we obtained is 230 K, below which  $\tau_c$  becomes temperature independent. © 2010 American Institute of Physics. [doi:10.1063/1.3494531]

Although relaxor ferroelectrics (RFEs) have been found for more than 50 years and have been intensively investigated, a precise interpretation of their dielectric properties has not been established.<sup>1,2</sup> Lead magnesium niobate PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> (PMN) can be regarded as an archetypal RFE. It is characterized by a broad and rather strongly frequency-dependent dielectric peak at radio frequencies, whose temperature for maximum permittivity  $T_m$  shifts to higher values with increasing frequencies. This frequency dispersion is observed in a frequency range from millihertz to gigahertz, and is commonly attributed to the temperature evolution of the broad distribution of relaxation times  $f(\tau)$ .<sup>1-4</sup> Infinite (or very large) relaxation time  $\tau$  usually means a glasslike "freezing" of the spectrum. The similarities between RFE and glass in macroscopic properties have been studied for a long time.<sup>5-7</sup> It has been found that in many RFEs the relationship between the probe frequency  $\omega$ and the temperature  $T_m$  can be described by the Vögel-Fulcher (VF) equation, similar to those observed in canonical glasses as follows:5,6

$$\omega = \omega_0 \exp\left[\frac{-E_a}{k_B(T_m - T_f)}\right],\tag{1}$$

where  $T_f$  is the static freezing temperature,  $\omega_0$  the attempt frequency, and  $E_a$  the activation energy. Consequently, a dipolar glass model for relaxors was proposed.<sup>5</sup>

However, Taganstev<sup>8</sup> argued that a similar situation may take place in dielectrics if the static permittivity  $\varepsilon_s(T)$  has a maximum at  $T_f$ . In this respect, the relaxation spectrum may broaden upon cooling without an infinite increase in  $\tau$  at  $T_f$ , that is, Eq. (1) does not necessarily imply the freezing of the spectrum. Later, the relaxor state of PMN was proposed to be a ferroelectric one broken up into nanodomains (not the dipolar glass state) under the constraint of quenched random electric fields,<sup>9–11</sup> which was originated from charged compositional fluctuations. In this letter, we investigate the dielectric relaxation behavior of PMN ceramics by careful Cole–Cole analysis. It seems that  $T_f$  derived from the fitting of Eq. (1) does not give a true value of freezing temperature.

PMN ceramics with a perovskite structure were prepared from high purity raw materials and sintered for 2 h at 1150 °C by a two-step procedure.<sup>12</sup> For dielectric measurement, disk samples with a thickness about 1 mm and a diameter about 10 mm were used. Gold electrodes were dc sputtered on both surfaces of the disk samples. The dielectric properties were measured as a function of temperature between 600 and 110 K (at a cooling rate of 0.8 K/min) using an LCR meter (Hewlett Packard 4274A) over a frequency range of 100 Hz to 100 kHz. Before measurements, the samples were thermally treated at a temperature much higher than  $T_m$  to remove any effects of aging or electric history.

Figure 1 shows the temperature dependence of the real  $(\varepsilon')$  and imaginary  $(\varepsilon'')$  parts of the relative dielectric permittivity at various frequencies. For  $\varepsilon'$ , it can be observed that its maximum value decreases with increasing frequencies and  $T_m$  shifts to higher temperatures, displaying a frequency dispersion. The value of  $T_m$  is 258.5 and 273.6 K at 100 Hz and 100 KHz, respectively, showing a shift in temperature  $\Delta T$  of approximately 15 K, which is in good agreement with previous reports.<sup>1-4</sup> For  $\varepsilon''$ , its temperature at maximum  $T'_m$  also shifts to higher values with increasing frequencies. The inset of Fig. 1 shows plots of  $\ln(\omega)$  versus  $T_m$  and  $T'_m$ .

Applying Eq. (1) to the experimental data, we can get the fitting results of  $\omega_0$ ,  $E_a$ , and  $T_f$  which are summarized in Table I. It can be seen that  $T_f$  is consistently about 205 K from fitting by  $T_m - \omega$  and  $T'_m - \omega$  relations. However, the value of  $\omega_0 (\sim 10^{15} \text{ Hz})$  is higher than the attempt frequency of ions in solid state materials which is only on the order of  $10^{12}$  Hz. Similar results have also been observed by Cheng *et al.*,<sup>13</sup> where a much higher value of  $\omega_0 (\sim 10^{20} \text{ Hz})$  was reported in 0.9PMN-0.1PbTiO<sub>3</sub>. It can also be found that the activation energy  $E_a$  derived from  $T'_m - \omega$  relation is 0.103 eV, much lower than that derived from  $T_m - \omega$  relation (0.145 eV). Therefore, the results obtained by fitting the dielectric response according to the VF law on probe frequency are not physically reasonable.

Downloaded 19 Dec 2010 to 158.132.161.9. Redistribution subject to AIP license or copyright; see http://apl.aip.org/about/rights\_and\_permissions

<sup>&</sup>lt;sup>a)</sup>Electronic mail: hqfan3@163.com.

<sup>&</sup>lt;sup>b)</sup>Author to whom correspondence should be addressed. Electronic mail: aphhuang@polyu.edu.hk.



FIG. 1. (Color online) Temperature dependence of the (a) real and (b) imaginary parts of the relative dielectric permittivity at 100 Hz, 1 kHz, 10 kHz, and 100 kHz.  $\Delta\varepsilon$  in (a) was obtained by fitting Eqs. (3) and (4). The inset in (b) shows the plots of  $\ln(\omega)$  vs  $T_m$  and  $T'_m$ . The solid curves in the inset were fitted according to the VF relation.

Knowing that the VF relation is also valid for the characteristic relaxation time  $\tau_c$  (mean or maximum cutoff),<sup>8,14</sup>

$$\tau_c = \tau_0 \exp\left[\frac{E_a}{k_B(T - T_f)}\right],\tag{2}$$

we use a Cole–Cole approach to study the relaxation process in PMN. The temperature dependence of  $\tau_c$  can be obtained by fitting the Cole–Cole model as follows:<sup>15</sup>

$$\varepsilon'(\omega) = \varepsilon_{\infty} + \frac{\Delta\varepsilon}{2} \left[ 1 - \frac{\sinh(\beta\psi)}{\cosh(\beta\psi) + \cos(\beta\pi/2)} \right], \quad (3)$$

TABLE I. Fitting results according to the VF relation.

	ω <sub>0</sub> (Hz)	$ au_0 \ ({ m s})$	$\begin{array}{c} E_a \\ (\mathrm{eV}) \end{array}$	$T_f$ (K)
$\overline{T_m - \omega [\text{Eq. (1)}]}$	$4.53 \times 10^{15}$	$2.21 \times 10^{-16}$	0.145	205.11
$T'_{m} - \omega$ [Eq. (1)]	$3.33 \times 10^{14}$	$3.00 \times 10^{-15}$	0.103	204.73
$\tau_c$ [Eq. (2)]	$5.92 \times 10^{9}$	$1.69 \times 10^{-10}$	0.018	230.53

$$\varepsilon''(\omega) = \left(\frac{\Delta\varepsilon}{2}\right) \frac{\sin(\beta\pi/2)}{\cosh(\beta\psi) + \cos(\beta\pi/2)},\tag{4}$$

where  $\psi = \ln(\omega \tau_c)$ ,  $\Delta \varepsilon = \varepsilon_s - \varepsilon_\infty$ ,  $\varepsilon_s$  the static permittivity,  $\varepsilon_\infty$  the permittivity at high frequency, and  $\beta = 1 - \alpha$ , where  $\alpha$  reflecting the distribution width of the relaxation time. For PMN, the frequency dependence of  $\varepsilon'$  and  $\varepsilon''$  can be described by using Eqs. (3) and (4), respectively. Figure 2 shows the experimental data (diamond points) and the corresponding fitting results (solid lines) at various temperatures, where a good agreement between experimental data and theoretical values were obtained.

Figure 3 shows the temperature dependence of the parameter  $\alpha$  and  $\tau_c$ . There exist two characteristic temperatures,  $T_1(\sim 275 \text{ K})$  and  $T_f(\sim 230 \text{ K})$ , for  $\alpha$  and  $\tau_c$ . Above  $T_1$ ,  $\alpha$  decreases with decreasing temperatures. Below  $T_1$ , the trend is reversed and  $\alpha$  tends to an almost temperature independent constant value for temperatures below  $T_f$ . For  $\tau_c$ , it displays a strong dispersion at a temperature above  $T_1$  and becomes temperature independent at below  $T_f$ , with a constant value around  $4 \times 10^{-4} \text{ s}$ .

Further analysis reveals that, between  $T_1$  and the maximum temperature  $T_{m,\Delta\varepsilon}$  [~244 K, the temperature for maximum  $\Delta\varepsilon$ , as shown in Fig. 1(a)],  $\tau_c$  can be well-described by Eq. (2). The obtained parameters  $\omega_0=5.92\times10^9$ ,  $E_a=0.018$  eV, and  $T_f=230.5$  K (see Table I) are physically reasonable. The  $\omega_0$  and  $E_a$  derived from  $\tau_c(T)$  are much lower than that obtained from the  $T_m - \omega$  and  $T'_m - \omega$  relations. Meanwhile, the freezing temperature  $T_f$  derived from  $\tau_c(T)$  does not coincide with the one obtained from the fitting of  $T_m - \omega$  and  $T'_m - \omega$  relations. This again suggests that the  $T_m - \omega$  and  $T'_m - \omega$  relations are not suitable for the determination of  $T_f$ , at least for Pb-based RFEs.

It is worth noting that Colla *et al.*<sup>16</sup> also reported that the most probable relaxation frequency tends to a constant value for temperatures below 230 K, which was consist with the  $T_f$ derive from  $\tau_c(T)$  in our case. Vakhrushev *et al.*<sup>17</sup> investigated the temperature dependence of the inverse correlation radius  $R_0$  of the ferroelectric fluctuation in PMN by neutron scattering and found that  $R_0$  also became temperature independent at T < 230 K.<sup>17</sup> This led us to conclude that the  $T_f$ =230.5 K is the freezing temperature for PMN samples. It seems dangerous to use the probe frequency as the characteristic frequency for relaxation at the peak temperature  $T_{n}$  [Eq. (1)] to derive the freezing temperature. Recent studies on PMN reveal that the polar nanoregions (PNRs) show a suddenly increase from 10 to 20 nm at around 225 K, which is close to the  $T_f$  in our study. Raman scattering results also confirm a soft mode-driven ferroelectric phase transition at around 225 K.18 These results clearly show that PMN undergoes a ferroelectric phase transition at  $T_f$ , below which PMN is in a nanodomain ground state, not the dipole glass state. The VF freezing in PMN implies that the relaxor behavior is a collective phenomenon where short range interactions between PNRs control the kinetics of the polarization fluctuations and the freezing process.<sup>5</sup> Above  $T_1$ , the short range interactions can be neglected and the characteristic relaxation time  $\tau_c$  would not follow the VF relationship. With decreasing temperatures, the kinetics of the polarization fluctuations may be controlled by the change in size of PNRs, and not by the interactions between them. Therefore the deviation of  $\tau_c$ from VF relationship starting at  $T_{m,\Delta\varepsilon}$  may be attributed to

Downloaded 19 Dec 2010 to 158.132.161.9. Redistribution subject to AIP license or copyright; see http://apl.aip.org/about/rights\_and\_permissions



the progressive coarsening of PNRs, which act as precursors of ferroelectric domains. An almost constant value of  $\tau_c$  below the freezing temperature implies that the nanodomains in PMN would not evolve further into much larger ones.

To summarize, the dielectric relaxation of PMN ceramics was investigated. A critical temperature  $T_1$  was con-



FIG. 3. (Color online) Temperature dependence of (a)  $\alpha$  and (b)  $\tau_c$ , which were obtained from the fitting of data shown in Fig. 2. The solid curve in (b) was fitted according to the VF relation.

FIG. 2. (Color online) Frequency dependence of the dielectric permittivity (real and imaginary parts) at various temperatures: (a) 251, (b) 262, (c) 273, and (d) 281 K. Diamond dots were the experimental data and the solid curves were simulated according to Eqs. (3) and (4).

firmed, below which a VF freezing process started. Below a "freezing" temperature around 230 K, the relaxation time became temperature independent, which implied that the PNRs cannot grow in size any more.

This work was supported by the Research Grants Council of the Hong Kong Special Administrative Region, China (Project No. PolyU5171/07E) and Hong Kong Polytechnic University (Project Nos. A-SA11 and A-PJ46).

- <sup>1</sup>A. A. Bokov and Z.-G. Ye, J. Mater. Sci. **41**, 31 (2006).
- <sup>2</sup>S. M. Ke, H. Q. Fan, H. T. Huang, and H. L. W. Chan, Appl. Phys. Lett. **93**, 112906 (2008).
- <sup>3</sup>L. E. Cross, Ferroelectrics **76**, 241 (1987).
- <sup>4</sup>W. Kleemann and R. Lindner, Ferroelectrics **199**, 1 (1997).
- <sup>5</sup>D. Viehland, S. J. Jang, L. E. Cross, and M. Wuttig, J. Appl. Phys. **68**, 2916 (1990).
- <sup>6</sup>G. Burns and F. H. Dacol, Phys. Rev. B 28, 2527 (1983).
- <sup>7</sup>G. Schmidt, Phase Transitions **20**, 127 (1990).
- <sup>8</sup>A. K. Tagantsev, Phys. Rev. Lett. **72**, 1100 (1994).
- <sup>9</sup>V. Westphal, W. Kleemann, and M. D. Glinchuk, Phys. Rev. Lett. **68**, 847 (1992).
- <sup>10</sup>J. Dec, W. Kleemann, V. Bobnar, Z. Kutnjak, A. Levstik, R. Pirc, and R. Pankrath, Europhys. Lett. 55, 781 (2001).
- <sup>11</sup>W. Kleemann, J. Dec, P. Lehnen, R. Blinc, B. Zalar, and R. Pankrath, Europhys. Lett. **57**, 14 (2002).
- <sup>12</sup>H. Q. Fan, L. T. Zhang, L. Y. Zhang, and X. Yao, Solid State Commun. 111, 541 (1999).
- <sup>13</sup>Z. Y. Cheng, L. Y. Zhang, and X. Yao, J. Appl. Phys. **79**, 8615 (1996).
- <sup>14</sup>A. E. Glazounov and A. K. Tagantsev, Appl. Phys. Lett. 73, 856 (1998).
- <sup>15</sup>K. S. Cole and R. H. Cole, J. Chem. Phys. 9, 341 (1941).
- <sup>16</sup>E. V. Colla, E. Y. Koroleva, N. M. Okuneva, and S. B. Vakhrushev, J. Phys.: Condens. Matter **4**, 3671 (1992).
- <sup>17</sup>S. B. Vakhrushev, B. E. Kvytkovsky, A. A. Nabereznov, N. M. Okuneva, and B. P. Toperverg, Ferroelectrics **90**, 173 (1989).
- <sup>18</sup>D. S. Fu, H. Taniguchi, M. Itoh, S. Koshihara, N. Yamamoto, and S. Mori, Phys. Rev. Lett. **103**, 207601 (2009).