

Estimation of Muscle Fiber Orientation in Ultrasound Images using Revoting Hough Transform (RVHT)

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1 *Abstract*

2 Ultrasound imaging has been frequently used for the study of muscle contraction,
3 including measurements of pennation angles and fascicle orientations. However, these
4 measurements were traditionally conducted by manually drawing lines on the
5 ultrasound images. In this study, we proposed a modified Hough transform (HT),
6 aiming at automatically estimating orientations of straight-line-shaped patterns, such
7 as muscle fibers and muscle-bone interface in ultrasound images. The new method
8 first located the global maximum in the HT accumulator matrix, which corresponded
9 to the most dominant collinear feature points globally, using the standard HT; then the
10 pixels close to the detected line were removed from the edge map, the HT
11 accumulator matrix was calculated again, i.e. revoting, and a new line was detected;
12 the iteration was repeated until the predefined termination conditions were satisfied.
13 The performance of the algorithm was tested using computer-generated images with
14 different levels of noises as well as clinical ultrasound images and compared with that
15 of the conventional method. It was found that the orientation estimation results
16 obtained by the new algorithm were well correlated ($R^2 = 0.9902$) with those obtained
17 using the traditional method, i.e., drawing lines manually and reading the angles with
18 the assistance of software. Further mean-difference plots revealed a difference of
19 0.18 ± 2.41 degree between the two methods at the 95% confidence level. In
20 comparison with the traditional method, the new algorithm was more capable of
21 handling with highly noisy data, and could avoid the aliasing problem, i.e., reporting
22 multiple lines instead of single expected line. The results of this study suggested that

1 the proposed revoting Hough transform can be potentially used for the reliable and
2 non-subjective automatic estimation of the orientations of muscle fibers in
3 musculoskeletal ultrasound images.

4
5 **Keywords:** Ultrasound, Muscle, Hough transform, Sonomyography

6 7 8 **Introduction**

9 Ultrasound imaging has been widely used to assess human muscles in both static and
10 dynamic conditions. In recent years, it has been employed to measure the quantitative
11 changes in muscle thickness (Misuri et al. 1997, Hodges et al. 2003), fiber pennation
12 angle (Narici et al. 1996, Fukunaga et al. 1997, Ito et al. 1998, Maganaris et al. 2002),
13 fascicle length (Misuri et al. 1997, Narici et al. 1996, Fukunaga et al. 1997, Ito et al.
14 1998, Maganaris et al. 2002, Mademli and Arampatzis 2005), and cross-sectional area
15 (Narici et al. 1996, Reeves et al. 2004, Maganaris et al. 2006) during isometric and
16 dynamic contractions. Since these architectural parameters change obviously with
17 contraction, they could potentially provide a noninvasive method of recording
18 activities of various muscles. During the measurement of muscle fiber length and
19 pennation angle as well as fascicle length, the detection of line structures is frequently
20 involved. Traditionally, the lines and angles in musculoskeletal ultrasound images
21 used to be detected manually, or interactively using software (Reeves et al. 1994, Itoi
22 et al. 2001), such as NIH Image (National Institutes of Health, Bethesda, MD, USA,

1 <http://rsb.info.nih.gov/nih-image>). Using the software, the orientation of a manually
2 drawn line on the studied image could be read. These methods were very
3 time-consuming and the manual detecting process was subjective. Recently, we
4 proposed the concept of sonomyography, which represents the signals about
5 continuous changes of muscle thickness and pennation angle, which are detected from
6 ultrasound images (Zheng et al. 2006, Shi et al. 2007a, 2007b, Guo et al. 2007). The
7 manual detection of the orientation of muscle fiber and fascicle greatly hindered the
8 real-time detection of muscle pennation angle for sonomyography. A real-time
9 automatic orientation/angle estimation method for musculoskeletal ultrasound images
10 is much desired for the further development and application of sonomyography
11 techniques.

12

13 The detection of a straight line in an image is a fundamental problem in computer
14 vision. The Hough transform (HT) (Hough et al. 1962) of slope-intercept
15 parameterization as well as its improved version, HT of angle-radius parameterization
16 (Duda and Hart 1972, Immerkar 1998), has been an established solution to the
17 problem. As a major extension of HT, the generalized Hough transform (Ballard 1981)
18 managed to detect more complex shapes, such as circles. While the probabilistic
19 Hough transform (Kiryati et al. 1991) only used a small number of edge/feature points,
20 selected from the original edge map, so as to significantly save computational time, at
21 the cost of slightly impaired detection performance. For the standard Hough transform
22 (SHT), many attentions have been paid to the aliasing problem, caused by the discrete

1 nature of digital image and the discretization errors of HT (Kiryati and Bruckstein
2 1991, Van Veen and Groen 1981), Brown 1983, Kiryati et al. 1991, Yuen and Ma 1997,
3 Lam et al. 1994). Using image-splitting and grouping, Princen et al (1990) proposed a
4 hierarchical approach to achieve a robust architecturally important solution to several
5 problems associated with SHT line detection, including the aliasing problem. For
6 large-sized images such as engineering drawings, Song and Lyu (2005) recently
7 reported a more comprehensive solution, utilizing both Hough space and image space
8 information. However, it is difficult to directly use these methods for the images with
9 high noise levels, such as ultrasound images with significant speckle noises.

10
11 In this study, we presented an improved HT method to identify the major muscle
12 fascicles orientations in musculoskeletal ultrasound images, which may contain
13 significant speckle noises. We proposed a revoting strategy to deal with the aliasing
14 problem in the line detection for ultrasound images. A thresholding method using the
15 data in HT space was proposed to control the detection of significant lines in the
16 ultrasound image. We tested the performance of this new algorithm using
17 computer-generated images with different levels of speckle noises and clinical
18 musculoskeletal ultrasound images.

20 **Methods**

21 *Standard Hough transform of angle-radius parameterization*

22 SHT uses the normal parameterization of a straight line in an image (Duda and Hart

1 1972),

$$2 \quad x \cos \theta_1 + y \sin \theta_1 = \rho_1 \quad (1)$$

3 where θ_1 is the angle between the normal of the line and the x-axis, ρ_1 is the
4 distance of the coordinates origin to the line. The parameters of all straight lines going
5 through a point (x_i, y_i) in the image space show up in the (ρ, θ) parameter space as a
6 sinusoidal curve, given by

$$7 \quad x_i \cos \theta + y_i \sin \theta = \rho \quad (2)$$

8 After transforming all edge/feature points to the (ρ, θ) space, the collinear points
9 will cross each other and an array measuring the crossing situation is accumulated.
10 Traditionally this array $H(\rho, \theta)$ is called accumulator array. The next stage of the
11 SHT is an exhaustive search for the maxima in the accumulator array, and a
12 predefined threshold is set so that all local values of $H(\rho, \theta)$ exceeding the threshold
13 can be recognized as the evidence of straight lines existing in the original image
14 space.

15

16 In summary, in SHT, the collinear edge/feature points in the image space show up as
17 peaks in the (ρ, θ) space. However, in the realization of SHT, there arise some issues:

18 1) digital image is by nature discrete, 2) when mapped into (ρ, θ) space, θ also has
19 to be sampled in a limited resolution and ρ has to be quantized, 3) $H(\rho, \theta)$ is also
20 represented on a discrete grid where only integer coordinates have values, 4) The
21 original image can suffer from various noises. These issues could cause problems of
22 aliasing, peak spreading or peak extension (Kiryati and Bruckstein 1991, Van Veen

and Groen 1981), Brown 1983, Kiryati et al. 1991, Yuen and Ma 1997, Lam et al. 1994).

Revoting Hough transform (RVHT)

To test the feasibility of using HT methods for the line orientation detection in musculoskeletal sonograms which are usually degraded by speckle noises, a modified Hough transform named as revoting Hough transform (RVHT) was adopted in this paper. The global maximum in the accumulator array, voted by all the edge/feature points, was first detected. Then all the feature points close to this line were removed from the edge map. With the updated edge map, the new accumulator array was computed and used to detect the global maximum by voting again. More lines could be identified by repeating this revoting procedure, as shown in Fig. 1. When the image was very noisy, the removal width could be extended from the basic value, 1 pixel, to several pixels (6-12 pixels were selected for the musculoskeletal ultrasound images with resolutions of 10 pixels/mm to 12.5 pixels/mm in this study) to remove more neighboring feature points along the location of the detected line. The center of the image was used as the origin of the coordinate system in HT, as suggested by Immerkar (1998).

Experiments and Results

Comparison of SHT and RVHT using a computer-generated image

A testing image (256x256), as shown in Fig. 2(a), was generated using Matlab 6.5.

1 The distances from the vertexes of the larger equilateral triangle (with a side length of
 2 200 pixels) to the left, right and up borders of the image are all 28 pixels, while the
 3 distances from the vertexes of the smaller equilateral triangle (with a side length of
 4 100 pixels) to the borders of the image are all 78 pixels. The base sides of both
 5 triangles are in horizontal direction. The gray level between the two equilateral
 6 triangles was uniformly set to 64 and the background gray level was 0. Next, a new
 7 image (Fig. 2(b)), was created by adding a Gaussian noise with a mean of 64 (gray
 8 level) and a standard deviation of 16 to the original image. The edge map of Fig. 2(b),
 9 acquired using the Sobel edge detector (Gonzalez and Woods 1992), is shown in Fig.
 10 2(c). Using all edge pixels in Fig. 2(c), the accumulator array was then generated as
 11 shown in Fig.2(d), where the x -axis stands for θ (ranging from 0 to 360) and y -axis
 12 for ρ (ranging from 0 to the image diagonal length, 362 in this image), the labels
 13 for hereinafter accumulator arrays had same setting and therefore were omitted. Since
 14 in this implementation, the ‘angle’ is defined as the angle between the detected line
 15 and the vector pointing from the image up-left corner to the bottom-left corner,
 16 therefore for one single straight line, two angles were detected, i.e., θ and its
 17 inverted version along the same straight line, $\theta+180$. Subsequently, the 12 brightness
 18 peaks in Fig. 2(d) corresponded to the 6 vertices of the 2 triangles, respectively. The
 19 specific correspondences would be further illustrated later when they were removed
 20 one by one from the most-voted one. For the purpose of a better display, the
 21 accumulator array brightness was rescaled in each iteration, i.e., the current most
 22 voted points were also displayed as 22 gray levels, therefore, Fig.2(i) seems to have

1 more sinusoidal curves than Fig.2(d), but it's not the case. It's only because of the
2 rescaling of the displayed gray range after pixel removal was changed. The resolution
3 of $H(\rho, \theta)$ is 1 degree in x-axis and 1 pixel in y-axis, which could satisfy the
4 Yuen's quantization schemes (Yuen and Ma 1997). When the SHT threshold was set
5 to be 70% of the global maximum in $H(\rho, \theta)$, only the larger triangle was detected, as
6 indicated in Fig. 2(e). And when the threshold was decreased to 50% of the global
7 maximum to make the Hough voting procedure more sensitive, two sides of the inner
8 triangle could be detected (Fig. 2(f)). However, in this case, some extra lines were
9 also detected while the bottom side of the inner triangle was undetected, even though
10 it is obvious in the image. The main reason was that some lines generated large values,
11 i.e. bright region, in the accumulated array image. The maximum value was larger
12 than double of the value generated by the bottom side of the inner triangle. To test a
13 more noisy case, a Gaussian white noise with a mean of 64 and a standard deviation
14 of 32 was added to Fig. 2(a), producing a new image of Fig. 2(g). Following above
15 procedures, the corresponding new edge map and accumulator array were obtained
16 (Fig. 2(h) and (i)). Fig. 2(j), (k) and (l) shows the new detection results acquired using
17 threshold values of 70%, 50% and 40% of the global maximum
18 in $H(\rho, \theta)$ respectively. Under this noise condition, the right side of the smaller
19 triangle could not be detected with a 50% threshold. In addition, some extra lines
20 could be observed, such as those near the base side of the larger triangle. When the
21 threshold was further decreased to 40% of the global maximum in $H(\rho, \theta)$, more
22 extra lines were detected.

1

2 As a comparison, the results of applying our RVHT to the image of Fig. 2(g) are
3 presented in Fig. 3. Fig. 3(a) shows the obtained accumulator array, where the marked
4 locations correspond to the two directions of the same straight line. The detected
5 angle, defined as the angle between the detected line and the vector pointing from the
6 image up-left corner to the bottom-left corner as in the software of NIH Image
7 (Reeves et al. 1994), is $150/330^\circ$, which is correct according to the value used for the
8 image generation. Figure 3(b) shows the ‘original image’ (Fig. 2(g)) overlapped by
9 the detected line and Fig. 3(c) the updated edge map where the edge/feature points
10 corresponding to the detected line had been removed, with a removal width of 2 pixels.
11 Similarly, using the RVHT, $30/210^\circ$ and $90/270^\circ$ directions of the larger triangle, and
12 $90/270^\circ$, $150/330^\circ$ and $30/210^\circ$ of the smaller triangle were detected and shown in the
13 subsequent rows in Fig. 3 in turn.

14

15 *Application of RVHT on musculoskeletal ultrasound images*

16 From three healthy adult male volunteers, 45 ultrasound images on biceps and
17 forearm muscles were acquired by an ultrasound image system (ATL HDI 5000,
18 Philips Inc, Bothell, WA), and cropped to remove the imaging tags and retain the
19 image content only. The human subject ethical approval was obtained from the
20 relevant committee in the authors’ institution and informed consents were obtained
21 from subjects prior to the experiment. Totally 168 lines were detected using RVHT,
22 among which 165 were regarded as being valid according to visual verification. A

1 typical image and the corresponding products using RVHT are shown in Fig. 4, where
2 (a) is the original image, (b) its Sobel edge map, (c) the HT accumulator array of (b),
3 and (f) the detected lines after RVHT. The line detection results using SHT with
4 thresholds of 80% and 60% were demonstrated in Fig. 4(d) and (e), respectively.
5 Considering the complicated speckle noise conditions in the ultrasound images, the
6 peaks in the corresponding HT accumulator array image were no longer as ‘sharp’ as
7 those of the simulated image, as shown in Fig. 4(c). In such case, the removal width
8 for RVHT could be set to 12 pixels and the angles detected were marked in the figure
9 in the order they got detected.

10

11 At the same locations where lines were detected using RVHT, two operators manually
12 drew lines on the original images and read the drawn angles using software (NIH
13 Image). The angles estimated by the RVHT, operator #1 and operator #2 were defined
14 as ap , $aa1$ and $aa2$, respectively. To investigate how well the RVHT results fitted the
15 manually drawn values, we compared the RVHT result ap with the mean value of the
16 two operators $(aa1 + aa2) / 2$. As shown in Fig. 5, a very good linear correlation
17 between the results of the two methods was obtained ($R^2 = 0.9902$). Further mean –
18 difference plots (Bland and Altman 1986) for the results as illustrated in Fig. 6
19 showed that the difference between ap and $(aa1 + aa2) / 2$ was 0.18 ± 2.41 degree for
20 the 95% confidence level.

21

22 The ratio of the feature points, counted by the number of pixels in the edge map, of

the last and first detected lines could be controlled by the users. In this study, we used a ratio of 25%, and 5 lines could be normally detected in each image. A smaller ratio would cause more lines to be detected. This ratio together with the number of lines to be detected could be used as iteration termination conditions.

Discussions

From the results obtained in the current experiments, it was observed that the proposed RVHT had some advantages for the line/angle detection in the noisy images. Compared to SHT, the RVHT was inherently anti-aliasing as the feature points which had voted for a line were removed when the line was detected. As stated earlier, once the favored candidate line won the global voting, voices of these feature points were ignored in the subsequent voting, and so were those in the nearby neighborhoods (depending on the removal width). In case the image was very noisy, such as in many ultrasound images, the manual detection became more subjective and difficult. As demonstrated in this study, the proposed RVHT method could detect the lines with a performance comparable to that of manual operation. Moreover, the RVHT was almost automatic and could potentially save lots of manual work in comparison with the traditional way of orientation estimation in musculoskeletal ultrasound images. Therefore, the proposed RVHT has great potential for future image-guided US musculoskeletal analysis, especially for the automatic estimation of the muscle thickness and fascicle length. Furthermore, this new method was inherently objective, and when the US images to be processed are massive, the proposed method could be

1 more advantageous than the manual method.

2

3 In spite of the above advantages, the proposed RVHT could be improved in a number
4 of aspects. Similar to the selection of the threshold value in SHT, RVHT faces a
5 question of when to stop the revoting procedure. There are two possible solutions: 1)
6 If the number of lines to be detected is given, the program can be stopped when that
7 number is accomplished, 2) If we know the feature differences between the expected
8 lines and the unexpected ones, a threshold can be set according to the feature
9 differences. In this study, we used the ratio of the number of feature points in the last
10 and first detected lines to control the algorithm. This ratio was set to be 25% in this
11 study. We found that the larger this ratio, the better the feature points map of the
12 image could be and the less time the algorithm would consume. The adaptive
13 selection criteria of this ratio should be further investigated in the future studies. This
14 is particularly important for the real-time detection of pennation angles in the
15 sonomyography technique, where the pattern of ultrasound images may change
16 significantly during muscle contractions.

17

18 We also observed that there were several quite large values of the difference between
19 the RVHT and the manual results. In those cases, it was noted that the detected lines
20 represented image strips with relatively large widths. The current RVHT tended to
21 locate the wide “line” along its edge, while the manual operation might more favor the
22 skeleton of that “line”. Thus, when the direction of the central skeleton of a strip did

1 not match that of its edges, a larger difference was generated between the angles
2 detected by the two methods. In addition, among the 168 lines detected from the 45
3 ultrasounds images using RVHT, 3 lines did not correspond to any visibly identified
4 lines in the image. According to our observation, the RVHT had counted together the
5 edge/feature points belonging to different muscle fibers when the fiber image was
6 quite blurred (subsequently the quality of the edge/feature points map was poor) or
7 several short irrelative line segments happened to be collinear. SHT also has the
8 similar defect, since detecting “broken line” in images is an inherent feature of the HT
9 method. An HT method reported previously for the detection of broken lines (Song
10 and Lyu 2005) could be integrated into the present method to solve this problem in the
11 future.

12

13 **Conclusion**

14 In this paper we proposed a modified Hough transform using a revoting strategy,
15 aiming at automatic estimation of the orientations of straight-line-shaped patterns in
16 musculoskeletal ultrasound images. The method re-arranged the voting procedure of
17 SHT to better locate the regional vote-leaders in the HT accumulator array under
18 noisy situations. The results of both computer-generated images and clinical
19 ultrasound images demonstrated that RVHT could provide an alternative approach for
20 the orientation estimation for the lines in the ultrasound images. Further studies are
21 required to achieve adaptive parameter selection for deciding the number of lines to
22 be detected. Ultrasound image enhancement methods can also be used to make lines

1 easier to be detected using the proposed method.

2

3

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Fig. 1 The diagram of the procedures of the proposed revoting Hough transform.

Fig. 2 Line detection results of a computer-generated image, using SHT. (a) the original image (256x256), (b) the image after adding Gaussian noise with a mean of 64 (gray level) and a standard deviation of 16, (c) the edge map acquired using Sobel edge detector, (d) the accumulator array, (e) the line detection results when the SHT threshold is set to 70% of the global maximum, (f) the results obtained with a threshold of 50% of the global maximum, (g) the noisier image obtained by adding to original image a Gaussian white noise with a mean of 64 and a standard deviation of 32, (h) the edge map of (g), (i) the accumulator array of (g), and (j), (k) and (l) are the line detection results using SHT with the threshold set to 70%, 50%, 40% of the global maximum, respectively. In each accumulator array image, grey levels 0 and 255 represent its minimum and maximum values.

Fig. 3 Line detection results for the image of Fig.1(g) using RVHT. (a) the accumulator array, with the global maximum locations marked out, which correspond to the two directions of the same straight line, (b) the first detected line, (c) the updated edge map after the feature points corresponding to the 1st line were removed, (d) the new HT accumulator array, with the new global maximum locations marked out, (e) the second detected line, (f) the updated edge map, (g)-(r) were arranged in the same fashion. Totally 6 lines were detected. In each accumulator array image, grey levels 0 and 255 represent its minimum and maximum values.

1 Fig. 4 Angle estimation results of a typical musculoskeletal ultrasound image. (a) the
2 original image, (b) the Sobel edge map, (c) the accumulator array, (d) and (e) the
3 results using SHT with thresholds of 80% and 60% respectively, (f) lines detected
4 using RVHT, totally 5 lines were detected and their angles (between the detected line
5 and the vector pointing from the up-left to bottom-left corner of the image) were
6 marked out. The removal width for RVHT was 12 pixels, and the ratio threshold of the
7 feature points (counts by number of pixels in the edge map) of the last and first lines
8 was set to be 25%.

9

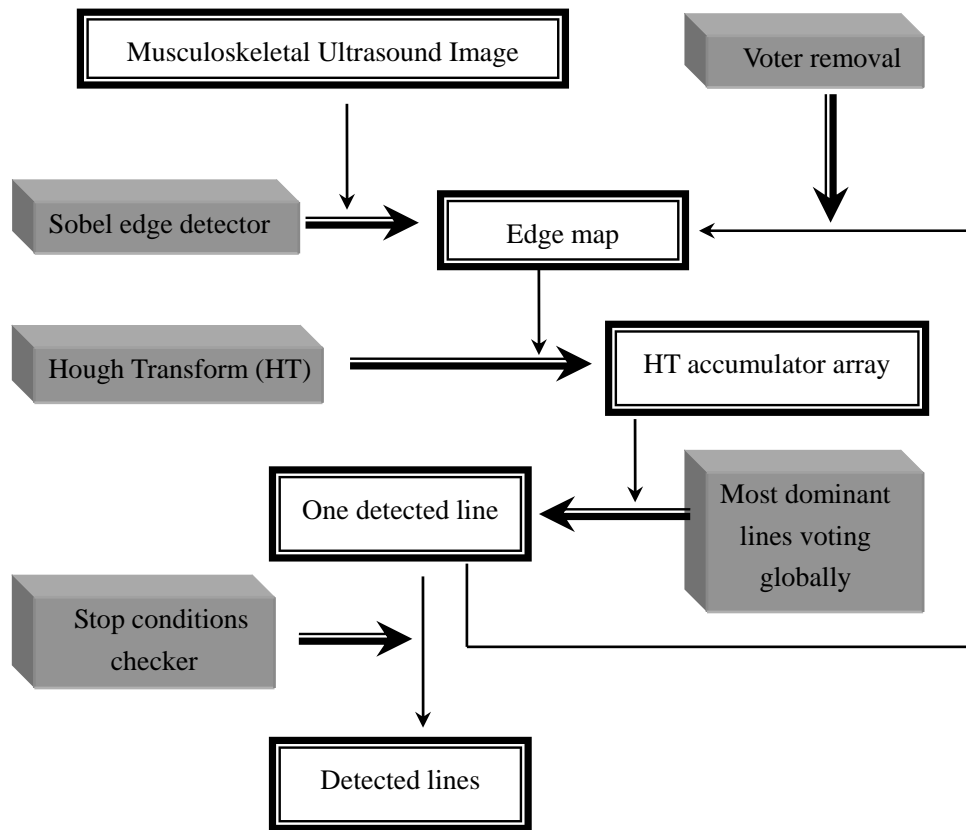
10 Fig. 5 The correlation between the angle estimation results obtained using RVHT and
11 those drawn manually. The x-axis represents the mean of manual results by two
12 operators and the y-axis represents the RVHT results. R is the Pearson product
13 moment correlation coefficient.

14

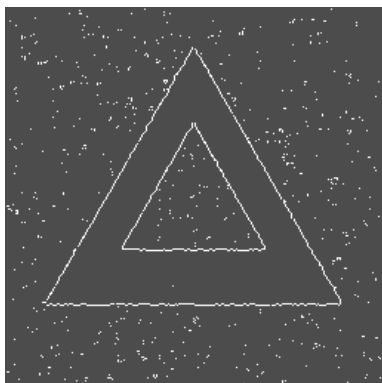
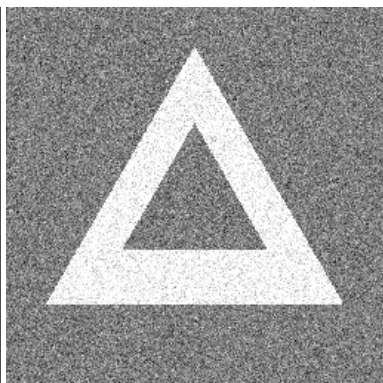
15 Fig. 6 Comparison of the results obtained using the RVHT and manual methods. ap ,
16 $aa1$ and $aa2$ represent the angle estimation results obtained by the RVHT method,
17 operator 1 and operator 2, respectively. Mean and SD represent the mean value and
18 standard deviation of the difference $ap - (aa1+aa2)/2$.

19

Fig. 1



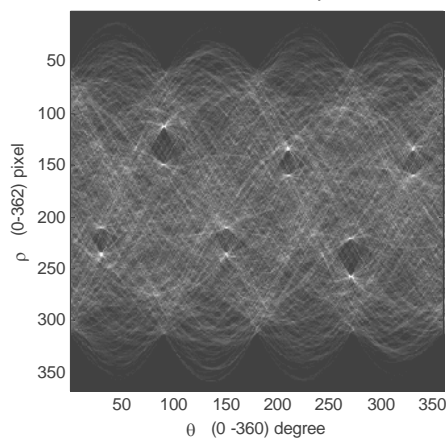
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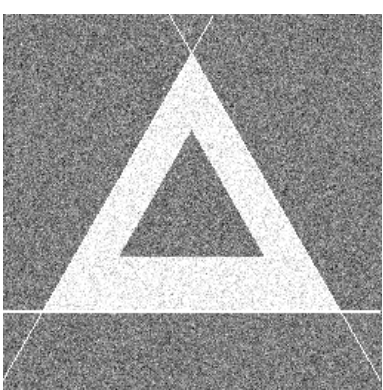
(a)
Accumulator Array

(b)

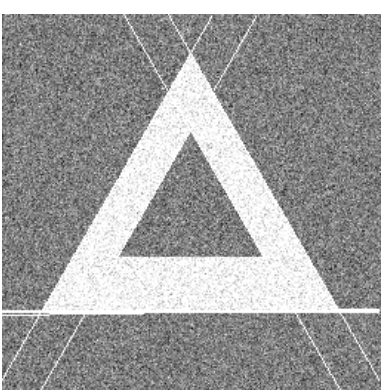
(c)



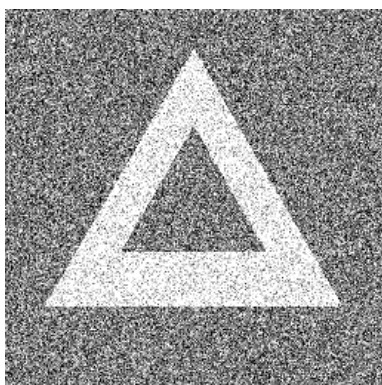
(d)



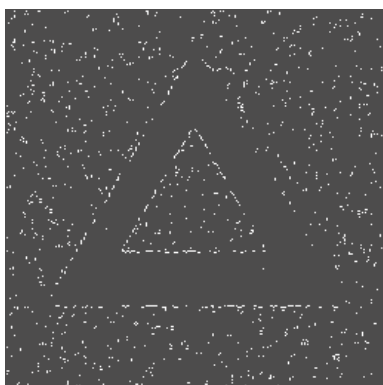
(e)



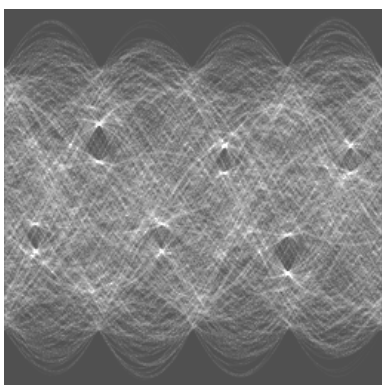
(f)



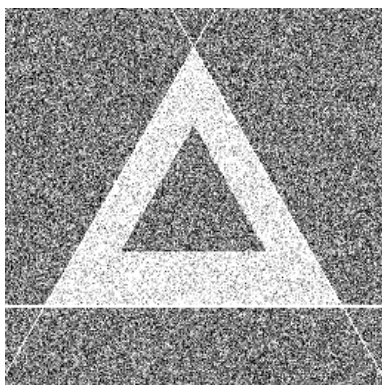
(g)



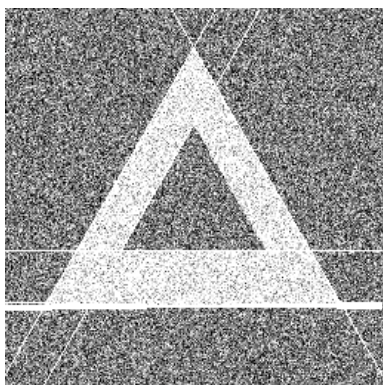
(h)



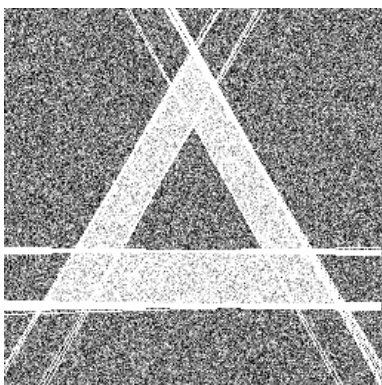
(i)



(j)

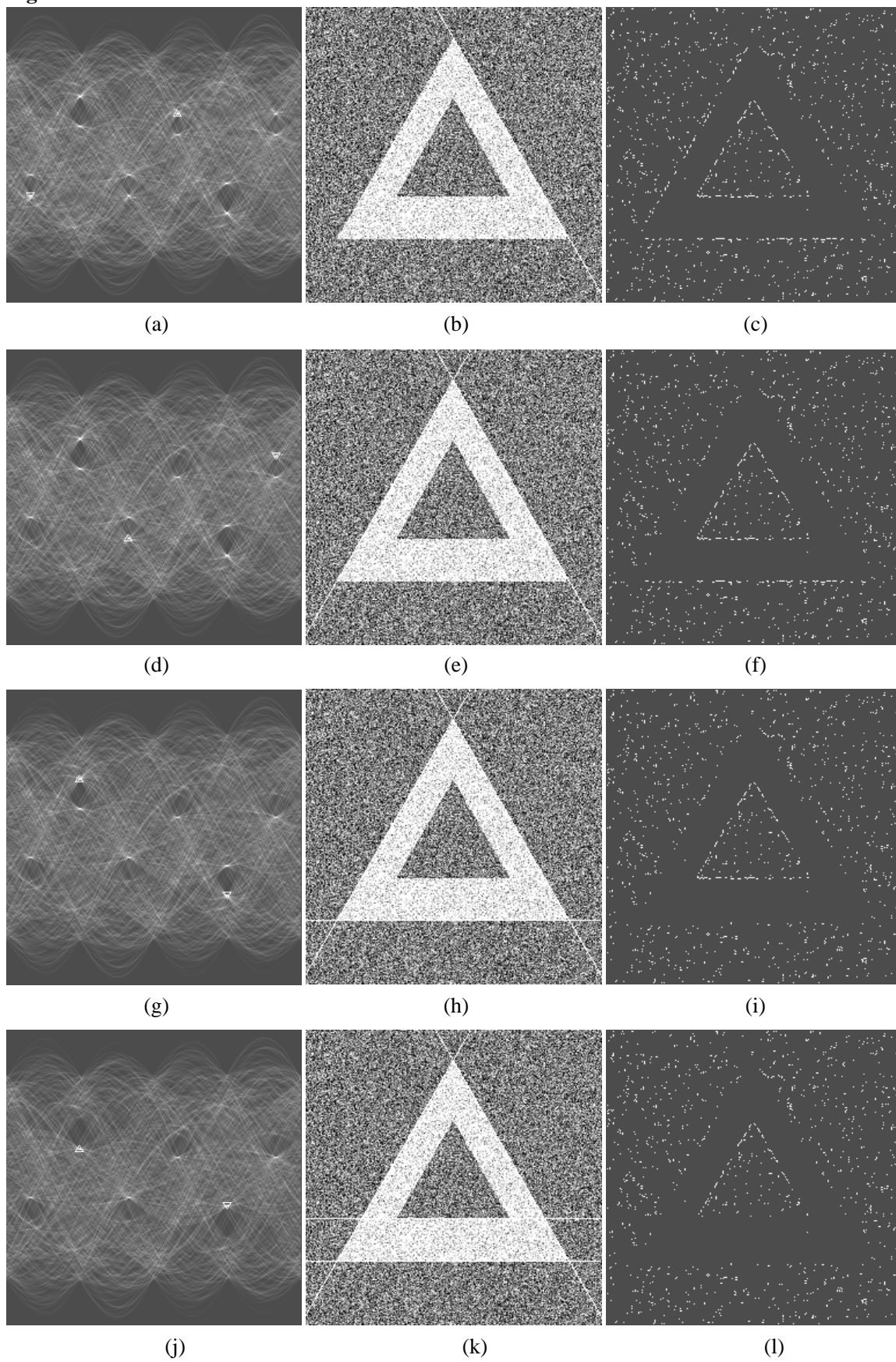


(k)

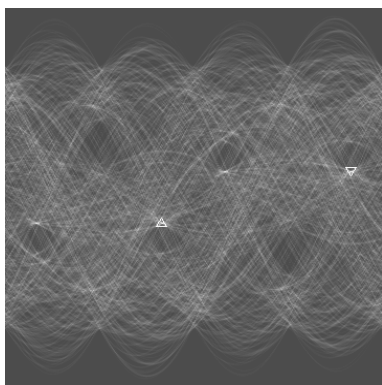


(l)

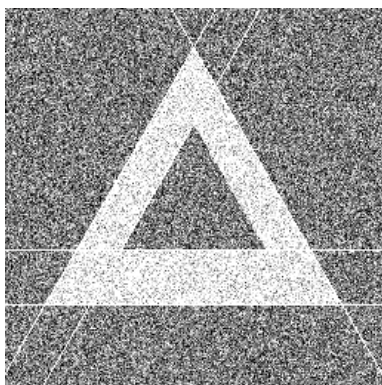
1 **Fig. 3**



1
2
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4
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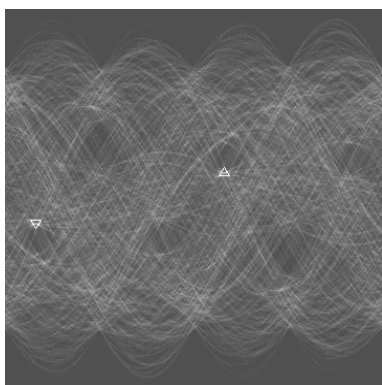
(m)



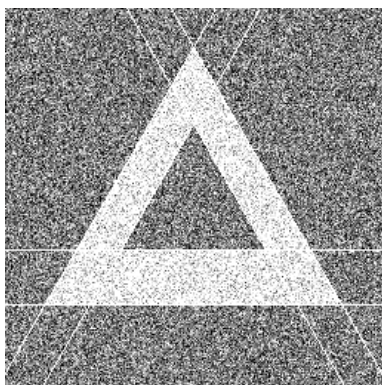
(n)



(o)



(p)

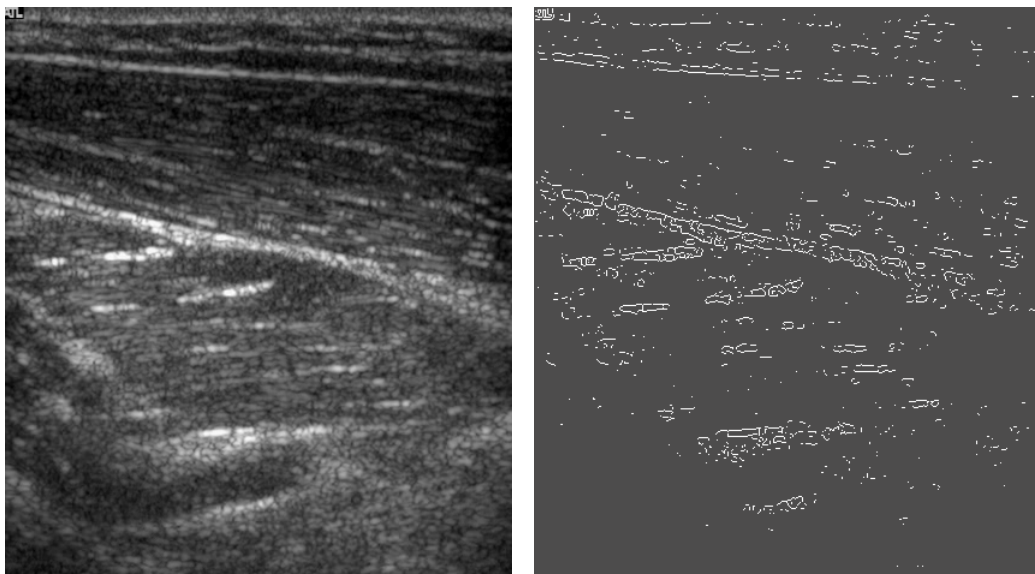


(q)



(r)

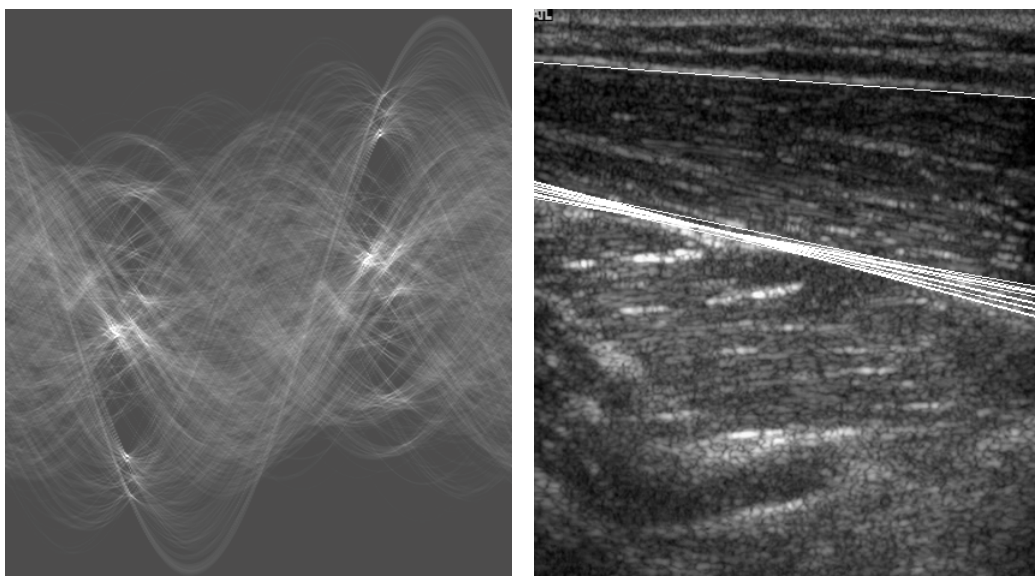
1 **Fig. 4**



(a)

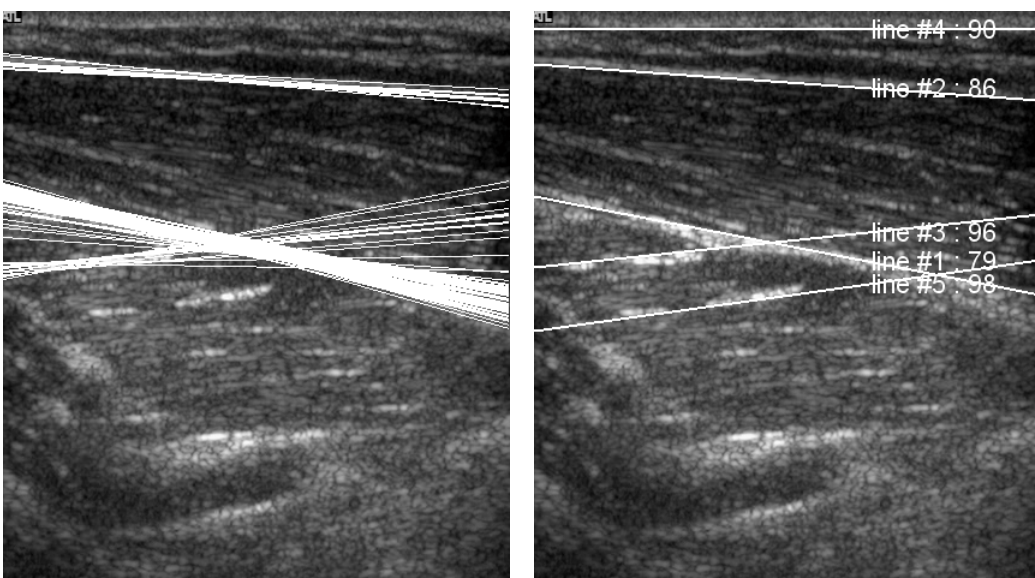
(b)

2



(c)

(d)



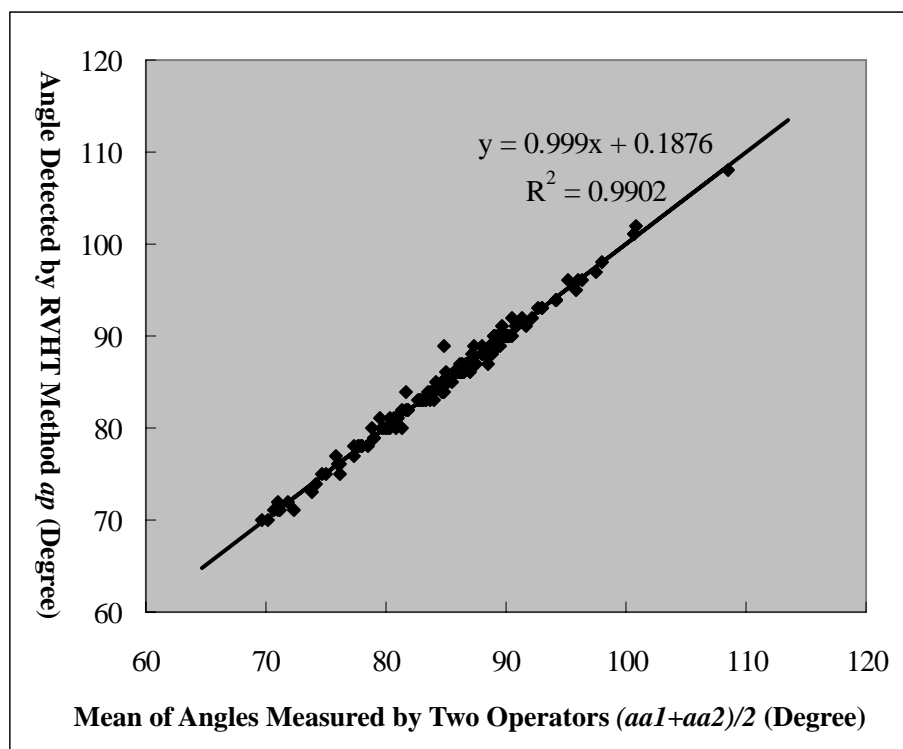
(e)

(f)

1 **Fig. 5**

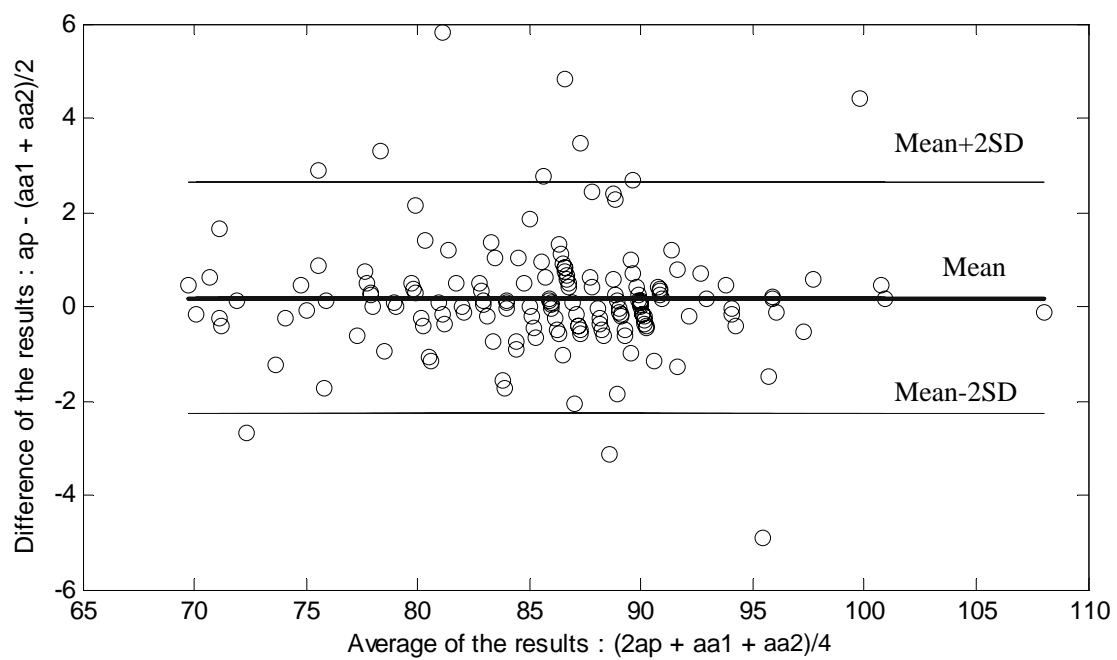
2

3



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1 **Fig. 6**



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