

Thermodynamic Analysis of a Power and Water Combined System with Geothermal Energy Utilization

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ABSTRACT: A novel combined system, integrated with a flashing Rankine cycle and humidification dehumidification (HDH) desalination unit, is proposed to achieve the energy utilization from geothermal water. The flashed steam is used to generate power while the remaining water is applied to heat the seawater for water production. Based on the coupling relation between the power and desalination unit, conservation equations based on the thermodynamic laws are constituted. Energy and entropy analysis of the combined system are achieved for determining the power and water production. Furthermore, the influence principles from the spraying temperature and terminal temperature difference of the seawater heater on the overall performance of the combined system are also focused. The simulation results indicate that the maximal net power from the flashing Rankine cycle reaches 157.0kW when the flashing temperature is 375.15K. Due to the leading role to determine total efficiency of the combined system, maximum values of 711.85kg^h⁻¹ for the water production and 43.98% for the total efficiency are obtained when the flashing temperature is 378.15K. Furthermore, it is also obtained that a lower value both for the seawater spraying temperature and terminal temperature difference of the seawater heater can help to improve the performance of the combined system.

- 23 **Keywords:** flashing Rankine cycle; humidification dehumidification; desalination; geothermal water; total
- 24 efficiency

Nomenclature

Roman symbols

| | |
|----------|---|
| h | enthalpy (kJkg^{-1}) |
| h_{fg} | latent heat (kJkg^{-1}) |
| L | length along the heat exchanger (mm) |
| m | mass flow rate (kg s^{-1}) |
| p | pressure (MPa); wet perimeter (m) |
| Q | heat load (kW) |
| RH | relative humidity |
| s | specific entropy ($\text{kJkg}^{-1}\text{K}^{-1}$); |
| S | concentration of seawater (gkg^{-1}); entropy rate ($\text{kJ s}^{-1}\text{K}^{-1}$) |
| T | temperature (K) |
| W | power (kW) |

Greek letters

| | |
|---------------|--|
| ε | effectiveness of the humidifier and dehumidifier |
| ρ | density (kgm^{-3}) |
| η | efficiency |
| ω | humidity ratio (gkg^{-1}) |

Subscripts

| | |
|-------|---------------------|
| a | air |
| b | brine |
| c | condenser |
| d | dehumidifier |
| da | dry air |
| e | exhaust |
| FE | flashing evaporator |
| fs | flashed steam |
| fw | flashed water |
| gen | generation |
| gw | geothermal water |
| h | humidifier |
| i | inlet |
| m | maximum |
| o | outlet |
| p | pump |
| SH | seawater heater |
| sw | seawater |

| | |
|-------|---------|
| t | total |
| tur | turbine |
| v | valve |
| w | water |

1. Introduction

In view of the unsustainable development in the past centuries, the crisis of energy and freshwater are becoming a reality gradually. As a result, energy and water supply with clean and efficient method has attracted more and more attentions. Thereinto, geothermal resources, which mainly contain geothermal dry steam, geothermal wet steam and geothermal water belongs to the renewable energy, and they are first applied investigated and applied to achieve the power generation all over the world [1, 2].

Jalilinasrabad [3] first designed a single flash cycle for power generation with geothermal energy, which has a temperature of 513K. Based on the developed mathematical models for thermodynamic analysis, it was found that the proposed scheme can obtain a maximum net power output, 31 MW, when the flashing and discharged pressures were fixed at 5.5 bar and 0.3 bar, respectively. For the sake of a optimized energy utilization, a double flash configuration was then advised, and the relevant maximum net power can arrive at 49.7 MW. In combination with the exergy analysis, a double flash cycle system for the Sabalan power plant was finally proposed. Yari [4] achieved a comparative investigation for different types of geothermal power plant, aiming to high temperature geothermal resources with a temperature of 503K. Mathematical models for each contained thermal cycle was developed, with model validation by previous published data. After the energy and exergy analysis, the results comparison was completed for clarifying the best cycle configurations. It was found that the thermal efficiency of the binary cycle with a regenerative ORC have the highest efficiency of 15.35%. Wang [5] introduced a Kalina cycle for further heat recovery of geothermal water from a primary flashing cycle, powered by the geothermal water with a temperature of 443K. Based on the established mathematical models of the flash-binary geothermal power generation system, the influences from critical thermal parameters are examined, and an optimization

45 method was also proposed to determine the best performance with exergy efficiency as the objective function. It
46 was discovered that the best exergy efficiency of the system can arrive at 37.01% under the prescribed input
47 boundaries. Yang [6] proposed an organic Rankine cycle to generate power with geothermal resource from
48 abandoned oil wells, with a temperature of 383K. With R245fa as the cycling working fluid, a four-stage axial
49 turbine was appointed in the ORC, and an onsite test showed that the efficiency of the turbine and entire cycle can
50 reach 78.52% and 5.33%, respectively. The research results and method could give some significant references for
51 the desirable power plants with the geothermal energy from the abandoned oil wells.

52 Based on the aforementioned literature, it can be concluded that the configurations of the power system should
53 be determined by the temperature and components of the geothermal resources [7, 8]. For a high temperature
54 geothermal resource, the flashing cycle and low temperature power cycles [9-11] are always existing
55 simultaneously for the sake of energy cascade utilization. However, in most occasions, power and water are both in
56 rigid demand to satisfy the industrial production and life. Accordingly, in the binary power systems powered by
57 geothermal energy, searching an appropriate desalination method to replace the low temperature power cycle to
58 recover the carried heat of the water from the primary flashing section for water production can achieve the
59 problem. Recent years, the humidification dehumidification methods [12, 13], which has the great advantages, has
60 been one of the major research focus in the field of desalination.

61 A saturated air cycling within the HDH desalination unit was assumed to investigate the relevant system
62 performance by Campos [14]. Through the experimental test, the internal parameters were selected to minimize the
63 residual summation of the contained temperature values. Based on the validated the mathematical models, a
64 sensitive analysis from critical parameters on the water production capacity was completed. From the test results, it
65 was observed that the heat load of the solar heater, humidifier height and seawater mass flow rate were the most
66 critical impact factors to change the production, while the influences from the ambient temperature was very slight.

67 Dual solar collectors to heat water and air simultaneously were applied in a HDH desalination system by
68 Rajaseenivasan [15], and the relevant experimental platform was built. After the test, it was found that the mass
69 flow rate and operation temperatures of the working fluid were related to the water producing capacity. An overall
70 efficiency of the system with the concave turbulators arrived at 67.6%. At the aspect of the water production, the
71 highest values reached 12.36, 14.14 and 15.23 kgm⁻² one day for the schemes without turbulators, convex and
72 concave turbulators, respectively. Siddiqui [16] studied the performance of an HDH desalination system operated
73 under vacuum environment. Based on the established mathematical models, it was found that the gain output ratio
74 would be raised after decreasing the humidification pressure. Kabeel [17] tested the performance of a HDH system
75 incorporated by an indirect solar dryer. It was discovered that the gain output ratio of the modified system was
76 enlarged by 29%, and it was raised with increasing the air flow rate. In addition of the solar energy, geothermal
77 energy was also used to power the HDH desalination unit by Mohamed [18] and Elminshawy [19]. After the
78 integration between the geothermal resource and HDH desalination unit, the relevant performance was investigated
79 by theoretical and experimental analysis, respectively. In spite of the different effect in each system, the common
80 viewpoint was gained that only the low temperature geothermal resource was suitable for the desalination system.

81 Due to the absence of the integration between the flashing Rankine cycle and the HDH desalination unit, the
82 present paper focuses on the performance of such combined system for power and water joint production. Based on
83 the thermodynamic laws, the mathematical models of the combined system were built, and then the corresponding
84 energy and entropy analysis for the subsystems and entire system were completed. Furthermore, the influences
85 from the seawater spraying temperature and terminal temperature difference of the seawater heater are also studied.
86 The research results provide significant references for the innovative design and further optimization of the power
87 and water combined systems.

88 2. System description

89 The detailed scheme of the novel power and water system, with flashing Rankine cycle and HDH desalination
90 cycle coupled, is exhibited in Fig. 1. Obviously, the power and water supply system consist of the flashing Rankine
91 cycle and HDH desalination cycle. For the aspect of the flashing Rankine cycle, the geothermal water is first
92 pressurized in the pump, and then flows into the flashing evaporator. After the sudden pressure declination,
93 saturated steam is obtained, and then the flashed steam flows into the steam turbine. During the expansion of the
94 steam, output power is obtained from the generator. Finally, the discharged steam from the turbine is condensed
95 under the cooling effect of the ambient seawater, with the temperature profile in Fig. 2 (a), and the condensate
96 become part of the backflow for the geothermal water.

97 At the bottom of the flashing evaporator, the hot flashed water enters the seawater heater to raised the
98 temperature of the preheated seawater from the dehumidifier, with the temperature profile shown in Fig. 2 (b). The
99 hot seawater is sprayed into the humidifier packings in the nozzles, and contact the humid air direct. As a result, the
100 temperature as well as the humidity ratio of the air is elevated, with the Psychrometric chart in Fig. 2 (c), transferring
101 heat and mass with the seawater, while the seawater is concentrated with the brine flowing out of the humidifier.
102 Afterwards, the hot humid air flows into the dehumidifier, and it is condensed while the ambient seawater is
103 preheated outside. Finally, due to the decrease of the humidity ratio for the humid air, freshwater is gained at the
104 bottom of the dehumidifier. With respect to the flashed geothermal water, it is cooled after the temperature of the
105 seawater is raised, and then it is throttled in the valve for an equilibrium pressure with the condensate from the
106 condenser. It can be concluded that the geothermal water is applied to drive the power plant and HDH desalination
107 system successively, and the discharged water flows back into the geothermal well finally.

108 For the sake of the mathematical models for the power and water combined system, assumptions are given out
109 to achieve the investigation successfully as follows:

110 (1) Both the flashing Rankine cycle and HDH desalination cycle run at steady-state conditions.

111 (2) Energy loss to the environment, changes of the potential and kinetic energy within the heat exchangers are
112 neglected.

113 (3) Fouling thermal resistance of the heat exchangers is not considered.

114 (4) Flow loss within the heat exchangers and pipes in the entire combined system is ignored.

115 3. Mathematical models

116 3.1 Flashing Rankine cycle

117 Water Pump

118 In order to utilize the geothermal water, a pump should be first installed to drive the water flow into the
119 flashing evaporator, and the consumed power can be calculated in Eq. (1) with $\eta_p=0.75$.

$$120 \quad W_p = \frac{m_{gw}}{\rho_{gw} \eta_p} (\Delta p_{FE} + \Delta p_v) = \frac{m_{gw} (h_{gw,p} - h_{gw,i})}{\eta_p} \quad (1)$$

121 where m_{gw} and ρ_{gw} are the mass flow rate and density of the inflow geothermal water, Δp_{FE} and Δp_v the pressure
122 drop in the flashing evaporator and value, and $h_{gw,i}$ and $h_{gw,p}$ are the specific enthalpy of the geothermal water at the
123 inlet and outlet of the pump. Besides the **energetic analysis** for the thermal process, the entropy analysis should also
124 be executed to inspect the corresponding feasibility and irreversible loss. Hence, the entropy generation rate during
125 the pump process, $S_{gen,p}$, can be expressed as follows:

$$126 \quad S_{gen,p} = m_{gw} (s_{gw,p} - s_{gw,i}) \quad (2)$$

127 where $s_{gw,i}$ and $s_{gw,p}$ are the specific entropy of the geothermal water at the inlet and outlet of the pump.

128 Flashing Evaporator

129 In order to obtain the steam from power generation, the geothermal water must first be flashed in the
130 evaporator. According to the theory of thermodynamics, flashing process of the water will occur when the pressure
131 suddenly drops, and then the saturated steam and water at a lower pressure will be attained. Obviously, according to
132 the mass and energy balance during the flashing, the conservation equations, including the mass, energy and

133 entropy, can be listed as follows:

$$134 \quad m_{gw} = m_{fs} + m_{fw} \quad (3)$$

$$135 \quad m_{gw} h_{gw,p} = m_{fs} h_{fs} + m_{fw} h_{fw} \quad (4)$$

$$136 \quad S_{gen,FE} = m_{fw} s_{fw} + m_{fs} s_{fs} - m_{gw} s_{gw,p} \quad (5)$$

137 where m_{fs} and m_{fw} are the mass flow rates of the flashed steam and water, h_{fs} and h_{fw} are the specific enthalpy of the
138 flashed steam and water, respectively, s_{fw} and s_{fs} the specific entropy of the flashed water, flashed steam.

139 **Steam Turbine**

140 The saturated steam from the top of the flashing evaporator flows into the steam turbine, and the output power
141 obtained from the generator can be calculated at the fixed value for $\eta_{tur}=0.8$ in Eq. (6).

$$142 \quad W_{tur} = m_{fs} (h_{fs} - h_{es}) \eta_{tur} \quad (6)$$

143 where h_{es} is the specific enthalpy of the discharged steam during an isentropic expansion. For the entropy analysis,
144 the entropy generation rate during the expansion can be calculated in Eq. (7).

$$145 \quad S_{gen,tur} = m_{fs} (s_e - s_{fs}) \quad (7)$$

146 where s_e is the specific entropy of the discharged steam out of the turbine. Hence, after the acquisition of the output
147 power from the turbine and the consumed power of the pump, the final net power can be calculated in Eq. (8) with

$$148 \quad \eta_m = \eta_g = 0.98.$$

$$149 \quad W_{net} = W_{tur} \eta_m \eta_g - W_p \quad (8)$$

150 **Condenser**

151 After the expansion process, the discharged steam from the turbine enters the condenser, and it is cooled and
152 condensed under the cooling effect of the ambient seawater. Consequently, the energy and entropy balance within
153 the condenser can be expressed as:

$$154 \quad Q_c = m_{fs} (h_e - h_c) = m_c (h_{sw,o} - h_{sw,i}) \quad (9)$$

$$S_{gen,c} = m_c (s_{sw,o} - s_{sw,i}) + m_{fs} (s_c - s_e) \quad (10)$$

where h_e and h_c represent the specific enthalpy of the discharged steam and the condensate, m_c the mass flow rate of the cooling seawater, $h_{sw,i}$ and $h_{sw,o}$ the corresponding specific enthalpy at the condenser inlet and outlet [20], $s_{sw,i}$ and $s_{sw,o}$ the corresponding specific entropy of the seawater, s_c the specific entropy of the condensate.

3.2 HDH desalination cycle

Seawater Heater

For the HDH desalination cycle, it is driven by the flashed water from the bottom of the flashing evaporator. Accordingly, the temperature of the seawater is elevated to a top value in the seawater heater, and the relevant heat transfer load can be calculated in Eq. (11).

$$Q_{SH} = m_{fw} (h_{fw} - h_{SH}) = m_{sw} (h_{sw2} - h_{sw1}) \quad (11)$$

where h_{SH} is the specific enthalpy of the flashed water at the outlet of the seawater heater, m_{sw} the mass flow rate of the involved seawater, h_{sw1} and h_{sw2} the corresponding specific enthalpy at the heater inlet and outlet. In addition of the heat load of the heater, the relevant entropy balance can also be described as:

$$S_{gen,SH} = m_{fw} (s_{SH} - s_{fw}) + m_{sw} (s_{sw2} - s_{sw1}) \quad (12)$$

where s_{SH} is the specific entropy of the flashed water at the outlet of the heater, while s_{sw1} and s_{sw2} are the specific entropy before and after the heating process.

Packed Bed Humidifier

In order to elevate the temperature and humidity ratio of the air for water production, packed bed is applied in the humidifier. Hence, the sprayed seawater and humid air contact direct, and heat and mass transferring processes arise simultaneously. During the humidification, the corresponding mass and energy balance can be described as:

$$m_{sw} - m_b = m_{da} (\omega_2 - \omega_1) \quad (13)$$

$$m_{sw} h_{sw2} - m_b h_b = m_{da} (h_{a2} - h_{a1}) \quad (14)$$

177 where m_b is the mass flow rate of the concentrated brine while m_{da} is the mass flow rate of the dry air, ω_1 and ω_2 the
 178 air humidity ratio at the inlet and outlet of the humidifier, h_{sw2} and h_b the specific enthalpy of the sprayed seawater
 179 and brine, h_{a1} and h_{a2} the specific enthalpy of the humid air at the inlet and outlet, respectively [21]. With respect to
 180 the entropy equation, the entropy generation rate within the humidifier, $S_{gen,h}$, can be acquired.

181

$$S_{gen,h} = m_b s_b - m_{sw} s_{sw2} + m_{da} (s_{a2} - s_{a1}) \quad (15)$$

182 where s_b represents the specific entropy of the hot brine at the bottom of the humidifier, while s_{a1} and s_{a2} are the
 183 specific entropy of the humid air before and after humidification.

184 **Dehumidifier**

185 After the humidification is completed, a heat exchanger is used to cool the hot humid air, and hence fresh
 186 water can be gained during the dehumidification. Consequently, the relevant conservation equations can be
 187 acquired.

188

$$m_w = m_{da} (\omega_2 - \omega_1) \quad (16)$$

189

$$m_{sw} (h_{sw1} - h_{sw,i}) = m_{da} (h_{a2} - h_{a1}) - m_w h_w \quad (17)$$

190 where m_w and h_w are the mass flow rate and specific enthalpy of the produced water from the dehumidified heat
 191 exchanger. Additionally, the corresponding entropy generation rate, $S_{gen,d}$ during the dehumidification can be
 192 acquired in Eq. (18).

193

$$S_{gen,d} = m_{sw} (s_{sw1} - s_{sw,i}) + m_{da} (s_{a1} - s_{a2}) + m_w s_w \quad (18)$$

194 where s_w stands for the specific entropy of the produced fresh water.

195 **Valve**

196 In order to discharge the cooled flashed water, the flashed water out of the seawater heater should be first
 197 throttled within the valve. The expression of isenthalpic process can be expressed as:

198

$$h_{SH} = h_v \quad (19)$$

where h_v is the specific enthalpy of the flashed water at the outlet of the valve. Furthermore, the entropy generation rate during the isenthalpic process can also be obtained.

$$S_{gen,v} = m_{fw}(s_v - s_{SH}) \quad (20)$$

where s_v stands for the specific entropy of the flashed water at the outlet of the valve.

Mixer

Afterwards, the throttled water joins the condensed water from the flashing Rankine cycle. Hence, the final cooled geothermal water can be obtained, and the relevant mass and energy balance during the mixing process can be expressed in Eq. (21) and Eq. (22).

$$m_{fw} + m_{fs} = m_{gw} \quad (21)$$

$$m_{fw}h_v + m_{fs}h_c = m_{gw}h_{gw,o} \quad (22)$$

where $h_{gw,o}$ is the specific enthalpy of the final geothermal water into the well, and the entropy generation rate during the mixing between the condensate and the flashed water can be obtained.

$$S_{gen,m} = m_{gw}s_{gw,o} - m_{fw}s_v - m_{fs}s_c \quad (23)$$

where $s_{gw,o}$ represents the specific entropy of the final geothermal water.

3.3 Assessment of the Combined System

After the **energetic analysis** of the combined system, obtaining the output power and the water production, the definition of total efficiency is proposed with the following expression.

$$\eta_t = \frac{m_w h_{fg} + W_{net}}{m_{gw}(h_{gw,i} - h_{gw,o})} \quad (24)$$

where h_{fg} is the latent heat of the produced water during dehumidification. Furthermore, after obtaining the entropy generation rate for all the involved processes, the total entropy generation rate can be calculated.

$$S_{gen,t} = S_{gen,p} + S_{gen,FE} + S_{gen,tur} + S_{gen,c} + S_{gen,d} + S_{gen,h} + S_{gen,SH} + S_{gen,v} + S_{gen,m} \quad (25)$$

Accordingly, mathematical models of the combined system are built, and then the performance simulation can be executed through the Matlab platform with the established equations.

4. Results and discussion

According to the stream conservation of mass, energy and entropy, the characteristics of power and water combined system driven by geothermal energy is initially simulated, with design conditions shown in Table 1. It can be observed that the mass flow rate and the temperature for the geothermal water is fixed at $m_{gw}=3\text{kgs}^{-1}$ and $T_{gw}=453.15\text{K}$, respectively. With respect to the HDH unit, the effectiveness both during the humidification and dehumidification are assumed as $\varepsilon=0.85$, while the seawater sprayed temperature and terminal temperature difference of the seawater heater are assumed at $T_{sw2}=353.15\text{K}$ and $TTD_{SH}=20\text{K}$.

4.1 Performance analysis of the flashing power subsystem

In the power and water combined system, the general Rankine cycle with flashing evaporator is first involved. The flashed steam flows into the steam turbine to realize the power generation. Consequently, the specific characteristics of the flashing power subsystem is calculated and presented in Fig. 3. With the increase of the flashing temperature, it is found that the net power, which is calculated as the output power from the turbine minus the power consumption of the geothermal water pump, will first rise to a net power of $W_{net}=157.0\text{kW}$ until the flashing temperature arrives at $T_{fs}=375.15\text{K}$. After surmounting the peak value condition, the value of net power declines continuously to $W_{net}=96.0\text{kW}$ at the case of $T_{fs}=423.15\text{K}$. Evidently, the net power from the Rankine cycle is determined jointly by the steam mass flow rate and the actual enthalpy drop during the expansion in the turbine. In view of the mass and energy balance within the flashing evaporator, it can be gained that the mass flow rate of the flashed steam will be reduced resulting from the increase of the flashing temperature, from $m_{fs}=0.51\text{kgs}^{-1}$ at $T_{fs}=363.15\text{K}$ to $m_{fs}=0.19\text{kgs}^{-1}$ at $T_{fs}=423.15\text{K}$. Finally, in combination with the continuous increase of the enthalpy drop with the inlet temperature elevation into the steam turbine, a maximum value of the net power is obtained as $W_{net}=157.0\text{kW}$ when the flashing temperature stays at $T_{fs}=375.15\text{K}$. Furthermore, in order to guarantee the safety of the steam turbine, the steam quality of the turbine exhaust is also calculated and present in Fig. 3. It can be inferred

that the flashing temperature should be lower than $T_{fs}=393.15\text{K}$, ensuring the quality of the discharged steam, x_e , is higher than 0.88, which is regarded as the lower limit for the turbine safety [22]. Accordingly, the effective mass flow rate varies from $m_{fs}=0.51\text{kgs}^{-1}$ at $T_{fs}=363.15\text{K}$ to $m_{fs}=0.36\text{kgs}^{-1}$ at $T_{fs}=393.15\text{K}$, while the relevant top and bottom net power is $W_{net}=157.0\text{kW}$ at $T_{fs}=375.15\text{K}$ and $W_{net}=147.93\text{kW}$ at $T_{fs}=393.15\text{K}$, respectively.

4.2 Entropy analysis of the HDH desalination subsystem

As demonstrated in the previous literature for the HDH desalination unit [23], the entropy analysis must be first executed to judge the actual feasibility of the thermal conditions. Hence, with the conditions of the maximum net power, the entropy generation for all the components within the combined system are calculated and exhibited in Fig. 4. Thereinto, due to the fixed input conditions for the flashing power subsystem, the entropy generation of the relevant components are also fixed, and the values are $S_{gen,p}=0.02\text{kWK}^{-1}$, $S_{gen,FE}=0.29\text{kWK}^{-1}$, $S_{gen,tur}=0.14\text{kWK}^{-1}$ and $S_{gen,c}=0.11\text{kWK}^{-1}$ for the geothermal water pump, flashing evaporator, turbine and the condenser, respectively. Taking all the values of entropy generation into comparison, it can be obtained that the flashing evaporation has the maximum irreversible loss among all the thermal processes, and the top weight approaches 40.4% when the air mass flow rate stays at $m_{da}=0.1\text{kgs}^{-1}$. Moreover, it is also observed that the negative region of the entropy generation emerges at the component of humidifier, within the range from $m_{da}=0.3\text{kgs}^{-1}$ to $m_{da}=0.4\text{kgs}^{-1}$. As a result, the cases with the aforementioned condition is not truly existing to achieve the water production.

4.3 Energetic analysis of the power and water combined system

After the entropy analysis of the HDH desalination subsystem, actually the entire combined system, the corresponding energetic analysis can be accomplished. During the entropy generation calculation, the flashing temperature is fixed at $T_{fs}=T_{fw}=375.15\text{K}$ to maximize the power generation. However, the conditions with a top net power can not ensure the maximum performance of the HDH desalination unit. As a result, three values of the flashing temperature with $T_{fs}=368.15\text{K}$, 375.15K and 378.15K are appointed to investigate the specific performance

266 of the combined system, and the water production capacity with the increasing air mass flow rate is presented in
 267 Fig. 5. Taking the thermodynamic performance based on first and second law into consideration, it is found each
 268 case has its own impossible conditions, and the produced water will rise with the increase of the flashing
 269 temperature. On the basis of the definition of effectiveness and heat capacity ratio (HCR) [24], the top values
 270 appears at the balance condition of the dehumidifier, $HCR_d=1$, with $m_w=456.93\text{kg}\cdot\text{h}^{-1}$, $635.48\text{kg}\cdot\text{h}^{-1}$ and $711.85\text{kg}\cdot\text{h}^{-1}$
 271 for the cases of $T_{fw}=368.15\text{K}$, 375.15K and 378.15K , respectively. Actually, based on the mass and energy
 272 equilibrium within the flashing evaporator, the mass flow rate of the remaining water from the bottom will rise with
 273 the increase of the flashing temperature. A higher mass flow rates both for the air and seawater are in demand to
 274 realize the fixed spraying temperature, $T_{sw2}=353.15\text{K}$, and terminal temperature difference of the seawater heater,
 275 $TTD_{SH}=20\text{K}$ when the flashing temperature increases. Taking the case of $HCR_d=1$ for instance, the relevant mass
 276 flow rate is elevated from $m_{da}=0.96\text{kg}\cdot\text{s}^{-1}$ and $m_{sw}=2.07\text{kg}\cdot\text{s}^{-1}$ at $T_{fw}=368.15\text{K}$ to $m_{da}=1.5\text{kg}\cdot\text{s}^{-1}$ and $m_{sw}=3.23\text{kg}\cdot\text{s}^{-1}$ at
 277 $T_{fw}=378.15\text{K}$. Due to an constant value for the humidity difference between the air streams at the inlet and outlet of
 278 the humidifier, a higher air mass flow rate also indicates a higher water production.

279 Different from the water production, the total efficiency of the combined system is jointly determined by the
 280 net output power, water production and the energy input of the geothermal water. As stated in Fig. 3, the top value
 281 of the net power appears as $W_{net}=157.0\text{kW}$ when the flashing temperature reaches $T_{fs}=375.15\text{K}$, and relevant net
 282 power are $W_{net}=155.79\text{kW}$ and 156.69kW at $T_{fs}=368.15\text{K}$ and 378.15K , respectively. In combination with the water
 283 production, the variation law of the total efficiency with the increasing air mass flow rate is obtained and presented
 284 in Fig. 6. In some extent, the change law of the total efficiency is consistent with that of the water production,
 285 because the profit of the combined system mainly comes from the aspect of water production. As a result, the total
 286 efficiency will also be elevated after the increase of the flashing temperature. Considering the case with the balance
 287 condition of the dehumidifier, $HCR_d=1$, it is seen that the total efficiency is promoted from $\eta_t=31.88\%$ at

288 $T_{fs}=368.15\text{K}$ to $\eta_t=43.98\%$ at $T_{fs}=378.15\text{K}$. The specific performance of the power and water combined system is
289 listed in Table 2. It can be validated that the efficiency elevation is mainly attributed to the increase of the water
290 production, from $m_w=456.93\text{kg}\cdot\text{h}^{-1}$ to $m_w=711.85\text{kg}\cdot\text{h}^{-1}$, and the energy input declination, from $Q_t=1440.06\text{kW}$ to
291 $Q_t=1430.55\text{kW}$.

292 **4.4 Size determination of the power and water combined system**

293 After the thermodynamic performance is obtained, all the parameters within the power and water combined
294 system are determined. Hence, the areas of the heat and mass transfer devices can be calculated based on the
295 mathematical models from He [25]. Thereinto, the plate heat exchangers (PHE), with the geometric details in Table
296 3, are applied for the condenser, seawater heater and dehumidifier, while packings are filled into the humidifier, and
297 the area details of the heat and mass transfer devices, under three flashing temperatures and respective balance
298 condition of the dehumidifier, are attained and presented in Table 4. It can be found that the area of the
299 dehumidifier has the dominant weight of all the heat and mass transfer areas. Taking the case of $T_{fs}=375.15\text{K}$ for
300 example, the area of the dehumidifier reaches $A_d=106\text{m}^2$, while the total areas are $A_t=236.45\text{m}^2$. Obviously, during
301 the dehumidification process, the heat load is transferred from the hot humid air to the feed seawater, and the
302 relevant coefficient is relatively low due to the participation of air.

303 **4.5 Influences from the critical parameters on the performance of the power and water combined system**

304 **A. Spraying temperature**

305 As the previous illustration, potential is existing at the respect of the HDH desalination unit to improve the
306 total efficiency of the combined system. Accordingly, sensitivity analysis from the parameter of spraying
307 temperature, T_{sw2} , is first investigated at the fixed flashing temperature of $T_{fs}=375.15\text{K}$, and the change laws of the
308 water production as well as the total efficiency is exhibited in Fig. 7. Once the flashing temperature is assumed to
309 be changeless, the temperature and mass flow rate of the geothermal water out of the flashing evaporator are also

310 fixed with $T_{fw}=375.15\text{K}$ and $m_{fw}=2.55\text{kgs}^{-1}$. It is found that a decreasing the spraying temperature into the
 311 humidifier is beneficial to improve the water producing. The top value of water production is raised with an
 312 amplitude of 27.62%, which is $\Delta m_w=154.75\text{kgh}^{-1}$ when the spraying temperature is regulated from $T_{sw2}=358.15\text{K}$ to
 313 $T_{sw2}=348.15\text{K}$. Actually, once a lower spraying temperature is required, to satisfy the energy balance within the
 314 HDH desalination unit, the mass flow rate both for the cycling air and seawater will rise, from $m_{da}=0.98\text{kgs}^{-1}$ and
 315 $m_{sw}=2.36\text{kgs}^{-1}$ at $T_{sw2}=358.15\text{K}$ to $m_{da}=1.8\text{kgs}^{-1}$ and $m_{sw}=3.52\text{kgs}^{-1}$ at $T_{sw2}=348.15\text{K}$. On the other hand, the
 316 spraying temperature declination also result in the descent of the humidity difference before and after the
 317 humidification process. Finally, the weight of the air mass flow rate to the water production exceeds that from the
 318 humidity difference, and a top value of water production, $m_w=714.94\text{kgh}^{-1}$, is obtained at the balance condition of
 319 the dehumidifier. Furthermore, at the aspect of the total efficiency, it completely rests with the variation of the
 320 water production and the released heat from the geothermal water since the net power is fixed at $W_{net}=157\text{kW}$. Due
 321 to the mass flow rate elevation in response to the spraying temperature descent, the total energy input of the
 322 combined system will also rise from $Q_t=1405.85\text{kW}$ at $T_{sw2}=358.15\text{K}$ to $Q_t=1461.01\text{kW}$ at $T_{sw2}=348.15\text{K}$. In the
 323 light of the different weight from the water production and total energy consumption, a maximum value is
 324 calculated as $\eta_t=43.30\%$ at $T_{sw2}=348.15\text{K}$ when the balance condition of the dehumidifier arrives. The specific
 325 performance of the power and water combined system at different spraying temperatures is listed in Table 5.

326 **B. Terminal temperature difference of the seawater heater**

327 Similar with the case for the spraying temperature, the terminal temperature difference of the seawater heater,
 328 TTD_{SH} , is also designated to explore the corresponding influence on the water production and total efficiency at the
 329 fixed flashing temperature of $T_{fs}=375.15\text{K}$, shown in Fig. 8. For a surface heat exchanger, it is evident that a lower
 330 terminal temperature difference means a better heat transfer performance. As a result, to the requirements of mass
 331 and energy balance within the HDH desalination unit, a higher mass flow rate of the air and seawater is necessary

to enhance the heat transfer characteristics of the seawater heater in response to a reduced value of terminal temperature difference. It is gained that the corresponding values for the mass flow rates are $m_{da}=1.6\text{kgs}^{-1}$ and $m_{sw}=3.43\text{ kgs}^{-1}$ at $TTD_{SH}=15\text{K}$, $m_{da}=1.33\text{kgs}^{-1}$ and $m_{sw}=2.88\text{ kgs}^{-1}$ at $TTD_{SH}=20\text{K}$ and $m_{da}=1.08\text{kgs}^{-1}$ and $m_{sw}=2.33\text{ kgs}^{-1}$ at $TTD_{SH}=25\text{K}$. As a result, the water production is raised with a magnitude of 46.91% after the regulation of the TTD_{SH} from $TTD_{SH}=25\text{K}$ to $TTD_{SH}=15\text{K}$. Moreover, owing to the great elevation of the water production, the final total efficiency is raised from $\eta_t=36.06\%$ to $\eta_t=44.18\%$ although the energy consumption from the geothermal water also rises from $Q_t=1379.56\text{kW}$ to $Q_t=1487.72\text{kW}$. The specific performance of the power and water combined system at different terminal temperature differences is listed in Table 6.

4.6 Validation of the power and water combined system

For the sake of ensuring the accuracy of the simulation results from the power and water combined system, the built mathematical models should be compared to the experimental or published data. In view of the novelty of the current coupled system, the flashing Rankine cycle power subsystem and HDH desalination unit are validated respectively. At the aspect of the general flashing Rankine cycle, the current simulation results are compared to the data from the double-flash geothermal power plant [4] based on the inlet parameters of the geothermal water, shown in Table 7. It is found that the maximum deviation arises with 2.9% for the mass flow rate of the flashed steam out of the flashing evaporator. With respect to the HDH desalination unit, the published results from Narayan [23] is prescribed to validate the current performance, shown in Fig. 9. During the comparison, two spraying temperatures with $T_{sw2}=353.15\text{K}$ and 363.15K , with the ambient temperature $T_{sw,i}=308.15\text{K}$, the effectiveness, $\varepsilon_h=\varepsilon_d=0.92$, the relative humidity, $RH_1=RH_2=1$, are involved. It is found that the maximum deviation of GOR emerges as 2.78% when the mass flow rate ratio are located at $m_{sw}/m_{da}=2$ with a spraying temperature of 363.15K . The small errors about the two involved subsystems verify the accuracy of the established mathematical models.

5. Conclusions

In the present paper, a novel power and water combined system powered with geothermal water is constituted.

The thermodynamic performance of the flashing Rankine power cycle and the HDH desalination unit is simulated and illustrated. Furthermore, the influences from the seawater spraying temperature and the terminal temperature difference of the seawater heater are also discussed. After the simulation and analysis, the concluded results are given as follows:

1. The net power of the flashing Rankine cycle varies with the evaporation temperature. A maximum value of the net power emerges as $W_{net}=157.0\text{kW}$ when the flashing temperature stays at $T_f=375.15\text{K}$, with a quality of $x_e=89.82\%$ to ensure the safety of the steam turbine.
2. Negative region of the entropy generation exists for the component of humidifier within the combined system, and the flashing evaporation has the maximum irreversible loss among all the involved processes, with a maximal weight of 40.4% at the prescribed range of the air mass flow rate.
3. A higher flashing temperature is effective to raise the water production, and the corresponding top value approach $m_w=711.85\text{kg}\cdot\text{h}^{-1}$ at the case of $T_{fw}=378.15\text{K}$. Due to the dominant weight of the water production to determine the energy conversion situation for the combined system, the maximum value of the total efficiency arrives at $\eta_t=43.98\%$ when the flashing temperature is $T_{fw}=378.15\text{K}$.
4. Due to the mass flow rate elevation to balance the mass and energy, reducing the spraying temperature and terminal temperature difference of the seawater heater can raise the performance of the combined system. The simulation results show that the improve amplitudes for the total efficiency are found with 15.28% and 22.52% in response to the variation difference of $\Delta T_{sw2}=10\text{K}$ and $\Delta TTD_{SH}=10\text{K}$.

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427

Table 1 Typical thermodynamic parameters of the power and water combined system

| m_{gw} (kgs ⁻¹) | T_{gw} (K) | S (gkg ⁻¹) | $\varepsilon_{h,d}$ | RH_1 | RH_2 | T_{sw0} (K) | T_{sw2} (K) | TTD_{SH} (K) | TTD_c (K) | PTD_c (K) | a (m ² m ⁻³) | H_h (m) |
|-------------------------------|--------------|--------------------------|---------------------|--------|--------|---------------|---------------|----------------|-------------|-------------|---------------------------------------|-----------|
| 3 | 453.15 | 35 | 0.85 | 1 | 0.9 | 288.15 | 353.15 | 20 | 15 | 5 | 157 | 0.3 |

Table 2 Specific parameters of the combined system at different flashing temperatures

| T_{fs} (K) | m_{da} (kgs ⁻¹) | m_{sw} (kgs ⁻¹) | x_e (%) | W_{net} (kW) | m_w (kgh ⁻¹) | Q_t (kW) | η_t (%) |
|--------------|-------------------------------|-------------------------------|-----------|----------------|----------------------------|------------|--------------|
| 368.15 | 0.96 | 2.07 | 90.57 | 155.79 | 456.93 | 1440.06 | 31.88 |
| 375.15 | 1.33 | 2.88 | 89.82 | 157.00 | 635.48 | 1432.78 | 40.39 |
| 378.15 | 1.50 | 3.23 | 89.51 | 156.69 | 711.85 | 1430.55 | 43.98 |

Table 3 Structure details of the plate type heat exchangers

| <i>PHE</i> | δ (mm) | S_p (mm ²) | W (mm) | b (mm) | β (°) |
|--------------|---------------|--------------------------|----------|----------|-------------|
| Evaporator | 0.45 | 260460 | 200 | 4.4 | 60 |
| Dehumidifier | 0.45 | 260460 | 200 | 4.4 | 60 |
| Condenser | 0.45 | 260460 | 200 | 4.4 | 60 |

Table 4 Area dimensions of the heat and mass transfer devices at the balance condition of the dehumidifier

| T_{fs} (K) | A_c (m ²) | A_{SH} (m ²) | A_d (m ²) | A_h (m ²) | Q_c (kW) | Q_{SH} (kW) | $Q_{h,d}$ (kW) |
|--------------|-------------------------|----------------------------|-------------------------|-------------------------|------------|---------------|----------------|
| 368.15 | 92.82 | 5.25 | 76.07 | 38.94 | 1073.34 | 200.35 | 365.38 |
| 375.15 | 84.58 | 6.76 | 106.10 | 39.01 | 987.26 | 277.90 | 508.13 |
| 378.15 | 81.10 | 7.63 | 116.58 | 39.06 | 950.48 | 312.76 | 569.25 |

Table 5 Specific parameters of the combined system at different spraying temperatures

| T_{sw2} (K) | m_{da} (kgs ⁻¹) | m_{sw} (kgs ⁻¹) | x_e (%) | W_{net} (kW) | m_w (kgh ⁻¹) | Q_t (kW) | η_t (%) |
|---------------|-------------------------------|-------------------------------|-----------|----------------|----------------------------|------------|--------------|
| 348.15 | 1.80 | 3.52 | 89.82 | 157.00 | 714.94 | 1461.01 | 43.30 |
| 353.15 | 1.33 | 2.88 | 89.82 | 157.00 | 635.48 | 1432.78 | 40.39 |
| 358.15 | 0.98 | 2.36 | 89.82 | 157.00 | 560.19 | 1405.85 | 37.55 |

Table 6 Specific parameters of the combined system at different terminal temperature difference of the seawater heater

| TTD_{SH} (K) | m_{da} (kgs ⁻¹) | m_{sw} (kgs ⁻¹) | x_e (%) | W_{net} (kW) | m_w (kgh ⁻¹) | Q_t (kW) | η_t (%) |
|----------------|-------------------------------|-------------------------------|-----------|----------------|----------------------------|------------|--------------|
| 15 | 1.60 | 3.43 | 89.82 | 157.00 | 753.72 | 1487.72 | 44.18 |
| 20 | 1.33 | 2.88 | 89.82 | 157.00 | 635.48 | 1432.78 | 40.39 |
| 25 | 1.08 | 2.33 | 89.82 | 157.00 | 513.04 | 1379.56 | 36.06 |

Table 7 Performance comparison of the flashing Rankine cycle between the current system and the double-flash geothermal power plant [4]

| | m_{gw} (kgs ⁻¹) | T_{gw} (K) | p_c (kPa) | T_{fs}/T_{fw} (K) | p_{gw} (kPa) | p_{FE} (kPa) | m_{fs} (kgh ⁻¹) | h_{fs} (kJkg ⁻¹) | h_e (kJkg ⁻¹) |
|-----------|-------------------------------|--------------|-------------|---------------------|----------------|----------------|-------------------------------|--------------------------------|-----------------------------|
| Current | 1 | 503.15 | 96.4 | 436.15 | 2797 | 666.86 | 0.15 | 2760.7 | 2531 |
| Yari [4] | 1 | 503.15 | 96.4 | 436.15 | 2795 | 666.5 | 0.15 | 2761 | 2531 |
| Error (%) | / | / | / | / | 0.07 | 0.05 | 2.9 | 0.01 | 0 |

438 **Fig. 1 Specific configuration scheme of the combined system for power and water production driven by geothermal energy**

439 **Fig. 2 Temperature profiles and psychrometric chart within the power and water combined system**

440 (a) Condenser

441 (b) Seawater Heater

442 (c) Psychrometric chart

443 **Fig. 3 Performance of the flashing Rankine cycle with the increase of the flashing temperature**

444 **Fig. 4 Entropy generation distribution of the components for the power and water combined system**

445 **Fig. 5 Water production of the power and water combined system with the increasing air mass flow rate at different flashing**

446 **temperatures**

447 **Fig. 6 Total efficiency of the power and water combined system with the increasing air mass flow rate at different flashing**

448 **temperatures**

449 **Fig. 7 Water production of the power and water combined system with the increasing air mass flow rate at different spraying**

450 **temperatures**

451 **Fig. 8 Total efficiency of the power and water combined system with the increasing air mass flow rate at different flashing**

452 **temperatures**

453 **Fig. 9 Comparison of GOR between the current results and the published values from Narayan [23]**

454

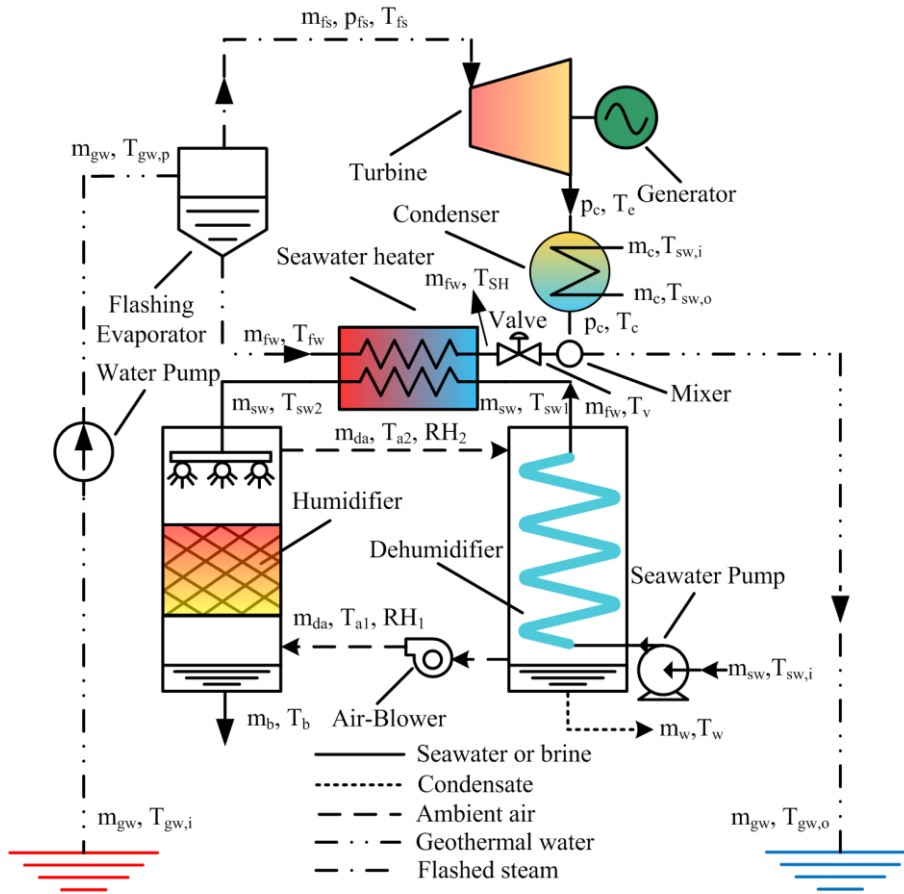
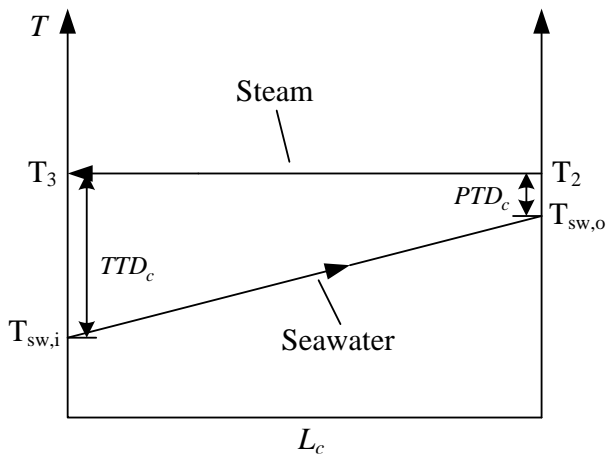
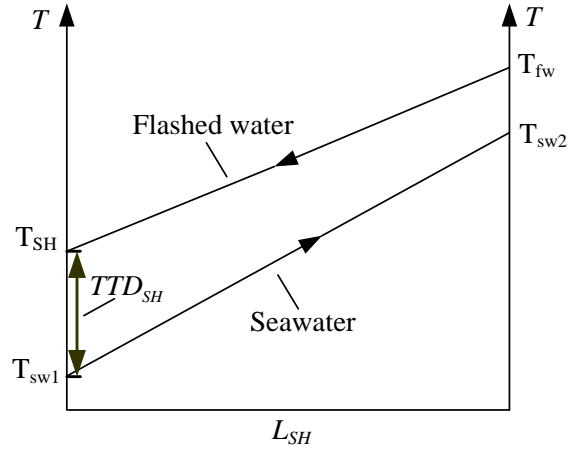


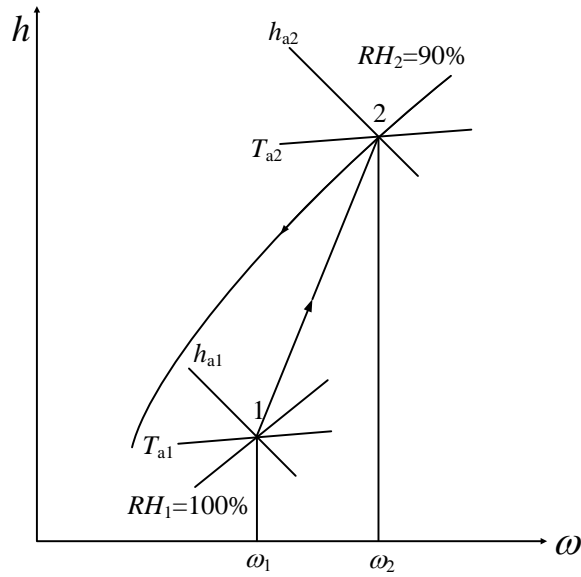
Fig. 1 Specific configuration scheme of the combined system for power and water production driven by geothermal energy



(a) Condenser



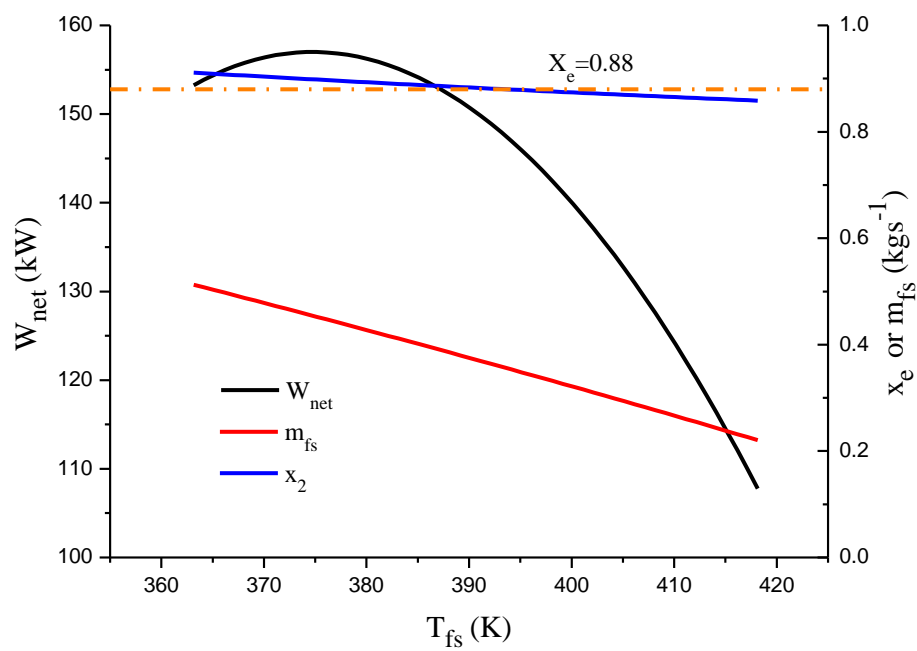
(b) Seawater heater



(c) Psychrometric chart

Fig. 2 Temperature profiles and psychrometric chart within the power and water combined system

463



464 Fig. 3 Performance of the flashing Rankine cycle with the increase of the flashing temperature

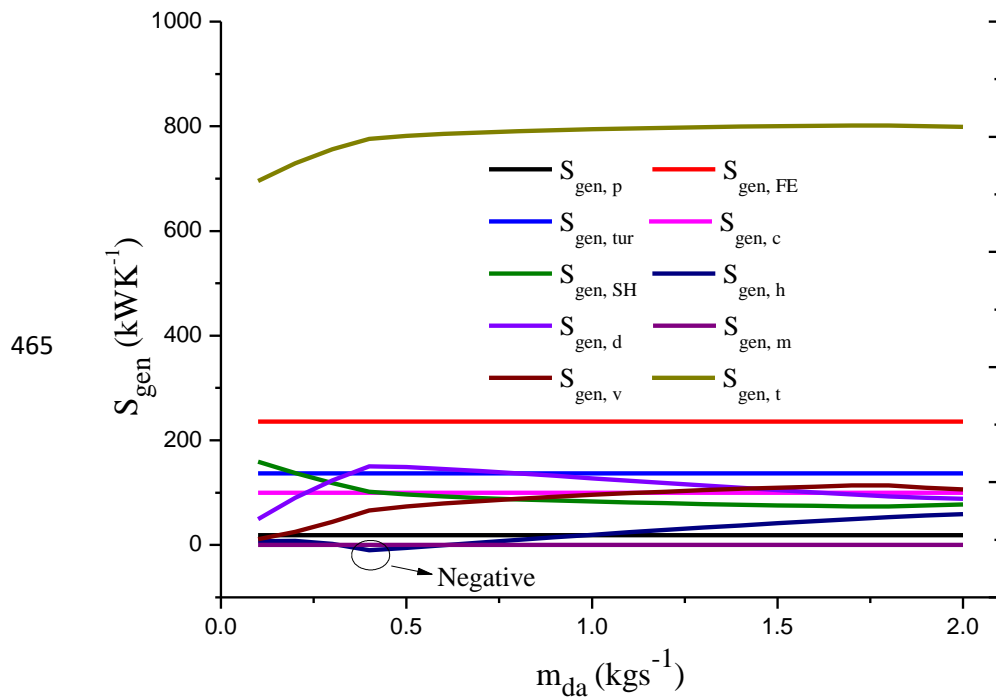
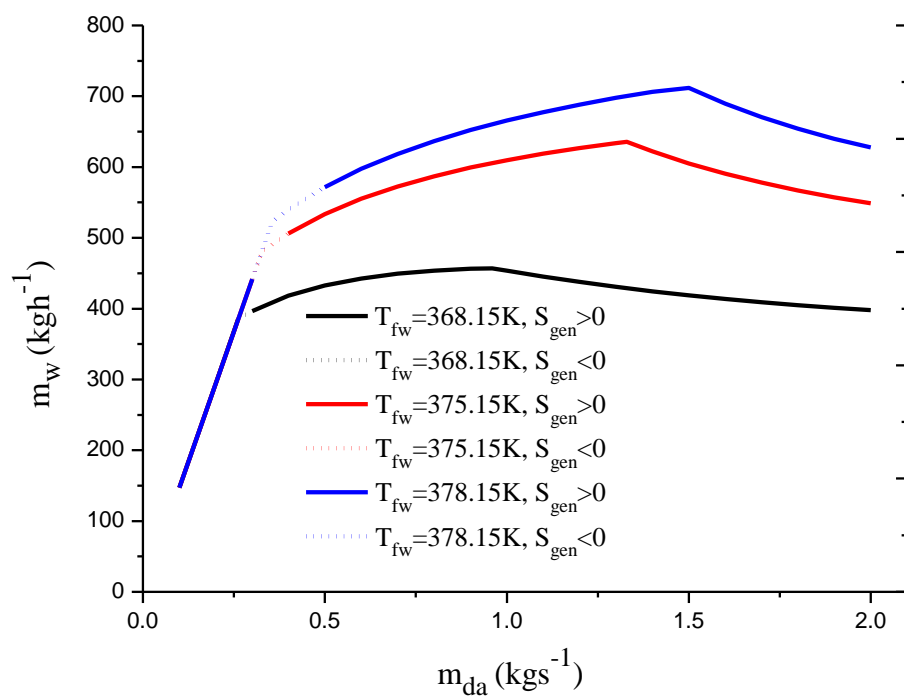


Fig. 4 Entropy generation distribution of the components for the power and water combined system

468

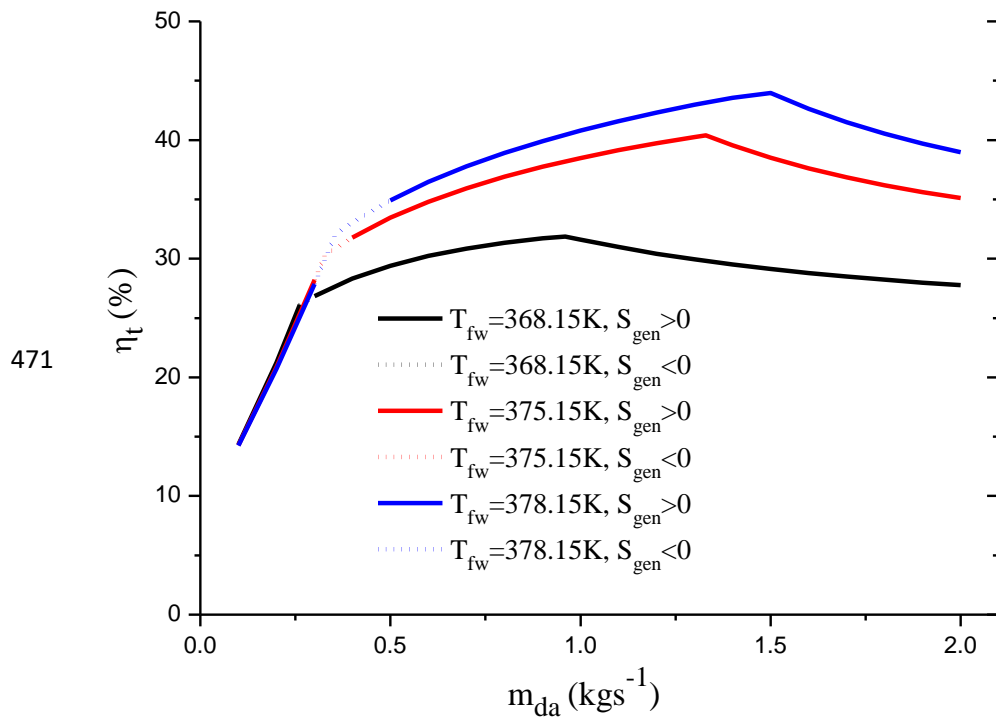


469

Fig. 5 Water production of the power and water combined system with the increasing air mass flow rate at different flashing

470

temperatures



472 Fig. 6 Total efficiency of the power and water combined system with the increasing air mass flow rate at different flashing
 473 temperatures

474

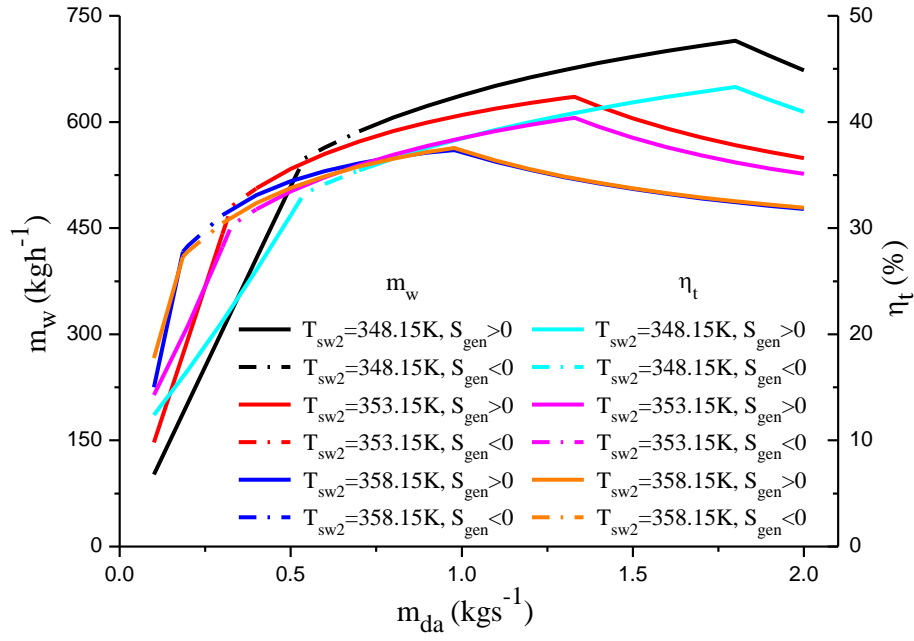


Fig. 7 Water production of the power and water combined system with the increasing air mass flow rate at different spraying temperatures

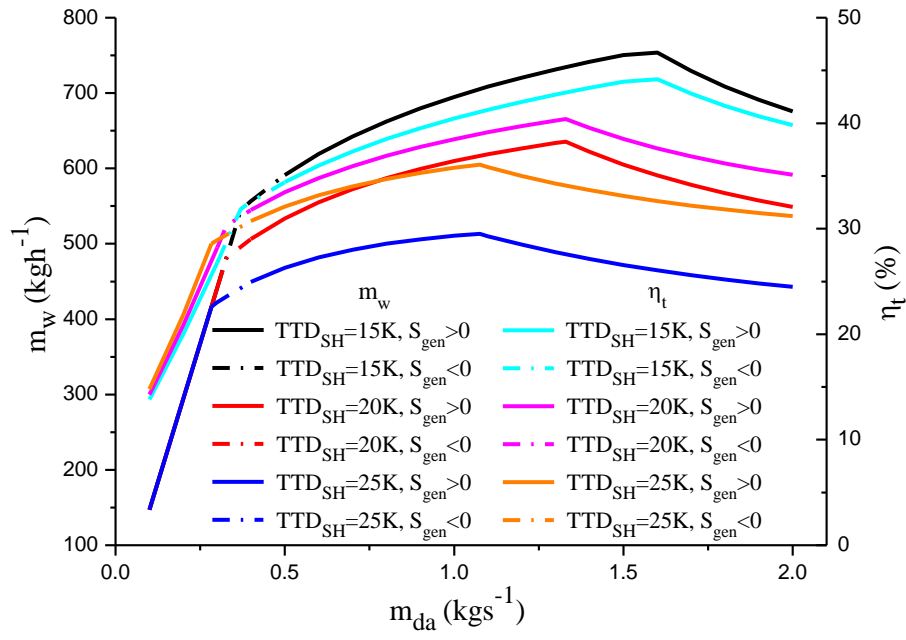
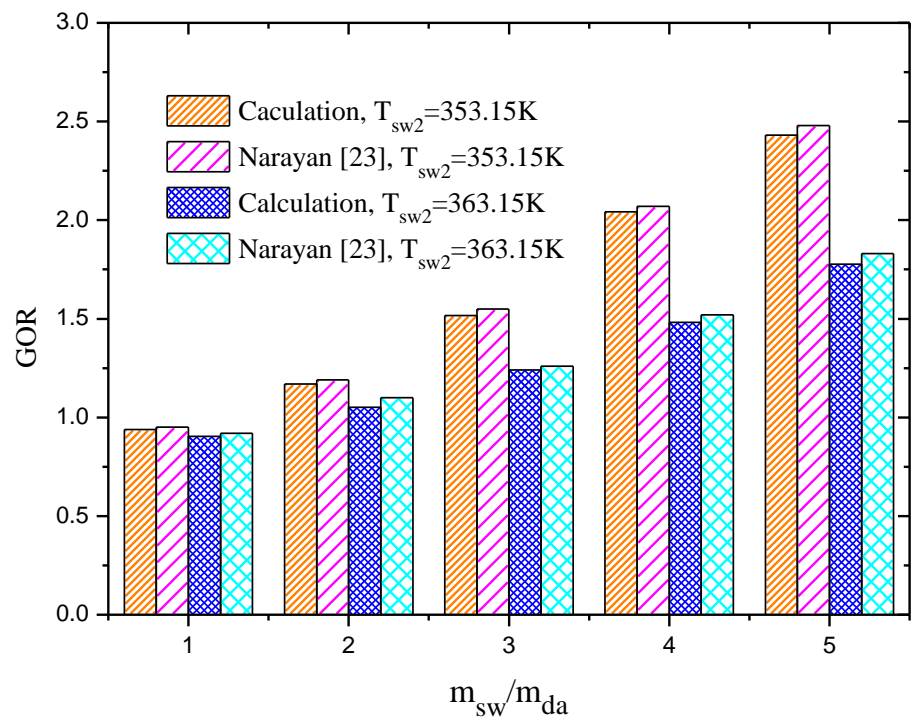


Fig. 8 Total efficiency of the power and water combined system with the increasing air mass flow rate at different flashing temperatures

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483

484 Fig. 9 Comparison of GOR between the current results and the published values from Narayan [23]

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