

Beidou Satellite Maneuver Thrust Force Estimation for Precise Orbit Determination

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Abstract Beidou satellites, especially Geostationary Earth Orbit (GEO) and Inclined Geo-Synchronous Orbit (IGSO) satellites, need to be frequently maneuvered to keep them in position due to various perturbations. The satellite ephemerides are not available during such maneuver periods. Precise estimation of thrust forces acting on satellites would provide continuous ephemerides during maneuver periods, and could significantly improve orbit accuracy immediately after the maneuver. This would increase satellite usability for both real-time and post processing applications. Using one year of observations from the Multi-GNSS Experiment (MGEX) network, we estimate the precise maneuver periods for all Beidou satellites and the thrust forces. On average, GEO and IGSO satellites in the Beidou constellation are maneuvered 12 and 2 times, respectively, each year. For GEO satellites, the maneuvers are mainly in-plane, while out-of-plane maneuvers are observed for IGSO satellites and a small number of GEO satellites. In most cases, the Beidou satellite maneuver periods last 15 to 25 min, but can be as much as 2 h for the few out-of-plane maneuvers of GEO satellites. The thrust forces acting on Beidou satellites are normally in the order of 0.1 to 0.7 mm/s². This can cause changes in velocity of GEO/IGSO satellites in the order of several decimeters per second. In the extreme cases of GEO out-of-plane maneuvers, very large

cross-track velocity changes are observed, namely 28 m/s, induced by 5.4 mm/s^2 thrust forces. Also, we demonstrate that by applying the estimated thrust forces in orbit integration, the orbit errors can be estimated at decimeter-level in along- and cross-track directions during normal maneuver periods, and 1 to 2 m in all the orbital directions for the enormous GEO out-of-plane maneuver.

Keywords Beidou; Maneuver Detection; Thrust force; Precise Orbit Determination

Introduction

Satellites tend to gradually deviate from their predefined orbits due to various perturbations. When this happens, the satellite master control station needs to take action to reposition satellites to keep their optimal constellation. This procedure is known as an orbital maneuver. Orbital maneuvers for operational satellites can be classified into two categories: in-plane maneuver and out-of-plane maneuver. An in-plane maneuver is generally implemented in the along-track direction, while an out-of-plane maneuver also applies a thrust force in the cross-track direction (Kelecy et al. 2007; Song et al. 2012). The frequency of maneuvers largely depends on the characteristics of orbits, especially their rotation periods (Hugentobler 1998). Due to the ellipticity of earth's equator, the resonance effect can lead to constant along-track acceleration for a GEO satellite, resulting in significant longitude drift (Sehna 1960). Moreover, the gravitational effects of the Sun, the Moon, as well as the Solar Radiation Pressure (SRP) also play important roles in satellite perturbations (Steigenberger et al. 2013).

The Chinese Beidou Navigation Satellite System (BDS) has a mixed constellation, consisting of 5 GEO satellites, 5 IGSO satellites, and 4 Medium Earth Orbit (MEO) satellites,

providing Asia regional coverage since 2012. Global coverage will be achieved by 2020 with a constellation of 5 GEO, 3 IGSO, and 27 MEO satellites (BeiDou 2013). For GEO and IGSO satellites, the 1:1 commensurability between their orbital period and the earth rotation period indicates that the resonance of satellite motion with geo-potential terms is quite obvious; the mean semimajor axes of GEO satellites may vary by ± 35 km due to the long period libration of 1,000 to 2,000 days (Hugentobler et al. 1999). This is the reason for implementing frequent east-west (along-track) station-keeping maneuvers for Beidou satellites (Du et al. 2014). It was reported that Beidou in-orbit GEO satellites needed east-west (along-track) station-keeping maneuvers every 25 to 35 days and north-south (cross-track) maneuvers about every 2 years (Xie et al. 2012). In addition, for IGSO satellites, the regular maintenance cycle was about 180 days (Prange et al. 2016). In 2013, a 50-day study of Beidou GEO satellites also presented that one to two maneuvers were executed for each satellite and that the dominant velocity change is in the along-track direction, reaching up to 100 mm/s (Dach et al. 2009; Steigenberger et al. 2013).

Frequent Beidou satellite maneuvers cause interruptions to satellite usability that may affect user positioning accuracy and availability. If the satellite maneuver can be successfully detected and the thrust forces accurately estimated, the satellite orbit during or shortly after maneuver can be precisely determined, and the satellite usability improved.

Much effort has been made to detect satellite maneuvers. Major maneuver detection and orbit determination techniques include: (1) the use of the satellite two line element (TLE) time history data (Kelecy et al. 2007; Patera 2008), which can reliably detect satellite thrust maneuvers down to centimeter per second level or less, but due to the inaccuracy of the raw TLE data, quite a large time lag of about 2 to 3 days can be induced into the detected maneuvers; (2) estimating thrust force parameters with precise observations; indeed some researchers prefer the short arc orbit determination strategy (Zhang et al. 2013). Generally

speaking, orbital maneuvers can be modeled as instantaneous velocity change in the radial (R), along-track (A) and cross-track directions (C) (Beutler et al. 1994; Jäggi et al. 2012), or as constant thrust forces in RAC directions lasting a period of time (Ju et al. 2017), or as rectangular range profile combined with post-maneuver sinusoids proposed by the navigation support office of European Space Operations Centre (ESOC) (Gienger and Pereira 2012). The first model is also known as an impulsive maneuver, and the last two are non-impulsive.

Low Earth Orbit (LEO) satellite maneuvers can be relatively easily handled with precise GPS observations in the reduced-dynamic orbit determination mode. Orbit determination modules for LEO satellites during maneuver have been developed in many software packages based on the above maneuver models, such as the EPOS, Bernese, GHOST and NUDTTK (Jäggi et al. 2012; Ju et al. 2017; Yoon et al. 2006). Centimeter-level orbit accuracy can be obtained for LEO maneuver satellites after calibration with these software packages (Ju et al. 2017; Yoon et al. 2006).

Compared to LEO satellites, maneuvers of navigation satellites are much more difficult to calibrate due to their high altitudes and a limited number of tracking stations. The ESOC's navigation support office has proposed a method to automate detection of orbital maneuvers for GNSS satellites. It is realized by first identifying the maneuver period with an a priori orbit, where the maneuver start time is defined when pseudorange residual exceeds the detection limit, end time is defined by the equation $Maneuver_{end} = Maneuver_{start} + \Delta v / \max Acc$, where Δv denoting the maneuver magnitude and $\max Acc$ representing the average acceleration generated by continuous firing of the corresponding satellite; then estimating the maneuver start and end times, magnitude (Δv) and post-maneuver sinusoids, according to the rectangular range profile combined with the post-maneuver sinusoids maneuver model. The start time of a maneuver can be easily detected with an accuracy of a few minutes, but it is difficult to determine the end time due to

the fact that the simulated/computed range data are synchronized with ionospheric-free phase and range data at the start of the pass. The satellite orbit is no longer smooth due to thrust force, and the reference orbit used for range computation does not fit the post-maneuver trajectory. The end time would be better determined by creating another set of simulated range data which synchronized with data at the end of the pass (Gienger and Pereira 2012). The classical maneuver detection procedure adopted at the Center for Orbit Determination in Europe (CODE) for the International GNSS Services (IGS) is based on the closest approach of two arcs calculated separately before and after the maneuver, where the instantaneous velocity change is determined as the difference between these two arcs at this point (Dach et al. 2009; Steigenberger et al. 2013). This method can effectively detect satellite maneuvers and shorten the post-maneuver recovery time for GNSS satellites. However, it treats the maneuvering process just as an impulse, while in fact, satellite maneuver thrust forces can last a period of time. Therefore, satellite maneuvers detected this way do not reflect the physical influence of thrust forces and fail to provide continuous orbits during maneuver periods.

Currently, Beidou IGSO/MEO satellite orbits have an accuracy of 1 to 2 dm during normal operation, and GEO orbits can be determined with decimeter-level accuracy in the radial direction and have 1 to 2 m 3-dimensional accuracies (Lou et al. 2016; Zhao et al. 2013). However, in case of a maneuver, the satellite precise ephemeris is not available on the day of the maneuver and even the days before or after the maneuver. Beidou satellite orbits during and shortly after maneuver periods may be improved by studying the feature of thrust forces. Precise estimation of maneuver start and end times, as well as the thrust amplitude, are greatly beneficial for precise orbit recovery.

We propose a procedure for Beidou satellite maneuver detection and estimation, including maneuver period detection, thrust-influenced position and velocity drift estimation,

and thrust force estimation, using observations from the MGEX network. In the next sections, we first briefly describe the methodology to detect satellite maneuver and estimate the thrust force. Then, the description is focused on the experiments and results obtained from one year of observation data (April 2014 to March 2015) from MGEX. Thereafter, validation of the estimated thrust forces is given, followed by conclusions in the last section.

Satellite maneuver detection and thrust force estimation

Satellite maneuvers are executed by thrust forces, which generate accelerations for the satellites to change their velocities and thus positions. The thrust forces are different from the natural perturbation forces which can be modeled and corrected, and they are generally unexpected and unknown. This characteristic of thrust forces leads to the failure of successive orbit determination for the satellite during maneuver period. If the maneuver forces can be precisely known and integrated into the dynamical models, satellite orbit can also be determined even during the maneuver period.

To obtain thrust forces acting on Beidou satellites, we need to identify the exact periods when orbital maneuvers take place. Two data sources, including broadcast ephemerides and ground tracking data, are used for this purpose. Normally, after an orbital maneuver, the Kepler elements of the orbit will have changed significantly, and therefore, by examining discontinuity of Kepler elements from consequent broadcast ephemeris for all satellites, potential periods of maneuver can be detected. Also, during and shortly after maneuvers, the broadcast ephemerides are normally set to “unhealthy”; this serves as another indicator. To even further narrow down the exact start and end times of any maneuver, carrier phase triple difference observations from ground monitoring stations are used. Using the broadcast ephemerides before the maneuver starts to estimate satellite positions, the ionospheric delay reduced by dual-frequency combination, **site-specific tropospheric delay estimated**

beforehand in a separate Precise Point Position (PPP) process with GPS observations using the Global Mapping Function (GMF) and the hydrostatic zenith delay eliminated according to Saastamoinen model, one should find that the triple difference residuals are close to zero. As is shown in the triple difference observation equation

$$\begin{aligned}\phi_{AB}^{jk}(t_2) - \phi_{AB}^{jk}(t_1) &= \frac{1}{\lambda} [\rho_{AB}^{jk}(t_2) - \rho_{AB}^{jk}(t_1)] + N_{AB}^{jk}(t_2) - N_{AB}^{jk}(t_1) \\ &= \frac{1}{\lambda} [\rho_{AB}^{jk}(t_2) - \rho_{AB}^{jk}(t_1)]\end{aligned}$$

where A and B stand for different stations, j and k donate different satellites, and t_1 and t_2 are the two successive observation epochs; $\phi_{AB}^{jk}(t_2)$ and $\phi_{AB}^{jk}(t_1)$ represent the double-differenced carrier phase observables divided the wave length λ , and $N_{AB}^{jk}(t_2)$ and $N_{AB}^{jk}(t_1)$ are the double-differenced ambiguities, and $\rho_{AB}^{jk}(t_2)$ and $\rho_{AB}^{jk}(t_1)$ donate the double-differenced geometrical distances between stations and satellites. Apart from the canceling of satellite and receiver clock errors in double difference process, the ambiguities are also effectively cancel in triple differencing. Since the normal satellite orbits are very smooth and can be well predicted by the broadcast ephemerides, the geometric distances between satellite and receiver can be accurately calculated. Therefore, quasi-zero triple difference residuals can be expected. However, during a maneuver, as the calculated satellite positions drift away from the true positions and the calculated geometric distances are not right, the triple difference residuals can shift away from zero as well. Immediately after the maneuver, the position changes of satellites become smooth again, and so do the triple difference residuals. Figure 1 shows the triple difference residuals with seven ground stations during the maneuver period of satellite C08 on Jan 9, 2015. All of the double difference observations are formed with observables between the satellite C08 and the station SIN1, which is in the middle of the tracking network, as shown in Figure 2 of next section; the other

satellite and station involved in the differential observations are marked in the figure. As can be seen, the start and end time of this maneuver can be clearly identified.

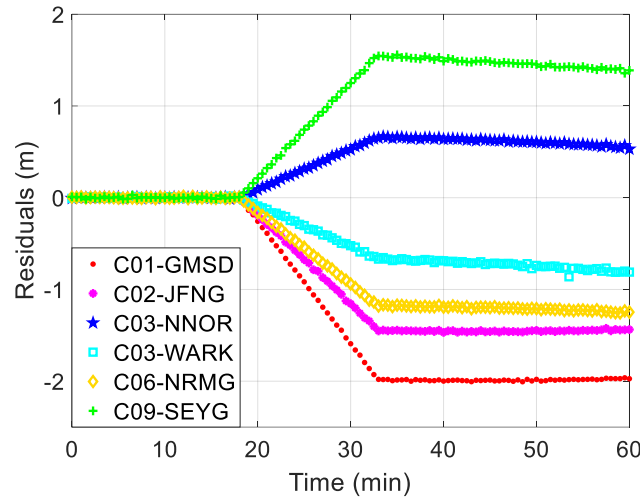


Fig. 1 Triple difference residuals during the maneuver period of satellite C08 on Jan 9, 2015. All the differential observations are formed among satellite C08, station SIN1 and another satellite/station marked in the figure

In order to extract thrust forces acting on a satellite, we need to identify the satellite movement due to the thrust forces. This can be achieved by comparing the orbits obtained from kinematic orbit determination and orbit integration without considering the thrust forces. Kinematic orbit determination utilizes GNSS measurements from a ground tracking network, without using any force models. Thus, the orbit movements from this method include all forces acting on the satellite. On the other hand, any orbit obtained through orbit integration method results from the integrations of forces. Without considering the thrust forces, the orbit differences between the kinematic and integration solutions must be caused by the thrust forces.

In data processing, kinematic orbit determination is performed from about 10 min before a maneuver to half an hour after. During this period, we only select those stations with

continuous carrier phase measurements, as this will ensure that there are no jumps in positions due to station changes. The measurement sampling interval we used is 30 seconds. The carrier phase double difference ionospheric-free combinations are used for satellite position determination, which will cancel most Beidou measurement errors. The tropospheric delay is corrected by the Hopfield model. Since only relative positions are required for this study, the initial ambiguities are fixed to constants at the starting epoch, where the satellite position is from the broadcast ephemeris. Also, the satellite position and velocity from broadcast ephemeris serve as the initial state for orbit integration. The reference frames and orbit models adopted during orbit integration are listed in Table 1. No SRP model was applied in the orbit integration, as most Beidou satellite maneuvers only last for about 20 min, the resulting orbit errors due to the neglected SRP effect is negligible.

Table 1 Reference frames and dynamic orbit models adopted in orbit integration

Reference frames	
Time system	GPS Time
Inertial frame	ICRF at J2000.0
Terrestrial frame	ITRF2008
Precession model	IAU 2000 Precession theory
Nutation model	IAU 2000R06 Nutation theory
EOP parameters	Polar motion & UT1 from IERS C04 series aligned to ITRF2008
Orbit models	
Geo-potential (static)	EGM2008 model up to degree and order 12 (+C21+S21) Solid earth tides: IERS 2010
Tidal variations in geo-potential	Ocean tides: FES2004 model Solid earth pole tide: IERS 2010 Oceanic pole tide: IERS 2010
Third-body	Sun, Moon, Jupiter, Venus, Mars as point masses
Ephemeris used	JPL DE405
SRP model	Not applied
Relativistic effects	Applied according to IERS 2010

201

202 To estimate changes in satellite velocity and acceleration due to maneuvering, the orbits
203 derived from kinematic orbit determination and integration were compared. First, the
204 differences of Kepler elements, position and velocity derived from these two methods are
205 calculated. Then, the thrust induced acceleration is also computed by the differential of
206 change in velocity. Since the kinematic orbit is quite noisy, caused by measurement noises
207 and poor geometry, a low-pass filter is used to reduce high-frequency noises in both velocity
208 and acceleration estimation. It has been noticed that orbit change due to maneuvering can
209 affect other perturbation forces, e.g., earth gravitational perturbation, and this can also lead to
210 further orbit change. Therefore, the acceleration derived from orbit difference only
211 approximately shows the true thrust forces. More accurate thrust forces are estimated through
212 orbit fitting for the kinematic orbit, assuming constants or linear changes based on the
213 approximate forces.

214

215 **Experiments and results**

216 We analyzed orbital maneuvers of all Beidou satellites for a period of one year (Apr 1, 2014
217 to Mar 31, 2015). The broadcast ephemerides are used for initial state calculation of
218 maneuvered satellites; the precise ephemerides are used to provide the positions of other
219 satellites in kinematic orbit determination, using observations taken from MGEX carrier
220 phase measurements.

221 For kinematic orbit determination, the number of MGEX stations available during the
222 study period is limited. Although the numbers of stations tracking GEO and IGSO satellites
223 were more than 10 and 30, respectively, about 5 to 20 stations were used in different cases of
224 satellite maneuvering due to the requirement of successive tracking and no cycle slips during

the orbit determination period. The limited number of tracking stations would lead to poor observation geometry, and thus the low orbit determination accuracy. An example of the tracking network is shown in Figure 2.

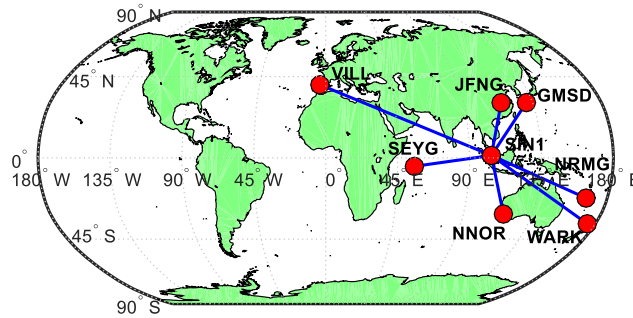


Fig. 2 Observation network in kinematic orbit determination of satellite C08 on Jan 9, 2015

To investigate the precision of kinematic orbit determination, the Position Dilution Of Precision (PDOP), which reflects the observation geometry, has been calculated for different satellites. Also, the DOPs in radial and horizontal directions of each satellite are analyzed, donated as the Vertical DOP (VDOP) and Horizontal DOP (HDOP). For simplicity, only the values of GEO satellite C03 and IGSO satellite C08 are listed (Table 2). Only 6 stations were available for C03 on May 5, 2014, and the PDOP was quite large, more than 260. The PDOPs of C03 and C08 ranged from around 100 to 200 during the rest of the maneuver days. On the other hand, the HDOPs were distinctly smaller and reduced by a factor of 10-20 compared to the VDOPs. Kinematic orbit determination has been done for two GEO and two IGSO satellites which were not maneuvered by the proposed method, and orbit accuracies were evaluated by comparing with precise ephemerides. The orbit determination period was 11:30-12:30 on Jan 5, 2015, and the HDOPs and VDOPs of the four satellites C02, C05, C06 and C09 were (10.09, 213.99), (7.84, 115.56), (11.90, 165.10) and (11.66, 123.99) respectively. The differences between the kinematic and precise orbits in RAC directions are

shown in Figure 3. The RMSs in the radial direction were somewhat large, at about 1.3 and 1.2 m for GEO and IGSO satellites, while in the along- and cross-track directions were just 0.03, 0.1 m for GEO and 0.08, 0.07 m for IGSO satellites, respectively. The better orbit accuracies in along- and cross-track directions are corresponding to the superior geometry strength in the horizontal direction.

Table 2 PDOPs for satellites in kinematic orbit determination

Satellite-Day	HDOP	VDOP	PDOP
C03-Apr 10, 2014	12.08	131.14	131.69
C03-May 5, 2014	11.97	262.53	262.80
C03-May 30, 2014	11.42	175.84	176.21
C03-Jun 26, 2014	9.56	198.94	199.17
C03-Jul 22, 2014	12.04	136.76	137.29
C03-Aug 18, 2014	11.74	203.11	203.45
C03-Sep 12, 2014	9.54	155.37	155.67
C03-Oct 3, 2014	10.36	177.63	177.93
C03-Oct 20, 2014	12.09	201.38	201.74
C03-Nov 10, 2014	10.95	160.27	160.64
C03-Dec 8, 2014	10.08	134.26	134.64
C03-Jan 5, 2015	11.21	165.32	165.70
C03-Feb 1, 2015	13.01	176.39	176.87
C03-Feb 28, 2015	10.10	126.00	126.41
C03-Mar 27, 2015	18.41	189.03	189.93
C08-Jul 11, 2014	10.52	195.11	195.40
C08- Jan 9, 2015	10.20	151.20	151.55

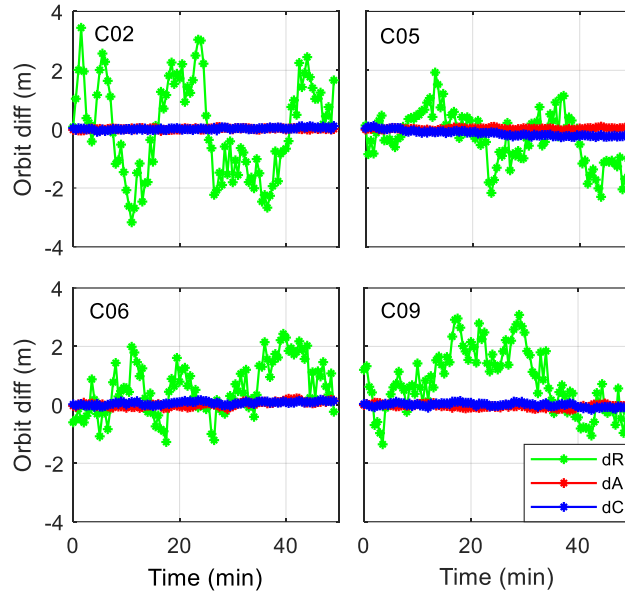


Fig. 3 Coordinate difference between kinematic and precise orbits for satellites C02, C05, C06 and C09. The orbit determination period is during 11:30-12:30 on Jan 5, 2015

In regards to the integrated orbit, an orbit was also computed for the unmaneuvered satellite C03 and compared with the precise orbit (Figure 4). The integration process started at 13: 20 on Jan 9, 2015. Coordinate drifts in RAC directions were all at decimeter-level for an integration length of 80 min. The drifts in the first half hour were less than 3 dm. The Beidou satellites normal maneuver periods are just around 20 min.

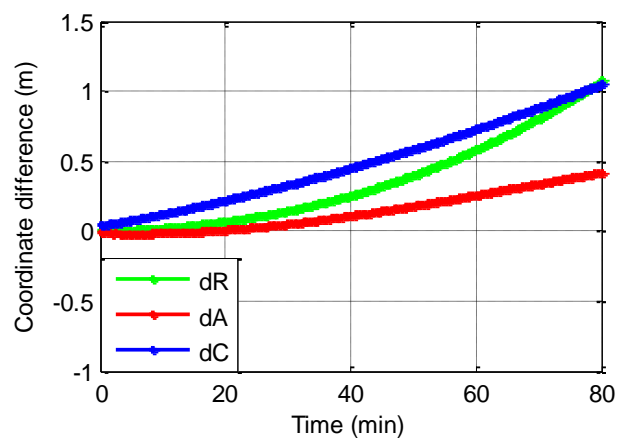


Fig. 4 Coordinate difference between integrated and precise orbits for satellite C03 since 13:20 on Jan 9, 2015

From triple difference residuals and the differences of these two orbit determination results, the Beidou satellite maneuver periods, the changes in velocity and Kepler elements, as well as thrust forces induced accelerations have been obtained. They are listed and analyzed in the rest of this section.

Maneuver periods

First, we try to identify maneuver periods for all Beidou satellites during the study period. There are 9 to 15 maneuvers for each GEO satellites, 2 maneuvers per IGSO satellites and no MEO satellite maneuvers shown in Table 3.

Table 3 Maneuver times detected for Beidou satellites during the study period

Periods	GEO					IGSO				
	C01	C02	C03	C04	C05	C06	C07	C08	C09	C10
Apr 2014-Jun2014	3	3	4	4	3	1	1	0	0	0
Jul 2014-Sep 2014	4	3	3	2	2	0	0	1	1	1
Oct 2014-Dec 2014	2	3	4	2	3	1	1	0	0	1
Jan 2015-Mar 2015	3	3	4	1	2	0	0	1	1	0
Total Maneuver	12	12	15	9	10	2	2	2	2	2

The unhealthy broadcast ephemerides epochs and exact maneuver periods of one GEO (C03) and one IGSO (C08) satellite are listed in Table 4. As can be seen, the Beidou broadcast ephemerides are set to “unhealthy” for a period of 6 to 8 h during maneuver periods. For the exact periods when thrust was being applied, they mostly range from 20 to 25 min for

GEO satellites and 11 to 22 min for IGSO satellites. Extremely long maneuver periods of 2 h or more, are found for GEO satellites, e.g., satellite C03 on Oct 20, 2014. This is due to the bi-annual north-south maneuver frequency reported in (Xie et al. 2012).

Table 4 Unhealthy broadcast ephemeris and exact maneuver periods

Satellite-Day	Unhealthy Broadcast EPH		Maneuver Periods	
C03-Apr 10, 2014	08:00:00-14:00:00	7 h	09:00:00-09:20:00	20.0 min
C03-May 5, 2014	09:00:00-14:00:00	6 h	09:24:30- 09:44:30	20.0 min
C03-May 30, 2014	11:00:00-16:00:00	6 h	11:24:30-11:44:30	20.0 min
C03-Jun 26, 2014	11:00:00-16:00:00	6 h	11:24:30-11:46:00	22.0 min
C03-Jul 22, 2014	11:00:00-16:00:00	6 h	11:25:00-11:46:00	21.0 min
C03-Aug 18, 2014	09:00:00-14:00:00	6 h	09:23:30-09:45:30	22.0 min
C03-Sep 12, 2014	11:00:00-16:00:00	6 h	11:24:30-11:45:30	21.0 min
C03-Oct 3, 2014	09:00:00-14:00:00	6 h	09:24:30-09:44:30	20.0 min
C03-Oct 20, 2014	18:00:00-01:00:00	8 h	18:55:30-20:53:00	117.5 min
C03-Nov 10, 2014	11:00:00-16:00:00	6 h	11:24:00-11:45:00	21.0 min
C03-Dec 8, 2014	08:00:00-13:00:00	6 h	08:24:30- 08:46:00	22.0 min
C03-Jan 5, 2015	09:00:00-14:00:00	6 h	09:22:30-09:45:30	23.0 min
C03-Jan 1, 2015	13:00:00-18:00:00	6 h	13:24:00-13:46:00	22.0 min
C03-Feb 28, 2015	13:00:00-18:00:00	6 h	13:22:30-13:47:00	24.5 min
C03-Mar 27, 2015	09:00:00-15:00:00	7 h	09:24:30-09:45:30	21.0 min
C08-Jul 11, 2014	09:00:00-14:00:00	6 h	09:12:00-09:29:00	17.0 min
C08- Jan 9, 2015	14:00:00-19:00:00	6 h	13:52:00-14:08:00	16.0 min

Figure 5 shows three examples of the satellite coordinate offsets in RAC directions due to the normal GEO maneuver, C03 on Jan 05,2015, the IGSO maneuver, C08 on Jan 09, 2015, and the extreme large GEO out-of-plane maneuver, C03 on Oct 20, 2014. For normal maneuvers, the time interval ranges from about 10 min before the maneuver to 7 min (C03) or 14 min (C08) after the maneuver. It is explicitly shown that the thrust forces are executed mainly in the along-track direction for C03 on Jan 5, 2015 and satellite position can deviate

more than 200 m in a half-hour. For C08, the maneuver is implemented in both along- and cross-track directions, and its position can shift more than 800 m and 200 m in these directions, respectively, during a half-hour period. Exceptionally large cross-track coordinate shifts have been observed for C03 on Oct 20, 2014 and plotted separately on the bottom right. The period ranges from about 5 min before to 10 min after the maneuver, and the orbit changes in RAC directions are approximately 700, 1500 and 1.4×10^5 m, respectively.

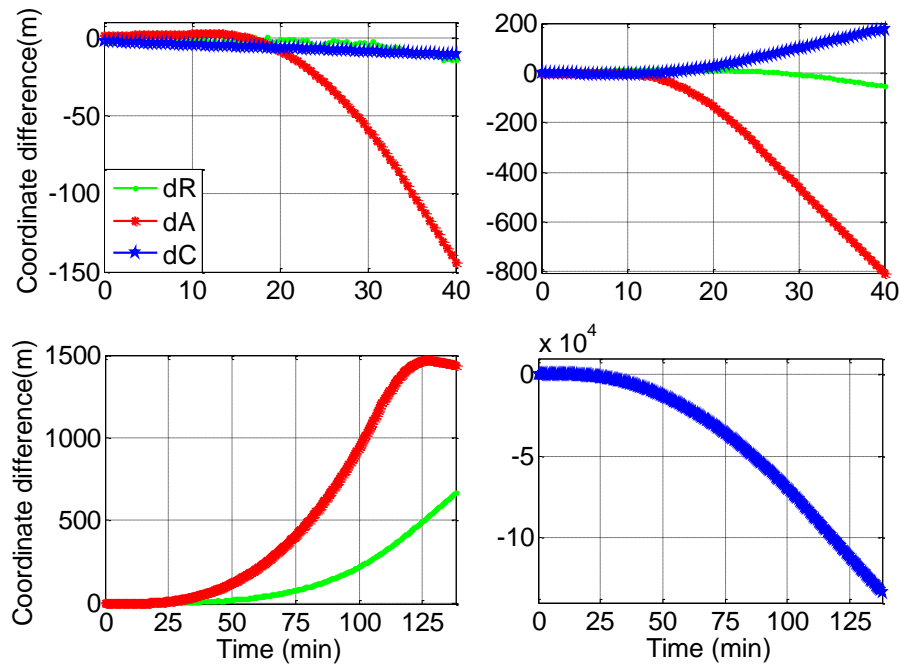


Fig. 5 Maneuvered satellites coordinate shifts in RAC directions. Satellite C03 on Jan 05, 2015 (*top left*), C08 on Jan 09, 2015 (*top right*) and C03 on Oct 20, 2014 (*bottom*)

Change of velocity and Kepler elements

Satellite velocity and Kepler elements change differently in different maneuver situations. The results show that all the IGSO satellites experience changes in velocity in both along- and cross-track directions of 0.4 to 0.6 m/s and 0.1 to 0.5 m/s, respectively; GEO satellites

normally experience change of velocity only in the along-track direction, with Δv ranging from about 0.1 to 0.15 m/s, but out-of-plane maneuvers also take place as exceptions to the rule as earlier mentioned. For simplicity, Table 5 only lists velocity changes due to maneuvers of GEO C03 and IGSO C08 in the study period. It shows that C03 normal maneuvers are in-plane and that velocity in the along-track direction decreases of 0.13 to 0.15 m/s. One exceptional case is on Oct 20, 2014 when the satellite has an out-of-plane maneuver and the velocity in the cross-track direction decreases by nearly 28.0 m/s. In regards to C08, out-of-plane maneuvers are implemented and the velocities reduce by about 0.6 and 0.1 m/s in the along- and cross-track directions, respectively.

Table 5 Maneuver-induced velocity changes of C03 and C08

Satellite-Day	dVR (m/s)	dVA (m/s)	dVC (m/s)	Satellite-Day	dVR (m/s)	dVA (m/s)	dVC (m/s)
C03-Oct 04, 2014	-0.0057	-0.1338	-0.0033	C03-Nov 10, 2014	-0.0102	-0.1467	-0.0012
C03-May 05, 2014	-0.0598	-0.1424	-0.0038	C03-Dec 08, 2014	0.0017	-0.1506	-0.0036
C03-May 30, 2014	-0.0136	-0.1396	-0.0057	C03-Jan 05, 2015	0.0187	-0.1547	-0.0006
C03-Jun 26, 2014	-0.0179	-0.1463	-0.0069	C03-Feb 01, 2015	-0.0004	-0.1494	-0.0033
C03-Jul 22, 2014	-0.0155	-0.1415	-0.0066	C03-Feb 28, 2015	-0.0133	-0.1518	-0.0018
C03-Aug 18, 2014	-0.0180	-0.1522	-0.0044	C03-Mar 27, 2015	-0.0104	-0.1385	-0.0019
C03-Sep 12, 2014	0.0030	-0.1307	-0.0061	C08-Jul 11, 2014	-0.0613	-0.6119	-0.0787
C03-Oct 03, 2014	-0.0124	-0.1294	-0.0001	C08-Jan 09, 2015	-0.0778	-0.5654	0.1247
C03-Oct 20, 2014	0.1135	-0.0004	-27.9977				

Figure 6 plots the changes of velocity of the maneuvered satellites, which are the same as those in Figure 5. For the in-plane maneuver of C03 on Jan 5, 2015, the along-track velocity decreases by 0.15 m/s and velocities in other two directions are merely changed. The satellite C08 on Jan 9, 2015 goes through an out-of-plane maneuver and velocity in the along- and cross-track directions drop and increase by 0.6 and 0.12 m/s, respectively. Special attention has been paid to the rare case of the GEO satellite out-of-plane maneuver, i.e., C03

on Oct 20, 2014. Different from normal maneuvers, where the satellite velocities simply either increase or decrease, the velocity change of the GEO out-of-plane maneuver is more complex. The satellite cross-track velocity decreases rapidly by about 28.0 m/s due to an almost constant acceleration in the first 100 min since the maneuver starts, meanwhile, the along-track velocity increases steadily by 0.42 m/s. Then after a time lag of around 5 min, the along-track velocity change comes back quickly to almost zero in approximately 13 min. In this whole process, the velocity in the cross-track direction reduces by 28.0 m/s, increases by 0.11 m/s in the radial direction, and there is a tiny change in the along-track direction.

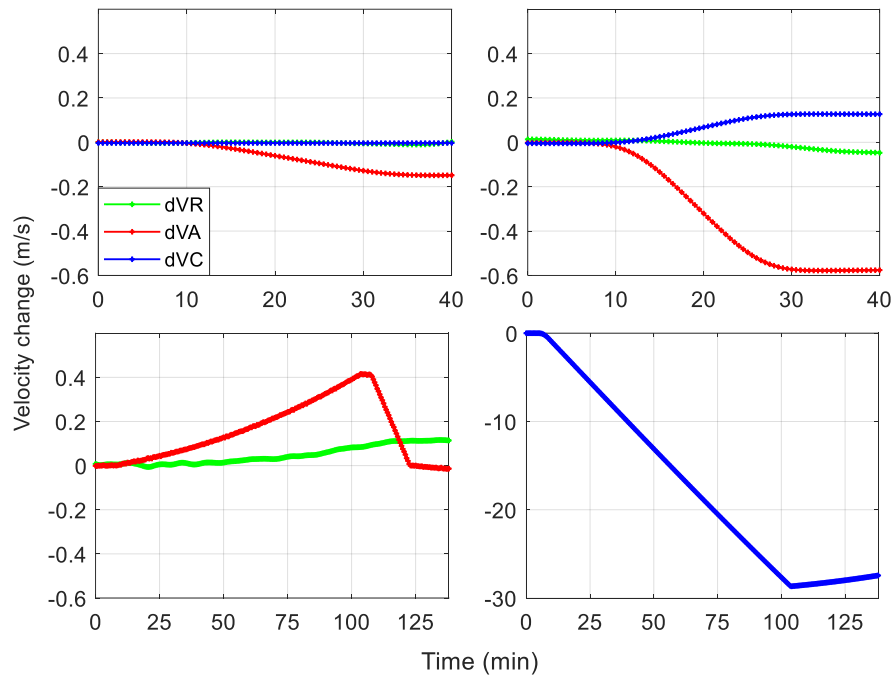


Fig. 6 Maneuvered satellite velocity changes in RAC directions. Satellite C03 on Jan 5, 2015 (*top left*), C08 on Jan 9, 2015 (*top right*) and C03 on Oct 20, 2014 (*bottom*)

The Kepler elements, i.e., the semimajor axis (a), eccentricity (e), inclination angle (i), argument of ascending node (Ω), argument of perigee (ω), and mean anomaly (M) change

differently according to maneuver types. For the two types of maneuvers, the in-plane maneuvers mainly increase/decrease a and e , and the out-of-plane maneuvers mainly change the orbital plane orientation elements. Satellite Kepler elements during maneuver period are derived epoch-wise based on the position and velocity vectors of the kinematic solution. They have been filtered to reduce observation noises. Comparisons of Kepler element changes since the initial epoch between kinematic and integrated orbits for the in-plane GEO maneuver, out-of-plane IGSO maneuver, and the exceptional case of GEO out-of-plane maneuver are shown in Figures 7, 8 and 9, respectively. As can be seen from Figure 7, elements representing the satellite ellipse size (a), shape (e), orientation inside the orbital plane (ω), and mean position of the satellite in the ellipse (M) have changed explicitly through the in-plane maneuver of C03. Due to the large along-track velocity change of C08, the changes of a and e are much larger than those of C03. Orbital plane orientation elements i and Ω are also adjusted due to the out-of-plane maneuver of C08. However, the changes can almost be ignored compared to the significant drops of i and Ω through the C03 extreme out-of-plane maneuver. The i and Ω of C03 have changed by about 0.38 deg and 15 deg due to the out-of-plane maneuver, respectively, which are approximately 160 and 37500 times larger than the variations in C08. In addition, other Kepler elements of C03 on Dec 20, 2014, e.g., a , ω and M , grow or reduce steadily first and then reverse the change in the last 13 min. On the other hand, by comparison of Figure 6 and Figure 7-9, it can be found that the semi-major axis has the same change pattern with the velocity change in the along-track component: when velocity in the along-track direction decreases, the satellite will be attracted much more by earth gravity, hence the reduction in semi-major axis, and vice versa. This phenomenon is in accordance with the law of conservation of energy.

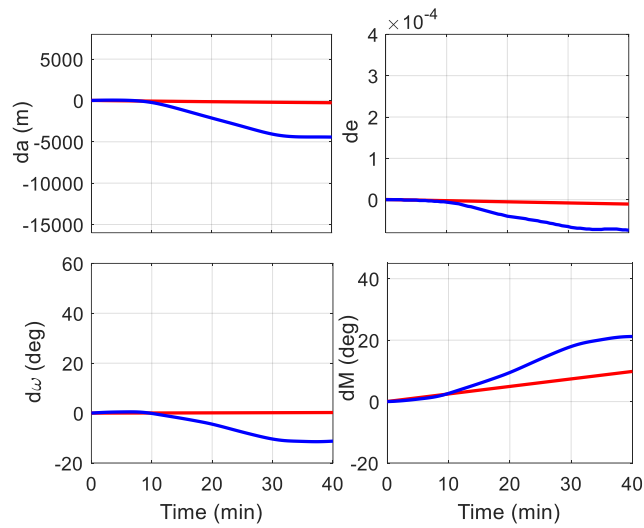


Fig. 7 Kepler element changes of kinematic (*blue*) and integrated orbits (*red*) for satellite C03 on Jan 5, 2015

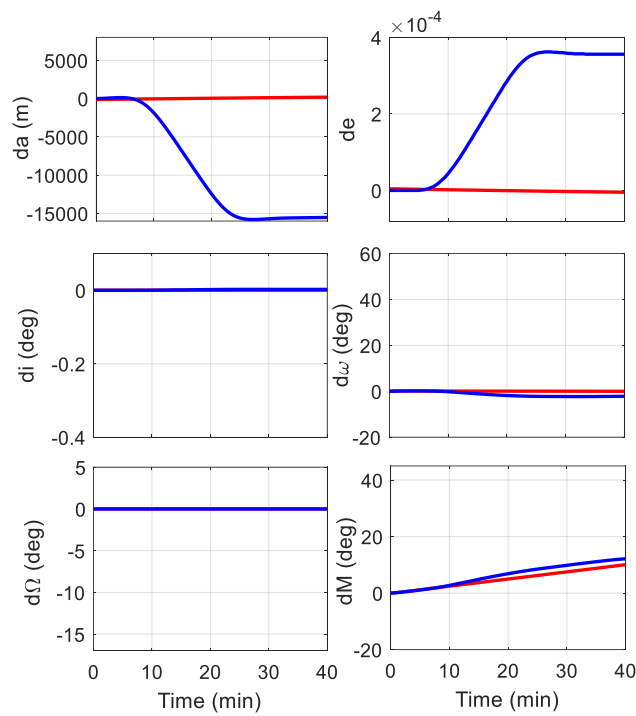


Fig. 8 Kepler element changes of kinematic (*blue*) and integrated orbits (*red*) for satellite C08 on Jan 9, 2015

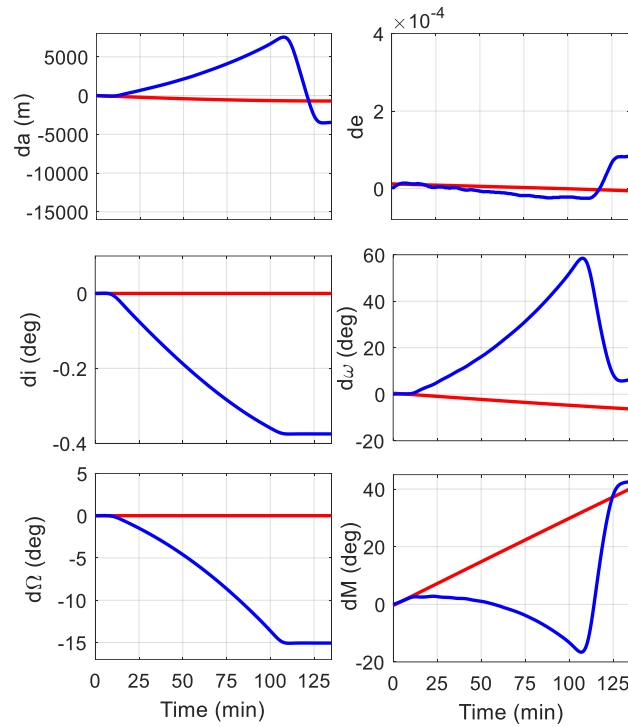


Fig. 9 Kepler element changes of kinematic (*blue*) and integrated orbits (*red*) for satellite C03 on Oct 20, 2014

Figure 10 compares the Kepler elements from broadcast ephemerides before and after the maneuver to the kinematic orbit for satellite C03 on Oct 20, 2014, as an instance. Similarly, it plots the change of Kepler elements with respect to the state at epoch 0. It can be seen that the kinematic orbit is essentially in agreement with the broadcast ephemerides before and after the maneuver.

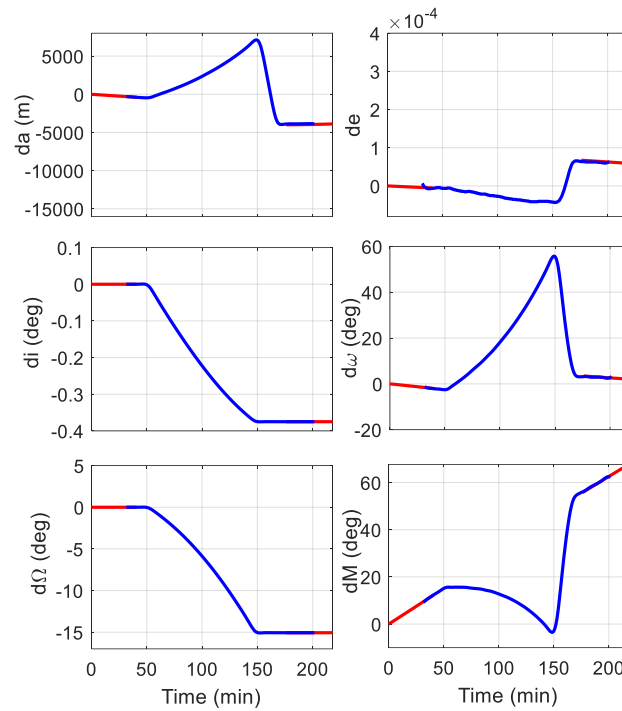


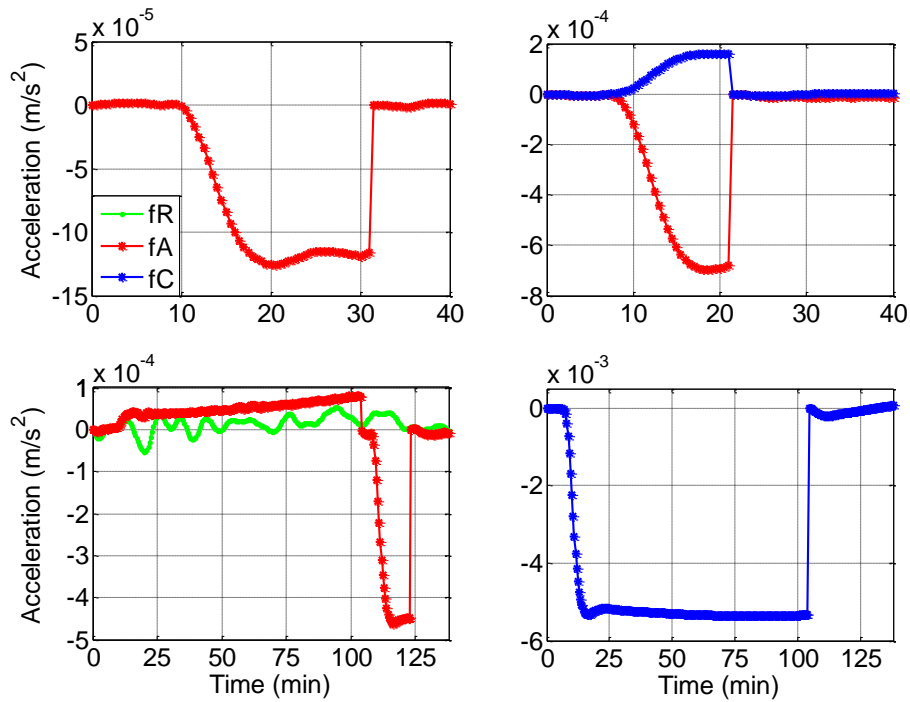
Fig. 10 Kepler element changes of kinematic (*blue*) and broadcast orbits (*red*) for satellite C03 on Oct 20, 2014

Accelerations induced by thrust forces

If maneuver thrust forces can be estimated accurately, they can be applied in the orbit integration process and thus, satellite orbits could be calculated continuously even during a maneuver period. Acceleration derived from the differential of changes in velocity can indicate the effect of thrust forces to some extent. Figure 11 shows thrust induced accelerations of three cases of maneuvers. It indicates that the accelerations (piecewise filtered) increase steadily at the beginning of the maneuver, and stay almost constant during the rest of the maneuver period. The in-plane maneuver of C03 on Jan 5, 2015 has an acceleration of 0.125 mm/s^2 in the along-track direction, as plotted on the top left. The accelerations in the along- and cross-track directions of C08 on Jan 9, 2015 can reach up to 0.70 and 0.15 mm/s^2 , respectively, shown on the top right. Thrust forces for C03 on Oct 20, 2014 in the out-of-plane maneuver are much larger and more complex with respect to the

400 executing periods and directions. Accelerations can be as large as 5.4 mm/s^2 in the
 401 cross-track direction (*bottom right*), and 0.45 and 0.04 mm/s^2 in the along-track and radial
 402 directions (*bottom left*).

403



404

405 **Fig. 11** Thrust induced accelerations on maneuvered satellites in RAC directions. Satellite
 406 C03 on Jan 5, 2015 (*top left*), C08 on Jan 9, 2015 (*top right*) and C03 on Oct 20, 2014
 407 (*bottom*)

408

409 Validation

410 Accuracies of the maneuver detection results are validated by integrating the estimated thrust
 411 forces into the dynamic model for orbit integration and comparing the result with the
 412 kinematic orbit. Integrated orbits with thrust forces applied should be consistent with the
 413 kinematic ones.

As examples, the estimated accelerations for C03 on Jan 5, 2015, C08 on Jan 9, 2015 and C03 on Oct 20, 2014 are introduced into the orbit integration processes. These calibrated maneuver orbits are then compared with the kinematic ones obtained directly from ground GNSS tracking data. Figure 12 shows their coordinate difference in RAC directions. The periods range from about 10 min before to 10 min after the maneuver. The RMSs of coordinate difference in RAC directions for C03 on Jan 5, 2015 are 1.41, 0.67 and 0.79 m, and 0.96, 0.82 and 0.66 m for C08 on Jan 9, 2015. It is clear that for these normal maneuvers, the corrected orbits during the maneuver period have accuracy at decimeter-level in the along- and cross-track directions compared to the kinematic orbits. For the exceptional case of the large C03 on Oct 20, 2014 out-of-plane maneuver, the calibrated orbit has an accuracy of 1.58, 1.03 and 2.38 m in RAC directions. Thus, continuous orbits of Beidou satellites during the maneuver periods can be obtained by orbit integration through this proposed method to an accuracy of sub-meters or 1 to 2 m.

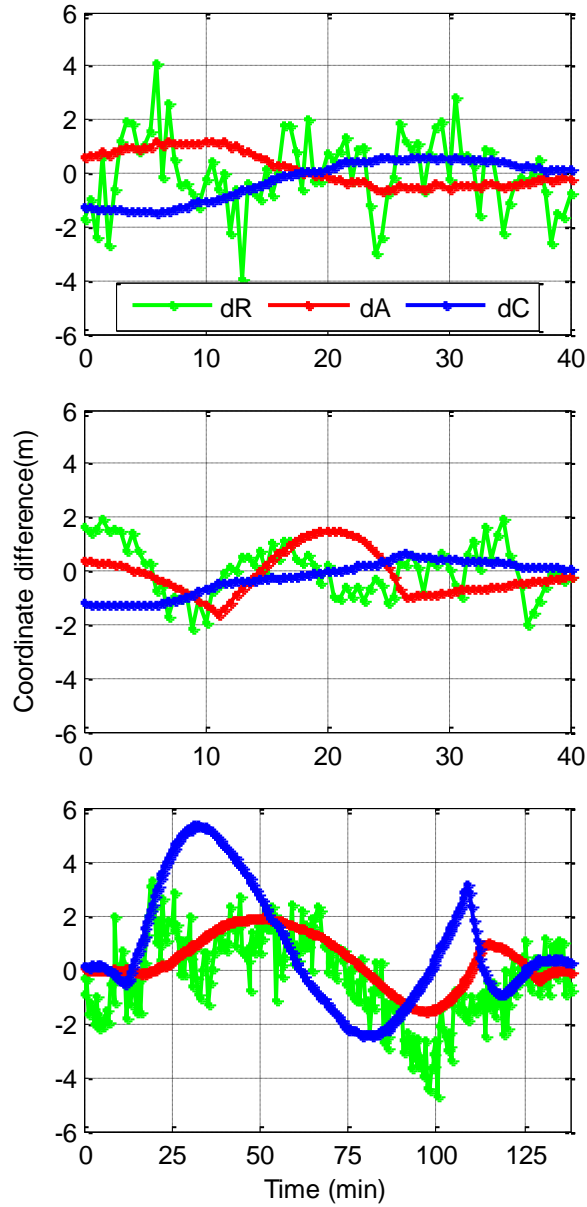


Fig. 12 Differences between corrected and kinematic orbits in RAC directions. Satellite C03 on Jan 5, 2015 (*top*), C08 on Jan 9, 2015 (*middle*) and C03 on Oct 20, 2014 (*bottom*)

Conclusions

Although the maneuver periods are only around 20 min for most Beidou satellites, the interruption of service is more than 6 h. Moreover, the accuracy of broadcast ephemeris available immediately after a maneuver is significantly lower than in normal situations, and

there is no precise ephemeris for the satellite on the day of maneuver. If the thrust forces on the satellite during the maneuver period can be estimated precisely, the interruption period for satellite navigation service could be significantly reduced, since tracking data before the maneuver can be used for orbit determination. We proposed a new algorithm to estimate the thrust forces acting on maneuver satellites using a ground tracking network. Both precise maneuver periods and thrust forces are estimated using carrier phase measurements.

In this study, Beidou observations of IGS MGEX network from Apr 2014 to Mar 2015 are used for the analysis. It can be concluded that:

(1) Compared to other navigation satellites, e.g., MEO, the Beidou GEO and IGSO satellites are frequently maneuvered, typically about 9 to 15 maneuvers per year for GEO satellites and 2 maneuvers per year for IGSO satellites.

(2) Both in-plane and out-of-plane maneuvers can be carried out for Beidou satellites. All maneuvers of IGSO satellites are out-of-plane, lasting 11 to 22 min; most GEO satellite maneuvers are in-plane, lasting 20 to 25 min. However the extreme cases of GEO out-of-plane maneuver can last about 2 h.

(3) Precise velocity changes during maneuver periods have been estimated using carrier phase measurements from a ground tracking network. For IGSO satellites, 0.4 to 0.6 m/s along-track and 0.1 to 0.5 m/s cross-track changes in velocity are applied; for GEO satellites, the velocity changes slightly over 0.1 m/s in the along-track direction due to general in-plane maneuvers. In the extreme case of C03 out-of-plane maneuver, a 28 m/s cross-track velocity change is applied.

(4) Accelerations induced by thrust forces during Beidou satellite maneuvers are normally in the range of 0.1 to 0.7 mm/s², which can be applied in either along- or cross-track directions.

In the extreme cases, the thrust force acting on a GEO satellite can reach 5.4 mm/s^2 , which is ten times more than the average forces in normal maneuvers.

(5) To verify the thrust force estimation accuracy, we applied the estimated forces into the satellite orbit integration process. The integrated orbits are at decimeter-level in along- and cross-track directions, compared with kinematic orbits obtained from ground tracking stations. Even for the extreme case, where two-hour maneuver was carried out, the integrated orbit can still reach 1 to 2 m in all RAC directions.

We have demonstrated that the thrust forces and maneuver periods of Beidou satellites can be precisely estimated by a GNSS ground tracking network. In our future work, the estimated thrust forces will be applied to the Beidou orbit determination program. This would obtain precise Beidou orbit during the maneuver periods and reduce service interruption time due to maneuvers.

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538

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