

# Thermodynamic assessment of an integrated molten carbonate fuel cell and absorption refrigerator hybrid system for combined power and cooling applications

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**Abstract:** A hybrid system is proposed to harvest the waste heat released in MCFC through integrating an absorption refrigerator as a bottoming cycle. A thermo-electrochemical model is used to describe the main irreversible losses in the system. The operating current density interval of the MCFC that enables the bottoming absorption refrigerator to effectively cool is determined. Numerical expressions for the equivalent power output and efficiency are derived to evaluate the performance of the hybrid system under different operating conditions. Compared to the stand-alone MCFC, the maximum power density and the corresponding efficiency of the hybrid system are found to be increased by 3.2% and 3.8%, respectively. The general performance characteristics and optimum operating regions for the hybrid system are revealed. Comprehensive parametric analyses are conducted to investigate how the hybrid system performance depends on various physical properties and working conditions such as working fluid internal irreversibility inside the absorption refrigerator, heat transfer coefficients, some thermodynamic losses related parameters, and the operating current density, temperature and pressure of the MCFC.

**Keywords:** Molten carbonate fuel cell; Absorption refrigerator; Hybrid system; Irreversible loss; Thermodynamic assessment

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## Nomenclature

$A$	Effective polar plate area of the MCFC ( $\text{m}^2$ )
$A_L$	Heat-transfer area between the MCFC and the environment ( $\text{m}^2$ )
$A_R$	Overall heat-transfer area of the absorption refrigerator ( $\text{m}^2$ )
$A_0$	Total heat-transfer area of the condenser and absorber ( $\text{m}^2$ )
$A_c$	Heat-transfer area of the evaporator ( $\text{m}^2$ )
$A_h$	Heat-transfer area of the generator ( $\text{m}^2$ )
$A_{re}$	Heat-transfer area of regenerator ( $\text{m}^2$ )
$b_1$	Ratio between $K_h$ and $K_0$
$b_2$	Ratio between $K_h$ and $K_c$
$c_1, c_2$	Integrated parameters in Eq. (14) ( $\text{W m}^{-2} \text{K}^{-1}$ )
$E$	Equilibrium potential (V)
$E_0$	Ideal standard potential (V)
$E_{act}$	Activation energy ( $\text{J mol}^{-1}$ )
$F$	Faraday's constant ( $\text{C mol}^{-1}$ )
$(-\Delta \dot{H})$	Total energies supplied to the hybrid system per unit time ( $\text{J s}^{-1}$ )
$\Delta h$	Molar enthalpy change of the electrochemical reactions ( $\text{J mol}^{-1}$ )
$I$	Operating electric current through the cell (A)
$I_r$	Internal irreversibility
$j$	Operating current density ( $\text{A m}^{-2}$ )
$j_0$	Exchange current density ( $\text{A m}^{-2}$ )
$j_c$	Lower bound operating current density of the MCFC ( $\text{A m}^{-2}$ )

$j_M$	Allowable maximum current density of the MCFC ( $\text{A m}^{-2}$ )
$j_S$	Stagnation operating current density of the MCFC ( $\text{A m}^{-2}$ )
$j_P$	Operating current density at $P_{\max}^*$ ( $\text{A m}^{-2}$ )
$K$	Heat-transfer coefficient in Eqs. (8) and (9) ( $\text{J m}^{-2} \text{K}^{-1} \text{s}^{-1}$ )
$K_L$	Heat-leakage coefficient ( $\text{J m}^{-2} \text{K}^{-1} \text{s}^{-1}$ )
$K_{re}$	Heat-transfer coefficient of the regenerator ( $\text{J m}^{-2} \text{K}^{-1} \text{s}^{-1}$ )
$n_e$	Number of electrons involved per electrochemical reaction
$P$	Power output (W)
$P_{AR}$	Equivalent power output of the absorption refrigerator (W)
$P^*$	Power density ( $\text{W m}^{-2}$ )
$P_C^*$	Power density at $j_C$ ( $\text{W m}^{-2}$ )
$P_M^*$	Power density at $j_M$ ( $\text{W m}^{-2}$ )
$P_{\max}^*$	Maximum power density of the hybrid system ( $\text{W m}^{-2}$ )
$p_i$	Partial pressures of specie $i$ (atm)
$q_L$	Heat-leakage rate from the MCFC to the environment ( $\text{J s}^{-1}$ )
$q_0$	Total heat-transfer rate from the condenser and absorber to the environment ( $\text{J s}^{-1}$ )
$q_c$	Heat-transfer rate from the cooled space to the evaporator ( $\text{J s}^{-1}$ )
$q_h$	Heat-transfer rate from the MCFC to the generator ( $\text{J s}^{-1}$ )
$q_{re}$	Heat-loss rate of the regenerator ( $\text{J s}^{-1}$ )
$R$	Universal gas constant ( $\text{J mol}^{-1} \text{K}^{-1}$ )
$\Delta S_h$	Rate of entropy flows into the working fluid at temperature $T_1$ ( $\text{J s}^{-1} \text{K}^{-1}$ )

$\Delta S_c$	Rate of entropy flows into the working fluid at temperature $T_2$ ( $\text{J s}^{-1} \text{K}^{-1}$ )
$\Delta S_0$	Rate of entropy flows out of the working fluid at temperature $T_3$ ( $\text{J s}^{-1} \text{K}^{-1}$ )
$T$	Operating temperature of MCFC (K)
$T_0$	Temperatures of the environment (K)
$T_1, T_2, T_3$	Temperatures of the working fluids in the generator, evaporator, condenser and absorber (K)
$T_c$	Temperature of the cooled space (K)
$U_m$	Overpotentials ( $m = an, cat$ or $ohm$ ) (V)

### ***Greek symbols***

$\varepsilon$	Effectiveness of the regenerator
$\eta$	Efficiency
$\eta_{AR}$	Efficiency of the absorber refrigerator
$\eta_c$	Efficiency at $j_c$
$\eta_p$	Efficiency at $P_{\max}^*$

### ***Subscripts***

an	Anode
cat	Cathode
ohm	Ohmic
AR	Absorption refrigerator

## 1. Introduction

Unlike conventional heat engines in which electricity is produced from chemical energy with the intermediate mechanical energy conversion, fuel cells are static energy conversion devices that directly convert the chemical energy in fuels into electricity [1, 2]. Fuel cells have the great potential to reduce greenhouse gas emissions and fossil fuel consumptions and have been considered to be one of the most promising power generation technologies [3]. MCFCs (molten carbonate fuel cells) use a molten carbonate electrolyte, which is usually a mixture of  $\text{Li}_2\text{CO}_3$  and  $\text{K}_2\text{CO}_3$ . At anode, the input hydrogen reduces  $\text{CO}_3^{2-}$  ions in the electrolyte to form  $\text{CO}_2$  and release two electrons. The produced  $\text{CO}_2$  are subsequently transported to the cathode. At cathode, new  $\text{CO}_3^{2-}$  ions are formed by combining the  $\text{CO}_2$  from the anode and the  $\text{O}_2$  from the air with the two electrons from the external circuit thus closing the chemical and electrical loops [4]. In the existing literature, most investigations on MCFCs have focused on aspects including materials fabrication [5, 6], further understanding of electrochemical processes and transport phenomena [7, 8], stack modeling and dynamic simulation [9-11], and cell-based carbon dioxide capture [12, 13]. Up to now, MCFCs have reached a level of maturity enough for commercialization in some countries such as USA, Germany, Japan, Italy and South Korea [14].

The R&D in MCFCs has made a great progress in solving problems such as corrosion issue, short lifetime, and high cost [15-17], however, the low power density is still a drawback that restricts the wide commercialization of MCFCs [18]. To improve the power density, many efforts have made on MCFC itself by optimizing the operating conditions and system layouts or by developing more advanced materials to reduce the polarization losses [19-23]. Alternatively, the high operating temperature of MCFC provides an opportunity of cogeneration with CHP (combined heat and power)

systems to recover the waste heat for additional applications, and thus, the power density of MCFC-based cogeneration systems could be enhanced with reference to that of the stand-alone mode MCFCs [24-36]. Gas turbines are often used as the bottoming cycle for MCFCs, a number of studies are performed on MCFC-GT (MCFC-gas turbine) hybrid systems fed with different fuels using different analysis approaches at different scales [24-29]. In addition to the common gas turbine engines, some scholars discussed the feasibilities of some other bottoming thermal cycles for MCFCs [30-35]. Zhang et al. [30, 31] employed a Carnot cycle and a Braysson cycle to recover the waste heat for additional power generation and revealed the effects of some operating conditions and designing parameters on the performance of the hybrid system. Sánchez et al. [32] compared a reciprocating engine with three bottoming thermal cycles (Rankine cycle, Brayton cycle and Stirling cycle) for an MCFC and showed that the Stirling engine was an alternative competitor over conventional gas turbines. Vatani et al. [33] considered an ORC (Organic Rankine Cycle) to recover the waste heat from an IR-MCFC (internal reforming-MCFC) with two different configurations, the first configuration was that the cathode outlet provided the heat for pre-reforming process and then entered ORC, and the second configuration was that the cathode outlet was simultaneously split into two streams for ORC and pre-reforming process. The global energy and exergy efficiencies of the latter configuration were found to be 60.45% and 57.75%, respectively, which were about 3% higher than that of the first configuration. Mamaghani et al. [34] proposed an MCFC-GT-ORC (Molten Carbonate Fuel Cell-Gas Turbine-Organic Rankine Cycle) hybrid plant, 4E (energetic, exergetic, economic and environmental) analyses were performed and the multi-objective optimum solutions showed that the exergetic efficiency of the hybrid plant was about 55%, which was approximately 19.4% larger than that of the sole MCFC system. Chen et al. [35] developed a hybrid system based

on a high-temperature fuel cell and a heat engine with a unified model including Carnot, Brayton, Otto, Diesel, Atkinson, and Braysson cycles. They investigated the effects of main irreversible losses in fuel cells and heat engines on the performance of the hybrid system and determined the optimum operating region of some important performance parameters.

Refrigeration systems play a crucial role in our daily lives as they could provide human comfort and food preservation [36]. Up to now, most of the installed refrigeration systems are conventional vapor compression cooling devices, which not only use ozone-depleting working fluids but also consume electricity [37-43]. An absorption refrigerator, enables to effectively cool by using heat instead of electricity, which has been widely used for waste heat recovery and air conditioning [44-50]. Recently, Silveira et al. [51] used the waste heat contained in the exhaust gases of an MCFC to run an absorption refrigerator for electricity and cold water production synchronously. This technology was demonstrated to be feasible by energy, exergy and economic analyses. However, thereafter, seldom works done on this MCFC/absorption refrigerator hybrid system. Further development and optimization are still required in order to make this system to be economical, reliable, efficient and even market-competitive.

In this study, a hybrid system that integrates a MCFC with an absorption refrigerator to simultaneously produce electricity and cooling is established to improve the overall performance. Numerical expressions for the power output and efficiency of the hybrid system are formulated by considering multiple irreversibilities such as the electrochemical irreversible losses inside the MCFC, internal irreversibilities inside the absorption refrigerator, regeneration losses in the regenerator, and heat-transfer irreversibilities between the MCFC and the absorption refrigerator and the surroundings. The general performance characteristics and optimum operating regions of the hybrid system are

revealed, and the operating current densities of the MCFC that enable the absorption refrigerator to function will be determined. The effects of some operating conditions and design parameters on the performance of the hybrid system will be discussed through comprehensive parametric analyses.

## 2. System description

The hybrid system proposed in this paper consists of a MCFC, a regenerator and an absorption refrigerator, as schematically shown in Fig. 1, where the absorption refrigerator is constituted by a generator, a condenser, an evaporator and an absorber. The MCFC converts the chemical energy in the fuel into electricity and waste heat. The electricity is delivered to the external circuit and the waste heat is collected and extracted for else uses. One part of the waste heat is transferred to the generator to drive the bottoming absorption refrigerator for cooling purposes, another part is transferred to compensate the regenerative losses, and the last part is leaked into the environment. In Fig. 1,  $P_{MCFC}$  is the electric power output of the MCFC,  $q_h$  is the heat-transfer rate from the MCFC at temperature  $T$  to the working fluid in the generator at temperature  $T_1$ ,  $q_c$  is the heat-transfer rate from the cooled space at temperature  $T_c$  to the working fluid in the evaporator at temperature  $T_2$ ,  $q_0$  is the total heat-transfer rate from the working fluids in the condenser and absorber at temperature  $T_3$  to the environment at temperature  $T_0$ ,  $q_L$  is the heat-leakage rate from the MCFC to the environment, and  $q_r$  is the heat loss rate in the regenerator.

To conveniently describe the main irreversible losses existing in the system, some simplifications and assumptions are made [52-55]: (1) Both MCFC and absorption refrigerator are operated under steady state conditions; (2) Operating temperature and pressure are uniform and constants in the MCFC; (3) Electrochemical reactions are completely proceed; (4) Internal electric current and fuel crossover are negligible; (5) Working fluids in the absorber and condenser shares the same



temperature; (6) Working fluids in the absorption refrigerator flows constantly and exchanges heat continuously with external heat reservoirs; (7) Work input required by the solution pump in the absorption refrigerator is negligible; (8) Heat transfers within the system obey Newton's law.

## 2.1. The MCFC

When the electrochemical reactions are proceeded inside the MCFC, some irreversible losses primarily originated from the anode overpotential, cathode overpotential and ohmic overpotential are inevitable. Adopted the electrochemical model proposed in Refs. [52, 53], the electric power output and efficiency of an MCFC can be, respectively, expressed as

$$P_{MCFC} = jA(E - U_{an} - U_{cat} - U_{ohm}), \quad (1)$$

and

$$\eta_{MCFC} = \frac{n_e F}{-\Delta h} (E - U_{an} - U_{cat} - U_{ohm}), \quad (2)$$

where

$$E = E_0 + \frac{RT}{n_e F} \ln \left[ \frac{p_{H_2,an} (p_{O_2,cat})^{0.5} p_{CO_2,cat}}{p_{H_2O,an} p_{CO_2,an}} \right], \quad (3)$$

$$E_0 = (242000 - 45.8T) / (n_e F), \quad (4)$$

$$U_{an} = 2.27 \times 10^{-9} j \exp \left( \frac{E_{act,an}}{RT} \right) p_{H_2,an}^{-0.42} p_{CO_2,an}^{-0.17} p_{H_2O,an}^{-1.0}, \quad (5)$$

$$U_{cat} = 7.505 \times 10^{-10} j \exp \left( \frac{E_{act,cat}}{RT} \right) p_{O_2,cat}^{-0.43} p_{CO_2,cat}^{-0.09}, \quad (6)$$

$$U_{ohm} = 0.5 \times 10^{-4} j \exp \left[ 3016 \left( \frac{1}{T} - \frac{1}{923} \right) \right], \quad (7)$$

## 2.2. The absorption refrigerator

The absorption refrigerator in the hybrid system begins to extract heat from the cooled space once some waste heat flow from the MCFC to the generator. The absorption refrigerator is operated

between three temperature levels given assumptions that the working fluids in the absorber and condenser have the same temperature (i.e.,  $T_3$ ) and exchange heat with the heat sinks at the same temperature (i.e.,  $T_0$ ) [56-59]. By considering the internal irreversible effects inside the working fluids and the external finite-rate heat transfer irreversibilities, one may obtain the maximum cooling rate  $R$  and the corresponding coefficient of performance  $\varepsilon$  of the absorption refrigerator for a given heat-transfer rate  $q_h$  and total heat-transfer area  $A_R$  [57, 58]:

$$R = q_c = \frac{q_h}{2} \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4 T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}, \quad (8)$$

and

$$\varepsilon = \frac{1}{2} \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4 T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}, \quad (9)$$

where  $a = 1 + (T_c - I_r B^2 T_0) / [(1+B)^2 T]$ ,  $I_r$  is the internal irreversibility factor that characterizes the irreversible extent inside cyclic working fluids,  $B = (\sqrt{b_2} - 1) / (1 + \sqrt{I_r b_1})$ ,  $K_h$  is the heat-transfer coefficient of the generator,  $K_0$  is the heat-transfer coefficient of the condenser or absorber, and  $K_c$  is the heat-transfer coefficient of the evaporator,  $b_1 = K_h / K_0$ ,  $b_2 = K_h / K_c$ ;  $A_0$  is the total heat-transfer area of the condenser and absorber,  $A_h$  and  $A_c$  are respectively the heat-transfer areas of the generator and evaporator,  $A_R = A_h + A_c + A_0$  is the overall heat-transfer area of the absorption refrigerator,  $C = (1+B)^2 / (A_R K)$  and  $K = K_h / [1 + \sqrt{I_r b_1}]^2$ .

As the exergy contents of electric power and cooling load are different, the equivalent power output  $P_{AR}$  and efficiency  $\eta_{AR}$  for absorption refrigerator can be expressed as [60, 61]:

$$P_{AR} = q_c \left| 1 - \frac{T_0}{T_c} \right| = \frac{q_h}{2} \left| 1 - \frac{T_0}{T_c} \right| \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4 T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}, \quad (10)$$

and

$$\eta_{AR} = \frac{P_{AR}}{q_h} = \frac{1}{2} \left| 1 - \frac{T_0}{T_c} \right| \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4 T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}. \quad (11)$$

### 2.3. The regenerator

The regenerator in the hybrid system functions as a counter-flow heat exchanger that absorbs the high-temperature heat contained in the exhaust products at temperature  $T$  to warm the inlet reactants at the ambient temperature  $T_0$ . Due to the irreversibility associated with heat transfer, some regenerative losses are inevitable and the rate of regenerative losses is often calculated as follows [30, 62]:

$$q_{re} = K_{re} A_{re} (1 - \varepsilon)(T - T_0), \quad (12)$$

### 2.4. Performance of the hybrid system

The heat-leak rate  $q_L$  is often assumed to be proportional to the temperature difference between the MCFC and the environment, thus  $q_L$  and  $q_1$  can be, respectively, expressed as [63, 64]

$$q_L = K_L A_L (T - T_0), \quad (13)$$

and

$$q_h = -\Delta \dot{H} - P_{MCFC} - q_{re} - q_L = -\frac{A \Delta h}{2F} \left[ (1 - \eta_{MCFC}) j - \frac{2F (c_1 + c_2)(T - T_0)}{-\Delta h} \right], \quad (14)$$

where  $K_L$  is the heat-leakage coefficient,  $A_L$  is the corresponding heat-transfer area,  $c_1 = [K_{re} A_{re} (1 - \varepsilon)] / A$  and  $c_2 = K_L A_L / A$  are two integrated parameters that not only depend on the heat-transfer irreversibilities but also depend on the geometric sizes of the regenerator and MCFC.

As shown by Eq. (14), the bottoming absorption refrigerator begins to absorb heat from the cooled space only when the formula (15) is valid

$$-\Delta \dot{H} - P_{MCFC} > q_{re} + q_L. \quad (15)$$

Combining Eq. (14), Eq. (15) can be explicitly rewritten as

$$j > j_c = \left[ \frac{2F}{-\Delta h(1 - \eta_{MCFC})} \right] [(c_1 + c_2)(T - T_0)], \quad (16)$$

where  $j_c$  is the lower bound operating current density of the MCFC from which the bottoming absorption refrigerator starts to work. Moreover, the allowable maximum current density  $j_M$  can be numerically determined by Eqs. (12) - (14) and the condition of  $P_{AR} > 0$ .

For  $j_c < j < j_M$ , the equivalent power output  $P$  and efficiency  $\eta$  of the hybrid system can be, respectively, expressed as

$$P = P_{MCFC} + q_c \left| 1 - \frac{T_0}{T_c} \right| = P_{MCFC} + \frac{q_h}{2} \left| 1 - \frac{T_0}{T_c} \right| \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}, \quad (17)$$

and

$$\begin{aligned} \eta &= \frac{P_{MCFC} + P_{AR}}{-\Delta \dot{H}} \\ &= \eta_{MCFC} + \frac{\left| 1 - \frac{T_0}{T_c} \right|}{2} \left[ 1 - \eta_{MCFC} + \frac{2F(c_1 + c_2)(T - T_0)}{j \Delta h} \right] \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_h} \right)^2 - 4T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_h} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_h} \right] \right\}. \end{aligned} \quad (18)$$

For  $j \leq j_c$  or  $j \geq j_M$ , the absorption refrigerator in the hybrid system works totally irreversibly,  $P_{AR} = 0$  and  $\eta_{AR} = 0$ , and the power output  $P$  and efficiency  $\eta$  of the hybrid system equal to that of the stand-alone MCFC, i.e.,

$$P = P_{MCFC}, \quad (19)$$

and

$$\eta = \eta_{MCFC} \cdot \quad (20)$$

### 3. Performance characteristics and optimum operating regions

Based on the mathematical model formulated in Section 2 and typical parameters summarized in Table 1 [52, 53, 55], numerical calculations can be used to reveal the general performance characteristics of the hybrid system. The power densities and efficiencies of the MCFC, absorption refrigerator and hybrid system varying with the operating current density of MCFC are shown in Fig. 2, where  $P_{MCFC}^* = P_{MCFC} / A$ ,  $P_{AR}^* = P_{AR} / A$  and  $P^* = P / A$  are, respectively, the power densities of the MCFC, absorption refrigerator and hybrid system,  $j_P$  and  $\eta_P$  are, respectively, the operating current density and efficiency corresponding to the hybrid system maximum power density  $P_{\max}^*$ ,  $P_C^*$  and  $\eta_C$  are, respectively, the power density and efficiency at  $j_C$ ,  $P_M^*$  and  $\eta_M$  are, respectively, the power density and efficiency at  $j_M$ ,  $j_S$  is the stagnation current density from which the fuel cell does not deliver electricity any more. It is seen that  $P^*$  first increases and then decreases as  $j$  is increased,  $\eta$  first decreases then slightly increases and thereafter continuously decreases with  $j$ . Figure 2 also shows that  $j_P$  is always different from  $j_{MCFC, P}$  since  $j_{MCFC, P}$  is always different from  $j_{AR, P}$ , where  $j_{MCFC, P}$  and  $j_{AR, P}$  are, respectively, the current densities corresponding to the maximum power density of MCFC  $P_{MCFC, \max}^*$  and the maximum power density of absorption refrigerator  $P_{AR, \max}^*$ . For the typical parameters given in Table 1, the hybrid system reaches  $P_{\max}^*$ , 1531.2 W m<sup>-2</sup>, at 2943 A m<sup>-2</sup>, and the MCFC reaches  $P_{MCFC, \max}^*$ , 1483.8 W m<sup>-2</sup>, at 2959 A m<sup>-2</sup>. Meanwhile,  $\eta_P$  and  $\eta_{MCFC, P}$  (i.e., efficiency of MCFC at  $P_{MCFC, \max}^*$ ) are 40.7% and 39.2%, respectively.  $P_{\max}^*$  is about 3.2% larger than  $P_{MCFC, \max}^*$ , and  $\eta_P$  is about 3.8% larger than  $\eta_{MCFC, P}$ . When  $0 < j \leq j_C$  or  $j \geq j_M$ , the curves of  $P^* \sim j$  and  $\eta \sim j$  are overlapped with that of

$P_{MCFC}^* \sim j$  and  $\eta_{MCFC} \sim j$ , respectively. When the operating current density is operated in the region of  $j_C < j < j_M$ , both power density and efficiency of the hybrid system is greater than that of the stand-alone MCFC. This fact clearly shows that the performance of the MCFC can be effectively improved by recovering the waste heat for cooling purposes through a bottoming absorption refrigerator.

As illustrated in Fig. 2, an increasing  $j$  not only lowers  $P^*$  but also debases  $\eta$  in the region of  $j > j_P$ . Combined  $P^*$  and  $\eta$  together with the thermoeconomic optimization criterion [65, 66] into consideration,  $j$  is suggested to situate in the following region

$$j_C < j \leq j_P. \quad (21)$$

Correspondingly, the optimum operating regions for  $P^*$  and  $\eta$  are, respectively, determined by

$$P_C^* < P^* \leq P_{\max}^*, \quad (22)$$

and

$$\eta_C > \eta \geq \eta_P, \quad (23)$$

when the hybrid system is operated in the above regions,  $\eta$  increases as  $P^*$  decreases, and vice versa.

#### 4. Results and discussion

As shown by Eqs. (17) - (20), the performance of the MCFC/absorption refrigerator hybrid system not only depends on a set of designing parameters and operating conditions such as heat-transfer coefficients (i.e.,  $K_h$ ,  $K_c$  and  $K_0$ ), heat-transfer areas (i.e.,  $A_h$ ,  $A_c$ ,  $A_0$  and  $A_R$ ), internal irreversibility of the absorption refrigerator  $I_r$ , polar plate area  $A$ , operating current density  $j$ , operating temperature  $T$  and operating pressure  $p$  of the MCFC, but also depends on

some thermodynamic losses related parameters ( i.e.,  $c_1$  and  $c_2$  ). In this section, we will discuss the effects of these parameters on the performance of the hybrid system through comprehensive parametric analyses.

#### 4.1. Effect of internal irreversibility

The internal irreversibility  $I_r = \Delta S_o / (\Delta S_h + \Delta S_c)$  is a parameter that characterizes the irreversible losses caused by mass transfer, friction, eddy and other irreversible effects inside the cyclic working fluid of the absorption refrigerator [56-58], where  $\Delta S_o = q_o/T_3$  is the entropy rate that flows out of the cyclic working fluid,  $\Delta S_h = q_h/T_1$  and  $\Delta S_c = q_c/T_2$  are entropy rates that flow into the cyclic working fluids. Figure 3 shows that  $P$  and  $\eta$  increase as  $I_r$  decreases in the region of  $j_c < j < j_M$ , and  $j_p$  shifts to a larger value as  $I_r$  decreases. The detailed numerical results in Table 2 indicate that the value of  $j_c$  does not vary with  $I_r$ , while both  $j_M$  and the effective operating current density interval  $\Delta j (=|j_M - j_c|)$  increase as  $I_r$  decreases. The black solid line in Fig. 3 represents a special case that the internal irreversible effect inside the working fluid can be neglected. In such a case, Eqs. (17) and (18) can be, respectively, reduced into

$$P = P_{MCFC} + \frac{q_h}{2} \left| 1 - \frac{T_0}{T_c} \right| \left\{ \left[ \left( a_1 + \frac{T_0 - T_c}{C_1 q_h} \right)^2 - 4T_c \left( \frac{1}{(1+B_1)^2 T} - \frac{1-T_0/T}{C_1 q_h} \right) \right]^{0.5} - \left[ a_1 + \frac{T_0 - T_c}{C_1 q_h} \right] \right\} \quad (24)$$

and

$$\eta = \eta_{MCFC} + \frac{\left| 1 - \frac{T_0}{T_c} \right|}{2} \left[ 1 - \eta_{MCFC} + \frac{2F(c_1 + c_2)(T - T_0)}{j \Delta h} \right] \left\{ \left[ \left( a_1 + \frac{T_0 - T_c}{C_1 q_h} \right)^2 - 4T_c \left( \frac{1}{(1+B_1)^2 T} - \frac{1-T_0/T}{C_1 q_h} \right) \right]^{0.5} - \left[ a_1 + \frac{T_0 - T_c}{C_1 q_h} \right] \right\}, \quad (25)$$

where  $a_1 = 1 + (T_c - B_1^2 T_0) / [(1+B_1)^2 T]$ ,  $B_1 = (\sqrt{b_2} - 1) / (1 + \sqrt{b_1})$ ,  $C_1 = (1+B_1)^2 / (A_R K_1)$ ,  $K_1 = K_h / [1 + \sqrt{b_1}]^2$ .

## 4.2. Effect of heat-transfer coefficient

Heat-transfer coefficients of working fluid  $K_i$  ( $i = h, c$  and  $0$ ) dramatically affect the performance of the absorption refrigerator and thus influence the overall performance of the hybrid system. The effects of heat-transfer coefficients on the hybrid system performance are shown in Fig.

4. When  $j$  is operated in the region of  $j_c < j < j_M$ ,  $P^*$  and  $\eta$  are monotonically increasing functions of  $K_h$  and monotonically decreasing functions of  $b_1$  and  $b_2$ ,  $j_p$  shifts to a larger value as  $K_h$  increases or as  $b_1$  and/or  $b_2$  decrease. It is seen from Fig. 4 (a) that  $j_c$  does not vary with  $K_h$ , whereas  $j_M$  and  $\Delta j$  increase as  $K_h$  is increased. Table 2 shows that  $j_c$  does not vary with  $b_1$  and  $b_2$ ,  $j_M$  and  $\Delta j$  obviously decrease as  $b_1$  increases, but  $j_M$  and  $\Delta j$  slightly decreases as  $b_2$  increases. The wine dash-dot line in Fig. 4 (a) represents a special case in which heat transfer coefficients of the absorption refrigerator tend to be infinitely large and the heat transfer irreversibilities between the working fluid and the external heat sources disappear. The black solid line in Fig. 4 (b) represents another special case that the heat-transfer coefficients  $K_c$  and  $K_0$  trend to be infinite large (i.e.,  $b_1 \rightarrow 0$  and  $b_2 \rightarrow 0$ ) for a given  $K_h$ . When heat-transfer coefficients are large enough,  $P^*$  and  $\eta$  can be still larger than zero even when  $j$  exceeds  $j_s$ . In this situation, the MCFC works as a heat reservoir of the absorption refrigerator rather than an electrochemical converter. The region  $j > j_s$  exceeds the optimum region of  $j_c < j \leq j_p$  although the system may work in it. When  $j$  is operated in the region  $j > j_s$ , the MCFC is totally irreversible [67], and the numerical expressions for  $P$  and  $\eta$  are, respectively, given by

$$P = \frac{q_{hl}}{2} \left| 1 - \frac{T_0}{T_c} \right| \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{C q_{hl}} \right)^2 - 4 T_c \left( \frac{1}{(1+B)^2 T} - \frac{1 - I_r T_0 / T}{C q_{hl}} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{C q_{hl}} \right] \right\}, \quad (26)$$

and



$$\eta = \frac{|1-T_0/T_c|}{2} \left[ 1 + \frac{2F(c_1+c_2)(T-T_0)}{j\Delta h} \right] \left\{ \left[ \left( a + \frac{I_r T_0 - T_c}{Cq_{hl}} \right)^2 - 4T_c \left( \frac{1}{(1+B)^2 T} - \frac{1-I_r T_0/T}{Cq_{hl}} \right) \right]^{0.5} - \left[ a + \frac{I_r T_0 - T_c}{Cq_{hl}} \right] \right\}, \quad (27)$$

$$\text{where } q_{hl} = -\frac{A\Delta h}{n_e F} \left[ j - \frac{n_e F (c_1 + c_2)(T - T_0)}{-\Delta h} \right].$$

### 4.3. Effect of operating temperature

The operating temperature  $T$  is an important operating condition that not only affects the thermodynamic losses but also affects the performances of the MCFC and the absorption refrigerator. Different from the effects of  $I_r$ ,  $K_h$ ,  $b_1$  and  $b_2$ , the effect of  $T$  on the performance of the hybrid system are in the entire range of  $j$ , as shown in Fig. 5. Both  $P^*$  and  $\eta$  increase as  $T$  increases, and the effect of  $T$  on the hybrid system performance becomes more significant with increasing  $T$ . Moreover, the values of  $j_P$ ,  $j_C$ ,  $j_M$  and  $\Delta j$  increase as  $T$  increases. A larger  $T$  not only increases the equilibrium potential but also reduces the anode, cathode and ohmic overpotentials, which improves the MCFC performance. In addition, a higher  $T$  creates a larger temperature difference  $(T-T_0)$ , which improves the absorption refrigerator performance and also causes larger thermodynamic losses simultaneously. As the performance enhancements in MCFC and absorption refrigerator are greater than the performance reduction resulting from the thermodynamic losses, a larger  $T$  is always preferable.

### 4.4. Effect of thermodynamic losses related parameters

The thermodynamic losses are not only related to the temperature gap between  $T$  and  $T_0$  but also associated with the integrated parameters  $c_1$  and  $c_2$ . As shown in Fig. 6 (a), the curves of  $P_{AR}^* \sim j$  and  $\eta_{AR} \sim j$  move rightward and  $P_{AR,\max}^*$  almost keeps invariant as  $c_1$  and/or  $c_2$  are increased. Both  $j_C$  and  $j_M$  increase as  $c_1$  and/or  $c_2$  are increased, while  $\Delta j$  decreases as  $c_1$

and/or  $c_2$  increase. As  $P_{MCFC}^*$  and  $\eta_{MCFC}$  are neither influenced by  $c_1$  nor affected by  $c_2$ ,  $P^*$  and  $\eta$  decrease at low current densities and increase at large current densities as  $c_1$  and/or  $c_2$  are increased, as shown in Fig. 6 (b). When  $c_1$  and/or  $c_2$  are larger enough, e.g., the wine dash-dot line case represented in Fig. 6,  $j_M$  may exceeds  $j_s$ . For this situation, the numerical expressions for  $P$  and  $\eta$  can be, respectively, expressed by Eqs. (26) and (27). The black solid lines in Fig. 6 represent a special case that the thermodynamic losses  $q_r$  and  $q_L$  can be negligible (i.e.,  $c_1 = 0$  and  $c_2 = 0$ ). In this case, the bottoming absorption refrigerator starts to absorb heat from the cooled space once the MCFC is put into operation, and Eqs. (14) and (16) can be, respectively, reduced into

$$q_h = -\frac{jA(1-\eta_{MCFC})\Delta h}{2F}, \quad (28)$$

and

$$j > j_C = 0. \quad (29)$$

#### 4.5. Effect of operating pressure

Similar to the effects of operating temperature  $T$ , the operating pressure  $p$  not only affects the MCFC performance but also affects the amount of waste heat transferred from the MCFC to the absorption refrigerator. The effect of  $p$  on the performance of the hybrid system is in the entire range of  $j$ , as shown in Fig. 7. Both  $P^*$  and  $\eta$  increase as  $p$  increases, and the effect of  $p$  on the hybrid system performance becomes more significant as  $p$  increases. Additionally, the values of  $j_P$ ,  $j_C$ ,  $j_M$ ,  $j_s$  and  $\Delta j$  increase with a larger  $p$ . Although a larger  $p$  benefits performance improvement, it also cost more electricity to compress the inlet reactants. The ambient operating pressure is the usual choice, as represented by the black solid line in Fig. 7.

## 5. Conclusions

An MCFC-based absorption refrigerator hybrid system was put forward to harvest the waste heat in the MCFC for cooling purposes. The effective operating current density interval of the MCFC permits the absorption refrigerator to function was determined and numerical expressions to evaluate the performance of the hybrid system were specified. It was found that the performance of the MCFC could be effectively improved by integrating with an absorption refrigerator. The general performance characteristics and optimum operating regions for the hybrid system were revealed. The effects of the operating current density, operating temperature and operating pressure of the MCFC, internal irreversibility and heat transfer coefficients of the absorption refrigerator, and some thermodynamic losses related parameters on the performance of the hybrid system were discussed by comprehensive parametric studies. The results obtained in the paper may offer some theoretical guidance for performance improvement of MCFCs through cogeneration systems.

## Acknowledgements

This work has been supported by the Natural Science Foundation of Zhejiang Province of China (Grant No. LQ14E06002), the National Natural Science Foundation of China (Grant No. 51406091), the Zhejiang Open Foundation of the Most Important Subjects (Grant No. xkzw108), and The Hong Kong Polytechnic University Research Project (Grant No. 1-YW1F).

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## Table captions

Table 1. Parameters used in the model [52, 53, 55].

Table 2. The values of  $j_C$ ,  $j_M$ ,  $\Delta j$ ,  $P_{\max}^*$ ,  $j_P$  for different values of  $I_r$ ,  $b_1$  and  $b_2$ , where the unmentioned parameters are given in Table 1.

## Figure captions

Fig. 1. Schematic diagram of an MCFC/absorption refrigerator hybrid system.

Fig. 2. Curves of (a) power densities and (b) efficiencies of the MCFC, absorption refrigerator, and hybrid system varying with the operating current density of the MCFC, where  $P_{MCFC}^* = P_{MCFC} / A$ ,  $P_{AR}^* = P_{AR} / A$  and  $P^* = P / A$  are, respectively, the power densities of the MCFC, absorption refrigerator and hybrid system;  $\eta_{MCFC}$ ,  $\eta_{AR}$  and  $\eta$  are, respectively, the efficiencies of the MCFC, absorption refrigerator and hybrid system;  $j_P$  is the operating current density at the maximum power density of hybrid system  $P_{\max}^*$ ,  $j_C$  and  $j_M$  are, respectively, the lower bound density and upper bound current density between which the absorption refrigerator functions,  $P_C^*$  and  $\eta_C$  are, respectively, the power density and efficiency at  $j_C$ ,  $P_M^*$  and  $\eta_M$  are, respectively, the power density and efficiency at  $j_M$ .

Fig. 3. Effect of internal irreversibility  $I_r$  on the performance of the hybrid system.

Fig. 4. Effect of (a) heat transfer coefficient  $K_h$ , and (b)  $b_1$  and  $b_2$  on the performance of the hybrid system.

Fig. 5. Effect of operating temperature  $T$  on the performance of the hybrid system.

Fig. 6. Effect of thermodynamic losses related parameters  $c_1$  and  $c_2$  on the performance of (a) absorption refrigerator, and (b) the hybrid system.

Fig. 7. Effect of operating pressure  $p$  on the performance of the hybrid system.

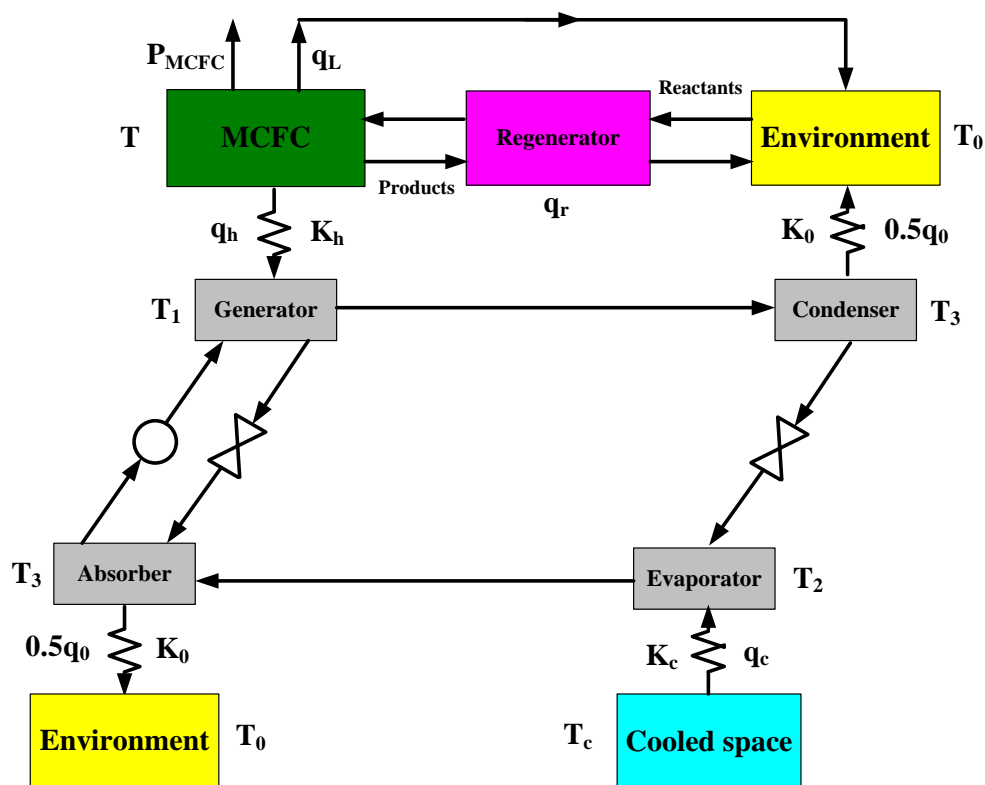
Table 1.

Parameter	Value
Faraday constant, $F$ (C mol <sup>-1</sup> )	96,485
Number of electrons, $n_e$	2
Universal gas constant, $R$ (J mol <sup>-1</sup> K <sup>-1</sup> )	8.314
Operating temperature, $T$ (K)	893
Operating pressure, $p$ (atm)	1.0
Anode gas compositions	60% H <sub>2</sub> /15% CO <sub>2</sub> /25% H <sub>2</sub> O
Cathode gas compositions	59% N <sub>2</sub> /8% O <sub>2</sub> /8% CO <sub>2</sub> /25% H <sub>2</sub> O
Activation energy in the anode, $E_{act,an}$ (J mol <sup>-1</sup> )	53500
Activation energy in the cathode, $E_{act,cat}$ (J mol <sup>-1</sup> )	77300
Effective polar plate area of the MCFC, $A$ (m <sup>2</sup> )	0.005
Operating temperature, $T$ (K)	893
Temperature of cooled space, $T_c$ (K)	293
Temperature of environment, $T_0$ (K)	313
Internal irreversibility of absorption refrigerator, $I_r$	1.1
Overall heat-transfer area of absorption refrigerator, $A_R$ (m <sup>2</sup> )	0.0001
Heat-transfer coefficient of the generator, $K_h$ (W K <sup>-1</sup> m <sup>-2</sup> )	1163
Constant, $c_1$ (W K <sup>-1</sup> m <sup>-2</sup> )	0.1
Constant, $c_2$ (W K <sup>-1</sup> m <sup>-2</sup> )	0.1
Constant $b_1$	1.0
Constant $b_2$	1.0

Table 2.

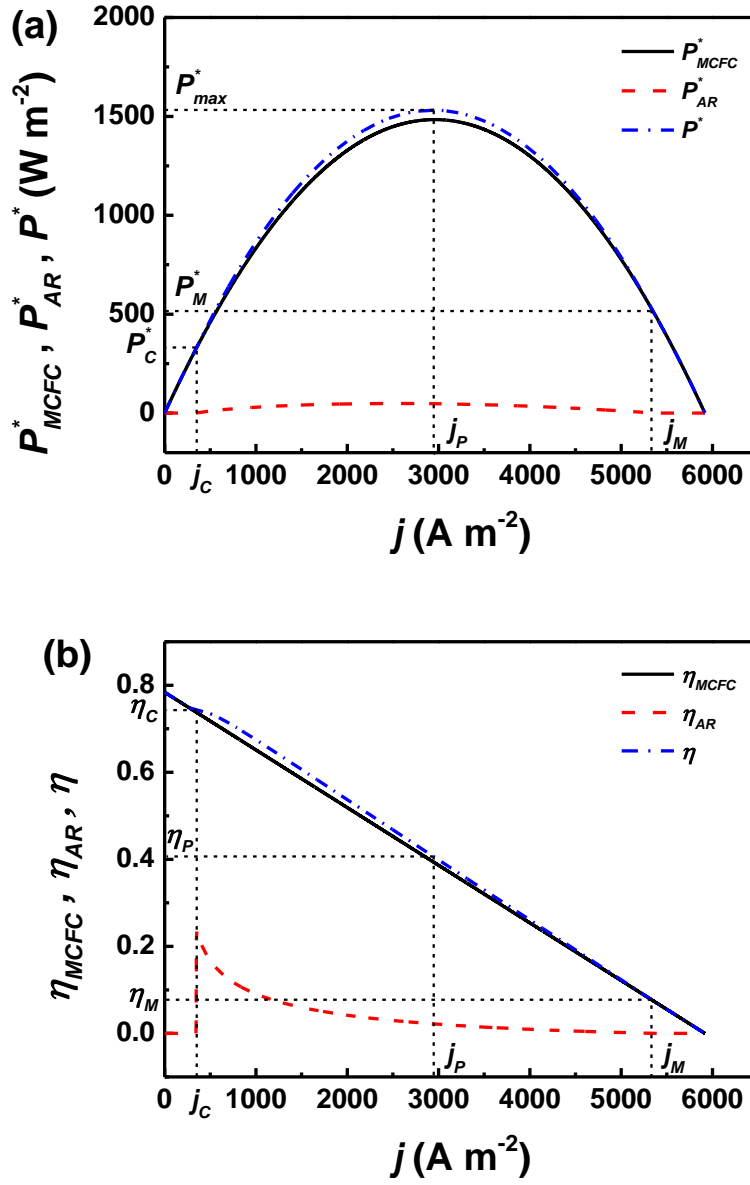
$I_r$	$b_1$	$b_2$	$j_C$	$j_M$	$\Delta j$	$P_{\max}^*$	$j_P$
1.0	1.0	0.1	346	5599	5253	1576.9	2942
		1.0	346	5599	5253	1540.2	2942
		$\infty$	346	5580	5234	1483.8	2959
	10	0.1	346	3709	3363	1504.8	2898
		1.0	346	3709	3363	1500.1	2910
		$\infty$	346	3641	3295	1483.8	2959
	$\infty$	0.1	-	-	-	1483.8	2959
		1.0	-	-	-	1483.8	2959
		$\infty$	-	-	-	1483.8	2959
1.1	1.0	0.1	346	5357	5011	1558.3	2945
		1.0	346	5357	5011	1531.2	2943
		$\infty$	346	5307	4961	1483.8	2959
	10	0.1	346	3520	3174	1498.6	2899
		1.0	346	3520	3174	1495.5	2910
		$\infty$	346	3518	3172	1483.8	2959
	$\infty$	0.1	-	-	-	1483.8	2959
		1.0	-	-	-	1483.8	2959
		$\infty$	-	-	-	1483.8	2959
1.5	1.0	0.1	346	4426	4080	1513.4	2939
		1.0	346	4426	4080	1505.5	2940
		$\infty$	346	4421	4075	1483.8	2959
	10	0.1	346	2828	2482	1483.8	2959
		1.0	346	2828	2482	1483.8	2959
		$\infty$	346	2804	2458	1483.8	2959
	$\infty$	0.1	-	-	-	1483.8	2959
		1.0	-	-	-	1483.8	2959
		$\infty$	-	-	-	1483.8	2959

Fig. 1.



Schematic diagram of an MCFC/absorption refrigerator hybrid system.

Fig. 2.

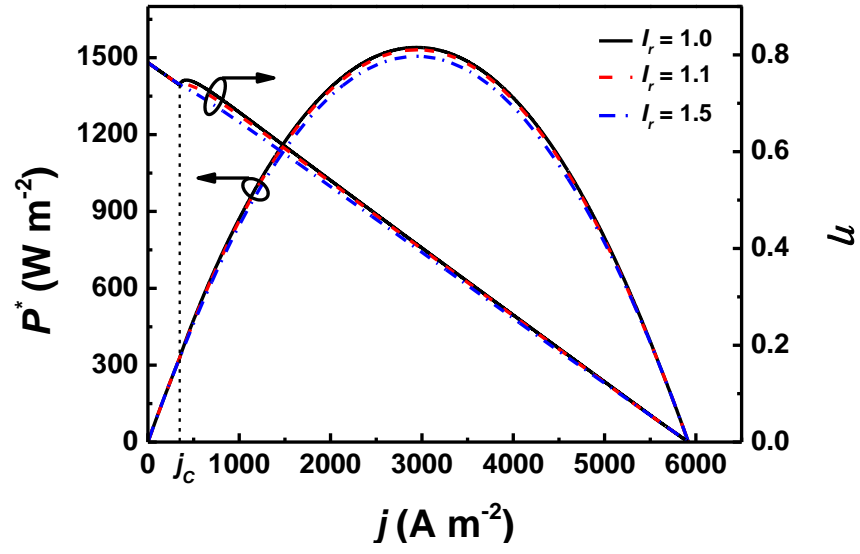


Curves of (a) power densities and (b) efficiencies of the MCFC, absorption refrigerator, and hybrid system varying with the operating current density of the MCFC, where  $P_{MCFC}^* = P_{MCFC} / A$ ,  $P_{AR}^* = P_{AR} / A$  and  $P^* = P / A$  are, respectively, the power densities of the MCFC, absorption refrigerator and hybrid system;  $\eta_{MCFC}$ ,  $\eta_{AR}$  and  $\eta$  are, respectively, the efficiencies of the MCFC, absorption refrigerator and hybrid system;  $j_P$  is the operating current density at the maximum power density of hybrid system  $P_{max}^*$ ,  $j_C$  and  $j_M$  are,



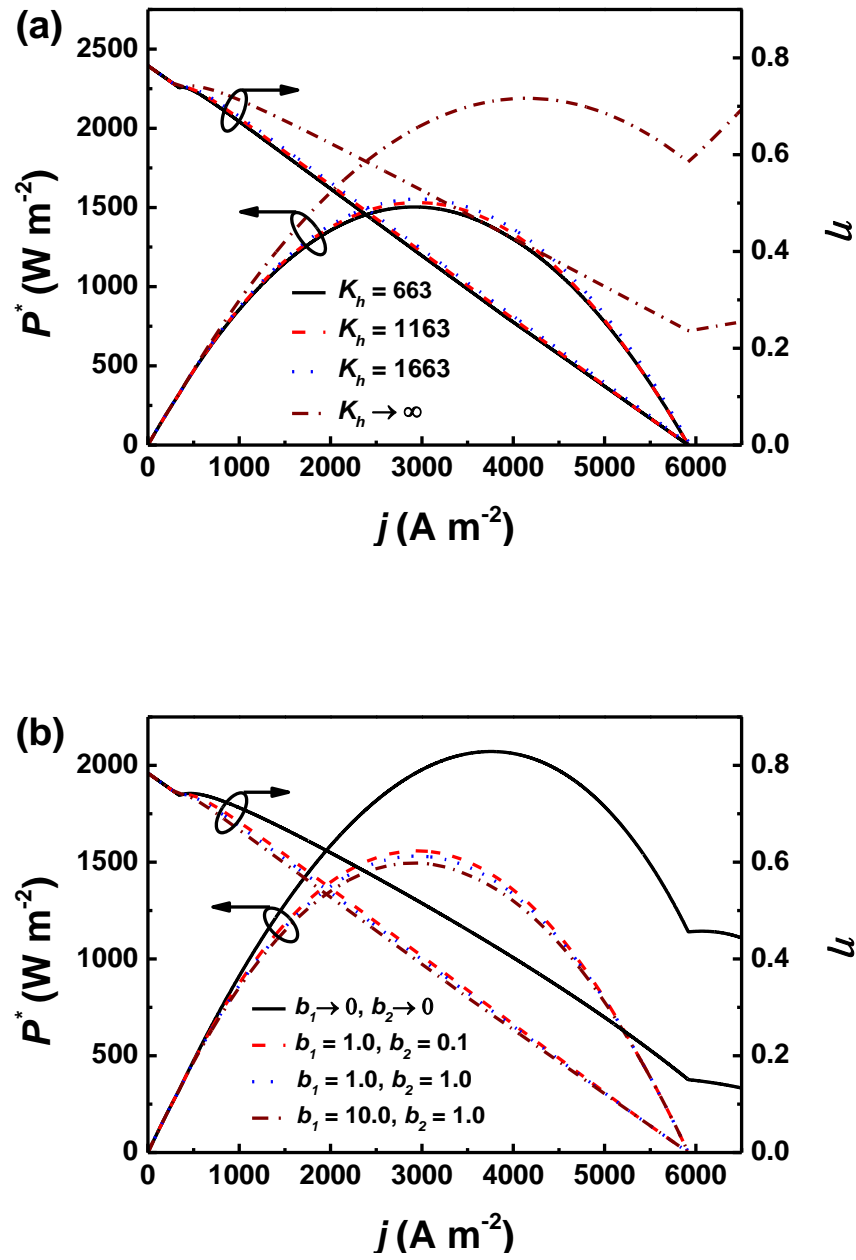
respectively, the lower bound density and upper bound current density between which the absorption refrigerator functions,  $P_C^*$  and  $\eta_C$  are, respectively, the power density and efficiency at  $j_C$ ,  $P_M^*$  and  $\eta_M$  are, respectively, the power density and efficiency at  $j_M$ .

Fig. 3.



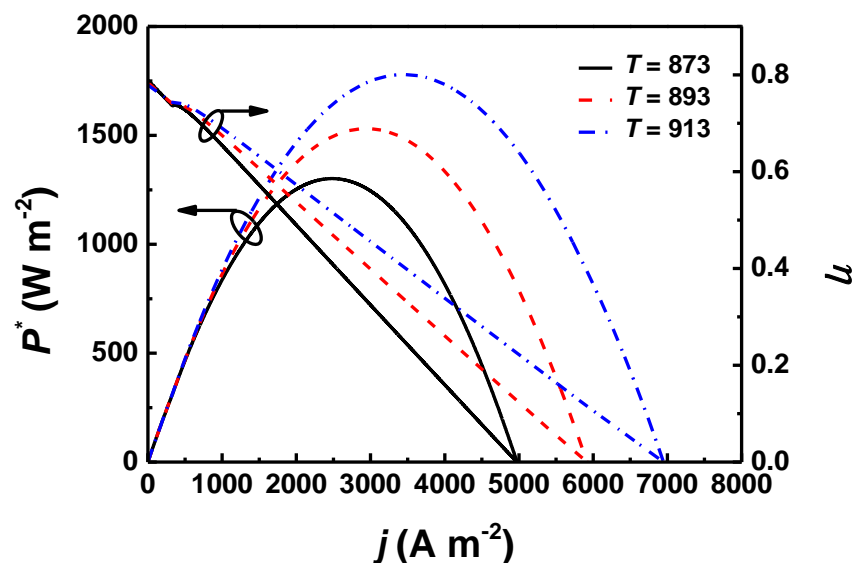
Effect of internal irreversibility  $I_r$  on the performance of the hybrid system.

Fig. 4.



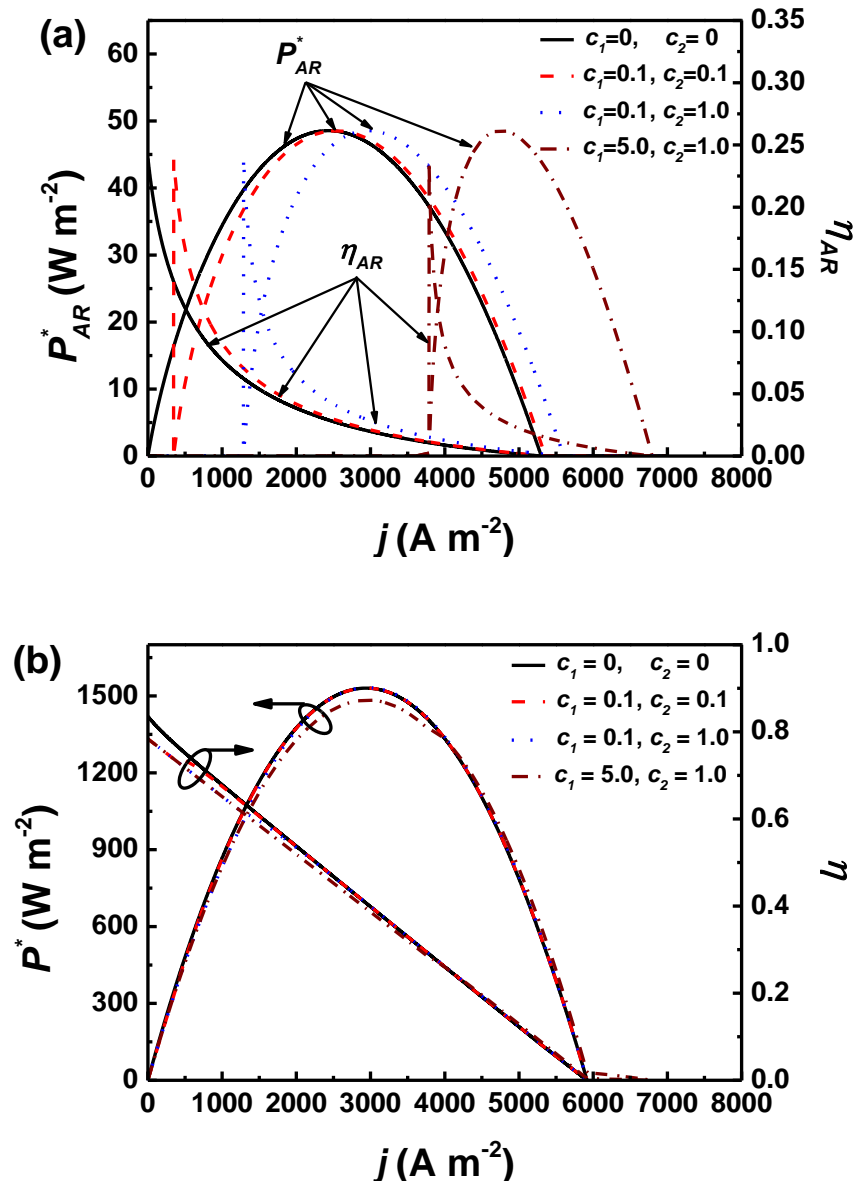
Effect of (a) heat transfer coefficient  $K_h$ , and (b)  $b_1$  and  $b_2$  on the performance of the hybrid system.

Fig. 5.



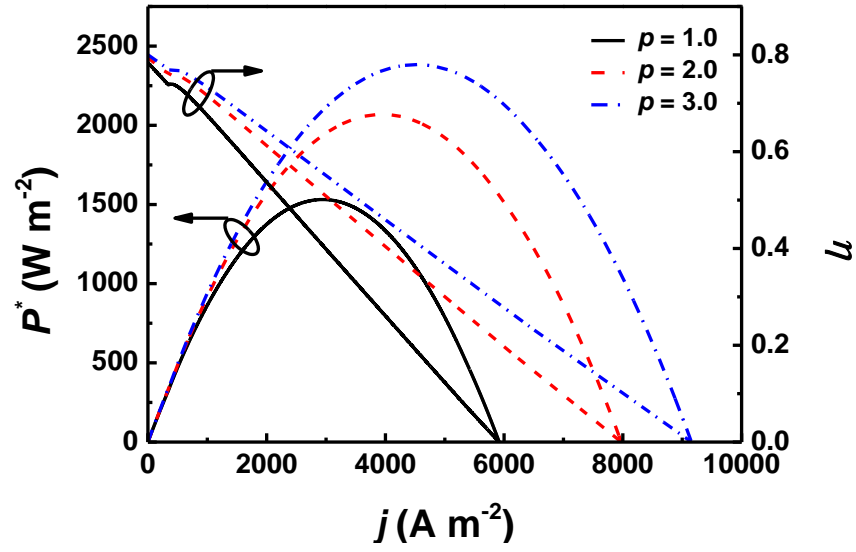
Effect of operating temperature  $T$  on the performance of the hybrid system.

Fig. 6.



Effect of thermodynamic losses related parameters  $c_1$  and  $c_2$  on the performance of (a) absorption refrigerator, and (b) the hybrid system.

Fig. 7.



Effect of operating pressure  $p$  on the performance of the hybrid system.