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3	River Stage Prediction Based on a Distributed Support Vector Regression
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8	Abstract:
9	An accurate and timely prediction of river flow flooding can provide time for the
10	authorities to take pertinent flood-protection measures such as evacuation. Various data-
11	derived models including LR (linear regression), NNM (the nearest-neighbor method) ANN
12	(artificial neural network) and SVR (support vector regression), have been successfully
13	applied to water level prediction. Of them, SVK is particularly highly valued, because it has the advantage over many data derived models in overcoming overfitting of training data
14	However SVR is computationally time-consuming when used to solve large-size problems
16	In the context of river flow prediction equipped with LR model as a benchmark and genetic
17	algorithm-based ANN (ANN-GA) and NNM as counterparts a novel distributed SVR (D-
18	SVR) model is proposed in the present study. It implements a local approximation to training
19	data because partitioned original training data is independently fitted by each local SVR
20	model. ANN-GA and LR models are also used to help determine input variables. A two-step
21	GA algorithm is employed to find the optimal triplets (C, ε, σ) for D-SVR model. The
22	validation results reveal that the proposed D-SVR model can carry out the river flow
23	prediction better in comparison with others, and dramatically reduce the training time
24	compared with the conventional SVR model. The pivotal factor contributing to the
25	performance of D-SVR may be that it implements a local approximation method and the
26	principle of structural risk minimization.
27	
28	Keywords: Water level prediction; D-SVR; Input selection; Parameter optimization

29 Introduction

As one of a number of nonstructural flood protection measures, an accurate and timely prediction of water levels in the station of interest is of great importance in helping the authorities determine whether to take measures and if do which measures would best mitigate potential flood damage. In the last two decades, with the development of software technology, many approaches affiliated to 'black box' techniques including NNM (nearest neighbor method), ANN (artificial neural network), and SVR (support vector regression) have been widely applied to flood prediction.

NNM has been reported in the literature to analyze rainfall-runoff and runoff/discharge processes and has been compared with ARX (autoregressive model with exogenous inputs), or ARMAX (autoregressive moving average model with exogenous inputs). NNM yielded satisfactory results (Yakowitz, 1987; Karlsson and Yakowitz, 1987; Galeati, 1990). The technique was extended to NNLPW (nearest neighbor linear perturbation model) for rainfall-runoff prediction (*Shamseldin and O'Connor, 1996*). Feature selection is
one of the most important aspects of pattern recognition, as used in the nearest neighbor
method. In the context of univariate time series such as discharge, the feature vector can
consist of several previous values (*Karlsson and Yakowitz, 1987; Galeati, 1990*).

46 Since the renaissance of ANNs in the late of 1980s, they have become the preferred 47 prediction approach for many researchers and have been applied to a variety of issues. While 48 some researchers in the literature employed ANNs alone for river flow forecasts (*Prochazka*, 49 1997; Thirumalaiah and Deo, 1998; Sheta and El-Sherif, 1999; Liong et al., 2000; Salas et 50 al., 2000; Qin et al., 2002; Cannon and Whitfield, 2002; Li and Gu, 2003; Huang et al., 2004; 51 Cheng et al., 2005; García-Pedrajas et al., 2006), many other researchers compared ANNs 52 with traditional statistical techniques for river flow flood predictions. Comparisons between 53 ANNs and AR (autoregressive) approaches appeared in the work of Raman and Sunilkumar 54 (1995), Elshorbagy and Simonovic (2000), Thirumalaiah and Deo (2000) and Kişi (2003). 55 Likewise, some studies were focused on comparisons between ANNs and ARMA (Jain et al., 56 1999; Abrahart and See, 2000; Castellano-Me'ndeza et al., 2004). The majority of studies 57 have proven that ANNs are able to outperform traditional statistical techniques. Further, the 58 superiority of ANNs over nonlinear regression in predicting river flows has been attributed to 59 the possible existence of nonlinear dynamics, which are not well captured by the regression 60 technique. A hybrid ANN model developed by Wang et al. (2006) was used to predict daily 61 stream flow.

62 SVR, with highly similar structures to ANN, can learn from experimental data. SVR performs structural risk minimization (SRM) that aims at minimizing a bound on the 63 64 generalization error (*Kecman, 2001*). In this way, it creates a model with a minimized VC-65 dimension (named after the authors, Vapnik and Chervonenkis), which means good 66 generalization. Since SVR generalization performance does not depend on the dimensionality 67 of input space, it can be used with small data sets. However, ANN is data intensive, and has 68 to cover as many patterns as possible in order to perform well, and the generality of ANN is 69 difficult to control as a result of implementing the empirical risk minimization (ERM) 70 principle. Recently, some applications of SVR have been seen in the prediction of rainfall-71 runoff process, rainfall, and river flow. For example, Sivapragasam et al. (2001) performed 72 one-lead-day rainfall forecasting and runoff forecasting using SVR, in which the input data 73 are pre-processed by singular spectrum analysis, resulting in a high-dimensional input space. 74 Yu et al. (2004) proposed a scheme that combined chaos theory and SVM to forecast daily 75 runoff. Bray and Han (2004) applied SVM to forecast runoff, focusing on the identification 76 of an appropriate model structure and relevant parameters. Sivapragasam and Liong (2004) 77 used the sequential elimination approach to identify the optimal training data set and then 78 performed SVR to forecast the water level. Sivapragasam and Liong (2005) divided the flow 79 range into three regions, and employed different SVR models to predict daily flows in high, 80 medium and low regions. Lin et al. (2006) presented a SVR model to predict long-term 81 monthly flow discharge series, and a comparison with results of appropriate ARMA and 82 ANN models demonstrated the better performance of SVR. Yu et al. (2006) carried out a 83 real-time flood stage forecasting based on SVR in which a hydrological concept of the time 84 of response was employed to identify lags of inputs and a two-step grid search method was 85 used for finding optimal parameters.

86 However, a major drawback of SVR is that training time tends to increase 87 exponentially with the number of training samples. For example, according to the algorithm presented in this paper below, the time required is about two days for a magnitude of 1000 training data whereas it is only 40 minutes for a magnitude of 100 training data. Moreover, using a single model to learn large-size data may well lead to mismatch as there are different noise levels in different input regions (*Cheng et al., 2006b*), which is a normal scenario for those rivers characterized by seasonal flooding.

93 This paper mainly aims at developing a distributed SVR (D-SVR) model with a two-94 step GA parameter optimization method to carry out a prediction of river flow. In order to 95 evaluate the performance of D-SVR, prediction is also arrived at via linear regression (LR), 96 NNM, and ANN-GA (genetic algorithm-based ANN). As an extension of the previous study 97 (Chau et al., 2005), some of the background on LR and ANN-GA will be set aside in the 98 present paper. Thus, the paper is constructed as follows: firstly, the principle of SVR and D-99 SVR is introduced and following this NNM is briefly described. Secondly, in the section on 100 construction of models, an emphasis is placed to input selection, and parameter k in NNM 101 and parameters (C, ε, σ) in D-SVR are optimized. In the results and discussion section, 102 results reveal that D-SVR model outperforms the other three models, but with a larger 103 training time except for the conventional SVR. In the conclusion, it is suggested that 104 nonlinear models may achieve more notable advantages over LR in the case of rainfall-runoff 105 mapping.

106 SVR and Distributed SVR

107 Unlike classical adaptation algorithms that work in an L_1 or L_2 norm and minimize the 108 absolute value of an error or of an error square with ERM, SVR performs SRM (*Kecman*, 109 2001). In this way, it creates a model with good generalization. The SRM induction principle 110 and the methodology of SVR are briefly described below (*Gunn*, 1998; Dibike et al., 2001; 111 *Kecman*, 2001; Sivapragasam et al., 2001, Liong and Sivapragasam, 2002; Cherkassky and 112 Ma, 2004; Yu et al., 2006).

113 Statistical learning theory

114 We consider here standard regression formulation in general settings for predictive 115 learning. The goal is to estimate an unknown real-valued function in the relationship:

116

 $y = r(X) + \delta \tag{1}$

where δ is independent and identically distributed (i.i.d) zero mean random error (noise), X is a multivariate input and y is a scalar output. The estimation is made based on a finite number of samples (training data): (X_i, y_i) , $(i = 1, \dots, N)$. The training data are i.i.d. samples concreted according to some (unknown) ioint probability density function

120 generated according to some (unknown) joint probability density function

121

$$p(X, y) = p(X)p(y|X)$$

122 The unknown function in (1) is the mean of the output conditional probability (aka regression123 function)

124 $r(X) = \int y p(y|X) dy$ (3)

125 A class of functions $f(X, \omega)$ can be formulated to approximate the relationship between input 126 vector and the output variable, where ω is the parameter vector of the function. The problem 127 of learning is to select the best function $f(X, \omega_0)$ (learning machine) from $f(X, \omega)$ that can 128 predict the output v as accurately as possible. Generally, the quality of an approximation is

(2)

measured by the loss or discrepancy measure $L(y, f(X, \omega))$. Therefore, the best approximation function is that for which the following expected risk function $R(\omega)$ is as small as possible:

131 $R(\omega) = \int L(y, f(X, \omega))dp(X, y)$ (4)

132 It is known that the regression function (3) is the one minimizing prediction risk (4) with the 133 familiar squared loss function loss:

 $L(y, f(X, \omega)) = (y - f(X, \omega))^2$ ⁽⁵⁾

135 Note that the set of functions $f(X, \omega)$, $\omega \in \Lambda$ supported by a learning method may or may not 136 contain the regression function (3). Thus, the problem of regression estimation is the problem 137 of finding the best approximation function that minimizes the prediction risk function

138 $R(\omega) = \int (y - f(X, \omega))^2 dp(X, y)$

139 using only the training data. This risk function measures the accuracy of the learning 140 method's predictions of unknown target function r(X).

141 A difficulty arises in the process of calculating (6) because the probability distribution 142 p(X, y) is unknown. Therefore, it is necessary an induction principle for risk minimization. 143 One such principle is the ERM inductive principle. A straightforward method is to replace 144 the expected risk $R(\omega)$ by the empirical risk $R_{emp}(\omega)$

145
$$R_{emp}\left(\omega\right) = \frac{1}{N} \sum_{i=1}^{N} \left(y_i - f\left(X_i,\omega\right)\right)^2 \tag{7}$$

However, the ERM principle does not guarantee that the function $f_{emp}(X, \omega)$ that 146 minimizes the empirical risk $R_{emp}(\omega)$ converges to the true (or best) function $f(X, \omega_0)$ that 147 148 minimizes the expected risk $R(\omega)$ when the number of training data is limited, such that the 149 sample is small. In other words, a smaller error on the training set does not necessarily imply 150 higher generalization ability (i.e., a smaller error on an independent test set). To make the 151 most out of a limited amount of data, a novel statistical technique called SRM has been 152 developed (Vapnik 1995, 1998). The theory of uniform convergence in probability provides 153 bounds on the deviation of the empirical risk from the expected risk. This theory shows that 154 it is crucial to restrict the class of functions that the learning machine can implement to one 155 with a capacity that is suitable for the amount of available training data.

156 The SRM principle theoretically minimizes the expected risk based on the 157 simultaneous minimization of both the empirical risk and the confidence interval Ω . 158 Therefore, SRM can maintain a trade off between the accuracy of the training data and the 159 capacity of the learning machine so as to improve generalization of the model.

160 For $\omega \in \Lambda$ and N > h, a typical uniform VC bound on the expected risk (also called 161 generalization bound *R*), which holds with probability $1 - \eta$, has the following form (*Vapnik*, 162 1995, 1998):

134

$$R(\omega) \le R_{emp}(\omega) + \Omega(N, h, \eta) \tag{8}$$

164
$$\Omega(N,h,\eta) = \sqrt{\frac{h\left(\log\frac{2N}{h}+1\right) - \log\left(\frac{\eta}{4}\right)}{N}}$$
(9)

165 The parameter h is called the VC-dimension, and it describes the capacity of a set of 166 functions to represent the data set. The VC dimension is a measure of the model complexity

(6)

167 and is often proportional to the number of free parameters in the function $f(X,\omega)$. 168 Particularly when N/h is small, a small empirical risk does not guarantee a small value of the 169 actual risk. In this case, in order to minimize the actual risk $R(\omega)$, one has to minimize the 170 right-hand side of the inequality in (8) simultaneously over both terms. In order to do this, one has to make the VC dimension a controlling parameter. Therefore, the SRM inductive 171 172 principle is intended to minimize the risk functional with respect to both terms: the empirical risk $R_{emp}(\omega)$ and the confidence interval Ω . The VC confidence term in (8) depends on the 173 chosen class of functions, whereas the empirical risk depends on the one particular function 174 175 chosen by the training procedure. The objective here is to find that subset of the chosen set of 176 functions, such that the risk bound for that subset is minimized. This is done by introducing a 177 "structure" by dividing the entire class of functions into nested subsets (Fig. 1). SRM then 178 consists of finding that subset of functions which minimizes the bound on the actual risk. 179 This is done by simply training a series of machines, one for each subset, where for a given 180 subset the goal of training is simply to minimize the empirical risk. One then takes that 181 trained machine in the series whose sum of empirical risk and VC confidence is minimal 182 (Burges, 1998).

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Fig. 1 should be put here

185 In the real hydrological world, most issues of interest tend to be nonlinear. A linear 186 SVR is extremely limited. In order to deal with the nonlinearity, the input data, X, in input 187 space is mapped to a high dimensional feature space via a nonlinear mapping function, $\phi(X)$. 188 Hence, the underlying function becomes

$$f(X,\omega) = \omega \cdot \phi(X) + b \tag{10}$$

190 Therefore, the objective of the SVR is to find optimal ω , *b* and some parameters in kernel 191 function $\phi(X)$ so as to construct an approximation function of the underlying function.

192 When introducing Vapnik's ε -insensitivity error or loss function (see Fig. 2), the loss 193 function $L_{\varepsilon}(y, f(X, \omega))$ on the underlying function can be defined as

194
$$L_{\varepsilon}(y, f(X, \omega)) = |y - f(X, \omega)|_{\varepsilon} = \begin{cases} 0 & \text{if } |y - (\omega \cdot \phi(X) + b)| \le \varepsilon \\ |y - (\omega \cdot \phi(X) + b)| - \varepsilon & \text{otherwise} \end{cases}$$
(11)

where *y* represents observed value. Fig. 2 presents the concept of nonlinear SVR,
corresponding to Eq. (11). Similar to linear SVR (*Kecman, 2001; Yu et al., 2006*), the
nonlinear SVR problem can be expressed as the following optimization problem:

$$\begin{array}{l} \text{minimize} \quad R_{W,\xi_i,\xi_i^*} = \frac{1}{2} \|\omega\|^2 + C \sum_{i=1}^N (\xi_i + \xi_i^*) \\ \text{198} \\ \text{subject to} \quad \begin{cases} y_i - f(\phi(X_i), \omega) - b \leq \varepsilon + \xi_i \\ f(\phi(X_i), \omega) + b - y_i \leq \varepsilon + \xi_i^* \\ \xi_i, \xi_i^* \geq 0 \end{cases} \tag{12}$$

199 where, the term of $\frac{1}{2} \|\omega\|^2$ reflects generalization, and the term of $C\sum_{i=1}^{l} (\xi_i + \xi_i^*)$ stands for 200 empirical risk. The objective in Eq. (12) is to minimize them simultaneously, which implements SRM to avoid underfitting and overfitting the training data. ξ_i and ξ_i^* are slack variables, shown in Fig. 2 for measurements "above" and "below" an ε tube. Both slack variables are positive values. *C* is a positive constant that determines the degree of penalized loss when a training error occurs.

By introducing a dual set of Lagrange Multipliers, α_i and α_i^* , the minimization problem can be solved in a dual space. The objective function in dual form can be represented as (*Gunn*, 1998):

maximize
$$L_d(\alpha, \alpha^*) = -\varepsilon \sum_{i=1}^N (\alpha_i^* + \alpha_i) + \sum_{i=1}^N (\alpha_i^* - \alpha_i) y_i - \frac{1}{2} \sum_{i,j=1}^N (\alpha_i^* - \alpha_i) (\alpha_j^* - \alpha_j) (\phi(X_i) \cdot \phi(X_j))$$

subject to
$$\begin{cases} \sum_{i=1}^N (\alpha_i - \alpha_i^*) = 0 \\ 0 \le \alpha_i^* \le C, \quad i = 1, \cdots, N \\ 0 \le \alpha_i \le C, \quad i = 1, \cdots, N \end{cases}$$
(13)

208

There is no fixed guideline how to select an appropriate nonlinear function $\phi(X_i)$. 209 Furthermore, the computation of $(\phi(X_i) \cdot \phi(X_i))$ in the feature space may be too complex to 210 perform. An advantage of SVR is that the nonlinear function $\phi(X)$ need not be used. The 211 212 computation in input space can be performed using a "kernel" function $K(X_i, X_i) = (\phi(X_i) \cdot \phi(X_i))$ to yield inner products in feature space, avoiding having to 213 perform a mapping $\phi(X)$. In utilizing kernel functions, the key issue is to select admissible 214 kernel functions. The admissible kernel function should be any symmetric function in input 215 216 space which can represent a scalar product in feature space. The Mercer kernel functions belonging to a set of reproducing kernels (Vapnik, 1999; Kecman, 2001) can be proven 217 admissible. Therefore, any functions that satisfy Mercer's theorem can be used as a kernel. A 218 couple of commonly used kernels in SVR include: (1) linear $K(X_i, X_j) = X_i \cdot X_j$; (2) 219 polynomial with degree $d \quad K(X_i, X_j) = \left[(X_i \cdot X_j) + 1 \right]^d$;(3) multilayer perceptron 220

221
$$K(X_i, X_j) = \tanh[(X_i \cdot X_j) + b]$$
; (4) Gaussian RBF $K(X_i, X_j) = \exp(-\frac{\|X_i - X_j\|^2}{2\sigma^2})$. After

obtaining parameters α_i , α_i^* , and b_0 , the final approximation function of the underlying function is

224
$$f(X_i) = \sum_{i=1}^{N} (\alpha_k - \alpha_k^*) K(X_k \cdot X_i) + b_0, k = 1, \dots, n$$
(14)

where X_k stands for the support vector, α_k and α_k^* are parameters associated with support vector X_k , N and n represent the number of training samples and support vectors, respectively.

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- 229

Fig. 2 should be put here

230 SVR expressed in matrix notation

231 The standard quadratic optimization problem for an ε -insensitive function can be 232 expressed in matrix notation as (Gunn, 1998; Kecman, 2001)

233 minimize
$$L_d(x) = \frac{1}{2}x^T H x + C^T x$$
 (15)

234 where, H is Hessian matrix, x stands for Lagrangian Multipliers. They are expressed as

235
$$H = \begin{bmatrix} G & -G \\ -G & G \end{bmatrix}, \ C = \begin{bmatrix} \varepsilon - Y \\ \varepsilon + Y \end{bmatrix}, \text{ and } x = \begin{bmatrix} \alpha \\ \alpha * \end{bmatrix}$$

236 with constraints

237
$$x \cdot (1, \dots, 1, -1, \dots, -1) = 0$$
,

238
$$\alpha_i, \alpha_i * \ge 0, i = 1, \cdots, l.$$

239 G is an (l,l) matrix with entries $G_{ij} = [X_i^T X_j]$ for a linear regression, and $\alpha = [a_1, \dots, \alpha_l]$, $\alpha^* = [a_1^*, \dots, a_l^*], \varepsilon - Y = [\varepsilon - y_1, \dots, \varepsilon - y_l], \varepsilon + Y = [\varepsilon + y_1, \dots, \varepsilon + y_l].$ (Note that G_{ij} , as given 240

above, is a badly conditioned matrix and we rather use $G_{ij} = [X_i^T X_j + 1]$ instead). 241

242 In the case of the nonlinear regression, the learning problem is again formulated as the maximization of a dual Lagrangian (15). A similar matrix notation as Eq. (15) is expressed. 243 244 However, H here is with the changed Grammian matrix G that is now given as

245
$$G = \begin{bmatrix} G_{11} & \cdots & G_{1l} \\ \vdots & G_{ii} & \vdots \\ G_{l1} & \cdots & G_{ll} \end{bmatrix}$$

where the entries $G_{ii} = \phi^T(X_i)\phi(X_i) = K(X_i)(X_i), i, j = 1, \dots, l$. Based on the above matrix 246 form, a SVR programming is easy to make. 247

248 **D-SVR** Configuration

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Fig. 3 should be put here

250 A primitive idea of D-SVR is to partition the original training set into a couple of 251 subsets and then generate a local SVR for each subset independently. Further, an appropriate 252 data fusion approach (sometimes called aggregation) is employed to combine local 253 predictions into a hybrid output. Fig. 3 displays the configuration of D-SVR. First of all, 254 fuzzy c-means clustering algorithm is employed to split the original training set into Ltraining subsets. In the present study, water level variables are characterized by clear 255 256 seasonal variability, and so the raw training set is clustered into eight sub regions. Thus, each subset further serves for training L SVRs. For a new input X, L outputs $(Y_i, i=1, \dots, L)$ will 257 be generated by the D-SVR model and are associated with L degrees of membership 258 $(\mu_i, i=1, \dots, L)$. Degree of membership can be determined via the inverse of Square Euclidean 259 Distance between the new input X and C_i which is the center of *i*-th subset. Calculation is 260 formulated as follows: 261

262
$$\begin{cases} \mu_{i}=1 & \text{if } d_{i}=0, \quad i=1,\cdots,L\\ \mu_{i}=\left(\frac{1}{d_{i}}\right) / \left(\sum_{i=1}^{L}\frac{1}{d_{i}}\right) & \text{otherwise} \end{cases}$$
(16)

263 where,
$$\mathbf{d}_i = \|\mathbf{X} \cdot \mathbf{C}_i\|^2$$
 and $\sum_{i=1}^{L} \mu_i = 1, \mu_i \in [0,1]$.

After *L* outputs $(Y_i, i=1, \dots, L)$ and their degrees of membership $(\mu_i, i=1, \dots, L)$ are achieved, the combined output Y is

(17)

$$Y = \sum_{i=1}^{L} \mu_i Y_i$$

However, we found experimentally that there are some drawbacks in this D-SVR: 267 268 when training data is partitioned into several independent subsets without any overlapping, a 269 large prediction error occurs. Generally, the error is larger than that obtained by using a SVR model alone. Analysis also found that the SVR is weak at extrapolation. When an input is far 270 271 from its clustering center, the SVR will generate a weird prediction, usually quite large 272 although associated with a small degree of membership. In view of this, we attempted to 273 make the following improvement. We set the nearest neighboring two training subsets to 274 overlap one input region by one in the entire input space, thus the number of training data in 275 all sub models will be twice that of the original training data. Furthermore, only two 276 maximum degrees of membership are activated to contribute to the combined output Y. Therefore, the third box in Fig. 3 addresses this task, where μ_i (i = 1, 2) is the first two 277 maximum degree of membership in μ_i ($i = 1, \dots, n$), and Y_j (j = 1, 2) are corresponding 278 outputs as listed in the fourth box of Fig. 3. Finally, a combined output for D-SVR model is 279 $Y = \sum_{i=1}^{2} (\mu_i / \sum_{i=1}^{2} \mu_i) Y_i$ 280 (18)

281 Nearest-Neighbor Method (NNM)

282 The following is a brief review of the NN method (Galeati, 1990; Shamseldin and 283 O'Connor, 1996). Let $\{X(i), i = 1, N\}$ be a set of rainfall measurements or parameters related to the forecasting process being studied (e.g., temperature, soil saturation, etc.) expressed as 284 $X(i) = (P_i, P_{i-1}, P_{i-2}, \dots, P_{i-m+1})^T$ where P stands for feature information (various hydro-285 meteorological factors affecting runoff prediction (Galeati, 1990; Yakowitz, 1987), m is the 286 287 number of feature information contributing to feature vector or the vector dimension and 288 $\{Q(i), i = 1, N\}$ a set of discharges. Here, X and Q may be single or multiple variables. For 289 each feature vector X(i), there is an associated discharge O(i) observed at the same time 290 instant. Thus, the available historical data may be summarized into a set of pairs of feature 291 vectors X(i) and scalar discharges Q(i), as $\{X(i), Q(i) : i = 1, N\}$, where n is the total number of the data in the whole historical record. Thus, the NN prediction of Q(N+1) is obtained as: 292

293
$$\hat{Q}(N+1) = \frac{1}{k} \sum_{i \in S(X,N)} Q(i+1)$$
(19)

where S(X,N) denotes the indices of k, the nearest neighbors to the feature vector X(N). The meaning of "nearest neighbors" has to be interpreted according to the Euclidean distance: if 296 d(n) represents a vector of coordinates $d_1, d_2, ..., d_m$, the differences between the current 297 feature vector and past data, the Euclidean distant is defined as:

298 $||d|| = \left(\sum_{i=1}^{m} d_i^2\right)^{1/2}$ (20)

299 Therefore, if *i* is in *S* and *j* is not in *S*, then $||X(N) - X(i)|| \le ||X(N) - X(j)||$. Intuitively 300 speaking, the forecast $\hat{Q}(N+1)$ by the *k* nearest neighbor method is the sample average of 301 succeeding runoff of the *k* nearest neighbors in the database.

As an example from the work of Karlsson and Yakowitz (1987) displayed in Fig.4, for simplicity, it is supposed that the feature vector depends only on three values of past discharges (m=3) i.e. X(N) = [Q(N), Q(N-1), Q(N-2)], and it is assumed that k=4. The NN algorithm searches through all the consecutive triplets of the historical record for the four triplets closest (in a Euclidean sense) to the present feature vector. The predicted discharge is the mean of successive outflows (shown in Fig.4 as circles) from the four closest historical events.

309 Standardization of X and Q is usually necessary because it eliminates the units from 310 components or elements and reduces any differences in the range of values amongst 311 components such as rainfall and discharge with their different units and scales. In order to 312 reflect the relative importance because the more recent measurements in the feature vector 313 generally have a greater weight towards predicted values, the Euclidean distance can be

314 computed as a weighted Euclidean norm, i.e., $||d||_{w} = \left(\sum_{i=1}^{m} w_{i} \cdot d_{i}^{2}\right)^{1/2}$ where 315 $w = (w_{1}, w_{2}, \dots, w_{m})$ is a fixed sequence of positive numbers (weights). In the present study, an

315 $w = (w_1, w_2, \dots, w_m)$ is a fixed sequence of positive numbers (weights). In the present study, an 316 equivalent weight is assigned to each dimension in the feature vector because all variables 317 are water levels.

- Thus, the prediction model is $\hat{Q}(N+1) = \frac{1}{k} \sum_{i \in S(X,N)} Q(i+1)$. In order to reflect the relative contribution to prediction value, each of all *k* neighbors is set to a weight factor ω_i which is based on the Euclidean distance. The prediction model becomes
- 321 $\hat{Q}(N+1) = \frac{1}{k} \sum_{i \in S(X,N)} Q(i+1) \cdot \omega_i$ (21)

322 where, $\omega_i = \left\| d_i \right\|^{-2} / \sum_{i=1}^{k} \left\| d_i \right\|^{-2}$. Then, an optimal k has to be determined by calibration.

Generally, the data set is divided into two parts: one is used to construct the NN-predictors (constructing patterns); the other is used to calibrate parameters. Objective function optimizing k is set up as $J(k) = \sum (Q(i+1) - \hat{Q}(i+1))^2$, $i = 1, \dots N$, where Q(i+1) is observed value.

327

Fig. 4 should be put here

- 328 Construction of Models
- 329 Study Area

330 The channel reach studied is in the middle stream of the Yangtze River, which is the 331 largest river in China. It passes through Wuhan City, which is the capital of the Hubei 332 Province (see Fig. 5). The flow of the Yangtze River is quite unsteady and exhibits a seasonal 333 behavior. The flow is low during the winter months, and peak flow occurs during August and 334 September. A hydrological year is often classified into a flooding period and a nonflooding period, which are from June to October and from November to May, respectively. The water 335 336 level at the Luo-Shan station can be as low as 17.35 m during the nonflooding period and as 337 high as 31.04 m during the flooding period. The average water levels are 20.8 and 27.1 m 338 during the nonflooding and flooding periods, respectively. The purpose of this study is to 339 predict water levels of the downstream station, Han-Kou, by known water levels of the 340 upstream station, Luo-Shan. The lateral inflow is neglected, because it is very small in 341 comparison with the discharge of the main stream.

342

Fig. 5 should be put here

343 Data Preparation

A remarkable property of ANNs or SVRs is their ability to handle nonlinear, noise, and non-stationary data. However, with suitable data preparation beforehand, it is possible to improve the performance further (*Maier and Dandy, 2000; Bray and Han, 2004*). Data preparation involves a number of processes such as data collection, data division and datapreprocessing. Here, data division and data standardization belonging to data preprocessing will be covered.

350 Many research papers have discussed data division in the process of application of 351 ANN (ASCE, 2000; Chau et al., 2005). Typically, ANNs are unable to extrapolate beyond 352 the range of the data used for training. Consequently, poor forecasts/predictions can be expected when the validation data contains values outside of the range of those used for 353 354 training. It is also imperative that the training and validation sets are representative of the 355 same population. Often statistical properties (mean, variance, range) from them are compared 356 in order to measure the representatives. The similar data handling can be applied to SVR in 357 order to obtain the same baseline of comparison. Taking the same data splitting way as that 358 in Chau et al. (2005), the data are randomly divided into three sets: training, testing, and 359 validation. While 75% of the data are used for training, 25% are used for validation. The 360 training data are further divided into 2/3 for the training set and 1/3 for the testing set.

In the present study we extract 1,448 input-output data pairs of the following formatfrom the data record:

[X(t-4), X(t-2), X(t), Y(t+1)]

which shows that the water level of Y at Han-Kou for the next day can be mapped by water levels of X at Luo-Shan at the present day, two-day ahead and four-day ahead. A detailed description for the mapping format can be found in the section on inputs selection. It was ensured that the data used for training, testing, and validation represents the same population so there is no need to extrapolate beyond the range of their training data. Table 1 shows the statistical parameters, including the mean, standard deviation, minimum, maximum, and range, for the training, testing, and validation sets.

371

363

Table 1 should be put here

Generally, original data for different variables span different ranges. In order to ensure that all variables receive equal attention during the training process, they should be normalized. In this regard, it is not true for this case as shown in Table 1. However, due to restricted domain of independent variables of transfer functions in ANN and kernel functions in SVR, the raw data normalization is required. Additionally, normalization will improve the condition number of the Hessian in the optimization problem (*Gunn, 1998*). All data are scaled to the interval 0.1–0.9. The advantage of using [0.1, 0.9] rather than [0, 1] is that extreme (high and low) water levels, occurring outside the range of the calibration data, may be accommodated (*Hsu et al., 1995*). The scaling and reserve scaling processes are formulated below:

382
$$X_{norm} = 0.1 + 0.8 \times \left(\frac{X_i - X_{min}}{X_{max} - X_{min}}\right)$$
(22)

383
$$Y_{norm} = 0.1 + 0.8 \times \left(\frac{Y_i - Y_{min}}{Y_{max} - Y_{min}}\right)$$
(23)

384 $\hat{Y}_{i} = Y_{min} + \left(\frac{1.0}{0.8}\right) \times (\hat{Y}_{i,norm} - 0.1) \times (Y_{max} - Y_{min})$ (24)

385 where X_{norm} and Y_{norm} denote scaled appearance of the raw data X_i and Y_i , $\hat{Y}_{i,norm}$ stands for

the scaled prediction corresponding to Y_i , and \hat{Y}_i is the prediction of Y_i in original scale.

387 Inputs Selection

388 In model development the selection of appropriate input variables is important since it 389 provides the basic information about the system being modeled. However, determining 390 appropriate inputs is not an easy task. Generally, input determination can be divided into two 391 broad stages (Bowden et al., 2005). In the first stage, the objective is to reduce the 392 dimensionality of the original set of inputs, resulting in a set of independent inputs, which are 393 not necessarily related to the model output. As a matter of fact, the addition of unnecessary 394 variables would create a more complex model than is required. Moreover, the complex 395 model is susceptible to overfitting of training data. Therefore, it is imperative that variables 396 are independent of each other as system inputs. This subset of inputs can then be used in the 397 second stage to determine which of these inputs are related in some way to the output.

Bowden et al. (2005) presented a comprehensive review of approaches on input determination in the water resources and those approaches are broadly classified into five groups. In the present paper, a mixed approach is employed to find optimal inputs.

401 Usually, the number of input variables is not known a priori. A firm understanding of 402 the hydrologic system under consideration plays an important role in the successful 403 implementation of the model. For the present case, the travel time of flood between Luo-404 Shan and Han-Kou is determined to be about 24 hrs using the Muskingum method. In other 405 words, the flood at Han-Kou has a phase lag of approximately one day with that at Luo-Shan. So X(t) as an input is reasonable. In order to reduce the dimensionality of inputs, an 406 407 autocorrelation analysis on water levels on Luo-Shan was performed and is shown in Fig. 6. 408 An extreme good autocorrelation exists in water level series and any one input at least in the 409 first ten lags cannot be deleted according to this chart. A linear relation on water levels exists between Luo-Shan and Han-Kou. A stepwise linear model analysis on inputs (Luo-Shan 410 411 water levels) and output (Han-Kou water level) can help determine optimal inputs from a 412 viewpoint of the linear relationship. Fig. 7 is the result of a stepwise linear model. The 413 optimal linear mapping format between two hydrology stations is with three inputs X_{10} , X_8 , and X₆(corresponding to X (t), X (t-2), and X (t-4)) and one output Y (t+1). 414

415 Obviously, autocorrelation analysis and stepwise linear regression analysis cannot 416 capture any nonlinearity among inputs and between inputs and output. Further, sensitivity 417 analyses (computing the contribution to variance) (Nord and Jacobsson, 1998) and weights 418 analyses (Muttil and Chau, 2006) on inputs based on ANN are carried out to extract 419 nonlinear information. Notably, as Nord and Jacobsson (1998) reported in the conclusion of 420 their paper, due to the random starting conditions, important inputs remain changeable. In 421 addition, according to their evaluation criteria, results from both methods on the ranking of 422 inputs are not always consistent during training. An improvement is to employ the ANN-GA 423 model, which is with the architecture 3-3-1 described in the section of results, to obtain the 424 relative optimal initial weights and biases for an ANN model.

425 When ANN is initialized by weights and biases from GA optimization, a more stable 426 ANN model can be achieved and has a good generalization. Due to the fixed initial weights 427 and biases, evaluation results on input importance are steady, but results from two 428 approaches are still inconsistent. Based on the approach of Nord and Jacobsson (1998), X₉, 429 X_{10} , X_8 , X_3 , and X_6 are ranked in the top five important inputs. When adding X_3 , X_9 430 respectively to initial linear model based on X₆, X₈, and X₁₀, several models are generated. The performances of these models are listed in Table 2. From the perspective of AIC and 431 432 RMSE from LR and ANN-GA, choosing X₆, X₈, and X₁₀, i.e. X (t), X (t-2), and X (t-4), as 433 the optimal inputs is tenable. Finally, the optimal linear regression (LR) model is

- 434 Y(t+1) = 1.18X(t) 0.398X(t-2) + 0.229X(t-4) 5.08(25)
- 435 Fig. 6 should be put here
- 436 Fig. 7 should be put here
- 437 *Table 2 should be put here*
- 438 Parameters Tuning Strategy of D-SVM

439 Obtaining optimal α_i and α_i^* in Eq. (13) depends heavily on these parameters that dominate the nonlinear SVR including the cost constant C, the radius of the insensitive 440 441 tube ε , and the kernel parameters. In the present study, the Gaussian RBF is employed as 442 kernel function. So these parameters consist of a triplet (C, ε, σ) , whose components are 443 mutually dependent, and so changing the value of one parameter changes other parameters. 444 Therefore, a simultaneous or global optimization scheme such as GA can be helpful (*Cheng* 445 et al., 2006a). Due to lack of any a priori knowledge for their bounds, a two-step GA search 446 algorithm is recommended here, which is inspired by a two-step grid search method (Hsu et 447 al., 2003). First, a coarse range search was used to achieve the best region of these threedimensional grids. In the present study, coarse range partitions for C are $[10^{-2} \ 10^{0}]$, $[10^{0} \ 10^{2}]$, 448 $[10^2 5.0 \times 10^2]$, and $[5.0 \times 10^2 10^3]$. Coarse range partitions for ε are $[10^{-4} 10^{-3}]$, $[10^{-3} 10^{-2}]$, $[10^{-3} 10^{-2}]$ 449 2 10⁻¹], and [10⁻¹ 10⁰], and coarse range partitions for σ are [10⁻³ 10⁻²], [10⁻² 10⁻¹], [10⁻¹ 10⁰], 450 and $[10^{0} \ 10^{2}]$. There are 4³ grids, and one of them is selected as intervals of parameters for 451 452 the next step. Then, in the second step a further GA search for the triplets (C,ε,σ) will be 453 carried out in the selected intervals.

In order to avoid overfitting of training data, testing data and training data were evaluated at the same time according to GA's fitting degree function (i.e., RMSE), and weighted average of their fitting degrees was used as the fitting degree of each population in the process of GA operation.

458 Evaluation of Performance

459 Many measures for model evaluation have been documented in the literature of hydrology application (Legates and McCabe, 1999; Elshorbagy and Simonovic, 2000; 460 461 Luchetta and Manetti, 2003; Goswami et al., 2005). Several conventional measures such as correlation coefficient (r or R^2), efficiency coefficient (E), index of agreement (d), RMSE, 462 and so on, were critically reviewed by Legates and McCabe (1999), and the review suggested 463 464 that correlation coefficient is inappropriate for model evaluation. Legates and McCabe (1999) 465 suggested a complete assessment of model performance should include at least one 'goodness-of-fit' or relative error measure (e.g., E or d) and at least one absolute error 466 measure (e.g., RMSE or MAE) with additional supporting information. Herein, two 467 468 conventional evaluation criteria in hydrology, RMSE (root mean square error) and E 469 (efficiency coefficient), are used to measure performances of models based on training data, 470 testing data and validation data.

471 (1) RMSE

472
$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (Y_i - \hat{Y}_i)^2}$$
(26)

473 (2) E

474 Nash and Stucliffe (*1970*) defined the model coefficient of efficiency which ranges
475 from minus infinity to 1.0, with higher values indicating better agreement, as:

476
$$E = 1 - \frac{\sum_{i=1}^{N} (Y_i - \hat{Y}_i)^2}{\sum_{i=1}^{N} (Y_i - \overline{Y})^2}$$
(27)

477

where \hat{Y}_i = forecast water level, Y_i = observed water level, \overline{Y} = average observed flow, and 478 479 *N*=number of observations. RMSE provides a quantitative indication of the model absolute 480 error in terms of the units of the variable, with the characteristic that larger errors receive 481 greater attention than smaller ones. This characteristic can help eliminate approaches with 482 significant errors. However, some studies (Kachroo and Natale, 1992; Legates and McCabe, 483 1999) have reported that the index E is a rather crude index, being overly sensitive to 484 extreme values, because of the square differences in the definition, while being insensitive to 485 additive and proportional differences between model predictions and observations. This 486 feature will lead to the increasing influence of large floods on the calibrated parameter values 487 and thereby enhance the forecast accuracy of the larger floods. In the present study, however, 488 parameter calibration is not based on E, but rather on RMSE.

489 **Results and Discussion**

490 *Results from NNM*

The nearest-neighbor method belongs to typical pattern prediction. A good prediction can be achieved when testing or validation patterns are as similar as possible to those of the training data. In other words, a salient limitation of the NNM is that in no case can a value higher than the historical discharges be predicted. This is a deficiency which would severely limit the generality or even the plausibility of the NNM when used in real time forecasting (*Karlsson and Yakowitz, 1987*). However, for daily management purpose in which the interest is not centered on extreme values, it is viable. Therefore, it is viable for daily waterlevel prediction in the present study.

499 According to the principle of NNM, a key step is to find the optimal k (the number 500 of the nearest neighbors) based on the training data. An optimization process on k is graphed 501 in Fig. 8. The optimal k is 7 with RMSE tst of 0.234m and RMSE vali of 0.242m.

502 Fig. 8 should be put here

Fig. 9 should be put here

504 The upper pane in Fig. 8 displays 362 validation samples and comparison of absolute 505 errors between LR and NNW prediction models is exhibited in the lower pane of Fig. 9. As a whole, error curves from LR and NNW show the same trend. However, compared with LR, 506 507 the NNM exhibits larger error amplification at some particular points where local extremum 508 appear on the water level curve. Obviously, the performance of NNM is slightly poorer than 509 that of LR, which seems to be discrepant with the recognized fact that NNM can be superior to some linear models. Two potential aspects can contribute to the present phenomenon: first, 510 511 the prediction series are highly linear; second, training data is not enough for NNM which 512 make it not be able to efficiently capture these patterns reflecting local extremum points.

513 Results from ANN-GA

503

514 In the present study, the ANN-GA model played dual roles both as a counterpart model and as helping determine inputs for all models. Table 3 shows the process determining 515 516 optimal architecture of ANN based on a three-layer network assumption. So the main task of 517 this experiment was to find the optimal number of hidden nodes and number of training 518 epochs. Here, a testing set was employed to avoid overfitting of the training set based on the 519 early stop method. These values highlighted by bold and italic typeface in 'Test' column 520 exhibit optimal training epochs for different hidden nodes. Configuration of ANN 521 corresponding to the minimum of them may be relatively optimal. Obviously, the minimum 522 is 0.2285 corresponding to M = 3 and epoch=7000. Further, based on the selected 523 parameters M and epoch, inputs analysis can be performed as shown in the previous section 524 of input selection. Finally, the determined architecture of ANN for the present case is 3-3-1 with optimal training epoch of 7000. Corresponding RMSE for training, testing and 525 526 validation set are 0.213m, 0.223m, and 0.237m as shown in Table 6.

527Table 3 should be put here528Fig. 10 should be put here

529 Similar to Fig. 9, Fig. 10 describes prediction error processes from LR and ANN-GA. 530 While ANN-GA does not exhibit a good capturing capacity for local extremum points on the 531 curve of validation samples, it seems to exhibit a better capacity for capturing other points 532 than the LR model. Other than the small size of training samples, an unsteady prediction 533 result can contribute to the poor performance due to the unstable parameter optimization 534 method inherent in ANN although GA can lead to a relatively stable initial weights and 535 biases. In other words, the present ANN may still not an optimal ANN for this case.

536 *Results from D-SVR and Conventional SVR*

537 According to previous partition of original data set, samples in training, testing and 538 validation sets are, respectively, 724, 362, and 362. Experiment showed that computation

539 time may vary from about a couple of seconds to nearly half an hour when the number of 540 samples ranges from 50 up to about 300. The optimization process for C, ε, σ based on GA 541 will have to run hundreds of times, which is extremely time-consuming for large-size training 542 samples. Therefore, the present training data was partitioned into eight subsets with an 543 average size of 181 (724/4=181) samples due to the overlapping between two nearest subsets. When adding testing data to the training set, the sample number employed in using GA to 544 545 optimize parameters (C, ε, σ) for D-SVRs is 2172 in all, i.e., two times as the number of 546 training and testing samples $(2172=2\times(724+362))$. On the other hand, for conventional SVR 547 model, GA is also employed to find optimal triplets (C, ε, σ) for training set with the help of 548 testing set to control overfitting. Table 4 displays clustering centers and the size of training 549 and testing data associated with each subset for D-SVR model.

550

Table 4 should be put here

551 Based on the two-step GA search approach, the optimal values of triplet parameter 552 (C,ε,σ) for each subset are obtained as shown in Table 5. The composite training error 553 (RMSE) is 0.21m with a training time of about 2hrs, and support vectors are 68.5%. Further, 554 the testing error and validation error are 0.209m and 0.211m, as shown in Table 6. As a 555 comparison, the training, testing and validation errors from conventional SVR are 556 respectively 0.213m, 0.216m, and 0.236m, which are larger than those from D-SVR, in 557 particular for the validation error. Meanwhile, the training time in conventional SVR is far 558 larger than that in D-SVR, which is unaccepted for the current one-day-ahead prediction.

559 In addition, Fig. 11 displays the comparison of absolute errors between LR and D-SVR models. Their error curves exhibit similar trend, but D-SVR shows evident better 560 prediction capacity than LR in terms of absolute errors although predictions on local 561 562 extremum points are still not very good, which may be due to the property of the local 563 approximation performed by D-SVR model.

564

Table 5 should be put here

565 Fig. 11 should be put here

566 **Comparison among Models and Discussion**

567 Table 6 summarizes performance of different models from RMSE, E of validation 568 data, and training time. In view of its unacceptable training time, conventional SVR model 569 will be put aside in the discussion. Three nonlinear models, NNM, ANN-GA, and D-SVM, show a better performance than that of LR in terms of RMSE of training and testing. 570 571 However, only D-SVR exhibits a better generalization than LR in terms of RMSE of 572 validation data. The value of E also proves that D-SVR's efficiency is the best. A drawback 573 of D-SVR is computationally time-consuming due to hundreds of times parameters 574 optimization via GA.

575 In order to display the performance from nonlinear models, absolute error curves of 576 them were graphed in Fig. 12. Errors from these curves are with a very similar trend that 577 predictions are underestimated at some points whereas predictions are overestimated at other 578 points such as from 230 to 290 at the X-axis.

579 Although NNM, ANN-GA, and D-SVM are all nonlinear models, they are different 580 in essence. NNM and ANN are generally called nonlinear and non-parameter models unlike 581 LR with its fixed formula form. Therefore, their performance is related to many aspects including raw data quality, suitable data preprocessing, and even the ability of modelers, in particular for ANN. However, different from NNM and ANN-GA, D-SVR does not depend on pattern identification to carry out prediction. To certain extent, it may be called a parameter model or semi-parameter model which can be uniquely achieved under the SRM principle when the triplet parameters are selected. On the other hand, a fixed prediction result is never expected for ANN model due to the random starting conditions. Moreover, the principle of ERM tends to make ANN and NNM be weak in the aspect of generalization.

589 The D-SVR model performed a nonlinear approximation for each subset. Obviously, 590 a local nonlinear fitting from D-SVR should be better than an empirically global fitting from 591 LR. Therefore, if over-fitting is carefully avoided, it is inevitable that the D-SVR achieves a 592 better prediction in comparison with LR.

- 593Table 6 should be put here594Fig. 12 should be put here
- 595

596 Conclusions and Recommendations

597 As one of nonstructural flood protection measures, the future water level at a 598 downstream station was predicted by the water level series at an upstream station. Equipped 599 with LR model as a benchmark and ANN-GA and NNM as counterparts, a novel D-SVR 600 model was established to carry out the forecast using data collected from water level series at 601 the upstream Luo-Shan station and downstream Han-Kou station. ANN-GA and LR models 602 were also used to help determine input variables. A two-step GA algorithm was employed to 603 optimize the triplet parameters (C, ε, σ) for D-SVR model. The validation results revealed 604 that proposed D-SVR model can predict the water level better in comparison with the other 605 models, which may be because it implements a local approximation method and the principle 606 of SRM. However, compared with LR model, NNM and ANN-GA did not exhibit a powerful 607 mapping ability in the present case.

608 Certainly, the conclusion should not be hastily drawn that NNM and ANN are worse. 609 As a matter of fact, studies in the literature have reported that NNM and ANN are very 610 powerful in terms of nonlinear mapping. Associated with small-size training data, the present 611 case is characterized by a highly linear mapping relation, which restricts the power of NNM 612 and ANN. A complicated mapping between rainfall and runoff may be expected to really 613 expose their capabilities, which will be presented in a future study.

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Model variables		Statistical parameters						
and data sets	Mean	Standard deviation	Minimum	Maximum	Range			
$X_{t-4}(m)$								
Training set	23.46	3.71	17.37	30.96	13.59			
Testing set	23.46	3.71	17.35	30.93	13.58			
Validation set	23.46	3.71	17.37	31.04	13.67			
$X_{t-2}(m)$								
Training set	23.46	3.71	17.35	31.04	13.69			
Testing set	23.46	3.71	17.39	30.96	13.57			
Validation set	23.47	3.71	17.37	30.80	13.43			
$X_t(m)$								
Training set	23.47	3.71	17.37	30.96	13.59			
Testing set	23.46	3.71	17.35	30.93	13.58			
Validation set	23.46	3.71	17.37	31.04	13.67			
$Y_{t+1}(m)$								
Training set	18.64	3.75	12.20	25.71	13.51			
Testing set	18.64	3.75	12.26	25.70	13.44			
Validation set	18.64	3.75	12.21	25.69	13.48			

Table 1. Statistical Parameters for Training, Testing, and Validation Sets

Table 2 Akaike's Information Criterion (AIC) for Models

Model	RMSE_trn	RMSE_tst	RMSE_vali	AIC
	(m)	(m)	(m)	AIC
$LR(X_6, X_8, X_{10})$	0.2396	0.240	0.237	1.630
$LR(X_6, X_8, X_{10}, X_9)$	0.2395	0.242	0.238	1.632
$LR(X_6, X_8, X_{10}, X_3)$	0.2394	0.240	0.237	1.634
$ANN-GA(X_6, X_8, X_{10})$	0.213*	0.223*	0.237*	1.601*
ANN-GA (X_6, X_8, X_{10}, X_9)	0.210*	0.229*	0.245*	1.778*
ANN-GA (X ₆ ,X ₈ ,X ₁₀ ,X ₃)	0.210*	0.229*	0.242*	1.778*

*Average over ten time tests

Table 3 RMSE of Train and Test Set with Changing Hidden Nodes (M) and Epochs

M		2	;	3	4	4	Ę	5	(6	-	7
Epoch	Train	Test										
1000	0.2075	0.2326	0.2035	0.2399	0.1992	0.2775	0.1958	0.2364	0.1952	0.2788	0.4705	0.4533
3000	0.2075	0.2325	0.2080	0.9157	0.1980	0.2545	0.1937	0.7127	0.1857	0.3041	0.1855	0.3210
5000	0.6113	0.5673	0.2035	0.2399	0.1991	0.2573	0.1936	0.2873	0.1891	0.4448	0.1866	0.3679
7000	0.2148	0.2362	0.2032	0.2285	0.2008	0.2554	0.1869	0.2598	0.1905	0.4036	0.1902	0.4881
9000	0.2075	0.2325	0.2033	0.3080	0.1991	0.2769	0.1964	0.3792	0.1913	0.3381	0.1861	0.3975
11000	0.2075	0.2325	0.2021	0.2387	0.2002	0.3402	0.1942	0.5286	0.1869	0.2877	0.1831	0.3218
M	ł	8	(Ð	1	0	1	1	1	2	1	3
1000	0.1871	0.3467	0.1760	1.4003	0.1746	0.4095	0.1711	0.4803	0.1664	0.6671	0.1644	0.4986
3000	0.1783	0.3004	0.1701	0.3191	0.1682	0.6884	0.1666	0.6667	0.1574	0.3723	0.1564	0.5020
5000	0.1877	2.5142	0.1795	0.4923	0.1761	0.9704	0.1728	0.3499	0.1576	1.1967	1.0416	0.9948
7000	0.1823	1.0629	0.1769	0.5054	0.1776	0.3178	0.8488	0.8334	0.1596	0.3657	0.1540	0.5319
9000	0.1797	0.4496	0.1806	0.5123	0.1702	0.8181	0.1662	0.4935	0.1676	2.2748	0.1579	0.3514
11000	0.4303	0.4220	0.1785	0.6683	0.1695	0.5109	0.1688	0.7671	0.1649	0.5135	0.1577	0.3803
M	1	4	1	5	1	6	1	7	1	8	1	9
1000	0.1571	0.4847	1.5085	1.4068	0.1520	0.7772	0.1465	0.8242	0.1477	0.8621	0.1411	1.0257
3000	0.1505	0.7819	0.1486	0.5772	0.1544	0.9932	0.1508	0.5340	0.1324	0.7250	0.1327	0.7653
5000	0.1587	0.9445	0.1519	0.3877	0.1464	1.2091	0.1413	0.5150	0.1403	0.5975	0.1340	0.6271
7000	0.1600	0.4541	0.1459	0.6086	0.1461	0.7584	1.0348	0.9819	0.1316	0.5012	0.1387	0.7769
9000	0.1580	0.6617	0.1486	0.6439	0.1436	1.0023	0.1400	1.7086	0.1332	1.0227	0.1417	0.9096
11000	0.1552	0.5632	0.1465	1.2319	0.1467	0.7592	0.4745	0.4632	0.1362	0.8169	0.1341	2.5940

Note: values in Train and Test columns correspond to their RMSE

Table 4 Characteristics of Subsets Partitioned by FCM

Subset		Training & testing			
n	X(t-4)	X(t-2)	X(t)	Y(t+1)	data number
1	27.9	27.9	27.9	23.1	304
2	24.9	24.9	24.9	20.1	258
3	26.7	26.6	26.6	21.8	252
4	23.4	23.4	23.4	18.7	307
5	18.5	18.5	18.5	13.5	284
6	21.7	21.6	21.6	16.9	240
7	29.5	29.5	29.5	24.5	143
8	19.8	19.8	19.8	14.9	384
Sum					2172

Table 5 Calibration Results of Triplet Parameters (C, ε, σ) in D-SVR

Model		Tri	plet Paramet	ers	RMSE_trn	Percentage of SVs
		С	Е	σ	(m)	(%)
	Submodel1	242.83	0.0004	0.689		
	Submodel2	144.03	0.0065	0.422		
	Submodel3	80.53	0.0031	3.297		68.5
DSVP	Submodel4	724.31	0.0033	0.477	0.210	
D-SVK	Submodel5	239.29	0.0062	0.066	0.210	
	Submodel6	873.04	0.0231	0.527		
	Submodel7	894.02	0.0006	0.596		
	Submodel8	137.51	0.0035	0.922		
Conve	entional SVR	649.36	0.0049	0.515	0.213	68.6

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Table 6 Performances for Different Models

Model	RMSE_trn	RMSE_tst	RMSE_vali	E_vali	Training time
WIOUEI	(m)	(m)	(m)		(s)
LR	0.234	0.240	0.237	0.9960	-
NNM	-	0.234	0.242	0.9961	10
ANN-GA	0.213	0.223	0.237	0.9960	53
Conventional SVR	0.213	0.216	0.236	0.9960	153532
D-SVR	0.210	0.209	0.211	0.9968	7110



Fig. 1 Bound on Actual Risk Is Sum of Empirical Risk and Confidence Interval (adapted from Vapnik, 1998)

Support vector















Fig. 12 Comparison of absolute errors among NNM, ANN-GA, and D-SVR